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Design & Analysis of Algorithms

Topic: Minimum Cost Spanning Tree

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Minimum Spanning Tree

Spanning tree: A spanning tree T is a sub-graph of G(V,E), which has all the vertices covered with minimum possible number of edges (n-1).hence, a spanning tree does not contain cycles and it cannot be disconnected.

By the definition we can conclude that every connected and undirected graph G has at least one spanning tree. A disconnected graph does not have spanning tree.

Example:	G(V,E)	
Spanning tree possible:		

Weighted graph: If each edge of E has a weight, G is called a weighted graph.

Minimum Spanning Tree: In a weighted graph, a minimum spanning tree is a spanning tree that has minimum weight than all other spanning tree of the same graph. In real world situation, this weight can be measured as distance, congestion,traffic load or any arbitrary value denoted to the edges.

Problem:

Given an undirected, connected, weighted graph G=(V,E).

• We wish to find an acyclic subset $T \subseteq E$ that connects all the vertices and whose total weight:

$$w(T) = \sum_{(u, v) \in T} w(u, v)$$
 is minimized.

Where w(u,v) is the weight of edge (u,v).

• T is called a minimum spanning tree of G.

Solution:

- Using greedy method.
- Two algorithms:
 - ✓ Prim's algorithm.
 - ✓ Kruskal's algorithm.

Approach:

- The tree is built edge by edge.
- Let T be the set of edges selected so far.
- Each time a decision is made:
 - * Include an edge e to T s.t. : Cost (T)+w (e) is minimized, and $T \cup \{e\}$ does not create a cycle.

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References:

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