

Design and Analysis of Algorithms (Week1 Solution)

PCS-505

Note - You can find all the problem statements and their solutions on following link - [DAA Link](#)

Solution - 1

For *linear search*, we just need to scan the array from the beginning till the end, index 1 to index n , and check if the entry at that position equal to v or not. The pseudocode can be written as follows...

LINEAR-SEARCH (A, v)

```
1  for  $i = 1$  to  $A.length$ 
2      if  $A[i] == v$ 
3          return  $i$ 
4  return NIL
```

Solution - 2

A binary search divides a range of values into halves, and continues to narrow down the field of search until the unknown value is found. It is the classic example of a "divide and conquer" algorithm.

Iterative Approach

```
binarySearch(array, left, right, key):
    while left <= right:
        mid = left + (right - left) // 2
        if array[mid] == key:
            return mid
        elif array[mid] < key:
            left = mid + 1
        else:
            right = mid - 1
    return -1
```

Recursive Approach

```
binarySearch (array, left, right, key):
    if left <= right:
        mid = left + (right - left) // 2
        if array[mid] == key:
            return mid
        elif array[mid] < key:
            return binarySearch(array, mid + 1, right, key)
        else:
            return binarySearch(array, left, mid-1, key)
    else:
        return -1
```

Solution - 3

For an array `arr[]` of size `n` and block (to be jumped) size `m`, search at the indexes `arr[0]`, `arr[m]`, `arr[2m]`.....`arr[km]` and so on. Once the interval **`(arr[km] < key < arr[(k+1)m])`** is found, perform a linear search operation from the index **`km`** to find the element **`key`**.

jumpSearch(array, n, key):

```
jump = math.sqrt(n)
steps = jump
prev = 0
while array[int(min(steps, n)-1)] < key:
    prev = steps
    steps += jump
    if prev >= n:
        return -1

while array[int(prev)] < key:
    prev += 1
    if prev == min(steps, n):
        return -1

if array[int(prev)] == key:
    return prev

return -1
```

Solution - 4

For an array `arr[n]`, search at the indexes **`arr[0]`, `arr[1]`, `arr[2]`, `arr[4]`,.....,`arr[2k]`** and so on. Once the interval **`(arr[2k] < key < arr[2(k+1)])`** is found, perform a linear search or binary search operation from the index `2k` to find the element `key`.

exponentialSearch(array, n, key):

```
if array[0] == key:
    return 0
i = 1
while i < n and array[i] <= key:
    i = i * 2
return linearSearch (array, int(i/2), n, key)
return binarySearch(array, int(i/2), min(i, n-1), key)
```