

tr5frbj 12/08/24

Circuit Theory and Devices

Lab: LT Spice (2nd week onwards)

book: Engineering Circuit Analysis (9th edition)

Relative grading

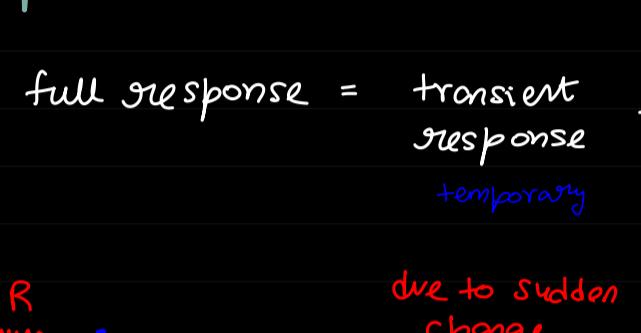
Labs	20%
Quiz	20%
Midsem	30%

Scientific calc

Course: 9 modules chapter 10 onwards
{continuation of BE3}

Lecture 1

⇒ Linear Circuits



System is linear if

$$Kx \rightarrow [\text{sys}] \rightarrow Ky$$

where K is constant

"R" Resistor: linear element ✓
 $V = iR$

"L" Inductor: linear element ✓

$$V = L \frac{di}{dt}$$

"C" Capacitor: linear element ✓

$$i = C \frac{dv}{dt}$$

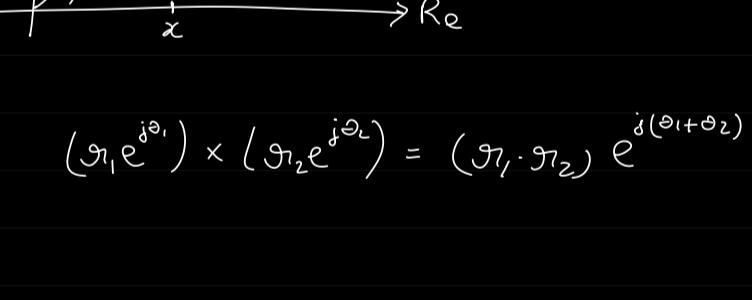
* Linear Electric Circuits:

consists of ⇒

① $R, L, C \rightarrow$ linear elements

② Independent voltage & current sources

③ Linear dependent sources



example would not have been

linear if $V_s = kV_x^2$

Note: diode and transistors are non-linear elements

* TRIGO

$$\sin(-\theta) = -\sin(\theta)$$

$$\cos(-\theta) = \cos(\theta)$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

sin tve All tve

tan tve cos tve

* at $t=0$,

$$(I_1 R + I_2 L - V_m) \cdot 1 + (I_2 R - I_1 L) \cdot 0 = 0$$

$$\boxed{I_1 R + I_2 L = V_m}$$

$$I_1 = \frac{\sqrt{m} R}{R^2 + L} \quad \boxed{I_1 = I_2 \cdot \frac{R}{L}} \Rightarrow \frac{I_1 R + I_2 L}{R^2 + L} = V_m \Rightarrow I_2 = \frac{\sqrt{m} R^2}{R^2 + L}$$

$$\Rightarrow (I_1 R + I_2 L - V_m) \cos(\omega t) + (I_2 R - I_1 L) \sin(\omega t) = 0$$

$$\Rightarrow (I_1 R + I_2 L - V_m) \cos(\omega t) + (I_2 R - I_1 L) \cdot 0 = 0$$

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* Section 10.1

(a) $Q_1 \rightarrow 5\sin(5t - 9^\circ)$

 $t=0 \Rightarrow 5\sin(-9^\circ) = -5\sin(9^\circ) = -0.782$

$t=0.01 \Rightarrow 5\sin(0.05 - 9^\circ) = -5\sin(8.95^\circ) \quad X$

\downarrow
radians

$5\sin\left(\frac{0.05 \times 80}{\pi} - 9^\circ\right) = 5\sin(2.86^\circ - 9^\circ)$
 $\Rightarrow -5\sin(6.14^\circ) = -0.534$

$t=0.1 \Rightarrow 5\sin(0.5 - 9^\circ) = 5\sin(28.64^\circ - 9^\circ) = 5\sin(19.64^\circ)$
 $\Rightarrow 1.6805$

(b) $4\cos 2t$

$t=0 \Rightarrow 4\cos(0) = 4$

$t=1 \Rightarrow 4\cos(2) = 3.997$

$t=1.5 \Rightarrow 4\cos(3) = 3.994$

(c) $3.2 \cos(6t + 15^\circ)$

$t=0 \Rightarrow 3.2 \cos(15^\circ) = 3.09$

$t=0.01 \Rightarrow 3.2 \cos(0.06 + 15^\circ) = 3.2 \cos(3.43^\circ + 15^\circ)$
 $\Rightarrow 3.2 \cos(18.43^\circ)$

$\Rightarrow 3.035$

$t=0.1 \Rightarrow 3.2 \cos(0.6 + 15^\circ) = 3.2 \cos(34.8^\circ + 15^\circ)$
 $= 3.2 \cos(49.8^\circ)$
 $= 2.086$

Q2) (a) $300\sin(628t) \rightarrow 300 \cdot \cos(628t - 90^\circ)$

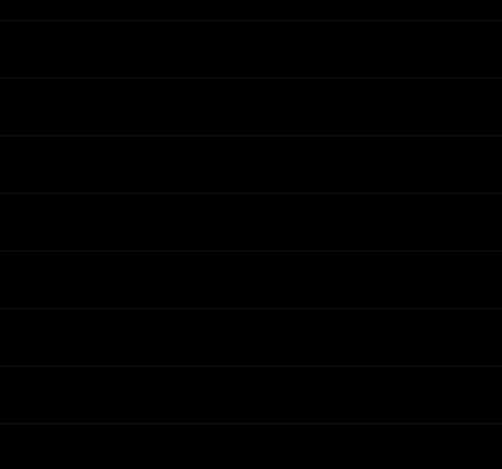
$4\sin(3\pi t + 30^\circ) \rightarrow 4\cos(3\pi t - 60^\circ)$

$14\sin(50t - 8^\circ) - 10\cos 50t \rightarrow$

Q3) $V_L = 10\cos(10t - 45^\circ)$

(a) $i_L = 5\cos 10t$

-45°



⇒ AC Power Analysis {Module: 3}



$$\cos(A) \cos(B) =$$

$$\frac{1}{2} [\cos(A+B) + \cos(A-B)]$$

Instantaneous power: $p(t) = v(t) \cdot i(t)$

$$v(t) = V_m \cdot \cos(\omega t + \theta)$$

$$i(t) = I_m \cdot \cos(\omega t + \phi)$$

$$p(t) = V_m \cdot \cos(\omega t + \theta) \cdot I_m \cdot \cos(\omega t + \phi)$$

$$p(t) = \frac{V_m I_m}{2} \cos(\theta - \phi) + \frac{V_m I_m}{2} \cos(2\omega t + \theta + \phi)$$

constant
(DC term)

twice frequency
(harmonic)

• Average Power

$$P_{avg} = \frac{1}{T} \int_0^T p(t) dt$$

$$= \frac{1}{T} \int_0^T \frac{V_m I_m}{2} \cos(\theta - \phi) dt + \frac{1}{T} \int_0^T \frac{V_m I_m}{2} \cos(2\omega t + \theta + \phi) dt$$

$$P_{avg} = \frac{V_m I_m}{2} \cos(\theta - \phi)$$

\downarrow
real number ✓
phasor ✗

$$\begin{aligned} \mathbf{I} &= I_m e^{j\phi} \\ \mathbf{I}^* &= I_m e^{-j\phi} \end{aligned}$$

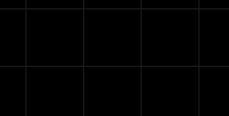
(conjugate)

* Avg. Power absorbed

• by a purely resistive element

$$P_{avg} = \frac{V_m I_m}{2} \cos(\theta - \phi)$$

\downarrow
here, phase diff = 0°



$$P_{avg} = \frac{V_m \cdot I_m}{2} = \frac{I_m^2 R}{2} = \frac{V_m^2}{2R}$$

• by a purely inductive element

$$P_{avg} = \frac{V_m I_m}{2} \cos(\theta - \phi)$$

\downarrow
here, phase diff = 90°



So,

$$P_{avg} = 0 \quad \text{for inductor}$$