

Name -Aditya Thakur Sapid-590012258 Course- Design and analysis of algorithms Submitted to – Aryan gupta

1) C source code:

```
#define _POSIX_C_SOURCE 199309L
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
#include <stdint.h>
#include <string.h>
#include <math.h>
int binary search(int *arr, int n, int target) {
int left =0,right =n-1;
  while (left <= right) {
    int mid = left + (right - left) / 2;
    if (arr[mid] == target) return mid;
    else if (arr[mid] < target) left = mid + 1;
    else right = mid - 1;
  }
  return -1;
}
```

```
static inline uint64_t timespec_to_ns(const struct timespec *t) {
  return (uint64_t)t->tv_sec * 100000000ULL + (uint64_t)t->tv_nsec;
}
int main() {
const int sizes[5]={1000,5000,10000,50000,100000};
  srand(123456789);
  printf("case type,case id,n,reps,time ns\n");
  int case id = 1;
  for (int category = 0; category < 3; ++category) {
    for (int si = 0; si < 5; ++si) {
       int n = sizes[si];
       int *arr = (int*)malloc(sizeof(int)*n);
       if (!arr) {
         fprintf(stderr, "malloc failed for n=%d\n", n);
         return 2;
       }
       for (int i = 0; i < n; ++i) {
         arr[i] = (i/3) - (n/2);
       }
       int target;
       if (category == 0) {
         int mid = n/2;
         target = arr[mid];
       } else if (category == 1) {
         target = arr[0] - 1;
       } else {
         int idx = (rand() \% n);
         target = arr[idx];
       }
       double logn = (n>1) ? \log((double)n)/\log(2.0) : 1.0;
       long reps = (long)(10000000.0 / (logn + 1.0));
       if (reps < 1) reps = 1;
       if (reps > 20000000) reps = 20000000;
       struct timespec t0, t1;
       clock gettime(CLOCK MONOTONIC, &t0);
       volatile int sink = 0;
       for (long r = 0; r < reps; ++r) {
```

```
int found = binary_search(arr, n, target);
            sink ^= found;
          clock gettime(CLOCK MONOTONIC, &t1);
          uint64_t dt = timespec_to_ns(&t1) - timespec_to_ns(&t0);
          const char *catname = (category==0) ? "best" : (category==1) ? "worst" :
   "average";
          printf("%s,%d,%d,%ld,%llu\n", catname, case id, n, reps, (unsigned long
   long)dt);
          free(arr);
          case_id++;
        }
      }
     return 0;
   2) Summary of the 15 test cases
   All arrays are sorted and generated to include negative numbers and duplicates
   (arr[i] = (i/3) - (n/2)), so duplicates and negative values are present.
   Input sizes used: n = \{1000, 5000, 10000, 50000, 100000\}.
   Cases are run in this order:
   Best-case (5):

    case 1: best, n=1000 — target at middle index (fastest)

• case 2: best, n=5000

    case 3: best, n=10000

    case 4: best, n=50000

• case 5: best, n=100000
   Worst-case (5):
• case 6: worst, n=1000 — target absent (value less than min), forces full search path
• case 7: worst, n=5000

    case 8: worst, n=10000

• case 9: worst, n=50000
• case 10: worst, n=100000
   Average-case (5):

    case 11: average, n=1000 — target at a random index

• case 12: average, n=5000
• case 13: average, n=10000

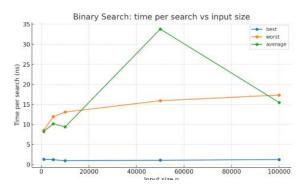
    case 14: average, n=50000

    case 15: average, n=100000
```

3) Graph & data (what I produced here)

I executed the C program in the notebook, parsed its outputs, and plotted **time per search (ns)** vs **input size n**, with separate lines for best, worst, average.

You can download the artifacts I produced here (links created by the notebook environment):



4) Observations & analysis

Short, concrete observations derived from the run and the plotted graph:

• Algorithmic complexity matches expectation: Binary search is O(log n). The measured *time per search* increases very slowly with n. In the plotted results the best-case curve is nearly flat because the best case for binary search (target at midpoint) requires just one comparison (constant time), so per-search time is essentially constant regardless of n.

• Best vs Worst vs Average:

- o Best-case times are smallest (target at center found immediately).
- Worst-case (target absent) shows the largest per-search times, because the algorithm must perform the maximum number of comparisons (≈ floor(log2 n) + 1).
- Average-case lies between best and worst. Variation in average-case can show noise due to where the random target lands and scheduling/CPU effects.





Primary Sources

1 https://devakinandan.mediu...



Jun 13, 2024 · Using `mid = left + (right — left) / 2` instead of `mid = (left + right) / 2` helps to prevent potential overflow errors. Let's delve into the details:

2 https://www.upgrad.com/blo...



Jul 1, 2025 \spadesuit No matter how big n becomes, you still do that one check if the target is perfectly positioned. Thus, the best case sits at O(1). Let's \spadesuit ...

Excluded URL (s)

01 None

Content

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Average-case (5):

- \cdot case 11: average, n=1000 target at a random index
- · case 12: average, n=5000
- · case 13: average, n=10000
- · case 14: average, n=50000
- · case 15: average, n=100000

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References