Social network Graph Link Prediction - Facebook Challenge

```
In [1]:
        #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xqboost: pip3 install xqboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import HDFStore,DataFrame
        from pandas import read hdf
        from scipy.sparse.linalg import svds, eigs
        import gc
        from tqdm import tqdm
```

1. Reading Data

Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree: 4.2399

Average in degree: 4.2399
Average out degree: 4.2399

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = rac{|X \cap Y|}{|X \cup Y|}$$

```
In [0]: #one test case
print(jaccard_for_followees(273084,1505602))
```

0.0

```
In [0]: #node 1635354 not in graph
print(jaccard_for_followees(273084,1505602))
```

0.0

```
In [0]: #for followers
        def jaccard_for_followers(a,b):
                 if len(set(train graph.predecessors(a))) == 0 | len(set(g.predecessor
        s(b))) == 0:
                    return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(train gra
        ph.predecessors(b))))/\
                                          (len(set(train graph.predecessors(a)).union(s
        et(train_graph.predecessors(b)))))
                return sim
            except:
                return 0
In [0]: print(jaccard_for_followers(273084,470294))
In [0]: #node 1635354 not in graph
        print(jaccard for followees(669354,1635354))
        0
```

2.2 Cosine distance

$$CosineDistance = \frac{|X \cap Y|}{|X| \cdot |Y|}$$

```
In [0]: #for followees
        def cosine for followees(a,b):
                if len(set(train graph.successors(a))) == 0 | len(set(train graph.suc
        cessors(b))) == 0:
                     return 0
                 sim = (len(set(train_graph.successors(a)).intersection(set(train_graph)
        .successors(b))))/\
                                             (math.sqrt(len(set(train_graph.successors(
        a)))*len((set(train_graph.successors(b))))))
                 return sim
            except:
                return 0
In [0]:
        print(cosine_for_followees(273084,1505602))
        0.0
In [0]: print(cosine_for_followees(273084,1635354))
        0
```

```
In [0]:
        def cosine for followers(a,b):
            try:
                 if len(set(train graph.predecessors(a))) == 0 | len(set(train graph.p
        redecessors(b))) == 0:
                     return 0
                 sim = (len(set(train graph.predecessors(a)).intersection(set(train gra
        ph.predecessors(b))))/\
                                              (math.sqrt(len(set(train graph.predecesso
        rs(a))))*(len(set(train_graph.predecessors(b)))))
                 return sim
            except:
                 return 0
In [0]: print(cosine for followers(2,470294))
        0.02886751345948129
In [0]: print(cosine for followers(669354,1635354))
        0
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-

- <u>1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html</u> (https://networkx.github.io/documentation/networkx-
- 1.10/reference/generated/networkx.algorithms.link analysis.pagerank_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

```
In [0]: if not os.path.isfile('data/fea sample/page rank.p'):
            pr = nx.pagerank(train_graph, alpha=0.85)
            pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
        else:
            pr = pickle.load(open('data/fea sample/page rank.p','rb'))
In [0]: | print('min',pr[min(pr, key=pr.get)])
        print('max',pr[max(pr, key=pr.get)])
        print('mean',float(sum(pr.values())) / len(pr))
        min 1.6556497245737814e-07
        max 2.7098251341935827e-05
        mean 5.615699699389075e-07
In [0]: #for imputing to nodes which are not there in Train data
        mean pr = float(sum(pr.values())) / len(pr)
        print(mean_pr)
        5.615699699389075e-07
```

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [0]: | #if has direct edge then deleting that edge and calculating shortest path
        def compute shortest path length(a,b):
            p = -1
            try:
                 if train_graph.has_edge(a,b):
                     train graph.remove edge(a,b)
                     p= nx.shortest_path_length(train_graph,source=a,target=b)
                     train graph.add edge(a,b)
                 else:
                     p= nx.shortest_path_length(train_graph,source=a,target=b)
                 return p
            except:
                 return -1
```

```
#testing
In [0]:
        compute_shortest_path_length(77697, 826021)
```

Out[0]: 10

```
In [0]: #testing
compute_shortest_path_length(669354,1635354)
Out[0]: -1
```

4.2 Checking for same community

```
In [0]:
         #getting weekly connected edges from graph
         wcc=list(nx.weakly_connected_components(train_graph))
         def belongs_to_same_wcc(a,b):
             index = []
             if train_graph.has_edge(b,a):
                 return 1
             if train_graph.has_edge(a,b):
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if (b in index):
                         train graph.remove edge(a,b)
                         if compute_shortest_path_length(a,b)==-1:
                             train_graph.add_edge(a,b)
                             return 0
                         else:
                             train_graph.add_edge(a,b)
                             return 1
                     else:
                         return 0
             else:
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if(b in index):
                         return 1
                     else:
                         return 0
In [0]: belongs_to_same_wcc(861, 1659750)
Out[0]: 0
In [0]: belongs to same wcc(669354,1635354)
Out[0]: 0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x,y) = \sum_{u \in N(x) \cap N(y)}^{} rac{1}{log(|N(u)|)}$$

```
In [0]: #adar index
         def calc_adar_in(a,b):
             sum=0
             try:
                 n=list(set(train_graph.successors(a)).intersection(set(train_graph.suc
         cessors(b))))
                 if len(n)!=0:
                     for i in n:
                         sum=sum+(1/np.log10(len(list(train_graph.predecessors(i)))))
                 else:
                     return 0
             except:
                 return 0
In [0]: calc_adar_in(1,189226)
Out[0]: 0
In [0]: calc_adar_in(669354,1635354)
Out[0]: 0
```

4.4 Is persion was following back:

```
In [0]: def follows_back(a,b):
    if train_graph.has_edge(b,a):
        return 1
    else:
        return 0

In [0]: follows_back(1,189226)

Out[0]: 1

In [0]: follows_back(669354,1635354)

Out[0]: 0
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz_centrality_(https://en.wikipedia.org/wiki/Katz_centrality)

https://www.geeksforgeeks.org/katz-centrality-measure/ (https://www.geeksforgeeks.org/katz-centrality-centrality-measure/) Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

$$x_i = lpha \sum_j A_{ij} x_j + eta,$$

where A is the adjacency matrix of the graph G with eigenvalues

 λ

The parameter

controls the initial centrality and

$$\beta$$

$$\alpha < \frac{1}{\lambda_{max}}$$
.

0.0007483800935562018

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm (https://en.wikipedia.org/wiki/HITS_algorithm)

```
In [0]: if not os.path.isfile('data/fea sample/hits.p'):
            hits = nx.hits(train graph, max iter=100, tol=1e-08, nstart=None, normaliz
        ed=True)
            pickle.dump(hits,open('data/fea sample/hits.p','wb'))
        else:
            hits = pickle.load(open('data/fea sample/hits.p','rb'))
In [0]: | print('min', hits[0][min(hits[0], key=hits[0].get)])
        print('max',hits[0][max(hits[0], key=hits[0].get)])
        print('mean',float(sum(hits[0].values())) / len(hits[0]))
        min 0.0
        max 0.004868653378780953
        mean 5.615699699344123e-07
```

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
import random
In [0]:
        if os.path.isfile('data/after eda/train after eda.csv'):
            filename = "data/after eda/train after eda.csv"
            # you uncomment this line, if you dont know the lentqh of the file name
            # here we have hardcoded the number of lines as 15100030
            # n train = sum(1 for line in open(filename)) #number of records in file
         (excludes header)
            n train = 15100028
            s = 100000 #desired sample size
            skip train = sorted(random.sample(range(1,n train+1),n train-s))
            #https://stackoverflow.com/a/22259008/4084039
In [0]: | if os.path.isfile('data/after eda/train after eda.csv'):
            filename = "data/after eda/test after eda.csv"
            # you uncomment this line, if you dont know the lentgh of the file name
            # here we have hardcoded the number of lines as 3775008
            # n test = sum(1 for line in open(filename)) #number of records in file (e
        xcludes header)
            n test = 3775006
            s = 50000 #desired sample size
```

skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))

#https://stackoverflow.com/a/22259008/4084039

```
In [0]: print("Number of rows in the train data file:", n_train)
    print("Number of rows we are going to elimiate in train data are",len(skip_train))
    print("Number of rows in the test data file:", n_test)
    print("Number of rows we are going to elimiate in test data are",len(skip_test))
```

Number of rows in the train data file: 15100028 Number of rows we are going to elimiate in train data are 15000028 Number of rows in the test data file: 3775006 Number of rows we are going to elimiate in test data are 3725006

In [0]: df_final_train = pd.read_csv('data/after_eda/train_after_eda.csv', skiprows=sk
ip_train, names=['source_node', 'destination_node'])
df_final_train['indicator_link'] = pd.read_csv('data/train_y.csv', skiprows=sk
ip_train, names=['indicator_link'])
print("Our train matrix size ",df_final_train.shape)
df_final_train.head(2)

Our train matrix size (100002, 3)

Out[0]:

	source_node	destination_node	indicator_link
0	273084	1505602	1
1	832016	1543415	1

Our test matrix size (50002, 3)

Out[0]:

	source_node	destination_node	indicator_link
(848424	784690	1
1	483294	1255532	1

5.2 Adding a set of features

we will create these each of these features for both train and test data points

```
    jaccard_followers
    jaccard_followees
    cosine_followers
    cosine_followees
    num_followers_s
    num_followees_s
    num_followers_d
    num_followees_d
    inter_followees
    inter_followees
```

```
In [0]:
        if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
            #mapping jaccrd followers to train and test data
            df final train['jaccard followers'] = df final train.apply(lambda row:
                                                     jaccard_for_followers(row['source_
        node'],row['destination_node']),axis=1)
            df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                                     jaccard for followers(row['source
        node'],row['destination node']),axis=1)
            #mapping jaccrd followees to train and test data
            df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                                     jaccard for followees(row['source
        node'],row['destination node']),axis=1)
            df final test['jaccard followees'] = df final test.apply(lambda row:
                                                     jaccard for followees(row['source
        node'],row['destination node']),axis=1)
                #mapping jaccrd followers to train and test data
            df_final_train['cosine_followers'] = df_final_train.apply(lambda row:
                                                     cosine for followers(row['source n
        ode'],row['destination node']),axis=1)
            df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                     cosine_for_followers(row['source_n
        ode'],row['destination node']),axis=1)
            #mapping jaccrd followees to train and test data
            df final train['cosine followees'] = df final train.apply(lambda row:
                                                     cosine_for_followees(row['source_n
        ode'],row['destination_node']),axis=1)
            df final test['cosine followees'] = df final test.apply(lambda row:
                                                     cosine for followees(row['source n
        ode'],row['destination_node']),axis=1)
```

```
In [0]:
        def compute features stage1(df final):
            #calculating no of followers followees for source and destination
            #calculating intersection of followers and followees for source and destin
        ation
            num followers s=[]
            num_followees_s=[]
            num followers d=[]
            num followees d=[]
            inter followers=[]
            inter_followees=[]
            for i,row in df_final.iterrows():
                try:
                     s1=set(train_graph.predecessors(row['source_node']))
                     s2=set(train graph.successors(row['source node']))
                 except:
                     s1 = set()
                     s2 = set()
                try:
                     d1=set(train_graph.predecessors(row['destination_node']))
                     d2=set(train graph.successors(row['destination node']))
                except:
                     d1 = set()
                     d2 = set()
                 num_followers_s.append(len(s1))
                 num_followees_s.append(len(s2))
                 num followers d.append(len(d1))
                 num_followees_d.append(len(d2))
                 inter_followers.append(len(s1.intersection(d1)))
                 inter_followees.append(len(s2.intersection(d2)))
            return num followers s, num followers d, num followees s, num followees d,
        inter_followers, inter_followees
```

```
In [0]: if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
            df_final_train['num_followers_s'], df_final_train['num_followers_d'], \
            df final train['num followees s'], df final train['num followees d'], \
            df final train['inter followers'], df final train['inter followees']= comp
        ute features stage1(df final train)
            df_final_test['num_followers_s'], df_final_test['num_followers_d'], \
            df final test['num followees s'], df final test['num followees d'], \
            df_final_test['inter_followers'], df_final_test['inter_followees']= comput
        e_features_stage1(df_final_test)
            hdf = HDFStore('data/fea_sample/storage_sample_stage1.h5')
            hdf.put('train_df',df_final_train, format='table', data_columns=True)
            hdf.put('test df',df final test, format='table', data columns=True)
            hdf.close()
        else:
            df final train = read hdf('data/fea sample/storage sample stage1.h5', 'tra
        in df',mode='r')
            df_final_test = read_hdf('data/fea_sample/storage_sample_stage1.h5', 'test
         df',mode='r')
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [0]: if not os.path.isfile('data/fea sample/storage sample stage2.h5'):
            #mapping adar index on train
            df final train['adar index'] = df final train.apply(lambda row: calc adar
        in(row['source node'],row['destination node']),axis=1)
            #mapping adar index on test
            df_final_test['adar_index'] = df_final_test.apply(lambda row: calc_adar_in
        (row['source node'],row['destination node']),axis=1)
            #mapping followback or not on train
            df_final_train['follows_back'] = df_final_train.apply(lambda row: follows_
        back(row['source_node'],row['destination_node']),axis=1)
            #mapping followback or not on test
            df_final_test['follows_back'] = df_final_test.apply(lambda row: follows_ba
        ck(row['source node'],row['destination node']),axis=1)
            #mapping same component of wcc or not on train
            df_final_train['same_comp'] = df_final_train.apply(lambda row: belongs_to_
        same wcc(row['source node'],row['destination node']),axis=1)
            ##mapping same component of wcc or not on train
            df final test['same comp'] = df final test.apply(lambda row: belongs to sa
        me wcc(row['source node'],row['destination node']),axis=1)
            #-----
            #mapping shortest path on train
            df final train['shortest path'] = df final train.apply(lambda row: compute
        shortest path length(row['source node'],row['destination node']),axis=1)
            #mapping shortest path on test
            df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_s
        hortest_path_length(row['source_node'],row['destination_node']),axis=1)
            hdf = HDFStore('data/fea_sample/storage_sample_stage2.h5')
            hdf.put('train df',df final train, format='table', data columns=True)
            hdf.put('test_df',df_final_test, format='table', data_columns=True)
            hdf.close()
            df final train = read hdf('data/fea sample/storage sample stage2.h5', 'tra
        in df',mode='r')
            df final test = read hdf('data/fea sample/storage sample stage2.h5', 'test
        df',mode='r')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges
 - · weight of outgoing edges
 - · weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges * weight of outgoing edges
 - · 2*weight of incoming edges + weight of outgoing edges
 - weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W=rac{1}{\sqrt{1+|X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
FB_featurization
In [0]:
        #weight for source and destination of each link
        Weight_in = {}
        Weight out = {}
        for i in tqdm(train graph.nodes()):
            s1=set(train graph.predecessors(i))
            w_{in} = 1.0/(np.sqrt(1+len(s1)))
            Weight in[i]=w in
            s2=set(train graph.successors(i))
            w_out = 1.0/(np.sqrt(1+len(s2)))
            Weight out[i]=w out
        #for imputing with mean
        mean weight in = np.mean(list(Weight in.values()))
        mean weight out = np.mean(list(Weight out.values()))
        100%
                                                                                    17
        80722/1780722 [00:11<00:00, 152682.24it/s]
In [0]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
            #mapping to pandas train
            df_final_train['weight_in'] = df_final_train.destination_node.apply(lambda
        x: Weight_in.get(x,mean_weight_in))
            df final train['weight out'] = df final train.source node.apply(lambda x:
        Weight out.get(x,mean weight out))
            #mapping to pandas test
            df_final_test['weight_in'] = df_final_test.destination_node.apply(lambda x
         : Weight_in.get(x,mean_weight_in))
            df final test['weight out'] = df final test.source node.apply(lambda x: We
        ight out.get(x,mean weight out))
            #some features engineerings on the in and out weights
            df_final_train['weight_f1'] = df_final_train.weight_in + df_final_train.we
        ight_out
            df final train['weight f2'] = df final train.weight in * df final train.we
        ight out
            df final train['weight f3'] = (2*df final train.weight in + 1*df final tra
        in.weight out)
            df_final_train['weight_f4'] = (1*df_final_train.weight_in + 2*df_final_tra
        in.weight out)
```

#some features engineerings on the in and out weights

df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weigh

df_final_test['weight_f2'] = df_final_test.weight_in * df_final_test.weigh

df final test['weight f3'] = (2*df final test.weight in + 1*df final test.

t out

t_out

weight out)

```
In [6]: if not os.path.isfile('C:\\Users\\admin\\Downloads\\storage sample stage3.h5'
       ):
           #page rank for source and destination in Train and Test
           #if anything not there in train graph then adding mean page rank
           df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda x:
       pr.get(x,mean_pr))
           df final train['page rank d'] = df final train.destination node.apply(lamb
       da x:pr.get(x,mean pr))
           df final test['page rank s'] = df final test.source node.apply(lambda x:pr
        .get(x,mean pr))
           df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda
       x:pr.get(x,mean pr))
           ======
           #Katz centrality score for source and destination in Train and test
           #if anything not there in train graph then adding mean katz score
           df final train['katz s'] = df final train.source node.apply(lambda x: katz
        .get(x,mean katz))
           df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x:
       katz.get(x,mean katz))
           df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.g
       et(x,mean katz))
           df final test['katz d'] = df final test.destination node.apply(lambda x: k
       atz.get(x,mean katz))
           #Hits algorithm score for source and destination in Train and test
           #if anything not there in train graph then adding 0
           df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits
        [0].get(x,0))
           df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x:
       hits[0].get(x,0)
           df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0
        ].get(x,0))
           df_final_test['hubs_d'] = df_final_test.destination_node.apply(lambda x: h
       its[0].get(x,0)
           ======
           #Hits algorithm score for source and destination in Train and Test
           #if anything not there in train graph then adding 0
           df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda
       x: hits[1].get(x,0))
           df_final_train['authorities_d'] = df_final_train.destination_node.apply(la
       mbda x: hits[1].get(x,0))
           df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x:
       hits[1].get(x,0)
           df final test['authorities d'] = df final test.destination node.apply(lamb
       da x: hits[1].get(x,0))
```

```
#========

hdf = HDFStore('C:\\Users\\admin\\Downloads\\storage_sample_stage3.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
else:
    df_final_train = read_hdf('C:\\Users\\admin\\Downloads\\storage_sample_stage3.h5', 'train_df',mode='r')
    df_final_test = read_hdf('C:\\Users\\admin\\Downloads\\storage_sample_stage3.h5', 'test_df',mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [0]:
        def svd(x, S):
            try:
                 z = sadj_dict[x]
                 return S[z]
            except:
                 return [0,0,0,0,0,0]
In [0]: #for svd features to get feature vector creating a dict node val and inedx in
         svd vector
        sadj_col = sorted(train_graph.nodes())
        sadj dict = { val:idx for idx,val in enumerate(sadj col)}
In [0]:
        Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).as
        fptype()
In [0]: U, s, V = svds(Adj, k = 6)
        print('Adjacency matrix Shape',Adj.shape)
        print('U Shape',U.shape)
        print('V Shape', V.shape)
        print('s Shape',s.shape)
        Adjacency matrix Shape (1780722, 1780722)
        U Shape (1780722, 6)
        V Shape (6, 1780722)
        s Shape (6,)
```

```
In [0]: if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
           df_final_train[['svd_u_s_1', 'svd_u_s_2','svd_u_s_3', 'svd_u_s_4', 'svd_u_
       s 5', 'svd u s 6']] = \
           df_final_train.source_node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u
       d 5','svd u d 6']] = \
           df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series
           df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_
       s_5', 'svd_v_s_6',]] = \
           df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v
       d 5','svd v d 6']] = \
           df_final_train.destination_node.apply(lambda x: svd(x, V.T)).apply(pd.Seri
       es)
           df_final_test[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s
       _5', 'svd_u_s_6']] = \
           df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
           df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_
       d 5','svd u d 6']] = \
           df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
           ______
           df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s
       _5', 'svd_v_s_6',]] = \
           df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
           df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_
       d 5', 'svd v d 6']] = \
           df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Serie
       s)
           _____
           hdf = HDFStore('data/fea sample/storage sample stage4.h5')
           hdf.put('train_df',df_final_train, format='table', data_columns=True)
           hdf.put('test df',df final test, format='table', data columns=True)
           hdf.close()
```

```
In [0]: # prepared and stored the data from machine learning models
# pelase check the FB_Models.ipynb

In [3]: df_final_train = read_hdf('C:\\Users\\admin\\Downloads\\storage_sample_stage4.
h5', 'train_df',mode='r')

In [4]: df_final_test=read_hdf('C:\\Users\\admin\\Downloads\\storage_sample_stage4.h5'
, 'test_df',mode='r')

In [102]: df_final_train.shape

Out[102]: (100002, 54)
```

num_followers_d feature is missing from stage file so we are calculating and adding it.

```
In [103]: def compute_num_followers_d(df_final):
    num_followers_d=[]
    for i,row in df_final.iterrows():
        try:
            d1=set(train_graph.predecessors(row['destination_node']))
        except:
            d1 = set()
            num_followers_d.append(len(d1))
        return num_followers_d

In [105]: df_final_train['num_followers_d']=compute_num_followers_d(df_final_train)

In [106]: df_final_test['num_followers_d']=compute_num_followers_d(df_final_test)

In [109]: df_final_train.shape

Out[109]: (100002, 55)
```

Preferential Attachment with followers and followees data of vertex

```
In [110]: #for train dataset of followers
    nfs=np.array(df_final_train['num_followers_s'])
    nfd=np.array(df_final_train['num_followers_d'])
    preferential_followers=[]
    for i in range(len(nfs)):
        preferential_followers.append(nfd[i]*nfs[i])
    df_final_train['prefer_Attach_followers']= preferential_followers
    df_final_train.head()
```

Out[110]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	273084	1505602	1	0	0.000000	0.0
1	832016	1543415	1	0	0.187135	0.0
2	1325247	760242	1	0	0.369565	0.
3	1368400	1006992	1	0	0.000000	0.0
4	140165	1708748	1	0	0.000000	0.0

5 rows × 56 columns

```
In [111]: #for test dataset of followers
    nfs=np.array(df_final_test['num_followers_s'])
    nfd=np.array(df_final_test['num_followers_d'])
    preferential_followers=[]
    for i in range(len(nfs)):
        preferential_followers.append(nfd[i]*nfs[i])
    df_final_test['prefer_Attach_followers']= preferential_followers
    df_final_test.head()
```

Out[111]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	848424	784690	1	0	0.0	0.0
1	483294	1255532	1	0	0.0	0.0
2	626190	1729265	1	0	0.0	0.0
3	947219	425228	1	0	0.0	0.0
4	991374	975044	1	0	0.2	0.0

5 rows × 56 columns

```
In [112]: #for train dataset of followees
    nfs=np.array(df_final_train['num_followees_s'])
    nfd=np.array(df_final_train['num_followees_d'])
    preferential_followees=[]
    for i in range(len(nfs)):
        preferential_followees.append(nfd[i]*nfs[i])
    df_final_train['prefer_Attach_followees']= preferential_followees
    df_final_train.head()
```

Out[112]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	273084	1505602	1	0	0.000000	0.0
1	832016	1543415	1	0	0.187135	0.0
2	1325247	760242	1	0	0.369565	0.
3	1368400	1006992	1	0	0.000000	0.0
4	140165	1708748	1	0	0.000000	0.0

5 rows × 57 columns

```
In [113]: #for test dataset of followees
    nfs=np.array(df_final_test['num_followees_s'])
    nfd=np.array(df_final_test['num_followees_d'])
    preferential_followees=[]
    for i in range(len(nfs)):
        preferential_followees.append(nfd[i]*nfs[i])
    df_final_test['prefer_Attach_followees']= preferential_followees
    df_final_test.head()
```

Out[113]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	848424	784690	1	0	0.0	0.0
1	483294	1255532	1	0	0.0	0.0
2	626190	1729265	1	0	0.0	0.0
3	947219	425228	1	0	0.0	0.0
4	991374	975044	1	0	0.2	0.0

5 rows × 57 columns

```
In [118]: df final test.columns
Out[118]: Index(['source node', 'destination node', 'indicator link',
                  'jaccard_followers', 'jaccard_followees', 'cosine_followers',
                  'cosine_followees', 'num_followers_s', 'num_followees_s',
                 'num_followees_d', 'inter_followers', 'inter_followees', 'adar_index',
                  'follows back', 'same comp', 'shortest path', 'weight in', 'weight ou
          t',
                 'weight_f1', 'weight_f2', 'weight_f3', 'weight_f4', 'page_rank_s',
                  'page rank d', 'katz s', 'katz d', 'hubs s', 'hubs d', 'authorities
          s',
                 'authorities d', 'svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4',
                 'svd_u_s_5', 'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3',
                 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2',
                 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1',
                 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6',
                 'num_followers_d', 'prefer_Attach_followers',
                  'prefer_Attach_followees'],
                dtvpe='object')
```

Adding feature svd_dot

svd dot is Dot product between sourse node svd and destination node svd features

```
In [29]: #for train datasets
s1,s2,s3,s4,s5,s6=df_final_train['svd_u_s_1'],df_final_train['svd_u_s_2'],df_f
inal_train['svd_u_s_3'],df_final_train['svd_u_s_4'],df_final_train['svd_u_s_5'
],df_final_train['svd_u_s_6']
s7,s8,s9,s10,s11,s12=df_final_train['svd_v_s_1'],df_final_train['svd_v_s_2'],d
f_final_train['svd_v_s_3'],df_final_train['svd_v_s_4'],df_final_train['svd_v_s
_5'],df_final_train['svd_v_s_6']

d1,d2,d3,d4,d5,d6=df_final_train['svd_u_d_1'],df_final_train['svd_u_d_2'],df_f
inal_train['svd_u_d_3'],df_final_train['svd_u_d_4'],df_final_train['svd_u_d_5'
],df_final_train['svd_u_d_6']

d7,d8,d9,d10,d11,d12=df_final_train['svd_v_d_1'],df_final_train['svd_v_d_2'],d
f_final_train['svd_v_d_3'],df_final_train['svd_v_d_4'],df_final_train['svd_v_d_5'],df_final_train['svd_v_d_6']
```

```
In [30]:
         svd dot u=[]
         for i in range(len(np.array(s1))):
             a=[]
             b=[]
             a.append(np.array(s1[i]))
             a.append(np.array(s2[i]))
             a.append(np.array(s3[i]))
             a.append(np.array(s4[i]))
             a.append(np.array(s5[i]))
             a.append(np.array(s6[i]))
             b.append(np.array(d1[i]))
             b.append(np.array(d2[i]))
             b.append(np.array(d3[i]))
             b.append(np.array(d4[i]))
             b.append(np.array(d5[i]))
             b.append(np.array(d6[i]))
             svd dot u.append(np.dot(a,b))
         df_final_train['svd_dot_u']=svd_dot_u
```

```
In [31]: | svd_dot_v=[]
         for i in range(len(np.array(s1))):
             a=[]
             b=[]
             a.append(np.array(s7[i]))
             a.append(np.array(s8[i]))
             a.append(np.array(s9[i]))
             a.append(np.array(s10[i]))
             a.append(np.array(s11[i]))
             a.append(np.array(s12[i]))
             b.append(np.array(d7[i]))
             b.append(np.array(d8[i]))
             b.append(np.array(d9[i]))
             b.append(np.array(d10[i]))
             b.append(np.array(d11[i]))
             b.append(np.array(d12[i]))
             svd_dot_v.append(np.dot(a,b))
         df_final_train['svd_dot_v']=svd_dot_v
```

```
In [32]: df_final_train.head()
```

Out[32]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	273084	1505602	1	0	0.000000	0.0
1	832016	1543415	1	0	0.187135	0.0
2	1325247	760242	1	0	0.369565	0.
3	1368400	1006992	1	0	0.000000	0.0
4	140165	1708748	1	0	0.000000	0.0

5 rows × 59 columns

```
→
```

```
In [33]: #for test dataset
s1,s2,s3,s4,s5,s6=df_final_test['svd_u_s_1'],df_final_test['svd_u_s_2'],df_fin
al_test['svd_u_s_3'],df_final_test['svd_u_s_4'],df_final_test['svd_u_s_5'],df_
final_test['svd_u_s_6']
s7,s8,s9,s10,s11,s12=df_final_test['svd_v_s_1'],df_final_test['svd_v_s_2'],df_
final_test['svd_v_s_3'],df_final_test['svd_v_s_4'],df_final_test['svd_v_s_5'],
df_final_test['svd_v_s_6']

d1,d2,d3,d4,d5,d6=df_final_test['svd_u_d_1'],df_final_test['svd_u_d_2'],df_final_test['svd_u_d_3'],df_final_test['svd_u_d_4'],df_final_test['svd_u_d_5'],df_
final_test['svd_u_d_6']
d7,d8,d9,d10,d11,d12=df_final_test['svd_v_d_1'],df_final_test['svd_v_d_2'],df_
final_test['svd_v_d_3'],df_final_test['svd_v_d_4'],df_final_test['svd_v_d_5'],
df_final_test['svd_v_d_6']
```

```
In [34]:
         svd dot u=[]
         for i in range(len(np.array(s1))):
             a=[]
             b=[]
             a.append(np.array(s1[i]))
             a.append(np.array(s2[i]))
             a.append(np.array(s3[i]))
             a.append(np.array(s4[i]))
             a.append(np.array(s5[i]))
             a.append(np.array(s6[i]))
             b.append(np.array(d1[i]))
             b.append(np.array(d2[i]))
             b.append(np.array(d3[i]))
             b.append(np.array(d4[i]))
             b.append(np.array(d5[i]))
             b.append(np.array(d6[i]))
             svd dot u.append(np.dot(a,b))
         df_final_test['svd_dot_u']=svd_dot_u
```

```
In [35]:
         svd dot v=[]
         for i in range(len(np.array(s1))):
             a=[]
             b=[]
             a.append(np.array(s7[i]))
             a.append(np.array(s8[i]))
             a.append(np.array(s9[i]))
             a.append(np.array(s10[i]))
             a.append(np.array(s11[i]))
             a.append(np.array(s12[i]))
             b.append(np.array(d7[i]))
             b.append(np.array(d8[i]))
             b.append(np.array(d9[i]))
             b.append(np.array(d10[i]))
             b.append(np.array(d11[i]))
             b.append(np.array(d12[i]))
             svd_dot_v.append(np.dot(a,b))
         df_final_test['svd_dot_v']=svd_dot_v
```

In [36]: df_final_test.head()

Out[36]:

	source_node	destination_node	indicator_link	jaccard_followers	jaccard_followees	cosine_fol
0	848424	784690	1	0	0.0	0.0
1	483294	1255532	1	0	0.0	0.0
2	626190	1729265	1	0	0.0	0.0
3	947219	425228	1	0	0.0	0.0
4	991374	975044	1	0	0.2	0.0

5 rows × 59 columns

```
In [37]: hdf = HDFStore('C:\\Users\\admin\\Downloads\\storage_sample_stage_4.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
```