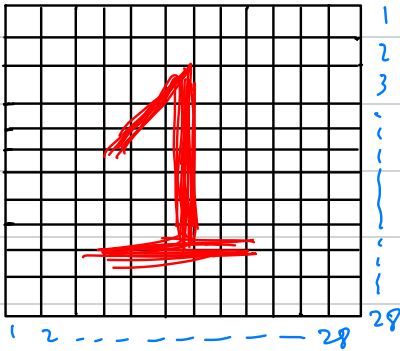


Neural Network : From Scratch

Digit Classifier : MNIST Dataset



28×28 → Pixels : Grayscale image

Total 70,000 samples

x_train → 60,000 sample

x_test → 10,000 sample.

$$\begin{aligned} \text{x_train} &= \overbrace{(60,000)}^{\text{no. of images}} \times \overbrace{(28 \times 28)}^{\text{pixel of an image}} \quad \# \text{shape} \\ \text{x_test} &= (10,000 \times 28 \times 28) \end{aligned}$$

The input of NN should be 1d tensor = vector.

$$\therefore (28, 28) \rightarrow (784)$$

$$\therefore \Rightarrow [60,000 \times 784] \text{ Shape.}$$

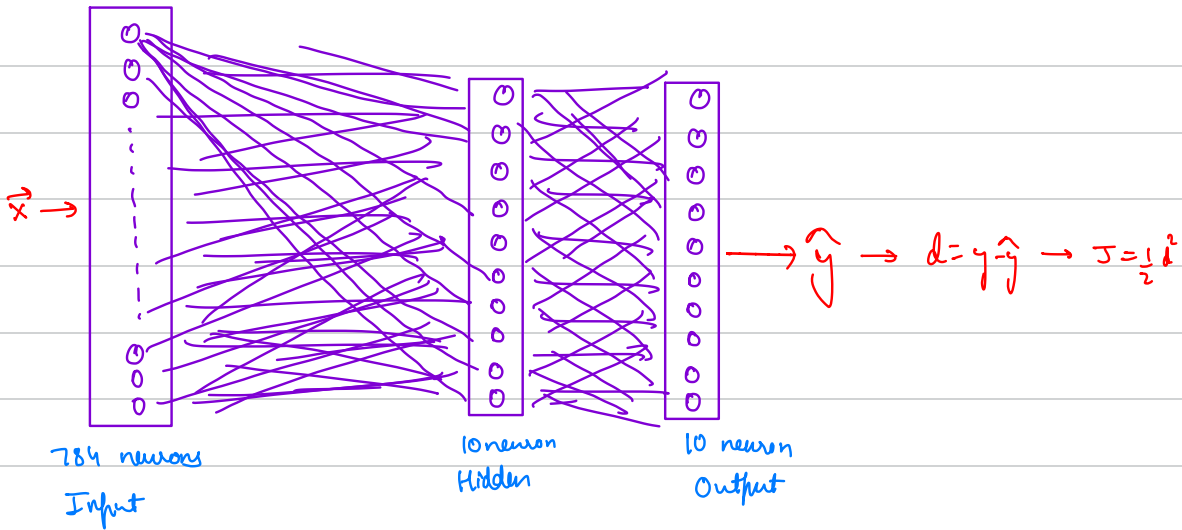
↓
R = each image

→ C = pixel in image.

$$\begin{bmatrix} 2 & 3 \\ 5 & 6 \\ 8 & 9 \end{bmatrix} \rightarrow [1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9]$$

then transpose.

$(784, 60000)$ $\rightarrow c = \text{each image.}$
 \downarrow
 $R = \text{pixel in img}$



$$w_1 = 10 \times 784$$

$$b_1 = 10, 1$$

$$w_2 = 10 \times 10$$

$$b_2 = 10, 1$$

$$\vec{w}_1 \cdot \vec{x} + \vec{b}_1 = \vec{z}_1$$

$$\vec{a}_1 = \text{Relu}(\vec{z}_1)$$

$$\vec{w}_2 \cdot \vec{a}_1 + \vec{b}_2 = \vec{z}_2$$

$$\vec{a}_2 = \text{Softmax}(\vec{z}_2)$$

$$dz_2 = a_2 - y$$

$$dw_2 = \frac{1}{m} \times dz_2 \times a_1(\tau)$$

$$db_2 = \frac{1}{m} dz_2$$

$$dz_1 = w_2 \cdot T \cdot dt + (dz_2) \times (z_1 > 0)$$

$$dw_1 = \frac{1}{m} \times dz_1 \times X \cdot T$$

$$db_1 = \frac{1}{m} (dz_1)$$