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# What is Backward Elimination?

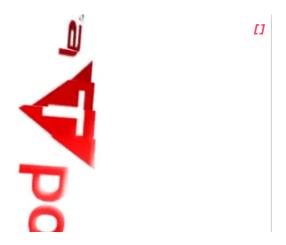
Backward elimination is a feature selection technique while building a machine learning model. It is used to remove those features that do not have a significant effect on the dependent variable or prediction of output. There are various ways to build a model in Machine Learning, which are:

- 1. All-in
- 2. Backward Elimination
- 3. Forward Selection
- 4. Bidirectional Elimination
- 5. Score Comparison

Above are the possible methods for building the model in Machine learning, but we will only use here the Backward Elimination process as it is the fastest method.

# Steps of Backward Elimination

Below are some main steps which are used to apply backward elimination process:



- **Step-1:** Firstly, We need to select a significance level to stay in the model. (SL=0.05)
- **Step-2:** Fit the complete model with all possible predictors/independent variables.
- Step-3: Choose the predictor which has the highest P-value, such that.
  - a. If P-value >SL, go to step 4.
  - b. Else Finish, and Our model is ready.
- Step-4: Remove that predictor.

**Step-5:** Rebuild and fit the model with the remaining variables.

# Need for Backward Elimination: An optimal Multiple Linear Regression model:

In the previous chapter, we discussed and successfully created our Multiple Linear Regression model, where we took **4 independent variables** (**R&D spend**, **Administration spend**, **Marketing spend**, **and state (dummy variables)) and one dependent variable (<b>Profit**). But that model is not optimal, as we have included all the independent variables and do not know which independent model is most affecting and which one is the least affecting for the prediction.

Unnecessary features increase the complexity of the model. Hence it is good to have only the most significant features and keep our model simple to get the better result.

So, in order to optimize the performance of the model, we will use the Backward Elimination method. This process is used to optimize the performance of the MLR model as it will only include the most affecting feature and remove the least affecting feature. Let's start to apply it to our MLR model.

# Steps for Backward Elimination method:

We will use the same model which we build in the previous chapter of MLR. Below is the complete code for it:

```
# import numpy as nm
import matplotlib.pyplot as mtp
import pandas as pd

#importing datasets
data_set= pd.read_csv('50_CompList.csv')

#Extracting Independent and dependent Variable
x= data_set.iloc[:, :-1].values
y= data_set.iloc[:, 4].values

#Catgorical data
from sklearn.preprocessing import LabelEncoder, OneHotEncoder
```

```
labelencoder_x= LabelEncoder()
x[:, 3] = labelencoder_x.fit_transform(x[:,3])
onehotencoder= OneHotEncoder(categorical_features= [3])
x = onehotencoder.fit_transform(x).toarray()
#Avoiding the dummy variable trap:
x = x[:, 1:]
# Splitting the dataset into training and test set.
from sklearn.model_selection import train_test_split
x_train, x_test, y_train, y_test= train_test_split(x, y, test_size= 0.2, random_state=0)
#Fitting the MLR model to the training set:
from sklearn.linear_model import LinearRegression
regressor= LinearRegression()
regressor.fit(x_train, y_train)
#Predicting the Test set result;
y_pred= regressor.predict(x_test)
#Checking the score
print('Train Score: ', regressor.score(x_train, y_train))
print('Test Score: ', regressor.score(x_test, y_test))
```

From the above code, we got training and test set result as:

Train Score: 0.9501847627493607 Test Score: 0.9347068473282446

The difference between both scores is 0.0154.

Note: On the basis of this score, we will estimate the effect of features on our model after using the Backward elimination process.

### **Step: 1- Preparation of Backward Elimination:**

• **Importing the library:** Firstly, we need to import the **statsmodels.formula.api** library, which is used for the estimation of various statistical models such as OLS(Ordinary Least Square). Below is the code for it:

import statsmodels.api as smf

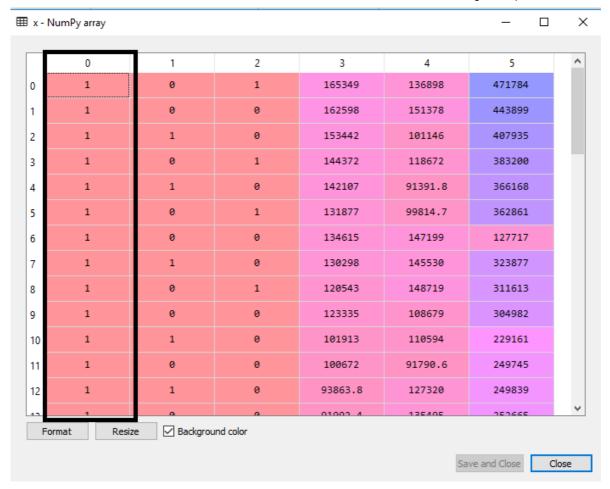
• Adding a column in matrix of features: As we can check in our MLR equation (a), there is one constant term  $b_0$ , but this term is not present in our matrix of features, so we need to add it manually. We will add a column having values  $x_0 = 1$  associated with the constant term  $b_0$ .

To add this, we will use **append** function of **Numpy** library (nm which we have already imported into our code), and will assign a value of 1. Below is the code for it.

```
x = nm.append(arr = nm.ones((50,1)).astype(int), values=x, axis=1)
```

Here we have used axis =1, as we wanted to add a column. For adding a row, we can use axis =0.

**Output:** By executing the above line of code, a new column will be added into our matrix of features, which will have all values equal to 1. We can check it by clicking on the x dataset under the variable explorer option.



As we can see in the above output image, the first column is added successfully, which corresponds to the constant term of the MLR equation.

### Step: 2:

- Now, we are actually going to apply a backward elimination process. Firstly we will create a new feature vector **x\_opt**, which will only contain a set of independent features that are significantly affecting the dependent variable.
- Next, as per the Backward Elimination process, we need to choose a significant level(0.5), and then need to fit the model with all possible predictors. So for fitting the model, we will create a regressor\_OLS object of new class OLS of statsmodels library. Then we will fit it by using the fit() method.
- Next we need p-value to compare with SL value, so for this we will use summary() method to get the summary table of all the values. Below is the code for it:

```
x_opt=x [:, [0,1,2,3,4,5]]
regressor_OLS=sm.OLS(endog = y, exog=x_opt).fit()
regressor_OLS.summary()
```

Output: By executing the above lines of code, we will get a summary table. Consider the below image:

		ssion Resul ======				
Dep. Variable:	у				0.951	
Model:		Adj. R-s			0.945	
Method:	Least Squares				169.9	
Date:	Mon, 14 Oct 2019			c):	1.34e-27	
Time:	17:49:58	Log-Like	lihood:		-525.38	
No. Observations:	50				1063.	
Of Residuals:	44				1074.	
Of Model:	5					
Covariance Type:	nonrobust					
coe	f std err	t	P> t	[0.025	0.975]	
const 5.013e+0	4 6884.820	7.281	0.000	3.62e+04	6.4e+04	
x1 198.788	8 3371.007	0.059	0.953	-6595.030	6992.607	
x2 -41.887	0 3256.039	-0.013	0.990	-6604.003	6520.229	
x3 0.806	0 0.046	17.369	0.000	0.712	0.900	
x4 -0.027	0 0.052	-0.517	0.608	-0.132	0.078	
x5 0.027	0 0.017	1.574	0.123	-0.008	0.062	
	14.782		atson:		1.283	
Prob(Omnibus):	0.001	Jarque-B	era (JB)	:	21.266	
		Prob(JB)			2.41e-05	
(urtosis:	5.572				1.45e+06	
Omnibus:	14.782 0.001 -0.948 5.572 	Durbin-W Jarque-B Prob(JB) Cond. No ovariance m 45e+06. Thi	atson: era (JB) : . ======= atrix of s might	the errors	1.283 21.266 2.41e-05 1.45e+06	S

In the above image, we can clearly see the p-values of all the variables. Here x1, x2 are dummy variables, x3 is R&D spend, x4 is Administration spend, and x5 is Marketing spend.

From the table, we will choose the highest p-value, which is for x1=0.953 Now, we have the highest p-value which is greater than the SL value, so will remove the x1 variable (dummy variable) from the table and will refit the model. Below is the code for it:

```
x_opt=x[:, [0,2,3,4,5]]
regressor_OLS=sm.OLS(endog = y, exog=x_opt).fit()
regressor_OLS.summary()
```

```
'statsmodels.iolib.summary.Summary'>
                      OLS Regression Results
  ______
                           y R-squared:
OLS Adj. R-squared:
Dep. Variable:
                                                            0.951
      OLS AUJ. N-3900. --

Least Squares F-statistic:

Mon, 14 Oct 2019 Prob (F-statistic):

18:03:48 Log-Likelihood:

AIC:
Model:
                                                            0.946
                                                            217.2
Method:
                                                         8.50e-29
Date:
No. Observations:
                                                          -525.38
                                                            1061.
Of Residuals:
                             45 BIC:
                                                             1070.
of Model:
                             4
Covariance Type:
                      nonrobust
______
                                        P>|t| [0.025 0.975
             coef std err
const 5.018e+04 6747.623 7.437
x1 -136.5042 2801.719 -0.049
                                       0.000
0.961
                                               3.66e+04 6.38e+04
                                               -5779.456 5506.447
         0.8059 0.046 17.571
-0.0269 0.052 -0.521
0.0271 0.017 1.625
                                                 0.714 0.898
-0.131 0.077
-0.007 0.061
                                       0.000
0.605
x2
к3
                                        0.111
_____
Omnibus:
Prob(Omnibus):
Skew:
Kurtosis:
                        14.892 Durbin-Watson:
                         0.001 Jarque-Bera (JB):
                                                           21.665
Skew:
                         -0.949 Prob(JB):
                                                         1.97e-05
Kurtosis:
                         5.608 Cond. No.
                                                          1.43e+06
Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
[2] The condition number is large, 1.43e+06. This might indicate that there are
strong multicollinearity or other numerical problems.
```

As we can see in the output image, now five variables remain. In these variables, the highest p-value is 0.961. So we will remove it in the next iteration.

• Now the next highest value is 0.961 for x1 variable, which is another dummy variable. So we will remove it and refit the model. Below is the code for it:

```
x_opt= x[:, [0,3,4,5]]
regressor_OLS=sm.OLS(endog = y, exog=x_opt).fit()
regressor_OLS.summary()
```

```
Out[12]:
<class 'statsmodels.iolib.summary.Summary'>
                        OLS Regression Results
.......
Dep. Variable:
                             y R-squared:
Model:
                             OLS Adj. R-squared:
                                                               0.948
Method:
Date:
                   Least Squares F-statistic:
Non, 14 Oct 2019 Prob (F-statistic):
18:08:41 Log-Likelihood:
                  Least Squares
                                                                296.0
                Mon, 14 Oct 2019
                                                            4.53e-30
Time:
                                                             -525.39
                              50 AIC:
46 BIC:
No. Observations:
                                                                1059
Df Residuals:
                                                                1066.
Df Model:
                               3
Covariance Type:
                       nonrobust
_____
            coef std err
                                           P>|t|
                                                   [0.025 0.975]
const 5.012e+04 6572.353 7.626
x1 0.8057 0.045 17.846
x2 -0.0268 0.051 -0.526
x3 0.0272 0.016 1.655
                                                  3.69e+04 6.34e+04
0.715 0.897
                                          0.000
                                                    0.715 0.897
-0.130 0.076
                                          0.000
                                          0.602
                                          0.105
                                                    -0.006
                                                               0.060
_____
                                                   _____
Omnibus:
                         14.838 Durbin-Watson:
                                                               1.282
Prob(Omnibus):
                           0.001 Jarque-Bera (JB):
                                                               21.442
Skew:
                           -0.949
                                  Prob(JB):
                                                             2.21e-05
                          5.586 Cond. No.
Kurtosis:
                                                             1.40e+06
[1] Standard Errors assume that the covariance matrix of the errors is correctly specifi
[2] The condition number is large, 1.4e+06. This might indicate that there are
strong multicollinearity or other numerical problems.
```

In the above output image, we can see the dummy variable(x2) has been removed. And the next highest value is .602, which is still greater than .5, so we need to remove it.

• Now we will remove the Admin spend which is having .602 p-value and again refit the model.

```
x_opt=x[:, [0,3,5]]
regressor_OLS=sm.OLS(endog = y, exog=x_opt).fit()
regressor_OLS.summary()
```

```
Jut|13|
<class 'statsmodels.iolib.summary.Summary'>
                      OLS Regression Results
                            y R-squared:
OLS Adj. R-squared:
Dep. Variable:
                                                             0.950
Model:
                                                             0.948
       Least Squares F-statistic:
Method:
                                                             450.8
                                Prob (F-statistic):
Log-Likelihood:
               Mon, 14 Oct 2019
Date:
                                                          2.16e-31
                 18:13:46
No. Observations:
                             50 AIC:
                                                             1057.
Of Residuals:
                             47
                                 BIC:
                                                              1063.
Of Model:
                              2
Covariance Type:
                      nonrobust
             coef std err
                                         P>|t|
                                                  [0.025 0.975]
const 4.698e+04 2689.933 17.464
x1 0.7966 0.041 19.266
x2 0.0299 0.016 1.927
                                         0.000
                                                 4.16e+04 5.24e+04
                                         0.000
                                                         0.880
                                                   0.713
                                         0.060
                                                   -0.001
                                                             0.061
-----
Omnibus:
                         14.677 Durbin-Watson:
                                                             1.257
Prob(Omnibus):
                          0.001
                                 Jarque-Bera (JB):
                                                             21.161
                          -0.939 Prob(JB):
Skew:
                                                          2.54e-05
                          5.575 Cond. No.
(urtosis:
------
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
  The condition number is large, 5.32e+05. This might indicate that there are
trong multicollinearity or other numerical problems
```

As we can see in the above output image, the variable (Admin spend) has been removed. But still, there is one variable left, which is **marketing spend** as it has a high p-value **(0.60)**. So we need to remove it.

• Finally, we will remove one more variable, which has .60 p-value for marketing spend, which is more than a significant level.

Below is the code for it:

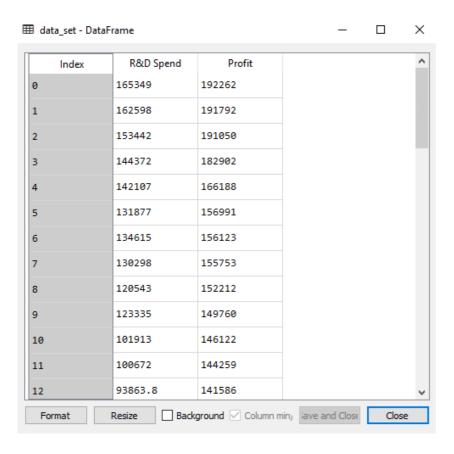
```
x_opt=x[:, [0,3]]
regressor_OLS=sm.OLS(endog = y, exog=x_opt).fit()
regressor_OLS.summary()
```

```
Out[14]:
class 'statsmodels.iolib.summary.Summary'>
                     OLS Regression Results
------
Dep. Variable:
                           y R-squared:
                           OLS Adj. R-squared:
                 Least Squares
Method:
                                F-statistic:
                                                           849.8
                                Prob (F-statistic):
              Mon, 14 Oct 2019
Date:
                                                        3.50e-32
Time:
                     18:16:40 Log-Likelihood:
                                                         -527.44
No. Observations:
                                AIC:
                            50
                                                           1059.
Of Residuals:
                            48
                                BIC:
                                                            1063.
of Model:
                            1
Covariance Type:
                     nonrobust
            coef std err
                                        P>|t|
                                               [0.025 0.975]
                           19.320
29.151
                                               4.39e+04 5.41e+04
     4.903e+04 2537.897
                                        0.000
onst
          0.8543
                   0.029
                                        0.000
                                                 0.795
                                                           0.913
_____
Omnibus:
                       13.727 Durbin-Watson:
                                                           1.116
rob(Omnibus):
                         0.001
                                Jarque-Bera (JB):
                                                           18.536
                        -0.911 Prob(JB):
                                                        9.44e-05
kew:
(urtosis:
                         5.361 Cond. No.
                                                         1.65e+05
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified
[2] The condition number is large, 1.65e+05. This might indicate that there are
strong multicollinearity or other numerical problems.
```

As we can see in the above output image, only two variables are left. So only the **R&D independent variable** is a significant variable for the prediction. So we can now predict efficiently using this variable.

# Estimating the performance:

In the previous topic, we have calculated the train and test score of the model when we have used all the features variables. Now we will check the score with only one feature variable (R&D spend). Our dataset now looks like:



### Below is the code for Building Multiple Linear Regression model by only using R&D spend:

```
# importing libraries
import numpy as nm
import matplotlib.pyplot as mtp
import pandas as pd
#importing datasets
data_set= pd.read_csv('50_CompList1.csv')
#Extracting Independent and dependent Variable
x_BE= data_set.iloc[:, :-1].values
y_BE= data_set.iloc[:, 1].values
# Splitting the dataset into training and test set.
from sklearn.model_selection import train_test_split
x_BE_train, x_BE_test, y_BE_train, y_BE_test= train_test_split(x_BE, y_BE, test_size= 0.2, random_state=0)
#Fitting the MLR model to the training set:
from sklearn.linear_model import LinearRegression
regressor= LinearRegression()
regressor.fit(nm.array(x_BE_train).reshape(-1,1), y_BE_train)
#Predicting the Test set result;
y_pred= regressor.predict(x_BE_test)
#Cheking the score
print('Train Score: ', regressor.score(x_BE_train, y_BE_train))
print('Test Score: ', regressor.score(x_BE_test, y_BE_test))
```

#### **Output:**

After executing the above code, we will get the Training and test scores as:

Train Score: 0.9449589778363044 Test Score: 0.9464587607787219

As we can see, the training score is 94% accurate, and the test score is also 94% accurate. The difference between both scores is **.00149**. This score is very much close to the previous score, i.e., **0.0154**, where we have included all the variables.

We got this result by using one independent variable (R&D spend) only instead of four variables. Hence, now, our model is simple and accurate.



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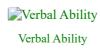


Python Design Patterns

# Preparation



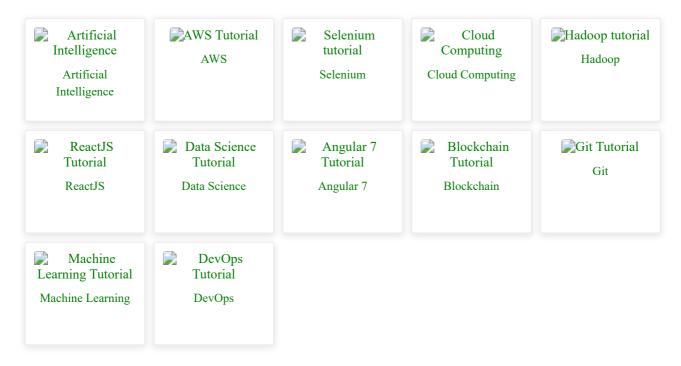








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