

```
In [3]: # Credits: https://github.com/keras-team/keras/blob/master/examples/mnist_cnn.
        py
        from datetime import datetime
        import keras
        from keras.datasets import mnist
        from keras.models import Sequential
        from keras.layers import Dense, Dropout, Flatten
        from keras.layers import Conv2D, MaxPooling2D
        from keras import backend as K
        from keras.initializers import he_normal
        from keras.layers.normalization import BatchNormalization

        batch_size = 128
        num_classes = 10
        epochs = 12
        # input image dimensions
        img_rows, img_cols = 28, 28
```

Using TensorFlow backend.

```
In [4]: (x_train, y_train), (x_test, y_test) = mnist.load_data()
```

Downloading data from <https://s3.amazonaws.com/img-datasets/mnist.npz>  
 11493376/11490434 [=====] - 1s 0us/step

```
In [5]: if K.image_data_format() == 'channels_first':
        x_train = x_train.reshape(x_train.shape[0], 1, img_rows, img_cols)
        x_test = x_test.reshape(x_test.shape[0], 1, img_rows, img_cols)
        input_shape = (1, img_rows, img_cols)
    else:
        x_train = x_train.reshape(x_train.shape[0], img_rows, img_cols, 1)
        x_test = x_test.reshape(x_test.shape[0], img_rows, img_cols, 1)
        input_shape = (img_rows, img_cols, 1)

        x_train = x_train.astype('float32')
        x_test = x_test.astype('float32')
        x_train /= 255
        x_test /= 255
        print('x_train shape:', x_train.shape)
        print(x_train.shape[0], 'train samples')
        print(x_test.shape[0], 'test samples')

        # convert class vectors to binary class matrices
        y_train = keras.utils.to_categorical(y_train, num_classes)
        y_test = keras.utils.to_categorical(y_test, num_classes)
```

x\_train shape: (60000, 28, 28, 1)  
 60000 train samples  
 10000 test samples

```
In [6]: print(y_train.shape)
```

(60000, 10)

```
In [0]: %matplotlib inline
import matplotlib.pyplot as plt
import numpy as np
import time
# https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4
# https://stackoverflow.com/a/14434334
# this function is used to update the plots for each epoch and error
def plt_dynamic(x, vy, ty):
    fig = plt.figure( facecolor='y', edgecolor='k')
    plt.plot(x, vy, 'b', label="Validation Loss")
    plt.plot(x, ty, 'r', label="Train Loss")
    plt.xlabel('Epochs')
    plt.ylabel('Categorical Crossentropy Loss')
    plt.legend()
    plt.grid()
    plt.show()
```

## Model 1: CNN with 3 ConvNets and 3X3 Kernel size.

```
In [8]: convnet3=Sequential() # Initializing the model

# First ConvNet
convnet3.add(Conv2D(32,kernel_size=(3,3),activation='relu',input_shape=input_shape))
convnet3.add(Conv2D(64,kernel_size=(3,3),activation='relu'))
convnet3.add(Dropout(0.25))
convnet3.add(Conv2D(128,kernel_size=(3,3), activation='relu'))

#maxpooling by (2,2 ) ,dropout,flattening
convnet3.add(MaxPooling2D(pool_size=(2,2)))
convnet3.add(Dropout(0.25))
convnet3.add(Flatten())

#hidden_layer
convnet3.add(Dense(256, activation='relu', kernel_initializer=he_normal(seed=Non
one)))
convnet3.add(Dropout(0.5))
convnet3.add(Dense(num_classes,activation='softmax'))
print(convnet3.summary())
```

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/framework/op\_def\_library.py:263: colocate\_with (from tensorflow.python.framework.ops) is deprecated and will be removed in a future version.

Instructions for updating:

Colocations handled automatically by placer.

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorflow\_backend.py:3445: calling dropout (from tensorflow.python.ops.nn\_ops) with keep\_prob is deprecated and will be removed in a future version.

Instructions for updating:

Please use `rate` instead of `keep\_prob`. Rate should be set to `rate = 1 - keep\_prob`.

Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 26, 26, 32)	320
conv2d_2 (Conv2D)	(None, 24, 24, 64)	18496
dropout_1 (Dropout)	(None, 24, 24, 64)	0
conv2d_3 (Conv2D)	(None, 22, 22, 128)	73856
max_pooling2d_1 (MaxPooling2D)	(None, 11, 11, 128)	0
dropout_2 (Dropout)	(None, 11, 11, 128)	0
flatten_1 (Flatten)	(None, 15488)	0
dense_1 (Dense)	(None, 256)	3965184
dropout_3 (Dropout)	(None, 256)	0
dense_2 (Dense)	(None, 10)	2570
Total params: 4,060,426		
Trainable params: 4,060,426		
Non-trainable params: 0		
None		

## Model Compilation

```
In [9]: start=datetime.now()
convnet3.compile(optimizer=keras.optimizers.Adam(), loss=keras.losses.categorical_crossentropy, metrics=['accuracy'])
convnet3_history=convnet3.fit(x_train,y_train,batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
print("Time taken to run this cell :", datetime.now() - start)
```

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/ops/math\_ops.py:3066: to\_int32 (from tensorflow.python.ops.math\_ops) is deprecated and will be removed in a future version.

Instructions for updating:

Use tf.cast instead.

Train on 60000 samples, validate on 10000 samples

Epoch 1/12

60000/60000 [=====] - 515s 9ms/step - loss: 0.1783 - acc: 0.9450 - val\_loss: 0.0405 - val\_acc: 0.9862

Epoch 2/12

60000/60000 [=====] - 512s 9ms/step - loss: 0.0608 - acc: 0.9814 - val\_loss: 0.0347 - val\_acc: 0.9892

Epoch 3/12

60000/60000 [=====] - 513s 9ms/step - loss: 0.0471 - acc: 0.9855 - val\_loss: 0.0285 - val\_acc: 0.9905

Epoch 4/12

60000/60000 [=====] - 515s 9ms/step - loss: 0.0358 - acc: 0.9889 - val\_loss: 0.0276 - val\_acc: 0.9903

Epoch 5/12

60000/60000 [=====] - 516s 9ms/step - loss: 0.0314 - acc: 0.9904 - val\_loss: 0.0272 - val\_acc: 0.9904

Epoch 6/12

60000/60000 [=====] - 514s 9ms/step - loss: 0.0266 - acc: 0.9912 - val\_loss: 0.0243 - val\_acc: 0.9928

Epoch 7/12

60000/60000 [=====] - 513s 9ms/step - loss: 0.0227 - acc: 0.9930 - val\_loss: 0.0233 - val\_acc: 0.9936

Epoch 8/12

60000/60000 [=====] - 514s 9ms/step - loss: 0.0195 - acc: 0.9934 - val\_loss: 0.0254 - val\_acc: 0.9927

Epoch 9/12

60000/60000 [=====] - 512s 9ms/step - loss: 0.0203 - acc: 0.9934 - val\_loss: 0.0210 - val\_acc: 0.9940

Epoch 10/12

60000/60000 [=====] - 511s 9ms/step - loss: 0.0173 - acc: 0.9943 - val\_loss: 0.0237 - val\_acc: 0.9937

Epoch 11/12

60000/60000 [=====] - 511s 9ms/step - loss: 0.0153 - acc: 0.9950 - val\_loss: 0.0219 - val\_acc: 0.9930

Epoch 12/12

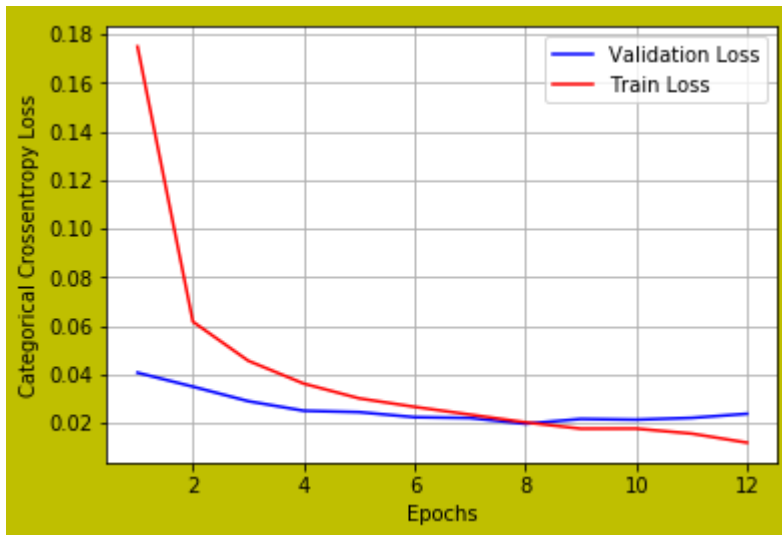
60000/60000 [=====] - 511s 9ms/step - loss: 0.0144 - acc: 0.9954 - val\_loss: 0.0252 - val\_acc: 0.9927

Time taken to run this cell : 1:42:38.202782

## Model Evaluation

```
In [0]: score=convnet3.evaluate(x_test,y_test,verbose=0)
test_score3=score[0]
test_accuracy3=score[1]
train_accuracy3=max(convnet3_history.history['acc'])
print('test score : ',test_score3)
print('test sccuracy : ',test_accuracy3)
# error plot
x=list(range(1,epochs+1))
vy=convnet3_history.history['val_loss'] #validation loss
ty=convnet3_history.history['loss'] # train loss
plt_dynamic(x, vy, ty)
```

test score : 0.023814157019101594  
test sccuracy : 0.9933



**Model 2: CNN with 5 ConvNets and 5X5 Kernel size.**

```
In [0]: convnet5=Sequential() # Initializing the model

# First ConvNet
convnet5.add(Conv2D(32,kernel_size=(5,5), activation='relu', padding='same', input_shape=input_shape))

#Second ConvNet
convnet5.add(Conv2D(64,kernel_size=(5,5),padding='same',activation='relu'))
convnet5.add(MaxPooling2D(pool_size=(2,2)))
convnet5.add(Dropout(0.25))

#Third ConvNet
convnet5.add(Conv2D(96,kernel_size=(5,5),padding='same',activation='relu'))
#maxpooling by (2,2) ,dropout,flattening
convnet5.add(MaxPooling2D(pool_size=(2,2)))
convnet5.add(Dropout(0.25))

#Fourth ConvNet
convnet5.add(Conv2D(128,kernel_size=(5,5), padding='same', activation='relu'))
convnet5.add(MaxPooling2D(pool_size=(2,2)))
convnet5.add(Dropout(0.25))

#fifth Convnet
convnet5.add(Conv2D(164,kernel_size=(5,5), padding='same', activation='relu'))
convnet5.add(MaxPooling2D(pool_size=(2,2)))
convnet5.add(Dropout(0.25))
convnet5.add(Flatten())

#hidden_layer
convnet5.add(Dense(256, activation='relu', kernel_initializer=he_normal(seed=None)))
convnet5.add(BatchNormalization())
convnet5.add(Dropout(0.5))
convnet5.add(Dense(num_classes,activation='softmax'))
print(convnet5.summary())
```

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/framework/op\_def\_library.py:263: colocate\_with (from tensorflow.python.framework.ops) is deprecated and will be removed in a future version.

Instructions for updating:

Colocations handled automatically by placer.

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorflow\_backend.py:3445: calling dropout (from tensorflow.python.ops.nn\_ops) with keep\_prob is deprecated and will be removed in a future version.

Instructions for updating:

Please use `rate` instead of `keep\_prob`. Rate should be set to `rate = 1 - keep\_prob`.

Layer (type)	Output Shape	Param #
=====		
conv2d_1 (Conv2D)	(None, 28, 28, 32)	832
conv2d_2 (Conv2D)	(None, 28, 28, 64)	51264
max_pooling2d_1 (MaxPooling2D)	(None, 14, 14, 64)	0
dropout_1 (Dropout)	(None, 14, 14, 64)	0
conv2d_3 (Conv2D)	(None, 14, 14, 96)	153696
max_pooling2d_2 (MaxPooling2D)	(None, 7, 7, 96)	0
dropout_2 (Dropout)	(None, 7, 7, 96)	0
conv2d_4 (Conv2D)	(None, 7, 7, 128)	307328
max_pooling2d_3 (MaxPooling2D)	(None, 3, 3, 128)	0
dropout_3 (Dropout)	(None, 3, 3, 128)	0
conv2d_5 (Conv2D)	(None, 3, 3, 164)	524964
max_pooling2d_4 (MaxPooling2D)	(None, 1, 1, 164)	0
dropout_4 (Dropout)	(None, 1, 1, 164)	0
flatten_1 (Flatten)	(None, 164)	0
dense_1 (Dense)	(None, 256)	42240
batch_normalization_1 (Batch Normalization)	(None, 256)	1024
dropout_5 (Dropout)	(None, 256)	0
dense_2 (Dense)	(None, 10)	2570
=====		
Total params: 1,083,918		
Trainable params: 1,083,406		
Non-trainable params: 512		
None		



## Model Compilation

```
In [0]: start = datetime.now()
convnet5.compile(optimizer=keras.optimizers.Adam(), loss=keras.losses.categorical_crossentropy, metrics=['accuracy'])
convnet5_history=convnet5.fit(x_train,y_train,batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
print("Time taken to run this cell :", datetime.now() - start)
```

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/ops/math\_ops.py:3066: to\_int32 (from tensorflow.python.ops.math\_ops) is deprecated and will be removed in a future version.

Instructions for updating:

Use tf.cast instead.

Train on 60000 samples, validate on 10000 samples

Epoch 1/12

60000/60000 [=====] - 843s 14ms/step - loss: 2.4664  
- acc: 0.1728 - val\_loss: 2.6763 - val\_acc: 0.1114

Epoch 2/12

60000/60000 [=====] - 840s 14ms/step - loss: 1.9119  
- acc: 0.2926 - val\_loss: 1.3380 - val\_acc: 0.5081

Epoch 3/12

60000/60000 [=====] - 817s 14ms/step - loss: 1.1535  
- acc: 0.5858 - val\_loss: 0.8421 - val\_acc: 0.7205

Epoch 4/12

60000/60000 [=====] - 803s 13ms/step - loss: 0.6639  
- acc: 0.7837 - val\_loss: 0.3669 - val\_acc: 0.8843

Epoch 5/12

60000/60000 [=====] - 811s 14ms/step - loss: 0.4424  
- acc: 0.8605 - val\_loss: 0.2923 - val\_acc: 0.9056

Epoch 6/12

60000/60000 [=====] - 785s 13ms/step - loss: 0.3275  
- acc: 0.8986 - val\_loss: 0.1812 - val\_acc: 0.9409

Epoch 7/12

60000/60000 [=====] - 772s 13ms/step - loss: 0.2779  
- acc: 0.9131 - val\_loss: 0.1614 - val\_acc: 0.9466

Epoch 8/12

60000/60000 [=====] - 773s 13ms/step - loss: 0.1989  
- acc: 0.9387 - val\_loss: 0.0968 - val\_acc: 0.9707

Epoch 9/12

60000/60000 [=====] - 737s 12ms/step - loss: 0.1471  
- acc: 0.9553 - val\_loss: 0.0644 - val\_acc: 0.9785

Epoch 10/12

60000/60000 [=====] - 743s 12ms/step - loss: 0.1208  
- acc: 0.9637 - val\_loss: 0.0545 - val\_acc: 0.9833

Epoch 11/12

60000/60000 [=====] - 818s 14ms/step - loss: 0.1005  
- acc: 0.9713 - val\_loss: 0.0454 - val\_acc: 0.9871

Epoch 12/12

60000/60000 [=====] - 843s 14ms/step - loss: 0.0895  
- acc: 0.9730 - val\_loss: 0.0482 - val\_acc: 0.9860

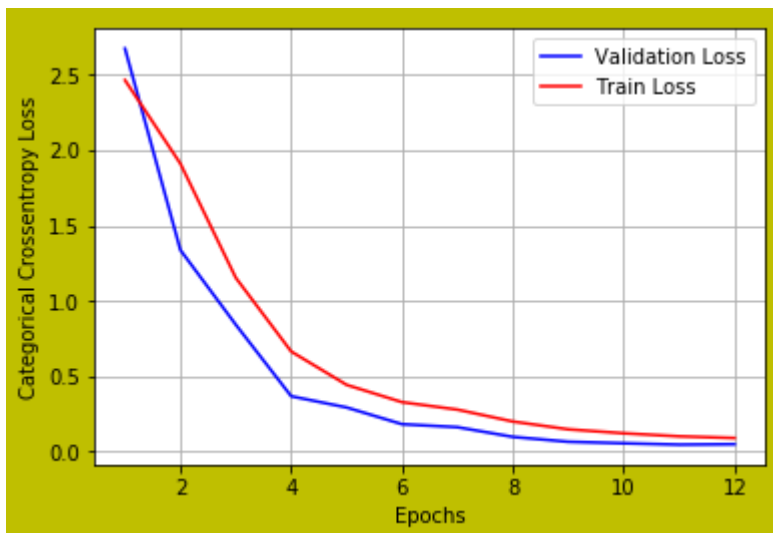
Time taken to run this cell : 2:39:47.573903

## Model Evaluation

```
In [0]: score=convnet5.evaluate(x_test,y_test,verbose=0)
test_score5=score[0]
test_accuracy5=score[1]
train_accuracy5=max(convnet5_history.history['acc'])
print('test score : ',test_score5)
print('test Accuracy : ',test_accuracy5)
# error plot
x=list(range(1,epochs+1))
vy=convnet5_history.history['val_loss'] #validation loss
ty=convnet5_history.history['loss'] # train loss
plt_dynamic(x, vy, ty)
```

test score : 0.048168362715619154

test Accuracy : 0.986



## Model 3: CNN with 7 ConvNets and 2X2 Kernel size.

```
In [0]: convnet7=Sequential() # Initializing the model

# First ConvNet
convnet7.add(Conv2D(16,kernel_size=(2,2), activation='relu', padding='same', input_shape=input_shape))

#Second Convnet
convnet7.add(Conv2D(32,kernel_size=(2,2), padding='same',strides=(2,2), activation='relu'))
#convnet7.add(MaxPooling2D(pool_size=(2,2)))
#convnet7.add(Dropout(0.25))

# 3rd ConvNet
convnet7.add(Conv2D(64,kernel_size=(2,2), padding='same', activation='relu'))

#maxpooling by (2,2 ),dropout,flattening
#convnet7.add(MaxPooling2D(pool_size=(2,2)))
convnet7.add(Dropout(0.15))

#fourth Convnet
convnet7.add(Conv2D(96,kernel_size=(2,2), padding='same', activation='relu'))
convnet7.add(MaxPooling2D(pool_size=(2,2)))
convnet7.add(Dropout(0.39))

#fifth Convnet
convnet7.add(Conv2D(128,kernel_size=(2,2), padding='same', activation='relu'))
convnet7.add(MaxPooling2D(pool_size=(2,2)))
convnet7.add(Dropout(0.3))

#sixth Convnet
convnet7.add(Conv2D(164,kernel_size=(2,2), padding='same', activation='relu'))

#seventh Convnet
convnet7.add(Conv2D(164,kernel_size=(2,2), padding='same', activation='relu'))

convnet7.add(MaxPooling2D(pool_size=(2,2)))
convnet7.add(Dropout(0.4))
convnet7.add(Flatten())

#hidden_layer
convnet7.add(Dense(256, activation='relu', kernel_initializer=he_normal(seed=Nonone)))#1 hidden layer
convnet7.add(BatchNormalization())
convnet7.add(Dropout(0.5))
convnet7.add(Dense(148, activation='relu', kernel_initializer=he_normal(seed=Nonone)))#2 hidden layer
convnet7.add(BatchNormalization())
convnet7.add(Dropout(0.5))
convnet7.add(Dense(128, activation='relu', kernel_initializer=he_normal(seed=Nonone)))#3 hidden layer
convnet7.add(BatchNormalization())
convnet7.add(Dropout(0.5))
convnet7.add(Dense(num_classes,activation='softmax'))
print(convnet7.summary())
```

Layer (type)	Output Shape	Param #
conv2d_6 (Conv2D)	(None, 28, 28, 16)	80
conv2d_7 (Conv2D)	(None, 14, 14, 32)	2080
conv2d_8 (Conv2D)	(None, 14, 14, 64)	8256
dropout_6 (Dropout)	(None, 14, 14, 64)	0
conv2d_9 (Conv2D)	(None, 14, 14, 96)	24672
max_pooling2d_5 (MaxPooling2)	(None, 7, 7, 96)	0
dropout_7 (Dropout)	(None, 7, 7, 96)	0
conv2d_10 (Conv2D)	(None, 7, 7, 128)	49280
max_pooling2d_6 (MaxPooling2)	(None, 3, 3, 128)	0
dropout_8 (Dropout)	(None, 3, 3, 128)	0
conv2d_11 (Conv2D)	(None, 3, 3, 164)	84132
conv2d_12 (Conv2D)	(None, 3, 3, 164)	107748
max_pooling2d_7 (MaxPooling2)	(None, 1, 1, 164)	0
dropout_9 (Dropout)	(None, 1, 1, 164)	0
flatten_2 (Flatten)	(None, 164)	0
dense_3 (Dense)	(None, 256)	42240
batch_normalization_2 (Batch Normalization)	(None, 256)	1024
dropout_10 (Dropout)	(None, 256)	0
dense_4 (Dense)	(None, 148)	38036
batch_normalization_3 (Batch Normalization)	(None, 148)	592
dropout_11 (Dropout)	(None, 148)	0
dense_5 (Dense)	(None, 128)	19072
batch_normalization_4 (Batch Normalization)	(None, 128)	512
dropout_12 (Dropout)	(None, 128)	0
dense_6 (Dense)	(None, 10)	1290
Total params: 379,014		
Trainable params: 377,950		
Non-trainable params: 1,064		

None

## Model compilation

```
In [0]: start=datetime.now()
convnet7.compile(optimizer=keras.optimizers.Adam(), loss=keras.losses.categorical_crossentropy, metrics=['accuracy'])
convnet7_history=convnet7.fit(x_train,y_train,batch_size=batch_size, epochs=epochs, verbose=1, validation_data=(x_test, y_test))
print("Time taken to run this cell :", datetime.now() - start)
```

Train on 60000 samples, validate on 10000 samples

Epoch 1/12

60000/60000 [=====] - 142s 2ms/step - loss: 1.8961 - acc: 0.3754 - val\_loss: 1.5272 - val\_acc: 0.4652

Epoch 2/12

60000/60000 [=====] - 145s 2ms/step - loss: 0.4249 - acc: 0.8774 - val\_loss: 0.0784 - val\_acc: 0.9765

Epoch 3/12

60000/60000 [=====] - 141s 2ms/step - loss: 0.1882 - acc: 0.9518 - val\_loss: 0.0854 - val\_acc: 0.9789

Epoch 4/12

60000/60000 [=====] - 131s 2ms/step - loss: 0.1409 - acc: 0.9645 - val\_loss: 0.0484 - val\_acc: 0.9870

Epoch 5/12

60000/60000 [=====] - 130s 2ms/step - loss: 0.1121 - acc: 0.9717 - val\_loss: 0.0372 - val\_acc: 0.9907

Epoch 6/12

60000/60000 [=====] - 140s 2ms/step - loss: 0.0965 - acc: 0.9760 - val\_loss: 0.0347 - val\_acc: 0.9915

Epoch 7/12

60000/60000 [=====] - 132s 2ms/step - loss: 0.0887 - acc: 0.9779 - val\_loss: 0.0382 - val\_acc: 0.9907

Epoch 8/12

60000/60000 [=====] - 139s 2ms/step - loss: 0.0812 - acc: 0.9799 - val\_loss: 0.0353 - val\_acc: 0.9920

Epoch 9/12

60000/60000 [=====] - 142s 2ms/step - loss: 0.0769 - acc: 0.9807 - val\_loss: 0.0340 - val\_acc: 0.9919

Epoch 10/12

60000/60000 [=====] - 144s 2ms/step - loss: 0.0680 - acc: 0.9835 - val\_loss: 0.0358 - val\_acc: 0.9911

Epoch 11/12

60000/60000 [=====] - 146s 2ms/step - loss: 0.0670 - acc: 0.9836 - val\_loss: 0.0286 - val\_acc: 0.9934

Epoch 12/12

60000/60000 [=====] - 150s 3ms/step - loss: 0.0667 - acc: 0.9833 - val\_loss: 0.0309 - val\_acc: 0.9911

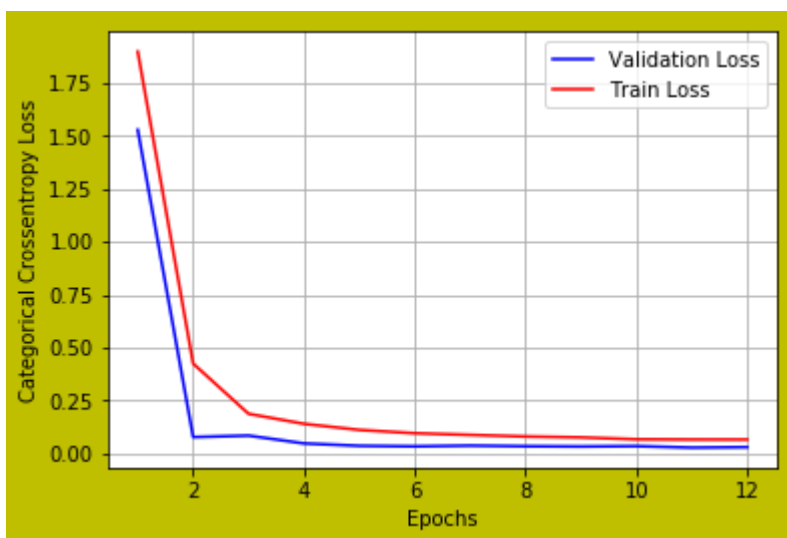
Time taken to run this cell : 0:28:02.350113

## Model Evaluation

```
In [0]: score=convnet7.evaluate(x_test,y_test,verbose=0)
test_score7=score[0]
test_accuracy7=score[1]
train_accuracy7=max(convnet7_history.history['acc'])
print('test score : ',test_score7)
print('test Accuracy : ',test_accuracy7)
# error plot
x=list(range(1,epochs+1))
vy=convnet7_history.history['val_loss'] #validation loss
ty=convnet7_history.history['loss'] # train loss
plt_dynamic(x, vy, ty)
```

test score : 0.03093639321749797

test Accuracy : 0.9911



```
In [11]: from prettytable import PrettyTable
x = PrettyTable()
x.field_names = ["Model", "Training Accuracy", "Test Accuracy", "Time Taken"]
x.add_row(["3ConvNet with kernel 3x3 ",0.9961, 0.9933, "1:42"])
x.add_row(["5ConvNet with kernel 5x5",0.9730, 0.9860, "2:39"])
x.add_row(["7ConvNet with kernel 2x2", 0.9833, 0.9911, "0:28"])
print(x)
```

Model	Training Accuracy	Test Accuracy	Time Taken
3ConvNet with kernel 3x3	0.9961	0.9933	1:42
5ConvNet with kernel 5x5	0.973	0.986	2:39
7ConvNet with kernel 2x2	0.9833	0.9911	0:28