

$$\min_{x \in \mathbb{R}^+} f(x) = - \sum_{i,j} w_{ij} x_{ij} \quad (f(x) \Rightarrow \text{Expected Value})$$

$$\text{s.t.} \quad g_1(x) = \sum x_i c_i - 81.5 \leq 0$$

$$h_1(x) = \sum x_i - 11 = 0$$

$$h_2(x) = \sum x_{i,1} - 1 = 0$$

$$g_2(x) = \sum x_{i,2} - 5 \leq 0$$

$$g_3(x) = -\sum x_{i,2} + 3 \leq 0$$

$$g_4(x) = \sum x_{i,3} - 5 \leq 0$$

$$g_5(x) = -\sum x_{i,3} + 2 \leq 0$$

$$g_6(x) = \sum x_{i,4} - 3 \leq 0$$

$$g_7(x) = -\sum x_{i,4} + 1 \leq 0$$

$x_i \Rightarrow$ No. of players/team
 $w_i \Rightarrow$ team level projection
 \Rightarrow position level projection

$c_i \Rightarrow$ team level cost

$$3 \leq \text{DEF} \leq 5 \quad | \quad 2$$

$$1 \leq \text{FWD} \leq 3 \quad | \quad 4$$

$$2 \leq \text{MID} \leq 5 \quad | \quad 3$$

$$\text{GK} = 1 \quad | \quad 1$$

2 DEF \rightarrow 8m

1 GK \rightarrow 4m

1 FWD/MID \rightarrow 4.5

1. bench cost

Second variable
to make this NLP

80% - starting

15% - bench

5% - not in squad

m. - avg. min

$x_{i,j}$

$$x_{Min} = 0.8x_M + 0.15x_B + \frac{3}{8}$$

Change this to 2-outcomes

plays \Rightarrow 90% doesn't play 10%

Assuming every player in XI

has p % chance of playing,

$$EV = (p) \sum_{i,j} w_{ij} x_{ij} + (1-p) B_1 + (1-p)^2 B_2 + (1-p)^3 B_3$$

| Team | # GK / team | # DEF / team | # MID / team | # FWD / team |
|------|-------------|--------------|--------------|--------------|
| 1 | | | | |
| 2 | | | | |
| 3 | | | | |
| . | | | | |
| . | | | | |
| . | | | | |
| . | | | | |
| 20 | | | | |

$$\min_{x \in \mathbb{R}} f(x_c) = \sum_{i,j} w_{i,j} x_{i,j} c_{i,j}$$

player $\rightarrow w_{i,j}$
 $p \rightarrow p \cdot \frac{1}{x_{min}}$

$w_{i,j} \Rightarrow$ team level proj.

$c_{i,j} \Rightarrow$ bench / starting x_i split

$x_{i,j} \Rightarrow$

$p \Rightarrow$ probability vector

s.t. $g_1(x_c) = \sum x_i c_i - 100 \leq 0$

$$h_1(x) = \sum_i \sum_j x_{i,j} - 15 = 0 \Rightarrow \text{inactive}$$

$$h_2(x) = \sum x_{i,1} - 2 = 0$$

$$h_3(x) = \sum_{i=1}^{15} x_{i,2} - 5 = 0$$

$$h_4(x) = \sum_{i=1}^{15} x_{i,3} - 5 \leq 0$$

$$h_5(x) = \sum_{i=1}^{15} x_{i,4} - 3 \leq 0$$

$$g_2(x) = \sum_{i=1}^{11} x_{i,2} - 5 \leq 0$$

$$g_3(x) = -\sum_{i=1}^{11} x_{i,2} + 3 \leq 0$$

$$g_4(x) = \sum_{i=1}^{11} x_{i,3} - 5 \leq 0$$

$$g_5(x) = -\sum_{i=1}^{11} x_{i,3} + 2 \leq 0$$

$$g_6(x) = \sum_{i=1}^{11} x_{i,4} - 3 \leq 0$$

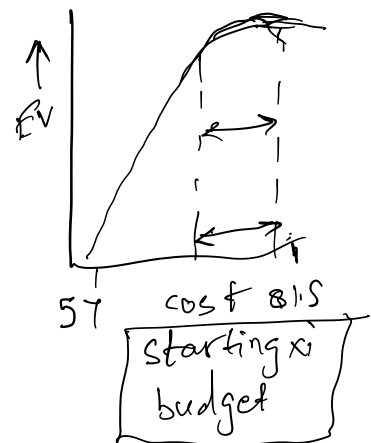
$$g_7(x) = -\sum_{i=1}^{11} x_{i,4} + 1 \leq 0$$

$$g_8(x) = \sum x_{1,j} \leq 3$$

\vdots

$$g_{27}(x) = \sum x_{20,j} \leq 3$$

cost X $p \leftarrow$
 cost 4 \leftarrow



- Introduction \Rightarrow (JK)

(FPL - 30s)
(EV model)

Problem statement \Rightarrow
(problem statement)

10pm
10/11

\rightarrow objective fn. (AJ)
(w matrix)

\rightarrow x & $c \rightarrow$ 2 variables NLP (Jw)

\rightarrow constraints (AR)