

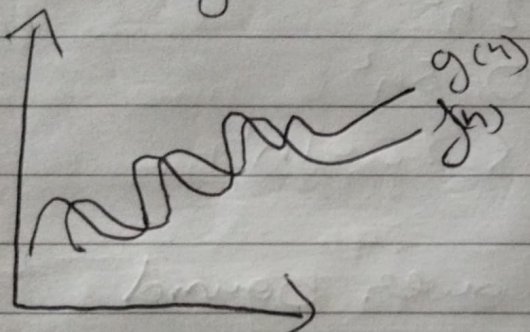
Assignment-1

DAA

→ These notations are used to tell the complexity of an algorithm

→ It describes the algorithm efficiency & performance in a meaningful way.

1) big oh notation - The function $f(n) = O(g(n))$, if & only if there exists a const (C, K) &
 $f(n) \leq C g(n)$ for all $n, n \geq K$



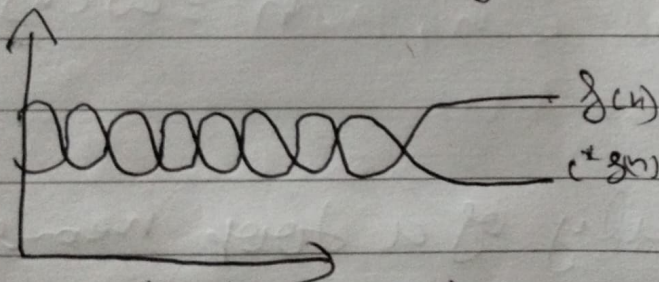
$$f(n) = O(g(n))$$

$$\text{if } f(n) \leq C g(n)$$

$$\forall n \geq n_0$$

so, constant $C > 0$

2) big omega notation - The function $f(n) = \Omega(g(n))$, if there exist a true constant (C, K) such that
 $f(n) \geq C g(n)$ for $n, n \geq K$

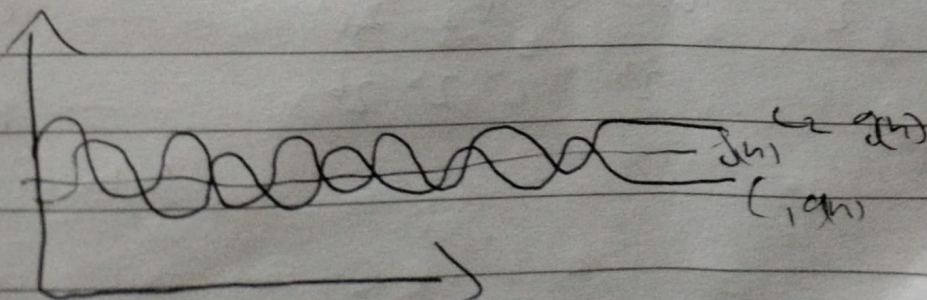


$$f(n) = \Omega(g(n))$$

$$f(n) \geq C \cdot g(n)$$

$$\forall n \geq n_0 \text{ \& } C > 0$$

3) big theta notation
Similarly



$$f(n) = \Theta(g(n))$$

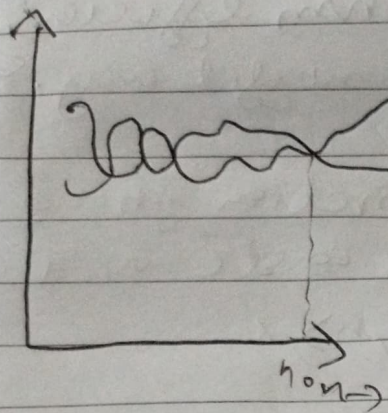
$$\text{if } C_1 g(n) \leq f(n) \leq C_2 g(n)$$

$$\forall n \geq n_0, \max(C_1, C_2)$$

4) Small o notation

$f(n) = o(g(n))$: $g(n)$ is upper bound of $f(n)$ if & only if

$$f(n) < c g(n)$$



$\forall n > n_0$ and for all constants $c > 0$

$$n = o(n^2)$$

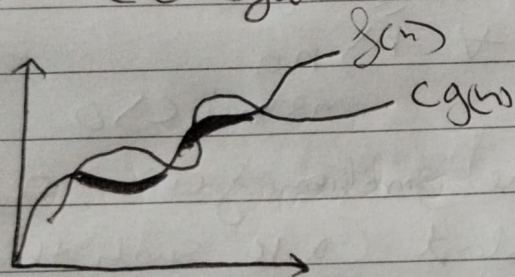
$$n < n^2$$

$$2n^2$$

$$0.5n^2$$

5) Small omega

$$n < o o o n^2 n_0$$



lower bound

$$f(n) = \omega g(n)$$

$$f(n) > c \cdot g(n)$$

$$\forall n > n_0 \quad \forall c > 0$$

$$n^2 = \omega(n)$$

Q2) for $i = 1$ to n

$$\{ \quad i = i \times 2$$

$\}$

\therefore time complexity of a loop means the no of time it was to run

i	1	2	4	8	16	32	-----	2^k
	2^0	2^1	2^2	2^3	2^4	2^5	2^6	n

$i = 1, 2, 4, 8, 16, 32, \dots, 2^k$ this means

k

i.e $2^k = n$

$$k = \log_2 n$$

$$k \log_2 2 = \log_2 n \Rightarrow$$

$$\log_2 2 = 1$$

$$TC = O(\log n)$$

Q3) $T(n) = \begin{cases} 3(T(n-1), n) & n > 0 \\ 1 & n = 0 \end{cases}$

by forward substitution

$$T(n) = 3 T(n-1)$$

$$T(0) = 3(T(-1)) = 0$$

$$T(1) = 3 T(0) = 3$$

$$T(2) = 3 T(1)$$

$$= 3 \times 3 = 9$$

$$T(3) = 3 T(2)$$

$$= 3 \times 9 = 27$$

$$\text{So, } T(n) = 3^n$$

$$TC = O(3^n)$$

Q4) $T(n) = \begin{cases} 2 T(n-1) - 1, n > 0 \\ 1 & n = 0 \end{cases}$

by forward substitution

$$T(0) = 1$$

$$T(1) = 2 T(0) - 1$$

$$= 2 - 1$$

$$T(2) = 2 T(1) - 1$$

$$= 2^2 - 2^1 - 1$$

$$T(3) = 2 T(2) - 1$$

$$= 2^3 - 2^2 - 2^1 - 1$$

$$2^n - 2^{n-1} - 2^{n-2} - 2^{n-3} - \dots - 2^3 - 2^2$$

$$= 2^n - (2^n - 1)$$

$$= 2^n - 2^n + 1 = 1$$

$$TC = O(1)$$


```

5) int i, s = 1;
   while (s <= n)
   {
       i++;
       s = s * i;
       printf("%d\n", i);
   }

```

2e

The value of i increases for each iteration. The value contained in 's' at the i th iteration is the sum of the first i + 1 integers. If k is the total no. of iterations taken by any prog.

$$1 + 2 + 3 + \dots + k$$

$$[k(k+1)/2] > n$$

$$s. k \sim O(\sqrt{n})$$

$$\therefore T.C = O(\sqrt{n})$$

```

(6) void function (int n)
{

```

```

    int i, count = 0;
    for (i = 1; i <= n; i++)
    {
        count++;
    }

```

2e
 $O(n)$ T.C

```

(7) void function (int n)
{

```

```

    int s, k, i, count = 0;
    for (i = n/2; i <= n; i++)
    {
        for (j = 1; j <= n; j = j * 2)
        {
            for (k = 1; k <= n; k = k * 2)
            {
                count++;
            }
        }
    }

```

553

$$TC = \log n * \log n$$

$$= O(n \log n)$$

$$TC = O(n \log n)$$

Q8) function (int n)

```

{
    if (n == 1)
    { return n;
    for (i = 1 to n)
    {
        for (j = 1 to n)
        {
            print j (" * ");
        }
    }
    function (n-3);
}

```

T.C = $O(n^2)$

Q9) void function (int n)

```

{
    for (i = 1 to n) {
        for (j = 1; j <= n; j = j + 1)
        {
            O(n)
            print j (" * ");
        }
    }
}

```

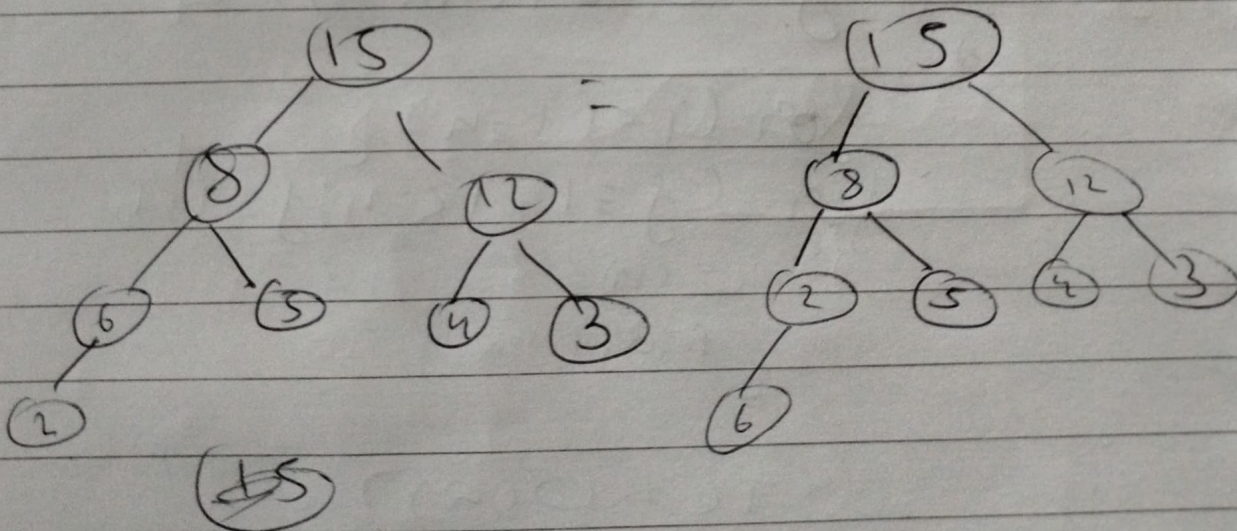
TC = $O(n^2)$

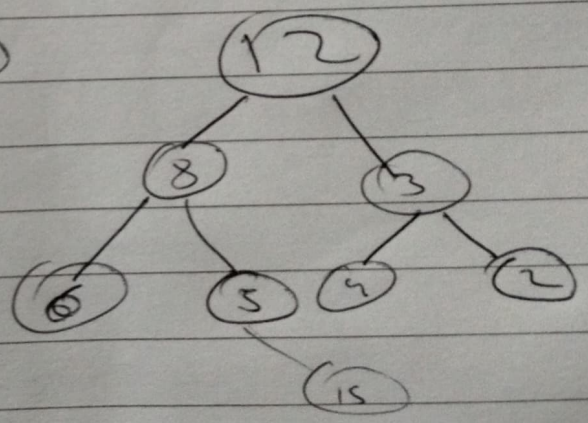
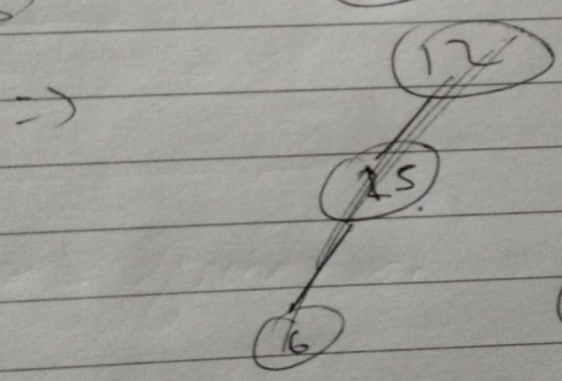
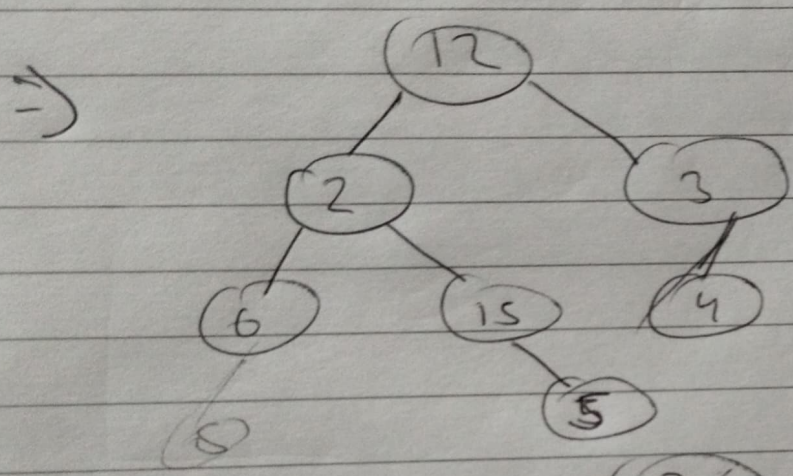
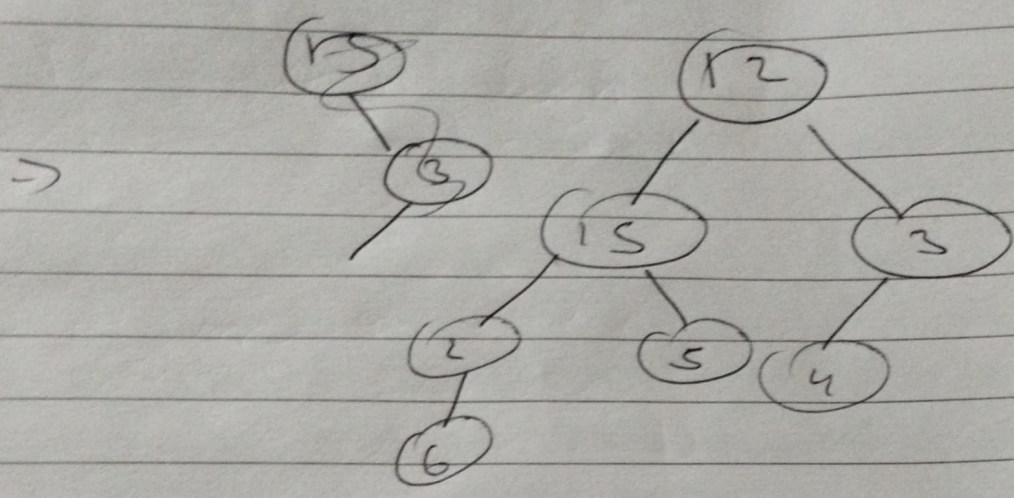
Q10) for the function $n^k \times c^n$, what is asymptotic notations b/w these funcⁿ assume, that $k \geq 1$ & $c > 1$ are const find out the val of c & n which holds n^k is $(O(c^n))$

Q11)

→ The time complexity of 'extractmin()' would depend on the underlying implementation of the data structure. if it's a binary heap, the time complexity would be $O(1)$ as the minimum element is always at the top. if it's a different data structure the complexity may vary.

Q12) Find max heap & del





∴ 15 is max so,

