

RA, TRC, DRC

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🏷️ Tags	

Schemas:

- `Employee(ename, city, state)`
- `Works(ename, company_name, salary)`
- `Company(company_name, city)`

✅ (a) Relational Algebra Query

Find the names of employees getting salary > 60,000 and working in TCS or WIPRO.

Interpretation:

We're looking for:

- Employees from `Works` where `salary > 60000`
- And `company_name = 'TCS' OR 'WIPRO'`
- Get their `ename`

Relational Algebra:

text

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$$\pi_{ename} (\sigma_{salary > 60000 \wedge (company_name = 'TCS' \vee company_name = 'WIPRO')} (Works))$$

✅ (b) Tuple Relational Calculus (TRC)

Find employees living in Cuttack and working in companies placed in Bhubaneswar

Breakdown:

- From **Employee**, find people from **city = 'Cuttack'**
- Join with **Works** and **Company**
- Only if company city is Bhubaneswar

TRC Query:

```
text
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{ e.ename | Employee(e) ∧ e.city = 'Cuttack' ∧
  ∃ w ∈ Works (e.ename = w.ename ∧
    ∃ c ∈ Company (w.company_name = c.company_name ∧ c.city = 'Bhubaneswar')) }
```

(c) Domain Relational Calculus (DRC)

Find names of employees getting salary more than 60,000

DRC Query:

```
text
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{ <ename> | ∃ cname, sal (Works(ename, cname, sal) ∧ sal > 60000) }
```

Here we just project the ename for all tuples in Works where salary > 60000.



Given Schema:

- `Student(roll_no, name, address)`
- `Marks(roll_no, subject_code, marks)`
- `Subject(subject_code, subject_name)`

✓ (a) Relational Algebra

Find the name of students who have got more than 80 marks in DBMS

Step-by-step:

1. `Subject.subject_name = 'DBMS'`
2. Join it with `Marks` to get those subject codes
3. From `Marks`, select `marks > 80`
4. Join with `Student` to get student names

✍ Relational Algebra:

```
text
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$$\pi_{\text{name}} ( \sigma_{\text{marks} > 80} ( (\text{Student} \bowtie \text{Marks}) \bowtie \sigma_{\text{subject\_name} = \text{'DBMS'}} (\text{Subject}) ) )$$

```

✓ (b) Tuple Relational Calculus (TRC)

Find students living in Bhubaneswar and scored > 80 in any subject

✍ TRC Query:

```
text
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{ s.name | Student(s)  $\wedge$  s.address = 'Bhubaneswar'  $\wedge$ 
```

```
∃ m ∈ Marks (s.roll_no = m.roll_no ∧ m.marks > 80)
}
```

✅ (c) Domain Relational Calculus (DRC)

Find students who have scored > 80 in DBMS

✍️ DRC Query:

```
text
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{ <name> |
  ∃ r, a, sc, sub, m (
    Student(r, name, a) ∧
    Marks(r, sc, m) ∧
    Subject(sc, sub) ∧
    sub = 'DBMS' ∧
    m > 80
  )
}
```

🧠 Declarative vs Procedural

Style	Meaning
Declarative	You describe what you want, not how to get it.
Procedural	You specify how to get the result step-by-step (like a recipe).

📊 Comparison Table

Feature	Relational Algebra (RA)	Tuple Relational Calculus (TRC)	Domain Relational Calculus (DRC)
Query Style	Procedural	Declarative	Declarative
Unit of operation	Sets / relations	Tuples	Domain values

Focus	How to retrieve data	What data is required	What data is required
Based on	Operations (σ , π , \bowtie , etc.)	Predicate logic	Predicate logic
Example Thinking	"Join A and B, then filter"	"There exists a tuple where..."	"There exists a value where..."
Readability (for logic)	Medium	High for logic-based reasoning	High for domain-level queries

Summary:

- **Relational Algebra (RA) = Procedural**
- **TRC & DRC = Declarative**
- All are part of the **theoretical foundation** of relational databases and query optimization.

Optimizing Tuple Relational Calculus (TRC) queries


This is about **rewriting them for better clarity, logical efficiency**, and often to prepare them for translation into **Relational Algebra or SQL**. Even though TRC is declarative and doesn't specify how to fetch data, we can still make it more efficient logically.

TRC Optimization Tips

1. Push Selections Closer to the Source

- If a condition is only on one relation, **don't wrap it in a larger expression**.
- Example:

```
{ t |  $\exists e \in \text{Employee}$  (t.name = e.name  $\wedge$  e.city = 'Cuttack') }
```

 Can be optimized as:

```
{ e.name | Employee(e)  $\wedge$  e.city = 'Cuttack' }
```

✓ 2. Avoid Unnecessary Existential Quantifiers

Bad:

```
{ t.name |  $\exists e \in \text{Employee} (t.name = e.name \wedge \exists w \in \text{Works} (e.name = w.name \wedge w.salary > 60000))$  }
```

Optimized:

```
{ e.name |  $\text{Employee}(e) \wedge \exists w \in \text{Works} (e.name = w.name \wedge w.salary > 60000)$  }
```

| Avoid creating temporary tuple variables (t) when not needed.

✓ 3. Minimize Joins

Combine joins when possible and **project only required attributes**.

Example (original):

```
{ s.name |  $\text{Student}(s) \wedge \exists m \in \text{Marks} (s.roll = m.roll \wedge \exists sub \in \text{Subject} (m.sub\_code = sub.code \wedge sub.name = 'DBMS' \wedge m.marks > 80))$  }
```

Optimized:

```
{ s.name |  $\text{Student}(s) \wedge \exists m \in \text{Marks} (s.roll = m.roll \wedge m.marks > 80 \wedge \exists sub \in \text{Subject} (m.sub\_code = sub.code \wedge sub.name = 'DBMS'))$  }
```

| Rearranged to keep filtering conditions close to their relations.

✓ 4. Use Implicit Projections

If the goal is to **return only one attribute**, declare it clearly:

Instead of:

$$\{ t \mid \exists s \in \text{Student} (t.\text{name} = s.\text{name} \wedge s.\text{address} = \text{'BBSR'}) \}$$

Use:

$$\{ s.\text{name} \mid \text{Student}(s) \wedge s.\text{address} = \text{'BBSR'} \}$$

✓ 5. Short-circuit disjunctions or repeated joins

Instead of:

$$\{ e.\text{name} \mid \text{Employee}(e) \wedge ((\exists w \in \text{Works} (e.\text{name} = w.\text{name} \wedge w.\text{company} = \text{'TCS'})) \vee (\exists w \in \text{Works} (e.\text{name} = w.\text{name} \wedge w.\text{company} = \text{'WIPRO'}))) \}$$

Use:

$$\{ e.\text{name} \mid \text{Employee}(e) \wedge \exists w \in \text{Works} (e.\text{name} = w.\text{name} \wedge (w.\text{company} = \text{'TCS'} \vee w.\text{company} = \text{'WIPRO'})) \}$$

Final Tips

- Optimize predicates (\wedge , \vee , \neg) logically.
- Minimize nesting and quantifiers.
- Always aim for **readability + minimal joins**.