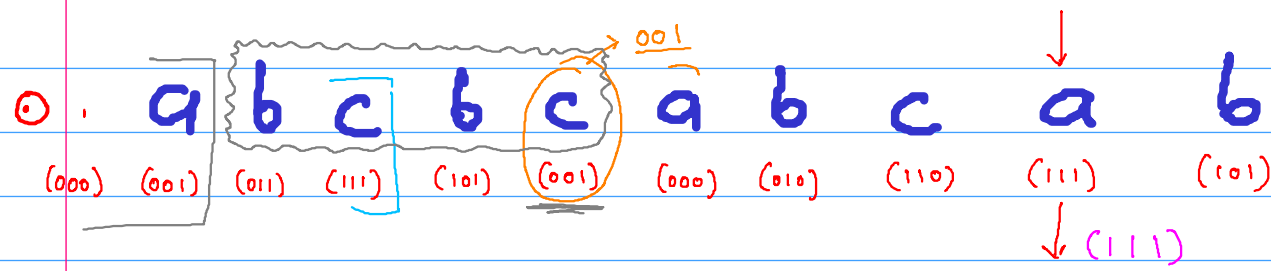


i → a b c  
0/e 0/e 0/e  
odd = 1  
even = 0

a b c



c → even  
b → even  
a → odd  
a even  
b even  
c even

a → odd → odd  
b → odd → odd  
c → odd → odd

odd - odd = even

odd - odd/even = even

$2m+1 - (2m+1) = 2(n-m)$  even

odd - even

$2m+1 - 2n = 2(m+n)+1$   
odd

INT Hash = 0; ans = 0;

```
MP[0] = 1;
for (auto c: s) {
    Hash ^= (1 << (c - 'a'));
    ans += MP[Hash]; MP[Hash]++;
}
return ans;
```

for (i = 0 - n)  
for (j = i - n)  
// for (i - j) even  
ans++;  
Time:  $O(n^3)$   
Space:  $O(1)$

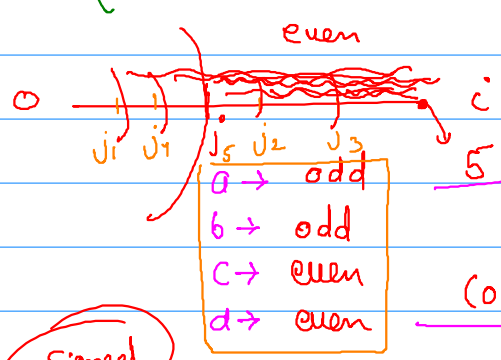
a b c b c d a d

for (i = 0 - n)  
for (j = i - n)  
if (even) ans++;  
Time:  $O(n^2)$   
Space:  $O(1)$

a b c d  
i (0 0 e e)

0 ————— i  
{ a → odd  
b → odd  
c → even  
d → even

{ odd → 1  
even → 0



(i)  
hash ^= (1 << (i \* h))

ans  
{ 0^1 = 1  
1^1 = 0 }  
int

Signed  
(31)  
32 31 ... 2 1 0

# 1915. Number of Wonderful Substrings

Medium 616 44 Add to List Share

A **wonderful** string is a string where **at most one** letter appears an **odd** number of times.

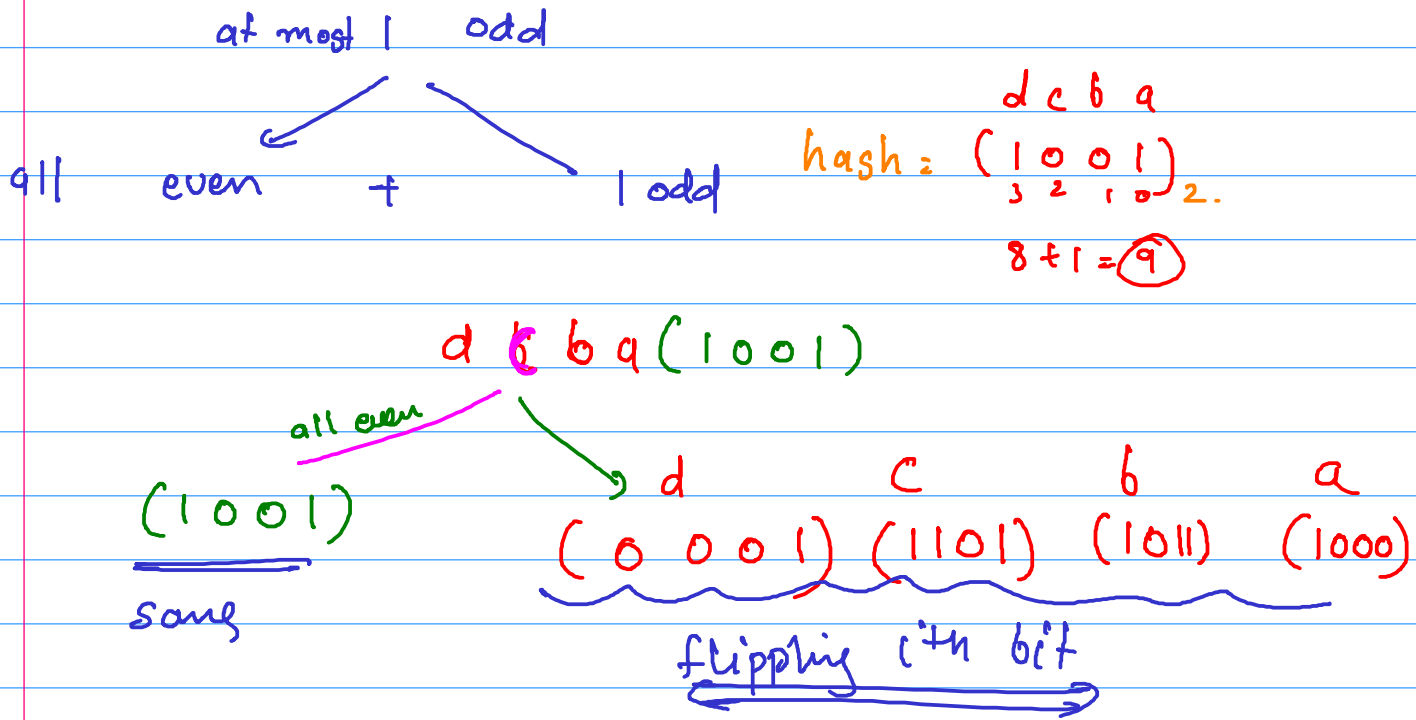
- For example, "ccjjc" and "abab" are wonderful, but "ab" is not.

Given a string `word` that consists of the first ten lowercase English letters ('a' through 'j'), return the **number of wonderful non-empty substrings** in `word`. If the same substring appears multiple times in `word`, then count **each occurrence** separately.

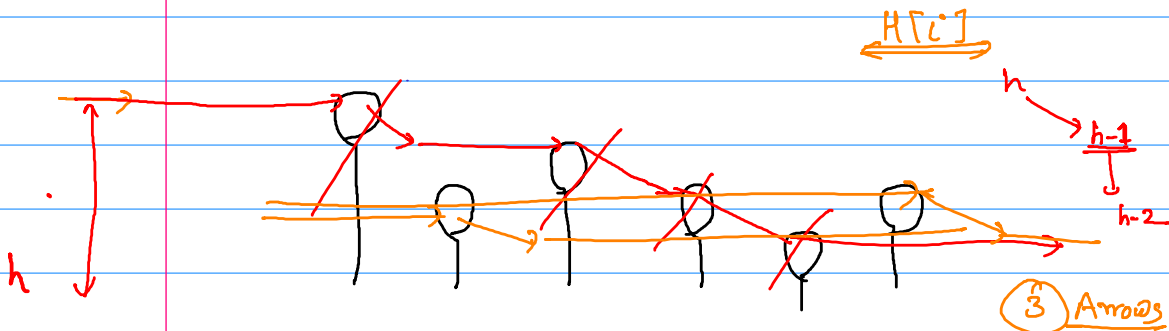
A **substring** is a contiguous sequence of characters in a string.

Example 1:

```
Input: word = "aba"
Output: 4
Explanation: The four wonderful substrings are underlined below:
- "aba" -> "a"
- "aba" -> "b"
- "aba" -> "a"
- "aba" -> "aba"
```



Q. [4 2 3 2 1 2]



[1, 2, 3, 4] = '4', [4, 3, 2, 1] = '1'

$[4, [4], 3, [2], 1, 2]$

$\text{int} \rightarrow \text{set} < >$   
 $\text{int} \rightarrow \text{set} < >$  indices.  
 $\downarrow$   $\text{standby. removal}$   
 $\text{sign. sign.}$   
 $[4] \rightarrow (x, 1)$   
 $[3] \rightarrow (x)$   
 $[2] \rightarrow (x, 5)$   
 $[1] \rightarrow (x)$

$[4] \rightarrow \cancel{x} 1$

$[3] \rightarrow \cancel{x} 0$

$[2] \rightarrow \cancel{x} 0$

$[1] \rightarrow 1$

$[2] \rightarrow 1$

$= 3$  Answers

$[4, [3], 2, [3], 2, 4]$

$\text{ans} = 1 + 1 + 1$

ans: 3

$[4] \rightarrow \cancel{x} 1$

$[3] \rightarrow \cancel{x} \cancel{x} \cancel{x} 0$

$[2] \rightarrow \cancel{x} 2$

Q. Given <sup>binary</sup> array. find maximal length subarray containing equal No. of 1s & 0s.

$[1, 1, 0, 1, 1, 0, 1, 0, 1, 1]$

$0 \rightarrow (-1)$

$\left( \begin{array}{l} 3 \rightarrow 1s \\ 2 \rightarrow 0s \end{array} \right)$   
 $\left( \begin{array}{l} 2 \rightarrow 1s \\ 1 \rightarrow 0s \end{array} \right)$

$[1, 1, -1, 1, 1, -1, 1, -1, 1, 1]$

$\Downarrow$   
(Largest subarray with sum = 0)

Q. Given a binary matrix find largest rectangle in matrix having equal No. of 1's & 0's and return its area.

1	0	1	1	0
1	0	1	0	1
1	1	1	1	1
0	1	1	0	0
0	1	1	1	1

②

1	-1	-1
1	-1	-1

1	0	0
1	0	1
1	1	0

$R_1 \rightarrow$   
 $R_2 \rightarrow$

0	0	0
1	-1	-1
2	-2	0
3	-1	-1

③

2	-2	0
---	----	---

Maximum length  
Sub array, sum = 0

$3 \times 2 = 6$

Time:  $O(N^3)$   
 Space:  $O(N) \rightarrow$  HashMap

$1 \leq N \leq 100$
$1 \leq M \leq 100$

# STACK & Queue:

STACK : LIFO

↳  
PUSH  $\rightarrow O(1)$   
POP  $\rightarrow O(1)$   
Top  $\rightarrow O(1)$

Arrays:

① Arrays:

② Linked list

③ 2-Queue

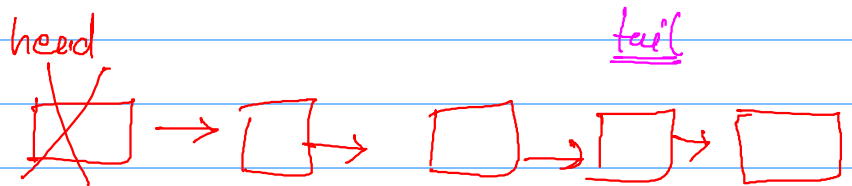
(top  
Arr)



pop head = head  $\rightarrow$  next

Queue

Linked list

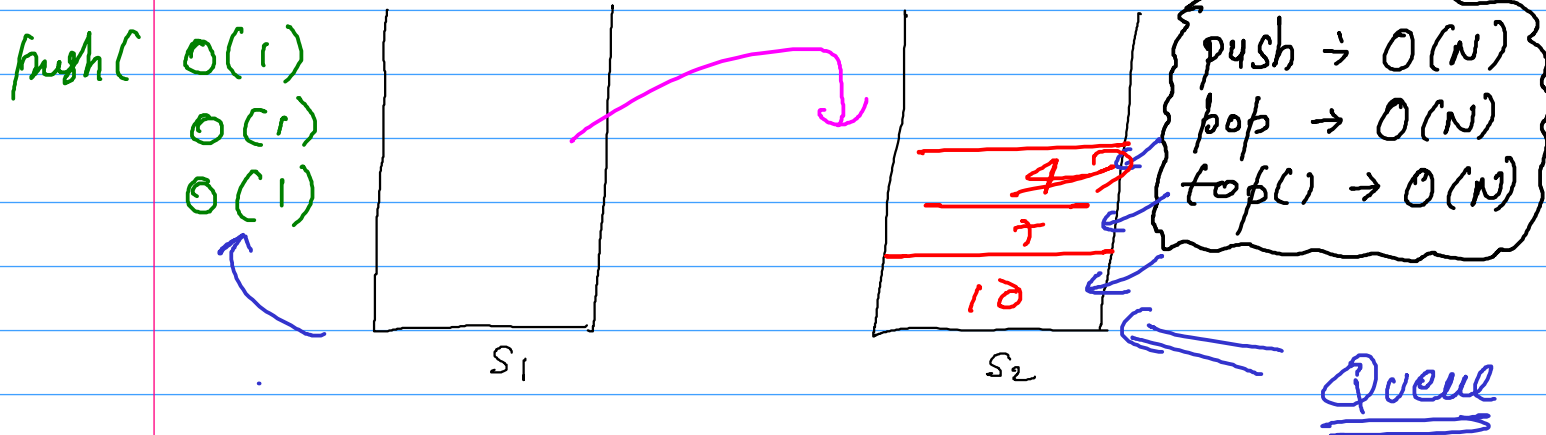


== x == x == x == x ==

Implemented Queue using 2 stacks that  
support INSERT() DELETE() FRONT()  
(w/o using any extra variable);

S.poll()

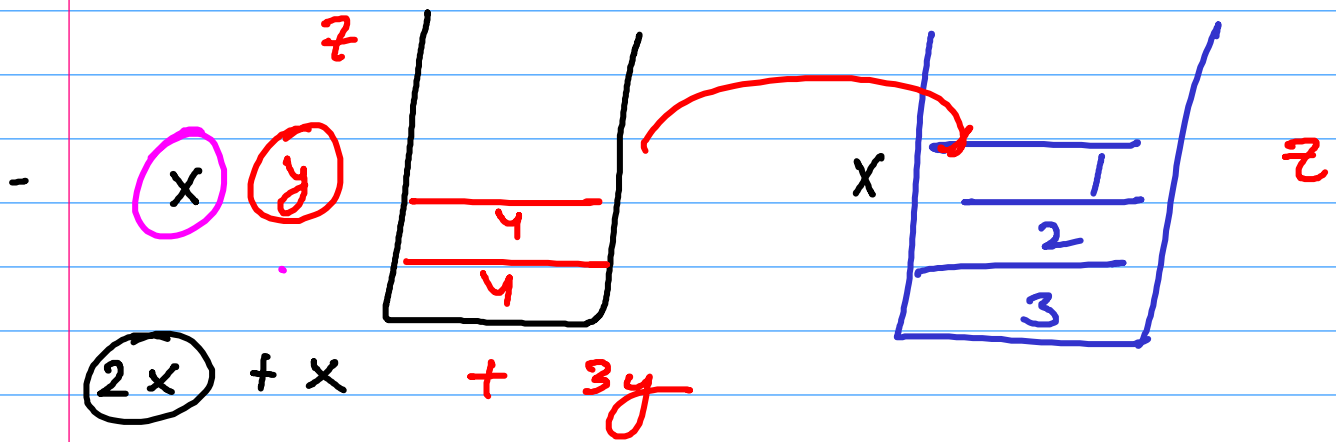
$push(1) \rightarrow push(2) \rightarrow push(3) \rightarrow pop() \rightarrow pop()$  FRONT  
 $push(4) \rightarrow push(7) \rightarrow pop() \rightarrow push(10) \rightarrow pop() \rightarrow pop()$



$O(N) \rightarrow N$  pop Constant

pop & front: Amortized T.C.  $O(1)$

push  $O(1)$

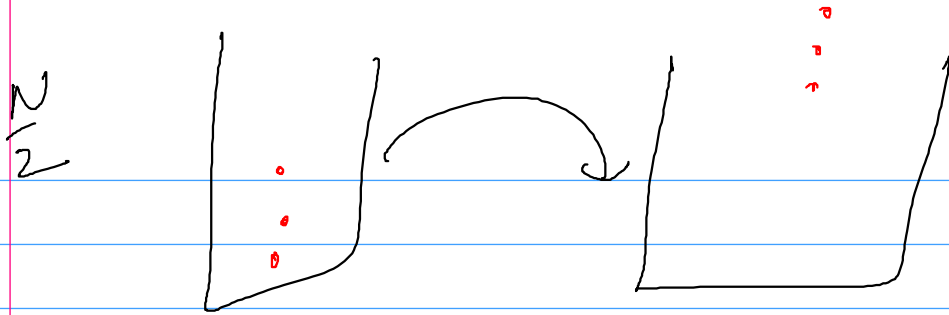


$$\frac{N}{2} + \left( \frac{N}{2} \times \frac{N}{2} \right) \frac{N^2}{4} x + x = 3(x)$$

$3(4)$   
 $3(2)$

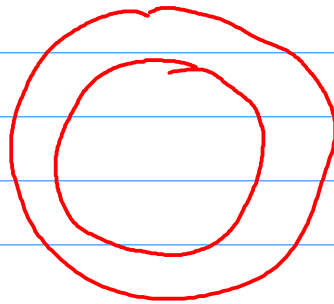
$3(x_1 + y + z + \dots)$

$$\frac{N^2}{2} + \left( \frac{N}{2} \right) \left( \frac{N}{2} \right) 3(N) = O(N) \approx O(N)$$



$$\begin{aligned}
 & \xrightarrow{\quad} \frac{N}{2} + \frac{N}{2} + \frac{N}{2} + \frac{N}{2} + O(1) + O(1) + O(1) + O(1) \\
 & \approx \underline{O(2N)}
 \end{aligned}$$

① Circular Queue:  
 ↓  
 Array



= x = x = x = y =

```

merge(l, r, A)
{
    if (l == r) return;
    mid = (l + r) / 2; // O(1)
    merge(l, mid, A); // O(N)
    merge(mid + 1, r, A); // O(N)
    merge(l, mid, r, A); // O(N)
}

```

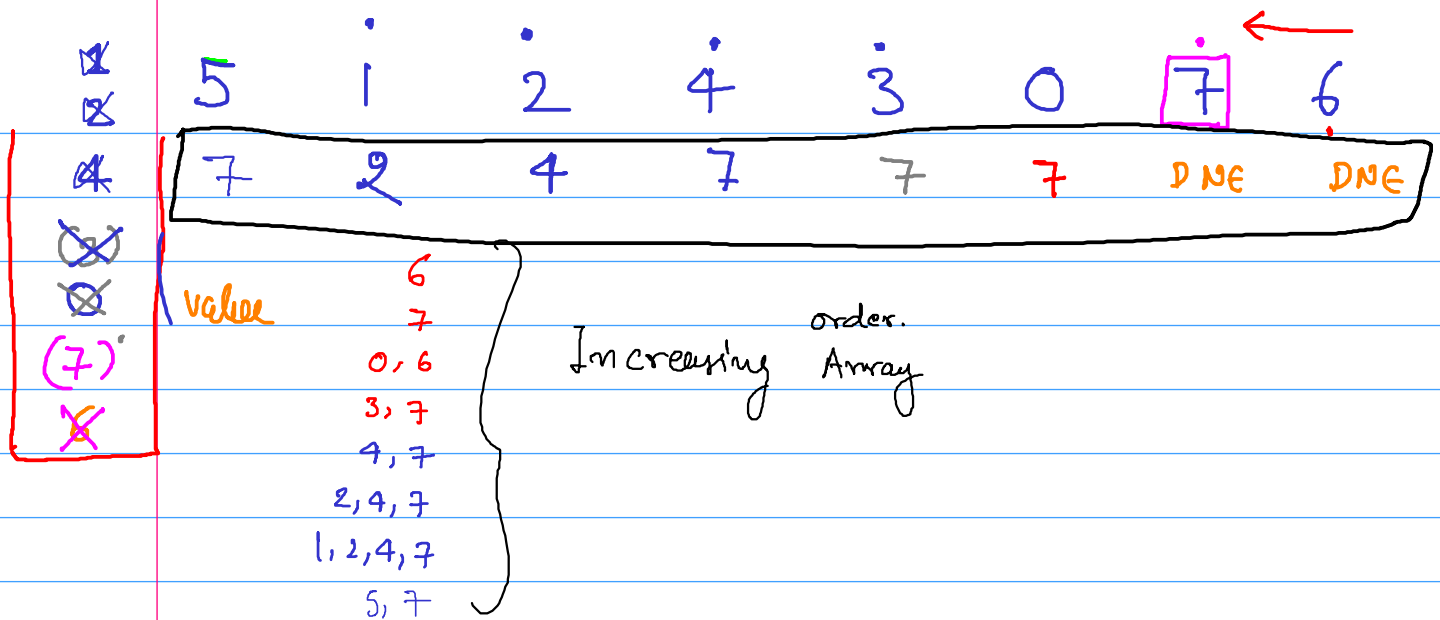
Valid parentheses:

{ }, [ ], ( )

( )

① Next - Greater Element in An array.

	0	1	2	3	4	5	6	7	8
Array:	5	1	2	4	3	0	7	6	INF
	6	2	3	6	6	6	8	8	
	(7)	(2)	(4)	(7)	(7)	(7)	(INF)	(INF)	



```

Stack <int> s; // Indices.
Vector<int> NG(N);
for (int i = n-1; i >= 0; i--) {
    while (!s.empty() and A[s.top()] <= A[i])
        s.pop();
    if (s.empty()) NG[i] = N;
    else NG[i] = s.top();
    s.push(i);
}

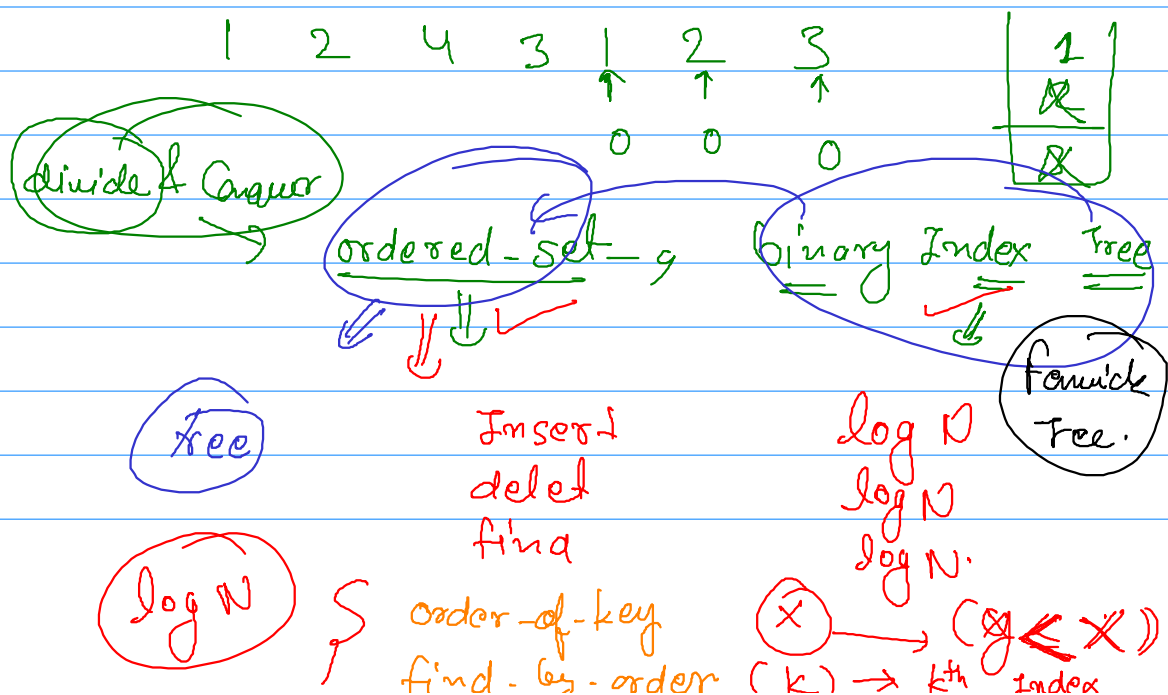
```

Time:  $O(N)$

Space:  $O(N)$

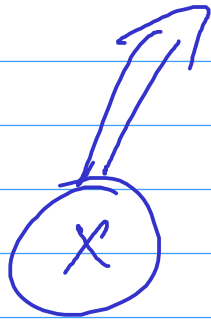
Stack

①





[ 1 2 4 3 1 2 3 ]



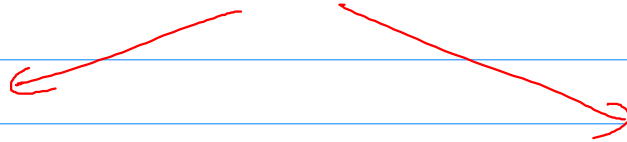
$A[i] > A[j]$   $i < j$

[ 1, 2, 4, 3, 1, 2, 3 ]

ans [ 1 2 1 0 ]  
~~1 2 1 0~~

[ 4, 3, 2, 1 ]

(4,0) (3,1) (2,2) (1,3) { 3, 2, 1, 0 }



[ (4,0) (3,1) ]

[ (2,2) (1,3) ]

{ [(4,0)] [(3,1)] }

{ [(2,2)] [(1,3)] }

{ [(3,1), (4,0)] }

{ [(1,3), (2,2)] }

[ (1,3), (2,2), (3,1), (4,0) ]

(3,1) (4,0)

(1,3) (2,2)

i=0

j=0

```

32 void merge(int l, int r, vector<pair<int,int>> &arr){
33     if(l >= r) return;
34     int mid = (l + r) / 2;
35     merge(l, mid, arr);
36     merge(mid + 1, r, arr);
37     Count(l, mid, r, arr);
38 }
39 vector<int> countSmaller(vector<int>& nums) {
40     int n = nums.size();
41     ans.resize(n, 0);
42     vector<pair<int, int>> arr(n);
43     for(int i = 0; i < n; i++){
44         arr[i] = make_pair(nums[i], i);
45     }
46     merge(0, n - 1, arr);
47     return ans;
48 }
49 };
50
2 public:
3     vector<int> ans;
4     void Count(int l, int mid, int r, vector<pair<int,int>> &arr){
5         int sz1 = mid - l + 1;
6         int sz2 = r - mid;
7         vector<pair<int,int>> a(sz1);
8         vector<pair<int,int>> b(sz2);
9         for(int i = l; i <= mid; i++) a[i - l] = arr[i];
10        for(int i = mid + 1; i <= r; i++) b[i - (mid + 1)] = arr[i];
11        int i = 0, j = 0;
12        while(i < sz1){
13            if(j < sz2 and a[i].first > b[j].first){
14                j++;
15            } else{
16                ans[a[i].second] += j;
17                i++;
18            }
19        }
20        i = 0; j = 0;
21        int k = l;
22        while(i < sz1 and j < sz2){
23            if(a[i].first < b[j].first){
24                arr[k++] = a[i++];
25            } else{
26                arr[k++] = b[j++];
27            }
28        }
29        while(i < sz1) arr[k++] = a[i++];
30        while(j < sz2) arr[k++] = b[j++];
31    }

```

Description Solution Discuss (435) Submissions

### 907. Sum of Subarray Minimums

Medium 3448 230 Add to List Share

Given an array of integers `arr`, find the sum of  $\min(b)$ , where `b` ranges over every (contiguous) subarray of `arr`. Since the answer may be large, return the answer **modulo**  $10^9 + 7$ .

#### Example 1:

Input: `arr = [3,1,2,4]`

Output: 17

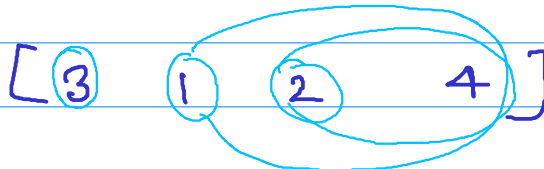
Explanation:

Subarrays are `[3]`, `[1]`, `[2]`, `[4]`, `[3,1]`, `[1,2]`, `[2,4]`, `[3,1,2]`, `[1,2,4]`, `[3,1,2,4]`.

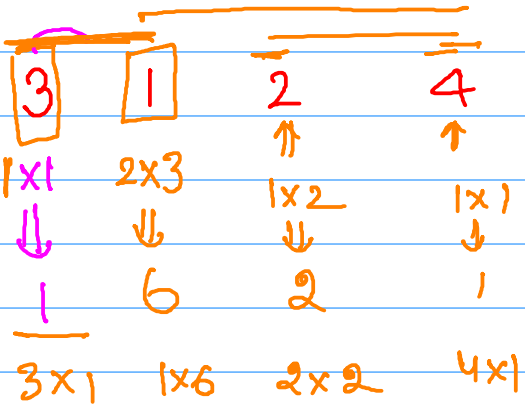
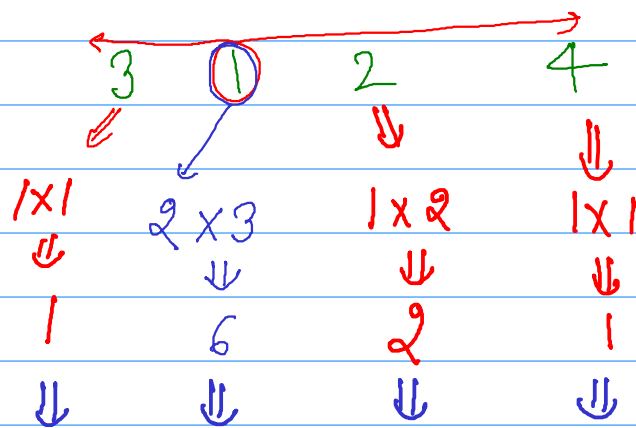
Minimums are 3, 1, 2, 4, 1, 1, 2, 1, 1, 1.

Sum is 17.

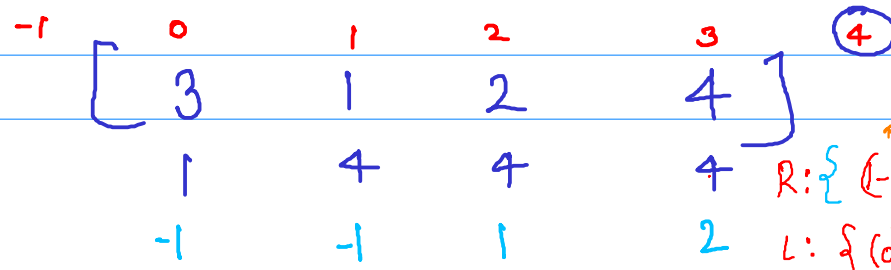
#### Example 2:



$\{a_0, a_1, a_2, a_3, a_4\}$   
 $3 \times 3 = 9$   
 $2 \times 4 = 8$



$3 \times 1 + 1 \times 6 + 2 \times 2 + 4 \times 1 = 3 + 6 + 4 + 4 = 17$



Next S  
Pre S

$R: \{(-0), (4-1), (4-2), (4-3)\}$   
 $L: \{(0-1), (1+1), (2-1), (3-2)\}$

$$R \times L \{ 1 \times 1 \quad 3 \times 2 \quad 2 \times 1 \quad 1 \times 1 \}$$

$$3 \times 1 + 1 \times 6 + 2 \times 2 + 1 \times 1 = 3 + 6 + 4 + 1 = 14$$

Q1 Circular Array Next Greater:

↓  
1, 2, 1, 1, 2, 1  
(2 -1 2) 2 -1 -1

1, 2, +1  
[2 -1 2]

1, 2, 1

3  
5  
5  
2  
3  
5

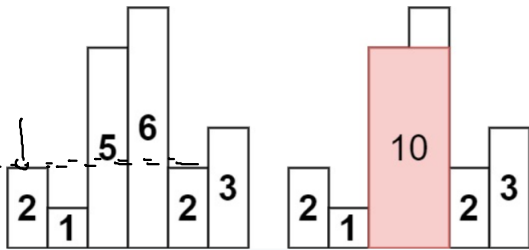
[1, 2, 3, 5, 3, 3, 5, 5, 1]  
2 3 5 -1 5 5 -1 -1 2

#### 84. Largest Rectangle in Histogram

Hard 9818 144 Add to List Share

Given an array of integers `heights` representing the histogram's bar height where the width of each bar is 1, return the area of the largest rectangle in the histogram.

Example 1:



Input: heights = [2,1,5,6,2,3]

Output: 10

Explanation: The above is a histogram where width of each bar is 1.

The largest rectangle is shown in the red area, which has an area = 10 units.

$$\text{Area} = \text{ATi} \cdot (L - R)$$

NS  
PS  
LENGTH  
(R-L-1)

1 0 1 2 3 4 5 6  
2 5 6 2 3  
R: 1 6 4 4 6 6  
L: -1 -1 1 2 1 4  
1 6 2 1 4 1  
2x1 6x6 5x2 6x1 2x4 3x1  
(R-1) (L+1) 10 6 8  
8 2  
R-L+1 = R-1-L-1+1 = (R-L-1)

# 85. Maximal Rectangle

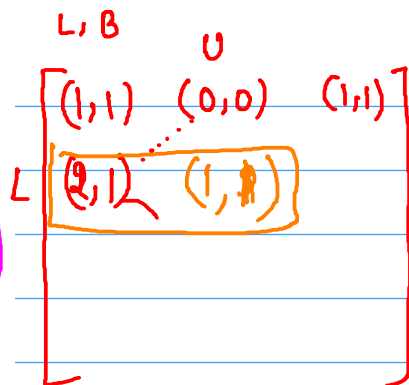
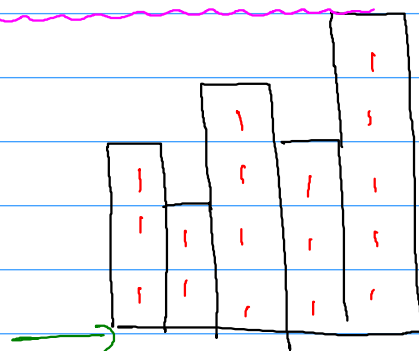
Hard 6555 105 Add to List Share

Given a rows x cols binary matrix filled with 0's and 1's, find the largest rectangle containing only 1's and return its area.

Example 1:

1	0	1	0	0
1	0	1	1	1
1	1	1	1	1
1	0	0	1	0

Input: matrix = [[["1","0","1","0","0"],["1","0","1","1","1"],["1","1","1","1","1"],["1","0","0","1","0"]]  
Output: 6  
Explanation: The maximal rectangle is shown in the above picture.



$$l = 1 + \min(U_L, L_L)$$

$$b = 1 + \min(U_B, L_B)$$

$$X * A[i]$$

$$R_1 \rightarrow (0 - n)$$

$$R_2 \rightarrow (R_1 - n)$$

$$Ans(0 - m)$$

$$O(n^2 \cdot m)$$

$$Space(n \times m)$$

```

1 class Solution {
2 public:
3     int maximalRectangle(vector<vector<char>>& mat) {
4         int n = mat.size();
5         int m = mat[0].size();
6         vector<vector<int>> g(n, vector<int>(m, 0));
7         for(int i = 0; i < n; i++){
8             for(int j = 0; j < m; j++){
9                 g[i][j] = (mat[i][j] == '1');
10                if(i > 0) g[i][j] += g[i-1][j];
11            }
12        }
13        int ans = 0;
14        for(int r1 = 0; r1 < n; r1++){
15            for(int r2 = r1; r2 < n; r2++){
16                int ht = r2 - r1 + 1, c = 0;
17                for(int j = 0; j < m; j++){
18                    int sum = g[r2][j];
19                    if(r1 > 0) sum -= g[r1-1][j];
20                    if(sum == ht) c++;
21                    else c = 0;
22                }
23                ans = max(ans, ht * c);
24            }
25        }
26        return ans;
27    }
28 };

```

$$Time: O(n^2 \cdot m)$$

$$Space O(n \cdot m) \quad g[r_2][0] - g[r_1-1][0]$$

Example 1:

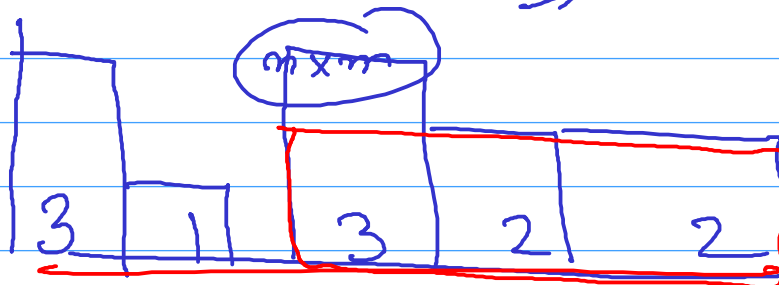
1	0	1	0	0
1	0	1	1	1
1	1	1	1	1
1	0	0	1	0

$$2 \times 3 = 6$$

Example 1:

1	0	1	0	0
1	0	1	1	1
1	1	1	1	1
1	0	0	1	0

1	0	1	0	0
2	0	2	1	1
3	1	3	2	2
4	0	0	3	0



$O(n \times m)$

$O(n \times m)$

$O(n \times m)$

```

28 int maximalRectangle(vector<vector<char>>& mat) {
29     int n = mat.size(), ans = 0;
30     int m = mat[0].size();
31     vector<int> row(m, 0);
32     for(int i = 0; i < n; i++){
33         for(int j = 0; j < m; j++){
34             if(mat[i][j] == '1'){
35                 row[j]++;
36             }else{
37                 row[j] = 0;
38             }
39         }
40         ans = max(ans, getans(row));
41     }
42     return ans;
43 }
44 
```

```

3 int getans(vector<int> &arr){
4     int n = arr.size();
5     vector<int> ns(n, n), ps(n, -1);
6     stack<int> s;
7     for(int i = n - 1; i >= 0; i--){
8         while(!s.empty() and arr[s.top()] >= arr[i])
9             s.pop();
10        if(!s.empty())ns[i] = s.top();
11        s.push(i);
12    }
13    while(!s.empty())s.pop();
14    for(int i = 0; i < n; i++){
15        while(!s.empty() and arr[s.top()] >= arr[i])
16            s.pop();
17        if(!s.empty())ps[i] = s.top();
18        s.push(i);
19    }
20    int ans = 0;
21    for(int i = 0; i < n; i++){
22        int l = ps[i], r = ns[i];
23        int ar = arr[i] * (r - l - 1);
24        ans = max(ans, ar);
25    }
26    return ans;
27 }

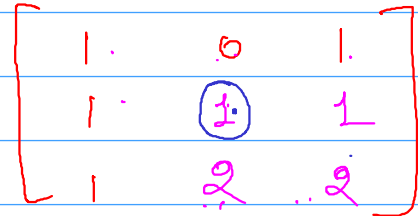
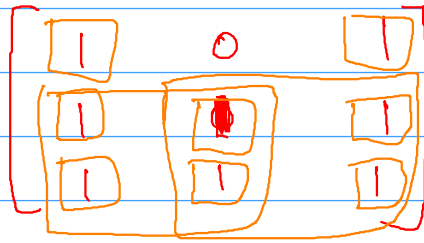
```

Time:  $O(n \times (n + n))$

Space:  $(n + n + n + n)$

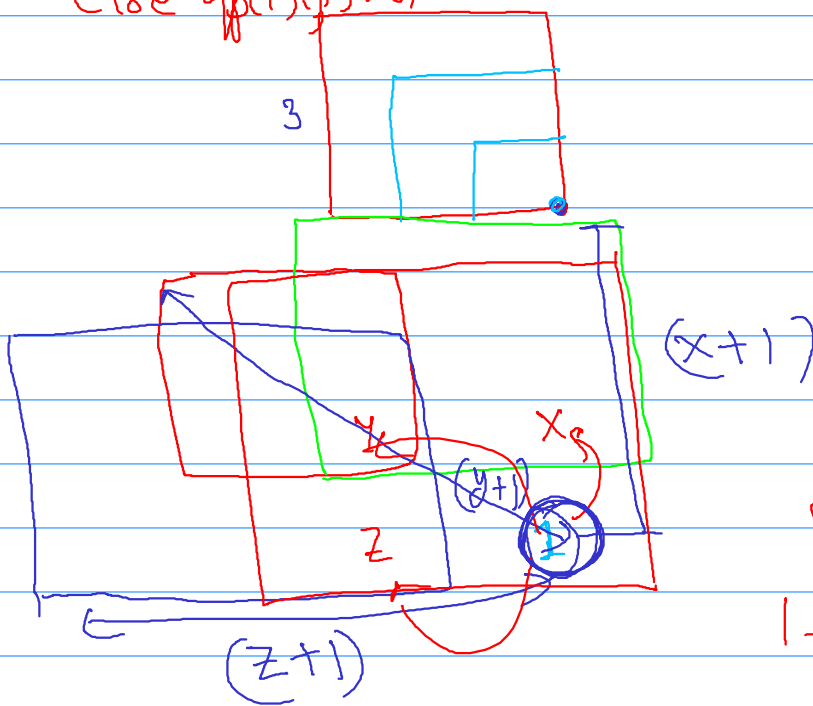
row ns ps stack

Q Count. No. of Square Submatrices containing all ones in a binary matrix.

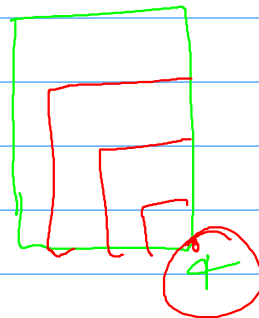


Sum 10

if  $(m(i,j) == 1)$   $dp[i][j] = 1 + \min(dp[i-1][j-1], dp[i-1][j], dp[i][j-1])$   
 else  $dp[i][j] = 0$



$\min(x+1, y+1, z+1)$   
 $1 + \min(x, y, z)$



Q on .. No. of rectangular Submatrices having all ones in a binary matrix.

$$\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

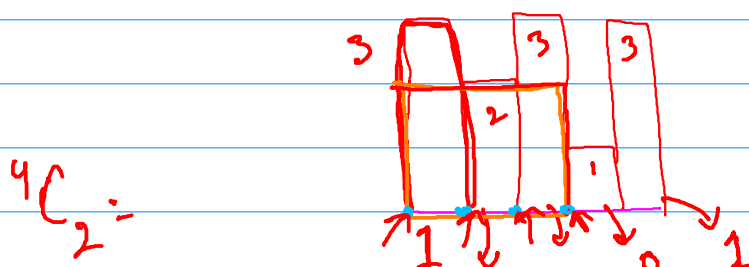
$$1 \leq N, M \leq 100$$

$$O(N \cdot N \cdot M) \quad (10^6)$$

$$\begin{matrix} \rightarrow & \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix} & \begin{matrix} 1 \\ 2 \\ 3 \end{matrix} & \begin{matrix} 0 \\ 1 \\ 2 \end{matrix} \end{matrix}$$

$$1 \leq N, M \leq 1000$$

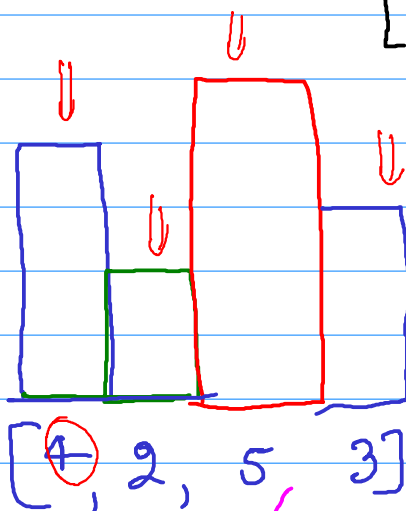
$$10^9 \text{ op}$$



$$4C_2 =$$

$$\frac{4 \times 3}{2} = \left( \frac{3 \times (3+1)}{2} \right) (1+1) (2+1)$$

$$= 7$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$


$$[1, 2, 5, 3]$$

## 155. Min Stack

Easy 7969 617 Add to List Share

Design a stack that supports push, pop, top, and retrieving the minimum element in constant time.

Implement the `MinStack` class:

- `MinStack()` initializes the stack object.
- `void push(int val)` pushes the element `val` onto the stack.
- `void pop()` removes the element on the top of the stack.
- `int top()` gets the top element of the stack.
- `int getMin()` retrieves the minimum element in the stack.

Example 1:

Input

```
["MinStack", "push", "push", "push", "getMin", "pop", "top", "getMin"]
[[], [-2], [0], [-3], [], [], [], []]
```

`stack<int> s;`

`stack<int> minS;`

`s.push(val);`  
`minS.push(min(x, val));`  
`x = min(x, val);`

`getMin() {`  
`return x;`  
`}`  
`pop() {`  
`s.pop();`  
`if (minS.pop());`  
`x = min(x,`  
`x = s.top());`  
`}`

using 1 stack.

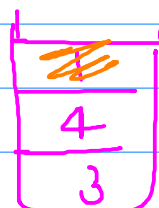
```
int x = -INF;
push(val);
{
    x = min(x, val);
    s.push(val);
    minS.push(x);
}
```

```
getMin() {
    return x;
}
```

```
pop() {
    s.pop();
    minS.pop();
    x = minS.top();
}
```

3 4 1 pop

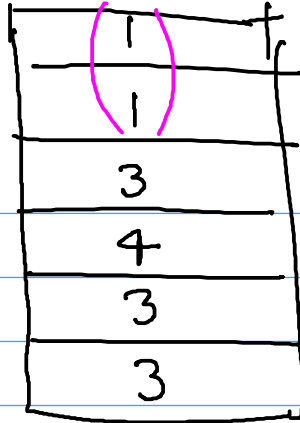
pop()



Min = 1  
 Min = 3



3 4 1



pair < int,

int MinE = ;

```
push(x) {
    if (s.empty()) {
        st.push(x); ✓
        MinE = x;
    }
    else {
        if (x >= MinE) {
            s.push(x); ✓
        }
    }
}
```

} else {

```
{ int nval = 2x - minE;
  s.push(nval); ←
  MinE = x;
}
```

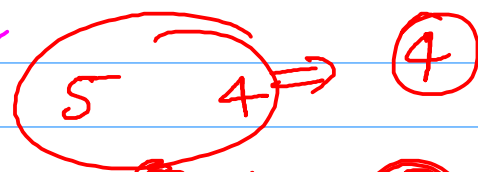
MinE > X

MinE + x > 2x

MinE > X > 2x - minE.

J-

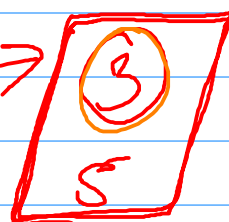
4



8 - 5 = 3

J-

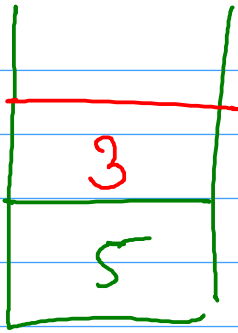
3 < 4



Nval = 2x(X) - MinE.

```
getMin()
return MinE;
```

```
top() { s.top()
    if (s.top() < MinE)
        return MinE;
    return s.top();
}
```



5, 4

MinE = 5

$$= 2 \times 4 - 3$$

$$= 8 - 3 = 5$$

$$8 - 5 = 3$$

MinE = 4

getMin()  
return MinE;

top() ?

if (s.top() < MinE)  
return MinE;  
return s.top();

pop() ?

if (s.top() < MinE) {

MinE = 2 \* MinE - s.top();

}

s.pop();

$$Nval = 2 \cdot x - minVal.$$

$$minE = 2 \times \underset{\substack{\uparrow \\ minE}}{x} - \underset{\substack{\downarrow \\ s.top()}}{Nval}$$

$$2 \times MinE - s.top()$$

$$Min = \underset{min}{2x} - \underset{s.top()}{Nval}$$

$$Min > x$$

$$Min + x > x + x$$

$$Min + x > 2x$$

$$x > 2x - Min$$

$$Nval = 2x - Min$$

$$\text{minE} > x$$

$\text{Nval} < \text{Min}$   $\leftarrow \text{Nval} = 2 * x - \text{Min}$   
 $\text{S.push(Nval)}$   
 $\text{Min} = x;$

$\text{pop() \{}$

$\text{if (S.top() < Min) \{}$

$\text{Min} = 2 * \text{Min} - \text{S.top()}$

$$\text{Nval} = 2 * x - \text{Min}$$

$$\text{Min} = 2 * x - \text{Nval}$$

$\text{S.pop()};$