## ENV 790.30 - Time Series Analysis for Energy Data | Spring 2024 Assignment 2 - Due date 02/25/24

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#### **Submission Instructions**

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., "LuanaLima\_TSA\_A02\_Sp24.Rmd"). Then change "Student Name" on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

### R packages

R packages needed for this assignment: "forecast", "tseries", and "dplyr". Install these packages, if you haven't done yet. Do not forget to load them before running your script, since they are NOT default packages.

```
#Load/install required package here
# installing packages
# install.packages("forecast")
# install.packages("tseries")
# install.packages("dplyr")
# install.packages("lubridate")
# install.packages("ggplot2")
# loading packages
library("forecast")
## Registered S3 method overwritten by 'quantmod':
##
     method
                       from
     as.zoo.data.frame zoo
library("tseries")
library("dplyr")
##
## Attaching package: 'dplyr'
  The following objects are masked from 'package:stats':
##
##
       filter, lag
```

```
## The following objects are masked from 'package:base':
##

## intersect, setdiff, setequal, union

library("lubridate")

##

## Attaching package: 'lubridate'

## The following objects are masked from 'package:base':
##

## date, intersect, setdiff, union

library("ggplot2")
```

#### Data set information

Consider the data provided in the spreadsheet "Table\_10.1\_Renewable\_Energy\_Production\_and\_Consumption\_by\_Source.x on our **Data** folder. The data comes from the US Energy Information and Administration and corresponds to the December 2023 Monthly Energy Review. The spreadsheet is ready to be used. You will also find a .csv version of the data "Table\_10.1\_Renewable\_Energy\_Production\_and\_Consumption\_by\_Source-Edit.csv". You may use the function read.table() to import the .csv data in R. Or refer to the file "M2\_ImportingData\_CSV\_XLSX.Rmd" in our Lessons folder for functions that are better suited for importing the .xlsx.

```
#Importing data set

# checking working directory
getwd()

## [1] "/home/guest/ENV797_APJ_S24_NEW/Assignments/RMD"

# loading data using read.csv
# NOTE - R not letting me change my working directory to be my project folder, so
# I moved the file to Assignments > RMD (current wd) as a workaround

renewable_energy_full <- read.csv(
    file="Table_10.1_Renewable_Energy_Production_and_Consumption_by_Source.csv",
    header = TRUE, dec = ".", sep=",",stringsAsFactors = TRUE)

# converting Month column to date object using lubridate
renewable_energy_full$Month <- ym(renewable_energy_full$Month)

# renaming Month column to "Date"
colnames(renewable_energy_full)[colnames(renewable_energy_full) == "Month"] <- "Date"</pre>
```

### Question 1

You will work only with the following columns: Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption. Create a data frame structure with these three time series only. Use the command head() to verify your data.

```
# creating subset of data with Total Biomass Energy Production,
# Total Renewable Energy Production, Hydroelectric Power Consumption by date
renewable_energy_sub <- renewable_energy_full %>%
select(
    Date,
```

```
Total.Biomass.Energy.Production,
    Total.Renewable.Energy.Production,
    Hydroelectric.Power.Consumption)
# Verifying data
head(renewable_energy_sub)
           Date Total.Biomass.Energy.Production Total.Renewable.Energy.Production
## 1 1973-01-01
                                          129.787
                                                                             219.839
## 2 1973-02-01
                                          117.338
                                                                             197.330
## 3 1973-03-01
                                         129.938
                                                                             218.686
## 4 1973-04-01
                                         125.636
                                                                             209.330
## 5 1973-05-01
                                         129.834
                                                                             215.982
## 6 1973-06-01
                                         125.611
                                                                             208.249
    Hydroelectric.Power.Consumption
## 1
                               89.562
## 2
                               79.544
## 3
                               88.284
## 4
                               83.152
## 5
                               85.643
```

### Question 2

## 6

Transform your data frame in a time series object and specify the starting point and frequency of the time series using the function ts().

82.060

```
# transforming data into ts object
# start date is Jan 1, 1973
# frequency is 12 (monthly data)
renewable_energy_ts <- ts(renewable_energy_sub,start=c(1973,1),frequency=12)
renewable_energy_ts</pre>
```

```
##
             Date Total.Biomass.Energy.Production
## Jan 1973 1096
                                          129.787
## Feb 1973 1127
                                          117.338
## Mar 1973 1155
                                          129.938
## Apr 1973 1186
                                          125.636
## May 1973 1216
                                          129.834
## Jun 1973 1247
                                          125.611
## Jul 1973 1277
                                          129.787
## Aug 1973 1308
                                          129.918
## Sep 1973 1339
                                          125.782
## Oct 1973 1369
                                          129.970
## Nov 1973 1400
                                          125.643
## Dec 1973 1430
                                          129.824
## Jan 1974 1461
                                          130.807
## Feb 1974 1492
                                          118.091
## Mar 1974 1520
                                          130.727
## Apr 1974 1551
                                          126.583
## May 1974 1581
                                          130.789
## Jun 1974 1612
                                          126.611
## Jul 1974 1642
                                          130.756
## Aug 1974 1673
                                          130.763
```

## Sep 1974		126.637
## Oct 1974		130.718
## Nov 1974		126.506
## Dec 1974		130.674
## Jan 1975	1826	127.269
## Feb 1975	1857	114.942
## Mar 1975	1885	127.251
## Apr 1975	1916	123.139
## May 1975	1946	127.303
## Jun 1975	1977	123.241
## Jul 1975	2007	127.288
## Aug 1975	2038	127.321
## Sep 1975	2069	123.210
## Oct 1975	2099	127.312
## Nov 1975	2130	123.180
## Dec 1975	2160	127.277
## Jan 1976	2191	145.049
## Feb 1976	2222	135.695
## Mar 1976	2251	145.051
## Apr 1976	2282	140.363
## May 1976	2312	145.047
## Jun 1976	2343	140.405
## Jul 1976	2373	145.088
## Aug 1976		145.110
## Sep 1976	2435	140.436
## Oct 1976	2465	145.114
## Nov 1976	2496	140.651
## Dec 1976	2526	145.364
## Jan 1977	2557	156.220
## Feb 1977	2588	141.176
## Mar 1977	2616	156.217
## Apr 1977	2647	151.161
## May 1977	2677	156.186
## Jun 1977	2708	151.153
		155.920
	2738 2769	
0		156.081
C-F	2800	151.110
## Oct 1977	2830	156.172
## Nov 1977		151.000
## Dec 1977	2891	155.935
## Jan 1978	2922	173.128
## Feb 1978	2953	156.387
## Mar 1978	2981	173.136
## Apr 1978	3012	167.349
## May 1978	3042	172.923
## Jun 1978	3073	167.340
## Jul 1978	3103	172.912
## Aug 1978	3134	173.189
## Sep 1978	3165	167.455
## Oct 1978	3195	173.169
## Nov 1978	3226	167.557
## Dec 1978	3256	173.060
## Jan 1979	3287	182.600
## Feb 1979	3318	165.096

		1979	3346	182.881
##	Apr		3377	176.844
##	May	1979	3407	182.782
##		1979	3438	176.833
##		1979	3468	182.700
##	Aug	1979	3499	182.808
##	Sep	1979	3530	176.891
##	Oct	1979	3560	182.752
##	Nov	1979	3591	176.949
##		1979	3621	182.770
##	Jan	1980	3652	209.829
##	Feb	1980	3683	196.310
##	Mar	1980	3712	209.727
##	Apr	1980	3743	202.894
##	May	1980	3773	209.548
##	Jun	1980	3804	202.723
##	Jul	1980	3834	209.554
##	Aug	1980	3865	209.675
##	Sep	1980	3896	202.905
##	Oct	1980	3926	209.717
##	Nov	1980	3957	202.945
##	Dec	1980	3987	209.671
##	Jan	1981	4018	220.544
##	Feb	1981	4049	199.248
##	Mar	1981	4077	220.595
##	Apr	1981	4108	213.467
##	-	1981	4138	220.433
	•	1981	4169	213.237
##	Jul	1981	4199	220.392
##	Aug	1981	4230	220.428
##	_	1981	4261	213.480
	Oct		4291	220.581
##	Nov	1981	4322	213.437
##	Dec	1981	4352	220.440
##	Jan	1982	4383	226.251
		1982	4414	204.375
##	Mar	1982	4442	226.157
##	Apr	1982	4473	218.821
##	-	1982	4503	226.135
##	•	1982	4534	218.866
##		1982	4564	226.202
##		1982	4595	226.168
##	_	1982	4626	218.947
	-	1982	4656	226.373
		1982	4687	218.948
		1982	4717	226.210
		1983	4748	246.575
		1983	4779	222.738
		1983	4807	246.610
##		1983	4838	238.625
##	-	1983	4868	246.647
##	•	1983	4899	238.736
##		1983	4929	246.651
##		1983	4960	246.695
πĦ	nug	1900	1000	Z <del>I</del> U.U3U

##	-	1983	4991	238.755
##		1983	5021	246.732
##	Nov	1983	5052	238.780
##	Dec		5082	246.871
##	Jan	1984	5113	251.483
##	Feb	1984	5144	235.169
##	Mar	1984	5173	251.529
##	Apr	1984	5204	243.277
##	May	1984	5234	251.408
##	Jun	1984	5265	243.303
##	Jul	1984	5295	251.632
##	Aug	1984	5326	251.638
##	Sep	1984	5357	243.596
##	Oct	1984	5387	251.974
##	Nov	1984	5418	244.068
##	Dec	1984	5448	252.042
##	Jan	1985	5479	256.315
##	Feb	1985	5510	231.512
##	Mar	1985	5538	256.336
##	Apr	1985	5569	247.599
##	May	1985	5599	255.881
##	Jun	1985	5630	247.643
##	Jul	1985	5660	256.159
##	Aug	1985	5691	256.301
##	Sep	1985	5722	247.997
##	Oct	1985	5752	256.175
##	Nov	1985	5783	248.070
##	Dec	1985	5813	256.246
##	Jan	1986	5844	249.178
##	Feb	1986	5875	224.922
##	Mar	1986	5903	248.837
##	Apr	1986	5934	240.788
##	May	1986	5964	248.822
##	Jun	1986	5995	240.837
##	Jul	1986	6025	249.011
##	Aug	1986	6056	249.176
##	Sep	1986	6087	241.074
##	Oct	1986	6117	248.974
##	Nov	1986	6148	241.122
##	Dec	1986	6178	249.352
##	Jan	1987	6209	244.137
##	Feb	1987	6240	220.511
		1987	6268	244.157
##		1987	6299	236.139
	-	1987	6329	244.007
	•	1987	6360	236.522
		1987	6390	244.359
##		1987	6421	244.396
	_	1987	6452	236.298
	-	1987	6482	244.059
		1987	6513	236.197
		1987	6543	244.104
		1988	6574	255.331
		1988	6605	238.853
ππ	100	1000		200.000

##		1988	6634	255.385
##	-	1988	6665	247.241
##	May	1988	6695	255.188
##		1988	6726	247.340
##		1988	6756	255.582
##	Aug	1988	6787	255.815
##	Sep	1988	6818	247.357
##	Oct	1988	6848	255.517
##	Nov	1988	6879	247.096
##	Dec	1988	6909	255.345
##	Jan	1989	6940	266.572
##	Feb	1989	6971	243.927
##	Mar	1989	6999	268.315
##	Apr	1989	7030	251.946
##	May	1989	7060	241.235
##	Jun	1989	7091	248.447
##	Jul	1989	7121	261.318
##	Aug	1989	7152	276.985
##	_	1989	7183	264.811
##	Oct	1989	7213	276.462
##	Nov	1989	7244	276.819
		1989	7274	282.520
		1990	7305	236.692
		1990	7336	226.266
		1990	7364	244.248
##		1990	7395	232.640
	-	1990	7425	210.108
	•	1990	7456	178.544
		1990	7486	219.713
##		1990	7517	245.632
##	_	1990	7548	239.932
	Oct		7578	235.437
		1990	7609	220.256
	Dec		7639	245.644
	Jan		7670	269.531
	Feb		7701	204.535
	Mar	1991	7729	214.374
##	Apr		7760	190.452
##	_	1991	7790	206.579
##		1991	7821	200.379
##		1991	7851	210.055
##			7882	250.834
	_	1991		
##	-	1991	7913 7943	267.735
##	Oct		7943 7974	249.408
##		1991	7974	241.541
##	Dec	1991	8004	267.033
##	Jan		8035	279.197
##	Feb	1992	8066	230.468
##	Mar		8095	221.177
##	Apr	1992	8126	210.172
##	May		8156	190.537
##		1992	8187	230.985
##		1992	8217	250.150
##	Aug	1992	8248	269.662

##	Sep	1992	8279	251.511
##	Oct	1992	8309	269.545
##	Nov	1992	8340	264.383
##	Dec	1992	8370	263.891
##	Jan	1993	8401	274.257
##	Feb	1993	8432	240.964
##	Mar	1993	8460	263.204
##	Apr	1993	8491	226.859
	-	1993		196.012
	•	1993		197.445
		1993		212.707
		1993		262.322
	_	1993		250.551
	_	1993		257.383
		1993		262.183
##	Dec	1993	8735	264.559
##	Jan	1994	8766	306.708
##	Feb	1994	8797	244.594
		1994		261.461
##	Apr	1994	8856	236.035
##	May	1994	8886	202.480
	•	1994		215.744
##	Jul	1994	8947	274.451
##	Aug	1994	8978	251.577
	_	1994		238.967
	-			271.599
				261.436
##	Dec	1994	9100	262.482
##	Jan	1995	9131	243.462
##	Feb	1995	9162	206.657
##	Mar	1995	9190	239.820
##	Apr	1995	9221	267.571
##	May	1995	9251	227.439
##	Jun	1995	9282	226.934
##	Jul	1995	9312	294.251
##	Aug	1995	9343	301.628
##	Sep	1995	9374	268.791
##	Oct	1995	9404	292.175
##	Nov	1995	9435	267.659
##	Dec	1995	9465	262.694
##	Jan	1996	9496	272.584
##	Feb	1996	9527	226.038
##	Mar	1996	9556	259.039
##	Apr	1996	9587	205.729
##	May	1996	9617	231.211
##	Jun	1996	9648	254.182
##	Jul	1996	9678	281.656
##	Aug	1996	9709	294.581
##	Sep	1996	9740	259.345
##	Oct	1996	9770	310.461
##	Nov	1996	9801	295.562
##	Dec	1996	9831	264.912
		1997		275.641
##	Feb	1997	9893	226.521

			9921	251.136
##	-		9952	252.010
			9982	268.515
			10013	231.690
			10043	259.985
##	Aug	1997	10074	264.422
##	Sep	1997	10105	250.744
##	Oct	1997	10135	305.656
##	Nov	1997	10166	264.591
##	Dec	1997	10196	256.998
##	Jan	1998	10227	278.211
##	Feb	1998	10258	212.209
##	Mar	1998	10286	240.963
##	Apr	1998	10317	240.612
##	May	1998	10347	250.239
##	Jun	1998	10378	186.089
##	Jul	1998	10408	246.326
##	Aug	1998	10439	254.237
##	Sep	1998	10470	248.270
##	Oct	1998	10500	267.922
##	Nov	1998	10531	230.488
##	Dec	1998	10561	273.362
##	Jan	1999	10592	272.260
##	Feb	1999	10623	220.539
##	Mar	1999	10651	212.177
##	Apr	1999	10682	249.920
##	May	1999	10712	289.264
##	Jun	1999	10743	236.090
##	Jul	1999	10773	264.292
##	Aug	1999	10804	258.854
##	Sep	1999	10835	244.140
##	Oct	1999	10865	228.256
##	Nov	1999	10896	254.125
##	Dec	1999	10926	235.215
##	Jan	2000	10957	222.067
##	Feb	2000	10988	246.169
##	Mar	2000	11017	263.209
##	Apr	2000	11048	254.609
##	May	2000	11078	254.678
##	Jun	2000	11109	227.712
##	Jul	2000	11139	255.348
##			11170	254.942
##	_	2000		240.331
##	-	2000		270.472
##			11262	261.335
##			11292	254.788
##		2001		228.434
##		2001		202.849
##			11382	219.649
##			11413	213.628
##			11443	211.506
##	-		11474	213.950
##		2001		221.842
##		2001		225.897
η π	5			

##	Sep	2001	11566	214.229
##	Oct	2001	11596	227.319
##	Nov	2001	11627	219.773
##	Dec	2001	11657	225.088
##	Jan	2002	11688	228.396
##	Feb	2002	11719	198.932
##	Mar	2002	11747	217.568
##	Apr	2002	11778	212.852
	-		11808	225.155
			11839	215.107
			11869	235.713
			11900	224.400
			11931	230.855
			11961	243.767
			11992	230.328
			12022	242.334
			12053	237.044
			12084	212.693
			12112	233.288
	-		12143	228.516
			12173	229.756
			12204	228.254
			12234	242.533
	_		12265	239.928
			12296	230.968
			12326	236.938
			12357 12387	233.698 251.160
			12418	251.160
			12449	236.689
			12478	248.532
			12509	247.253
	-		12539	244.383
	•		12570	244.075
			12600	257.042
			12631	254.446
	_		12662	243.019
	-		12692	253.520
			12723	247.286
			12753	264.199
			12784	264.707
##	Feb	2005	12815	247.271
##	Mar	2005	12843	260.043
##	Apr	2005	12874	246.929
##	May	2005	12904	255.790
##	Jun	2005	12935	252.466
##	Jul	2005	12965	266.332
##	Aug	2005	12996	266.097
##	Sep	2005	13027	255.348
##	Oct	2005	13057	261.121
##	Nov	2005	13088	256.532
##	Dec	2005	13118	268.550
##	Jan	2006	13149	276.647
##	Feb	2006	13180	247.274

##	Mar	2006	13208	265.069
##	Apr	2006	13239	250.384
##	May	2006	13269	261.125
##	Jun	2006	13300	261.960
##	Jul	2006	13330	274.809
##	Aug	2006	13361	277.063
##	Sep	2006	13392	267.952
##	Oct	2006	13422	275.120
##	Nov	2006	13453	270.475
##	Dec	2006	13483	283.636
##	Jan	2007	13514	290.845
##	Feb	2007	13545	261.666
##	Mar	2007	13573	285.146
##	Apr	2007	13604	278.386
##	May	2007	13634	286.010
			13665	281.995
##	Jul	2007	13695	295.653
##	Aug	2007	13726	295.523
			13757	287.603
			13787	299.416
			13818	297.828
##	Dec	2007	13848	312.007
##	Jan	2008	13879	331.138
			13910	300.535
			13939	321.487
			13970	314.073
			14000	324.185
			14031	313.335
			14061	330.507
			14092	333.607
	_		14123	318.840
	_		14153	330.125
##	Nov	2008	14184	327.317
			14214	323.102
##	Jan	2009	14245	318.353
##	Feb	2009	14276	294.389
##	Mar	2009	14304	319.356
##	Apr	2009	14335	303.489
	_		14365	319.032
##	Jun	2009	14396	321.739
##	Jul	2009	14426	343.841
##	Aug	2009	14457	348.551
##	Sep	2009	14488	332.374
			14518	346.472
##	Nov	2009	14549	348.333
##	Dec	2009	14579	360.689
##	Jan	2010	14610	377.071
			14641	347.952
			14669	384.094
			14700	368.922
	-		14730	376.012
			14761	372.328
			14791	385.443
			14822	389.064
	0			

##	Sep	2010	14853	377.355
##	Oct	2010	14883	386.771
##	Nov	2010	14914	386.602
##	Dec	2010	14944	400.917
##	Jan	2011	14975	400.710
			15006	359.327
			15034	394.959
			15065	373.481
			15095	385.273
			15126	389.673
			15156	399.454
			15187	402.931
			15218	387.218
			15248	397.994
			15279	400.892
			15309	420.525
			15340	399.385
			15371	373.028
			15400	388.074
			15431	368.981
			15461	387.318
			15492	377.792
			15522	379.862
			15553	386.269
			15584	366.955
			15614	373.976
			15645	368.902
			15675	383.017
			15706	391.713
			15737	354.251
			15765	397.835
			15796	386.469
			15826	404.782
			15857	
				401.893
			15887	419.452 413.684
	_		15918	395.313
			15949	
			15979	417.493
			16010	415.796
			16040	436.115
			16071	421.219
			16102	382.387
			16130	423.831
	-		16161	409.123
	•		16191	420.280
			16222	422.985
			16252	437.716
	_		16283	431.265
	-		16314	411.320
			16344	424.919
			16375	420.082
			16405	446.975
			16436	427.054
##	Feb	2015	16467	385.885

			16495	418.601
	_		16526	404.645
	•		16556	422.303
			16587	419.763
			16617	435.439
	_		16648	432.205
##	Sep	2015	16679	410.191
##	Oct	2015	16709	418.690
			16740	419.255
##	Dec	2015	16770	437.317
			16801	427.949
			16832	406.692
			16861	429.456
##	Apr	2016	16892	400.491
##	May	2016	16922	424.186
##	Jun	2016	16953	425.120
##	Jul	2016	16983	434.897
##	Aug	2016	17014	442.383
##	Sep	2016	17045	417.250
##	Oct	2016	17075	425.218
##	Nov	2016	17106	428.755
##	Dec	2016	17136	469.360
##	Jan	2017	17167	440.361
##	Feb	2017	17198	397.221
##	Mar	2017	17226	438.279
##	Apr	2017	17257	408.991
##	May	2017	17287	427.713
##	Jun	2017	17318	424.376
##	Jul	2017	17348	435.876
##	Aug	2017	17379	446.874
##	Sep	2017	17410	417.527
##	Oct	2017	17440	434.336
##	Nov	2017	17471	439.367
##	Dec	2017	17501	454.794
##	Jan	2018	17532	449.901
##	Feb	2018	17563	413.516
##	Mar	2018	17591	449.807
##	Apr	2018	17622	425.820
##	May	2018	17652	445.435
##	Jun	2018	17683	438.894
##	Jul	2018	17713	456.125
##	Aug	2018	17744	459.996
##	Sep	2018	17775	427.721
##	Oct	2018	17805	449.554
##	Nov	2018	17836	440.785
##	Dec	2018	17866	456.593
##	Jan	2019	17897	445.618
##	Feb	2019	17928	405.314
##	Mar	2019	17956	434.186
##	Apr	2019	17987	423.416
##	May	2019	18017	440.470
	•		18048	433.492
			18078	449.754
			18109	447.086

```
## Sep 2019 18140
                                            416.911
## Oct 2019 18170
                                           432.540
## Nov 2019 18201
                                           431.235
## Dec 2019 18231
                                           454.980
## Jan 2020 18262
                                           433.538
## Feb 2020 18293
                                           404.020
## Mar 2020 18322
                                           411.929
## Apr 2020 18353
                                           324.772
## May 2020 18383
                                           355.693
## Jun 2020 18414
                                           375.486
## Jul 2020 18444
                                           396.389
## Aug 2020 18475
                                           398.732
## Sep 2020 18506
                                           386.923
## Oct 2020 18536
                                           399.780
## Nov 2020 18567
                                           403.366
## Dec 2020 18597
                                           419.147
## Jan 2021 18628
                                           409.000
## Feb 2021 18659
                                           348.243
                                           410.780
## Mar 2021 18687
## Apr 2021 18718
                                           393.027
## May 2021 18748
                                           418.210
## Jun 2021 18779
                                           410.360
## Jul 2021 18809
                                           425.507
## Aug 2021 18840
                                           412.988
## Sep 2021 18871
                                           394.918
## Oct 2021 18901
                                           422.097
## Nov 2021 18932
                                           423.575
## Dec 2021 18962
                                           444.912
## Jan 2022 18993
                                           435.124
## Feb 2022 19024
                                           394.151
## Mar 2022 19052
                                           430.403
## Apr 2022 19083
                                           405.815
## May 2022 19113
                                           429.947
## Jun 2022 19144
                                           429.508
## Jul 2022 19174
                                           436.315
## Aug 2022 19205
                                           428.868
## Sep 2022 19236
                                           401.522
## Oct 2022 19266
                                           425.435
## Nov 2022 19297
                                           427.493
## Dec 2022 19327
                                           428.630
## Jan 2023 19358
                                           436.916
## Feb 2023 19389
                                           392.661
## Mar 2023 19417
                                           436.299
## Apr 2023 19448
                                           404.131
## May 2023 19478
                                           437.506
## Jun 2023 19509
                                            429.839
## Jul 2023 19539
                                           437.109
## Aug 2023 19570
                                           439.521
## Sep 2023 19601
                                           422.351
            Total.Renewable.Energy.Production Hydroelectric.Power.Consumption
## Jan 1973
                                                                          89.562
                                       219.839
## Feb 1973
                                                                          79.544
                                       197.330
## Mar 1973
                                       218.686
                                                                          88.284
## Apr 1973
                                       209.330
                                                                          83.152
```

## May 1973	215.982	85.643
## Jun 1973	208.249	82.060
## Jul 1973	207.800	77.400
## Aug 1973	203.432	72.936
## Sep 1973	185.300	59.029
## Oct 1973	193.514	62.967
## Nov 1973	195.326	69.063
## Dec 1973	220.755	90.131
## Jan 1974	231.010	99.500
## Feb 1974	210.188	91.476
## Mar 1974	226.384	94.950
## Apr 1974	223.218	95.969
## May 1974	227.793	96.337
## Jun 1974	218.976	91.719
## Jul 1974	221.909	90.437
## Aug 1974	214.197	82.727
## Sep 1974	200.900	73.610
## Oct 1974	200.312	68.931
## Nov 1974	200.068	72.773
## Dec 1974	211.046	79.542
## Jan 1975	214.319	86.356
## Feb 1975	198.008	82.404
## Mar 1975	224.384	96.386
## Apr 1975	215.679	91.791
## May 1975	223.695	95.581
## Jun 1975	217.798	93.550
## Jul 1975	216.202	87.900
## Aug 1975	206.312	77.892
## Sep 1975	194.934	70.756
## Oct 1975	206.489	78.060
## Nov 1975	208.436	84.171
## Dec 1975	217.911	89.510
## Jan 1976	236.073	89.904
## Feb 1976	221.374	84.626
## Mar 1976	237.807	91.629
## Apr 1976	224.756	83.378
## May 1976	234.082	88.065
## Jun 1976	229.595	88.182
## Jul 1976	235.984	89.807
## Aug 1976	228.336	82.153
## Sep 1976	211.665	70.186
## Oct 1976	218.818	72.690
## Nov 1976	209.968	68.463
## Dec 1976	216.239	69.900
## Jan 1977	228.907	71.630
## Feb 1977	194.523	52.424
## Mar 1977	225.781	68.518
## Apr 1977	216.602	64.508
## May 1977	221.823	64.629
## Jun 1977	211.752	59.609
## Jul 1977	215.097	58.130
## Aug 1977	214.871	57.830
## Sep 1977	208.974	56.835
## Oct 1977	216.727	59.480

##	Nov	1977	222.663	70.583
##	Dec	1977	235.754	78.744
##	Jan	1978	260.677	86.454
##	Feb	1978	233.933	76.606
		1978	258.863	84.951
##	Apr	1978	255.285	87.281
##	May	1978	272.691	99.185
##	Jun	1978	254.703	86.645
		1978	258.056	84.339
##	Aug	1978	250.652	76.518
##	Sep	1978	241.494	73.042
##	Oct	1978	241.095	67.184
##	Nov	1978	237.214	68.818
##	Dec	1978	250.285	76.162
##	Jan	1979	270.000	86.378
##	Feb	1979	239.377	73.446
		1979	273.485	89.483
##	Apr	1979	265.526	87.645
##	May	1979	283.727	99.903
		1979	264.118	86.230
		1979	262.394	78.573
		1979	257.423	73.393
	_	1979	243.468	65.516
##	Oct	1979	253.559	69.619
##	Nov	1979	255.317	77.213
		1979	262.637	78.457
##	Jan	1980	298.221	87.244
		1980	271.194	73.781
		1980	294.931	83.978
	_	1980	293.043	88.865
	•	1980	310.682	99.622
		1980	299.633	95.451
		1980	295.537	84.448
		1980	281.831	70.517
	_	1980	268.204	63.819
		1980	273.058	61.661
		1980	270.913	66.325
		1980	288.131	76.858
		1981	299.483	77.214
		1981	273.604	72.830
		1981	293.454	71.150
	_	1981	286.764	71.718
	•	1981	305.297	83.301
		1981	305.860	91.061
		1981	308.821	86.714
	_	1981	296.678	74.556
		1981	276.720	61.534
		1981	284.684	62.420
		1981	280.364	65.459
		1981	304.193	82.279
		1982	320.311	92.763
		1982	297.475	91.907
		1982		102.924
##	Apr	1982	316.183	96.303

##	May	1982	323.939	96.572
		1982	316.816	96.463
		1982	321.854	94.087
	_	1982	310.059	82.333
	_	1982	289.054	68.612
		1982	296.056	68.091
		1982	300.864	80.245
		1982	323.054	95.522
		1983	348.969	100.743
		1983	320.213	96.206
		1983	352.422	104.348
	_	1983	343.331	103.334
	•	1983	355.330	107.568
		1983	346.012	105.810
		1983	345.359	96.883
	_	1983	338.025	88.929
	_	1983	315.758	74.808
		1983	320.524	71.491
		1983	325.785	84.956
		1983	357.437	108.936
		1984	355.607	102.459
		1984	333.238	96.034
		1984	358.566	104.801
	_	1984	348.756	103.270
	•	1984	363.212	109.683
		1984 1984	344.623 348.366	99.261 94.772
			340.669	86.573
	_	1984	317.887	72.076
	_	1984 1984	326.373	71.968
		1984	323.172	76.704
		1984	343.652	88.949
		1985	353.933	94.973
		1985	323.067	89.219
		1985	344.083	85.029
		1985	334.259	84.276
	-	1985	349.644	91.284
		1985	332.457	82.425
		1985	332.393	73.612
		1985	328.026	68.980
	_	1985	315.367	64.761
	_	1985	327.776	69.105
		1985	330.222	79.075
		1985	346.947	87.328
		1986	326.552	73.934
		1986	307.952	80.075
		1986	349.995	98.081
		1986	338.487	94.922
	-	1986	345.587	93.958
	•	1986	334.442	90.562
		1986	335.334	83.094
		1986	325.501	73.104
	_	1986	316.539	72.767
	_	1986	325.125	73.498

##	Nov	1986	323.172	79.755
##	Dec	1986	341.787	89.397
##	Jan	1987	334.890	87.702
##	Feb	1987	296.606	73.264
##	Mar	1987	327.541	80.279
##	Apr	1987	315.231	76.163
##	May	1987	330.797	83.712
##	Jun	1987	311.957	72.271
		1987	317.495	69.864
##	Aug	1987	311.395	63.744
	_	1987	302.090	62.756
##	Oct	1987	309.095	61.964
##	Nov	1987	297.439	58.272
##	Dec	1987	319.908	72.753
##	Jan	1988	334.583	76.171
		1988	307.533	66.029
		1988	326.015	67.539
	_	1988	316.232	66.195
		1988	331.539	73.601
		1988	315.603	65.346
		1988	317.391	58.636
		1988	315.766	56.923
	_	1988	306.500	56.241
		1988	310.737	52.265
		1988	313.792	63.762
		1988	326.992	68.748
		1989	348.321	73.277
		1989	317.572	65.188
		1989	358.115	79.268
	_	1989	346.511	84.295
	•	1989	350.304	98.200
		1989	349.753	90.614
		1989	351.720	79.373
		1989	358.320	70.675
		1989	341.553	66.237
		1989	356.682	70.285
		1989	359.731	74.172
		1989 1990	367.555 329.327	76.402 83.078
		1990		
		1990	321.465 353.956	86.122 98.841
		1990		90.589
	-	1990	334.136 317.791	95.753
	•	1990	289.276	98.444
		1990	315.872	84.490
		1990	332.580	75.559
	_	1990	311.965	61.422
	-	1990	312.873	66.657
		1990	301.883	71.863
		1990	341.584	86.440
		1991	370.278	91.732
		1991	292.511	78.638
		1991	317.683	92.384
		1991	293.309	91.874
	1			32.011

##	May	1991	320.120	101.296
		1991	313.437	91.854
##	Jul	1991	309.257	86.984
##	Aug	1991	340.813	77.658
##	Sep	1991	345.122	65.997
##	Oct	1991	324.454	63.197
##	Nov	1991	318.757	66.085
##	Dec	1991	355.690	78.349
##	Jan	1992	366.577	77.844
##	Feb	1992	305.537	64.670
		1992	311.299	78.408
##	Apr	1992	292.073	70.180
##	May	1992	282.361	79.980
##	Jun	1992	323.546	80.819
##	Jul	1992	333.005	70.671
	_	1992	347.510	65.474
##	Sep	1992	324.027	60.474
##	Oct	1992	340.565	59.474
##	Nov	1992	345.048	69.964
##	Dec	1992	360.200	85.579
##	Jan	1993	373.255	88.873
##	Feb	1993	322.185	71.730
		1993	359.855	83.868
##	Apr	1993	330.605	90.980
##	May	1993	313.546	104.743
##	Jun	1993	304.450	95.182
		1993	309.916	84.360
	_	1993	346.577	71.587
##	Sep	1993	324.882	62.245
##	Oct	1993	331.480	62.087
##	Nov	1993	338.485	64.729
##	Dec	1993	352.074	76.662
		1994	388.854	72.773
		1994	323.751	69.738
		1994	354.509	80.508
##	Apr	1994	332.955	84.264
##	May	1994	303.865	88.353
		1994	313.708	85.343
		1994	366.741	79.712
	_	1994	333.540	69.257
	-	1994	307.933	56.561
		1994	343.569	59.757
		1994	338.304	65.325
		1994	348.732	75.959
		1995	336.872	84.852
		1995	299.810	85.447
		1995	346.752	97.479
	-	1995	361.046	83.847
	-	1995	333.643	94.791
		1995	342.092	103.128
		1995	400.977	93.729
	_	1995	399.583	83.175
	_	1995	349.815	68.333
##	Oct	1995	384.663	78.993

##	Nov	1995	366.200	87.148
##	Dec	1995	373.129	99.640
		1996	385.971	104.821
##	Feb	1996	343.243	108.488
		1996	385.026	115.603
##	Apr	1996	325.915	108.647
##	May	1996	356.221	113.485
		1996	375.816	108.928
		1996	395.278	98.519
	_	1996	398.870	89.620
	_	1996	347.920	75.536
		1996	400.155	77.094
		1996	387.043	80.374
		1996	378.537	103.400
		1997	397.124	112.458
		1997	342.279	107.528
		1997	381.623	119.397
	-	1997	374.093	109.441
		1997	398.347	116.635
		1997	362.325	117.564
		1997	382.540	108.011
		1997	370.673	91.802
	_	1997	343.197	79.836
		1997	402.188	84.394
		1997	355.868	80.900
		1997	355.807	88.252
		1998	386.269	98.328
		1998	323.378	102.347
		1998	360.492	108.119
	_	1998	348.763	97.610
	•	1998	374.487	113.264
		1998	309.019	110.348
		1998	358.537	97.785
		1998	354.150	85.678
	_	1998	332.989	71.060
		1998	345.379	64.434
		1998	309.809	68.310
		1998	370.867	85.937
		1999	383.582	100.724
		1999	328.183	97.902
		1999	334.062	109.456
	_	1999	355.198	93.280
	-	1999	401.370	98.936
		1999	353.158	104.294
		1999	379.433	101.288
	_	1999	360.215	87.778
		1999	328.356	71.283
		1999	308.985	67.908
		1999	337.650	72.210
		1999	332.407	85.198
		2000	319.978	86.468
		2000	334.369	76.714
		2000	366.040 364.110	91.110
##	whī	2000	364.110	97.207

## May 2000	361.267	93.560
## Jun 2000	326.724	85.931
## Jul 2000	351.077	82.333
## Aug 2000	343.214	74.999
## Sep 2000	312.937	60.736
## Oct 2000	341.025	58.639
## Nov 2000	339.223	65.377
## Dec 2000	333.069	67.181
## Jan 2001	303.197	64.323
## Feb 2001	272.585	59.617
## Mar 2001	301.844	69.868
## Apr 2001	288.028	61.460
## May 2001	290.338	65.427
## Jun 2001	298.272	70.723
## Jul 2001	297.654	61.686
## Aug 2001	304.239	64.534
## Sep 2001	279.069	52.054
## Oct 2001	292.015	51.980
## Nov 2001	283.668	52.589
## Dec 2001	302.843	66.010
## Jan 2002	314.861	74.364
## Feb 2002	279.136	68.894
## Mar 2002	302.856	71.682
## Apr 2002	309.709	82.729
## May 2002	331.378	90.973
## Jun 2002	326.674	96.262
## Jul 2002	337.792	86.906
## Aug 2002	311.593	71.938
## Sep 2002	302.858	58.300
## Oct 2002	315.739	58.589
## Nov 2002	309.716	67.319
## Dec 2002	328.629	73.933
## Jan 2003	318.956	70.287
## Feb 2003	291.767	67.489
## Mar 2003	330.201	82.578
## Apr 2003	327.749	84.478
## May 2003	345.099	100.297
## Jun 2003	341.209	97.536
## Jul 2003	342.647	84.765
## Aug 2003	333.101	78.381
## Sep 2003	308.470	63.055
## Oct 2003	313.818	62.878
## Nov 2003	314.096	67.268
## Dec 2003	347.074	82.039
## Jan 2004	347.154	78.419
## Feb 2004	321.055	71.357
## Mar 2004	342.168	78.184
## Apr 2004	334.068	71.270
## May 2004	344.066	81.955
## Jun 2004	346.968	86.161
## Jul 2004	353.034	79.562
## Aug 2004	344.004	73.672
## Sep 2004	328.252	70.032
## Oct 2004	332.739	64.360

##	Nov	2004	332.106	71.437
##	Dec	2004	367.856	89.431
##	Jan	2005	361.269	82.817
##	Feb	2005	333.479	73.722
##	Mar	2005	354.763	78.258
##	Apr	2005	342.863	78.675
##	May	2005	367.186	93.074
##	Jun	2005	362.264	91.384
##	Jul	2005	372.396	88.565
##	Aug	2005	356.107	73.582
##	Sep	2005	331.447	59.245
##	Oct	2005	339.018	61.438
##	Nov	2005	338.541	66.031
##	Dec	2005	360.826	75.546
##	Jan	2006	388.583	93.614
##	Feb	2006	348.049	84.487
##	Mar	2006	368.883	84.019
##	Apr	2006	367.940	97.432
##	May	2006	386.890	105.153
##	Jun	2006	383.011	101.532
##	Jul	2006	381.340	86.799
##	Aug	2006	370.019	74.137
##	Sep	2006	345.317	58.691
##	Oct	2006	353.690	58.192
##	Nov	2006	359.164	69.167
##	Dec	2006	376.761	73.685
##	Jan	2007	399.004	88.865
##	Feb	2007	343.865	63.349
##	Mar	2007	390.167	82.446
##	Apr	2007	383.102	81.515
##	May	2007	398.044	88.872
##	Jun	2007	382.096	77.850
##	Jul	2007	393.450	76.694
##	Aug	2007	386.428	68.037
##	Sep	2007	360.587	50.302
##	Oct	2007	374.075	50.485
##	Nov	2007	373.327	53.507
##	Dec	2007	397.970	62.582
##	Jan	2008	427.860	70.898
##	Feb	2008	388.671	64.108
##	Mar	2008	424.851	73.934
##	Apr	2008	421.184	75.862
##	May	2008	449.522	92.879
##	Jun	2008	444.695	99.553
##	Jul	2008	446.062	87.194
##	Aug	2008	431.761	72.434
##	Sep	2008	398.411	55.200
##	Oct	2008	412.573	52.783
##	Nov	2008	409.976	53.459
##	Dec	2008	428.996	71.179
##	Jan	2009	431.011	80.149
##	Feb	2009	386.812	60.775
##	Mar	2009	432.104	74.475
##	Apr	2009	431.059	87.927

## May 2009	456.231	100.858
## Jun 2009	455.356	99.744
## Jul 2009	455.962	79.789
## Aug 2009	449.335	66.808
## Sep 2009	421.927	59.228
## Oct 2009	450.940	67.186
## Nov 2009	456.527	71.678
## Dec 2009	481.882	84.378
## Jan 2010	489.844	76.371
## Feb 2010	449.090	70.252
## Mar 2010	499.560	71.262
## Apr 2010	482.552	65.158
## May 2010	507.544	85.570
## Jun 2010	517.750	101.861
## Jul 2010	508.593	83.651
## Aug 2010	497.073	68.647
## Sep 2010	476.105	58.909
## Oct 2010	489.125	60.334
## Nov 2010	500.488	66.744
## Dec 2010	524.855	79.053
## Jan 2011	530.909	87.112
## Feb 2011	490.715	82.336
## Mar 2011	553.169	106.231
## Apr 2011	538.506	106.435
## May 2011	554.011	111.187
## Jun 2011	553.885	109.700
## Jul 2011	549.374	106.743
## Aug 2011	534.036	87.905
## Sep 2011	500.175	72.940
## Oct 2011	517.691	67.515
## Nov 2011	528.710	70.562
## Dec 2011	552.823	80.973
## Jan 2012	539.035	78.842
## Feb 2012	494.125	69.207
## Mar 2012	541.244	88.400
## Apr 2012	519.621	89.716
## May 2012	546.977	97.728
## Jun 2012	528.771	90.960
## Jul 2012	520.168	90.388
## Aug 2012	513.269	78.592
## Sep 2012	475.610	60.064
## Oct 2012	491.516	56.300
## Nov 2012	489.078	63.915
## Dec 2012	527.556	78.420
## Jan 2013	542.692	84.715
## Feb 2013	487.697	69.668
## Mar 2013	541.012	70.063
## Apr 2013	551.448	85.631
## May 2013	578.378	97.072
## Jun 2013	563.561	93.434
## Jul 2013	572.289	92.993
## Aug 2013	542.610	73.813
## Sep 2013	514.219	57.871
## Oct 2013	543.689	58.682

##	Nov	2013	548.475	60.313
##	Dec	2013	574.712	72.090
##	Jan	2014	574.319	73.815
##	Feb	2014	507.326	59.356
##	Mar	2014	589.693	82.765
##	Apr	2014	583.144	86.801
##	May	2014	589.777	90.568
##	Jun	2014	590.788	87.838
##	Jul	2014	588.697	83.107
##	Aug	2014	560.101	67.582
##	Sep	2014	530.782	54.846
##	Oct	2014	557.457	58.547
##	Nov	2014	569.677	63.548
##	Dec	2014	593.827	76.186
##	Jan	2015	581.002	82.360
##	Feb	2015	533.488	76.040
##	Mar	2015	579.817	82.846
##	Apr	2015	569.898	76.671
##	May	2015	579.138	68.668
##	Jun	2015	564.673	69.653
##	Jul	2015	584.483	71.701
##	Aug	2015	572.778	65.245
##	Sep	2015	540.124	54.913
##	Oct	2015	557.167	56.743
##	Nov	2015	575.787	65.981
##	Dec	2015	607.572	79.041
##	Jan	2016	600.004	87.397
##	Feb	2016	582.468	82.362
##	Mar	2016	626.931	93.454
##	Apr	2016	590.484	88.296
##	May	2016	609.870	86.960
##	Jun	2016	594.461	79.284
##	Jul	2016	605.124	73.206
##	Aug	2016	592.159	66.771
##	Sep	2016	562.996	55.847
##	Oct	2016	585.197	59.160
##	Nov	2016	586.984	64.174
##	Dec	2016	651.738	76.865
##	Jan	2017	627.929	90.854
##	Feb	2017	581.036	81.485
##	Mar	2017	664.711	101.040
##	Apr	2017	635.896	100.345
##	May	2017	662.077	111.255
##	Jun	2017	643.105	104.323
##	Jul	2017	626.343	90.753
##	Aug	2017	612.943	75.180
##	Sep	2017	584.631	65.346
##	Oct	2017	615.446	60.386
		2017	614.560	67.859
##	Dec	2017	635.919	75.910
##	Jan	2018	653.150	85.519
##	Feb	2018	610.036	84.967
##	Mar	2018	669.313	88.236
##	Apr	2018	657.253	95.929

## May 2018	681.427	103.876
## Jun 2018	669.472	94.163
## Jul 2018	648.661	85.640
## Aug 2018	652.676	75.122
## Sep 2018	601.408	65.393
## Oct 2018	628.690	66.698
## Nov 2018	623.898	74.766
## Dec 2018	648.213	77.784
## Jan 2019	645.530	84.610
## Feb 2019	593.795 657.711	78.068
## Mar 2019	657.711	89.852
## Apr 2019	666.642 690.669	94.922 109.123
## May 2019 ## Jun 2019	661.828	95.801
## Jul 2019	667.695	84.875
## Aug 2019	648.350	77.038
## Sep 2019	613.803	63.210
## Oct 2019	634.265	62.459
## Nov 2019	621.355	68.982
## Dec 2019	651.174	73.284
## Jan 2020	649.110	83.587
## Feb 2020	632.884	88.262
## Mar 2020	642.361	81.284
## Apr 2020	561.380	79.139
## May 2020	619.030	102.279
## Jun 2020	637.875	95.534
## Jul 2020	633.731	91.243
## Aug 2020	619.356	79.443
## Sep 2020	584.297	63.732
## Oct 2020	612.749	64.181
## Nov 2020	630.734	71.286
## Dec 2020	641.695	73.385
## Jan 2021	637.388	83.799
## Feb 2021	552.930	68.706
## Mar 2021	678.059	72.404
## Apr 2021	651.233	66.155
## May 2021	689.525	79.530
## Jun 2021	656.848	80.025
## Jul 2021	651.269	75.397
## Aug 2021	648.898	69.360
## Sep 2021	620.767	58.080
## Oct 2021	650.143	58.458
## Nov 2021	663.620	66.102
## Dec 2021	706.622	80.393
## Jan 2022	697.568	82.562
## Feb 2022	651.899	72.746
## Mar 2022	733.189	83.377
## Apr 2022	712.467	68.465
## May 2022	742.753	79.700
## Jun 2022	725.578	88.670
## Jul 2022	713.262	83.824
## Aug 2022	672.494	72.106
## Sep 2022	632.729	58.093
## Oct 2022	659.196	49.022

## Nov 2022	685.824	61.068
## Dec 2022	680.383	69.706
## Jan 2023	701.741	76.048
## Feb 2023	659.745	63.745
## Mar 2023	734.657	69.017
## Apr 2023	699.747	59.646
## May 2023	740.660	93.759
## Jun 2023	691.709	66.434
## Jul 2023	711.895	72.463
## Aug 2023	711.962	72.150
## Sep 2023	666.253	56.284

### Question 3

Compute mean and standard deviation for these three series.

```
# calculating mean and standard deviation for each time series
# mean and sd for biomass
bioMass_mean_ts <- print(mean(renewable_energy_ts[,2]))</pre>
## [1] 279.8046
bioMass_stDev_ts <- print(sd(renewable_energy_ts[,2]))</pre>
## [1] 92.66504
# mean and sd for renewable energy
renewEnergy_mean_ts <- print(mean(renewable_energy_ts[,3]))</pre>
## [1] 395.7213
renewEnergy_stDev_ts <- print(sd(renewable_energy_ts[,3]))</pre>
## [1] 137.7952
# mean and sd for hydroelectric
Hydro_mean_ts <- print(mean(renewable_energy_ts[,4]))</pre>
## [1] 79.73071
Hydro_stDev_ts <- print(sd(renewable_energy_ts[,4]))</pre>
## [1] 14.14734
```

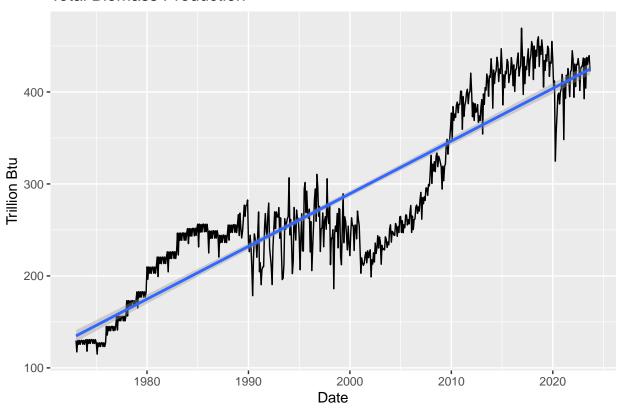
#### Question 4

Display and interpret the time series plot for each of these variables. Try to make your plot as informative as possible by writing titles, labels, etc. For each plot add a horizontal line at the mean of each series in a different color.

```
# plotting Total Biomass Production
ggplot(renewable_energy_sub,aes(x=Date,y=Total.Biomass.Energy.Production))+
    geom_line(color="black")+
    geom_smooth(method="lm")+
    labs(x="Date",y="Trillion Btu",title="Total Biomass Production")

## `geom_smooth()` using formula = 'y ~ x'
```

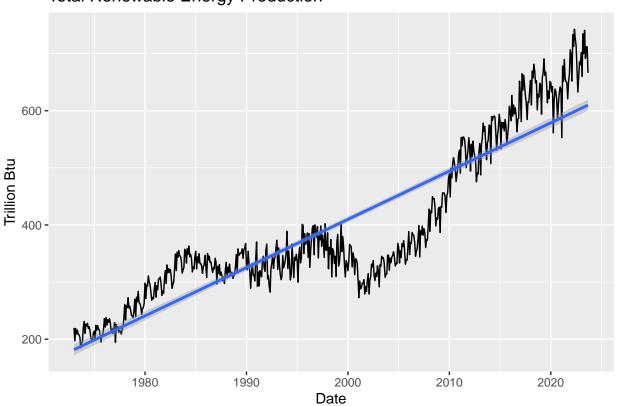
### **Total Biomass Production**



```
# plotting Total Renewable Energy Production
ggplot(renewable_energy_sub,aes(x=Date,y=Total.Renewable.Energy.Production))+
   geom_line(color="black")+
   geom_smooth(method="lm")+
   labs(x="Date",y="Trillion Btu",title="Total Renewable Energy Production")
```

## `geom\_smooth()` using formula = 'y ~ x'

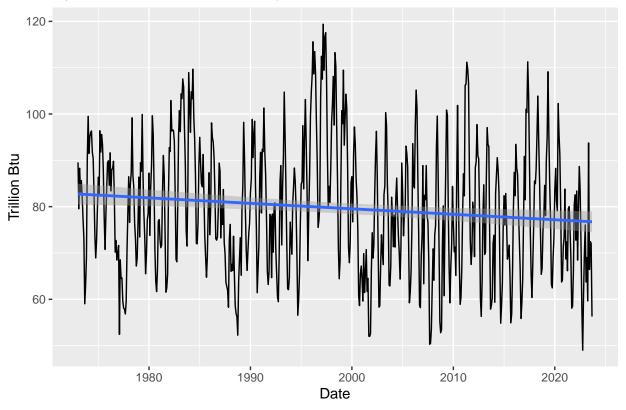
### **Total Renewable Energy Production**



```
# plotting Hydroelectric Power Consumption
ggplot(renewable_energy_sub,aes(x=Date,y=Hydroelectric.Power.Consumption))+
  geom_line(color="black")+
  geom_smooth(method="lm")+
  labs(x="Date",y="Trillion Btu",title="Hydroelectric Power Consumption")
```

## `geom\_smooth()` using formula = 'y ~ x'





Interpretation of Time Series Plots > Total Biomass Production: The plot shows an upward trend in production over time. We can see this from the highly positive slope of the trend line in blue. There also seems to be some seasonanality in the plot as similar cyclical patterns seem to repeat.

Total Renewable Energy Production: Similarly to biomass production, there appears to be a positive trend in renewable energy production over time. The plot is very similar to that of the Biomass plot, which is unsurprising given the increasing demand alternatives to fossil energy. Like above, there seems to be some seasonality.

Hydroelectric Power Consumption: There is a slight downward trend in hydroelectric power consumption over time. This is interesting and stands in constrast to Biomass and Renewables production. This downward trend could be because consumers are switching to alternative forms of renewable energy as production / availability increases.

### Question 5

Compute the correlation between these three series. Are they significantly correlated? Explain your answer.

 ${\tt Total.Biomass.Energy.Production}$ 

```
## Total.Biomass.Energy.Production
                                                           1.0000000
## Total.Renewable.Energy.Production
                                                           0.97074621
## Hydroelectric.Power.Consumption
                                                          -0.09656318
##
                                     Total.Renewable.Energy.Production
## Total.Biomass.Energy.Production
                                                            0.970746212
## Total.Renewable.Energy.Production
                                                            1.000000000
## Hydroelectric.Power.Consumption
                                                           -0.001768629
##
                                     Hydroelectric.Power.Consumption
## Total.Biomass.Energy.Production
                                                         -0.096563177
                                                         -0.001768629
## Total.Renewable.Energy.Production
## Hydroelectric.Power.Consumption
                                                          1.00000000
```

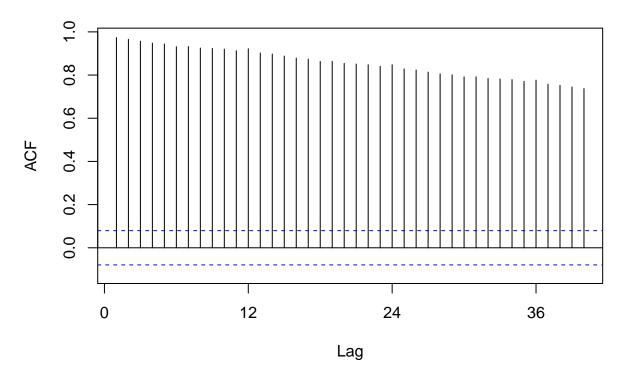
Answer: > It appears that biomass production and renewable energy production are highly correlated with a correlation coefficient of 0.97. This does not seem that surprising since both variables relate to the production of alternative forms of energy (non-fossil). Meanwhile, hydroelectric power consumption does not appear to be correlated with either biomass or renewable energy production based on the fact the correlation coefficients are > 0.1.

### Question 6

Compute the autocorrelation function from lag 1 up to lag 40 for these three variables. What can you say about these plots? Do the three of them have the same behavior?

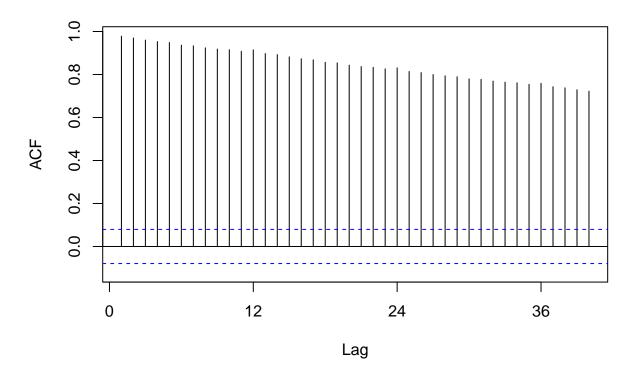
BiomassProd\_acf <- Acf(renewable\_energy\_ts[,2],lag.max=40)</pre>

### Series renewable\_energy\_ts[, 2]



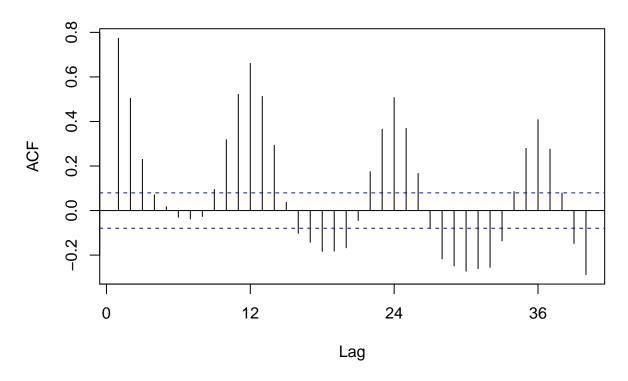
RenewablesProd\_acf <- Acf(renewable\_energy\_ts[,3],lag.max=40)</pre>

# Series renewable\_energy\_ts[, 3]



HydroConsump\_acf <- Acf(renewable\_energy\_ts[,4],lag.max=40)</pre>

### Series renewable\_energy\_ts[, 4]



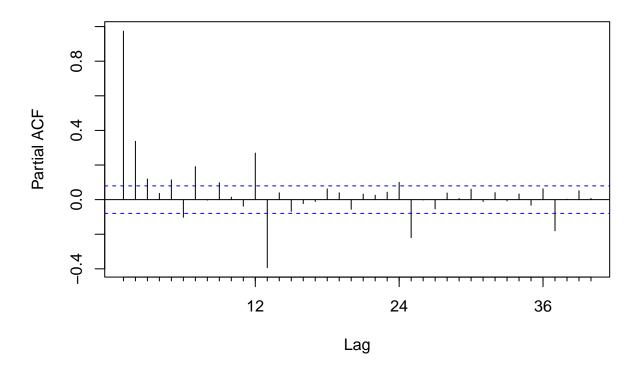
Answer: > The biomass and renewable energy ACF plots behave similarly,but the hydro power plot of ACF looks very different. The biomass and renewable energy plots show significant correlation within each dataset. ACF appears positive for all lags for these two time series. For hydro power, some autocorrelation is present, but the amplitudes don't appear as big compared to the first two time series, suggesting potentially less correlation between variables.

### Question 7

Compute the partial autocorrelation function from lag 1 to lag 40 for these three variables. How these plots differ from the ones in Q6?

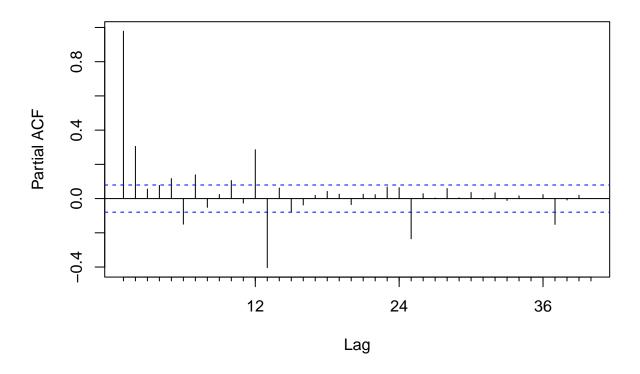
BiomassProd\_pacf=Pacf(renewable\_energy\_ts[,2],lag.max=40)

# Series renewable\_energy\_ts[, 2]



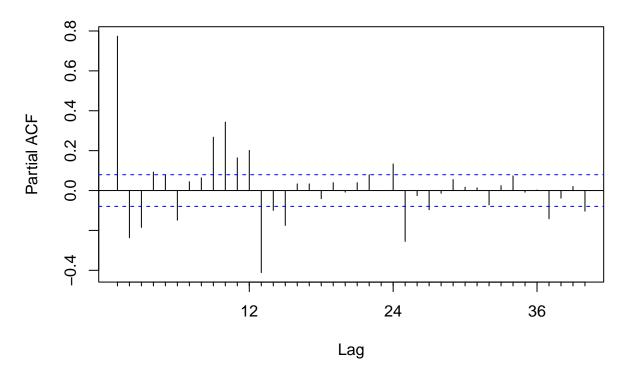
RenewablesProd\_pacf=Pacf(renewable\_energy\_ts[,3],lag.max=40)

# Series renewable\_energy\_ts[, 3]



HydroConsump\_pacf=Pacf(renewable\_energy\_ts[,4],lag.max=40)

## Series renewable\_energy\_ts[, 4]



Answer: > The PACF plots show us which lags are most significant within each time series. In other words, which instances within a specific variable are most correlated with each other. From these plots we should consider adding lags that breach the blue dotted line to our model as they may help us better explain trends / construct more accurate forecasts.