

AE 625 -Particle Methods in Fluid Flow  
Simulation  
Assignment 8: Report  
SPH Approximation of a function and it's  
Derivative

Aditi Taneja

$dx = 0.1$   
 $range = -1to1$   
 $hdx\_for\_cubic\_kernel = 0.7$   
 $hdx\_for\_gaussian\_kernel = 0.7$

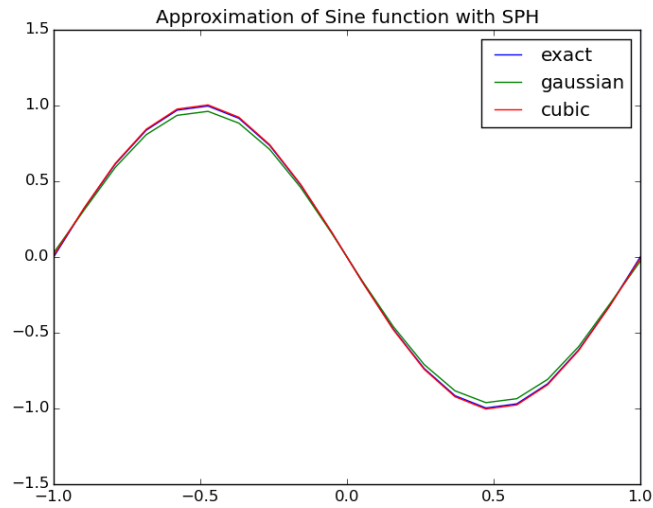


Figure 1: Approximation of Sine function with SPH (cubic and Gaussian kernel)

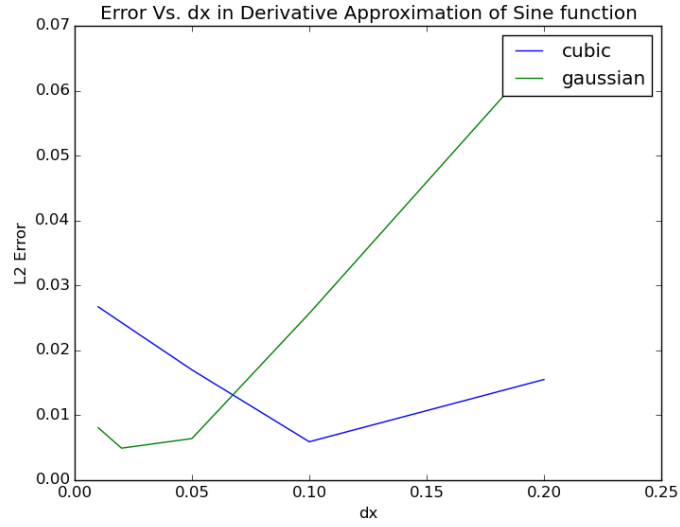


Figure 2: Variation of Error in approximation of sine function with dx(or number of points)

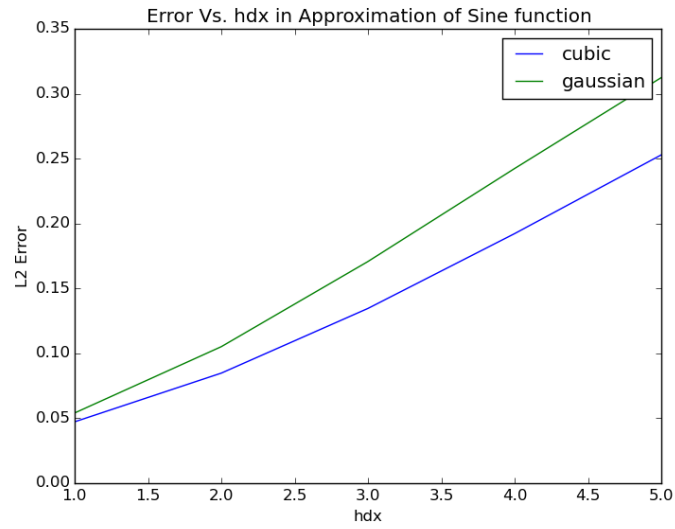


Figure 3: Variation of Error in approximation of sine function with hdx(or h)

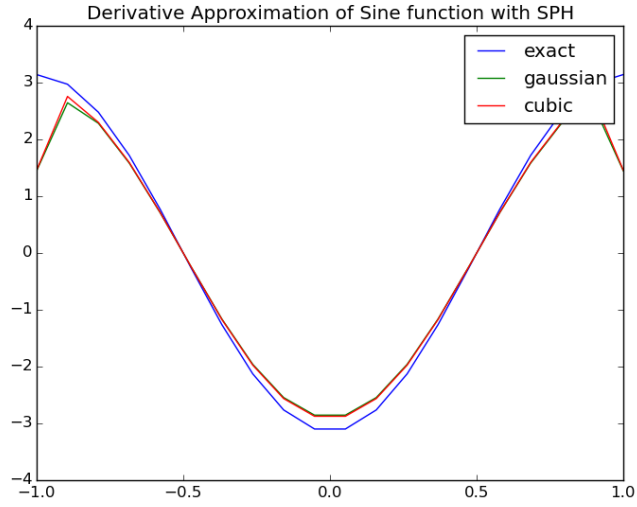


Figure 4: Approximation of derivative of Sine function with SPH (cubic and Gaussian kernel)

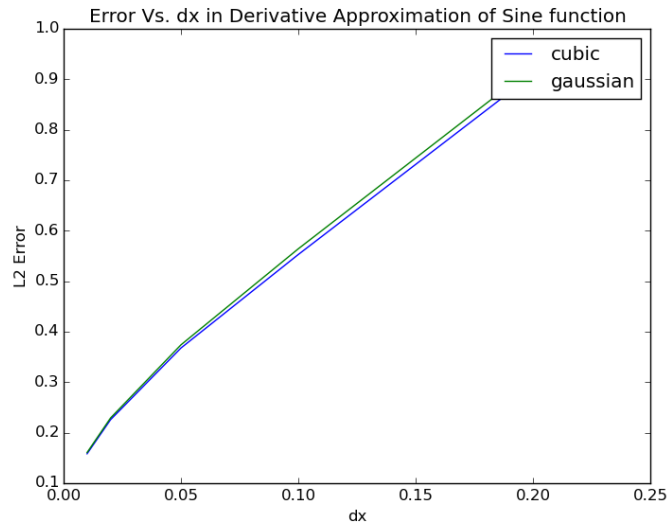


Figure 5: Variation of Error in approximation of derivative of sine function with dx(or number of points)

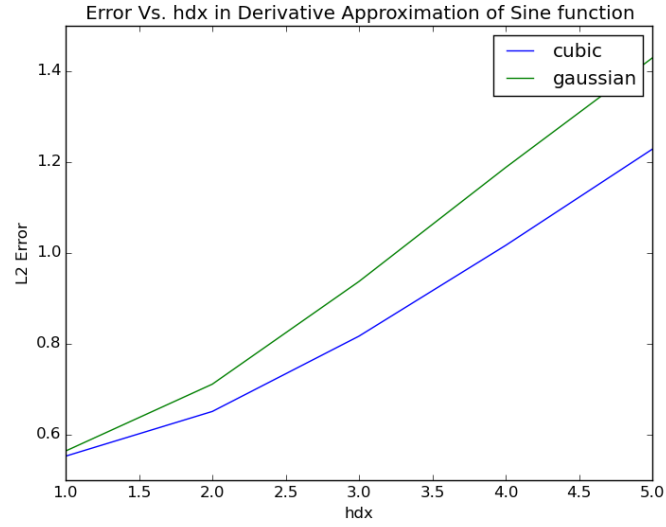


Figure 6: Variation of Error in approximation of derivative of sine function with hdx(or h)

#### Effect of Noise Addition

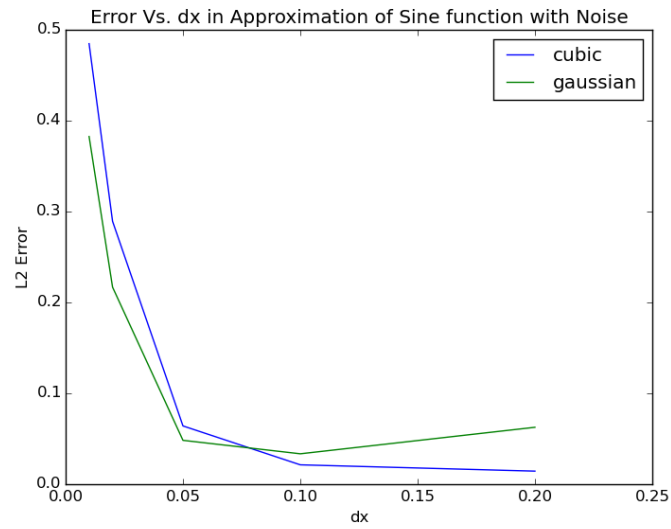


Figure 7: Variation of Error in approximation of sine function with dx(or number of points) with noise

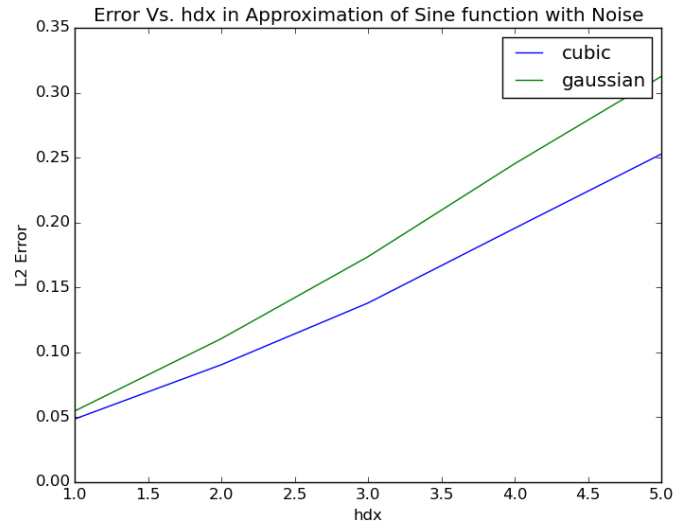


Figure 8: Variation of Error in approximation of sine function with  $hdx$ (or  $h$ ) with noise

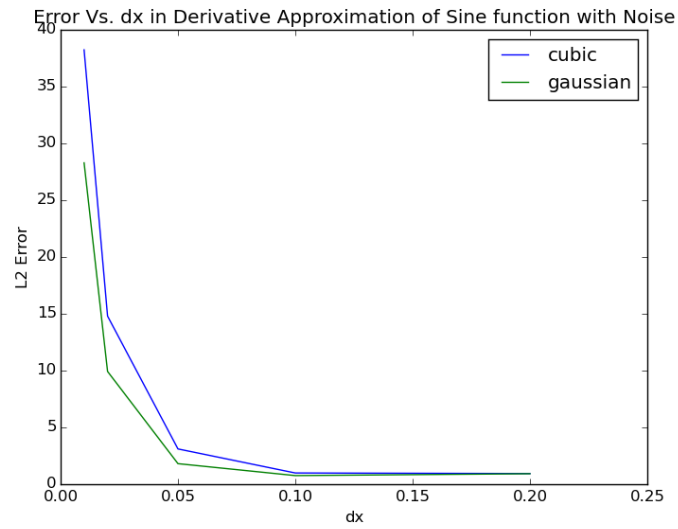


Figure 9: Variation of Error in approximation of derivative of sine function with  $dx$ (or number of points) with noise

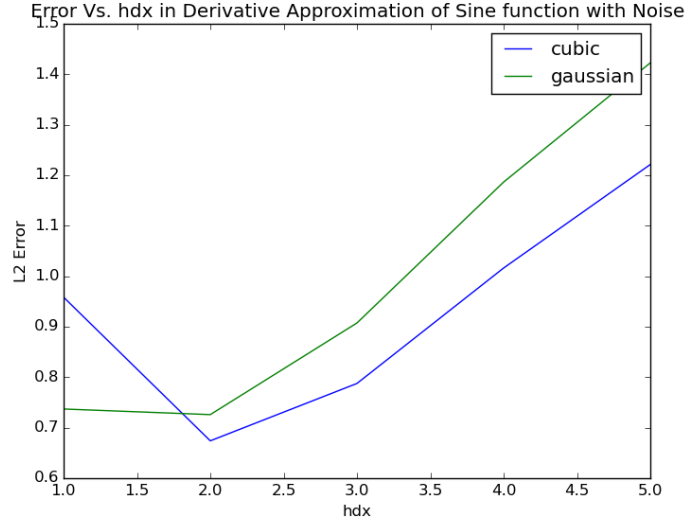


Figure 10: Variation of Error in approximation of derivative of sine function with  $hdx$ (or  $h$ ) with noise

Thus, from the above plots, it can be concluded that as the number of points in the domain are increased or  $dx$  is decreased, error decreases (for same  $hdx$ ) attains a minimum value and then increases. Also, with increase in  $hdx$  error increases. Noise addition in the particle position can lead to overall increase in error and disrupted plots.