

Heavy Weight Adj Set

```
maxwt[0] = 1; maxwt[1] = w[1];  
for i in range(2, len(w)):  
    maxwt = max{maxwt[i-1], maxwt[i-2]  
                + w[i]}  
  
return maxweight[len(w)];
```

this returns the max weight
to get the subset →

```
final = []  
final.add(maxwt[len(w)]) // end element  
for (i = len(w)-2; i ≥ 0; i -= 2) {  
    final.add(maxwt[i+2] - maxwt[i];  
}  
}
```

KNAPSACK PROBLEM

Budget \rightarrow weight constraint
maximize value of the item

Item	1	2	3	4
weight	2	3	4	5
value	3	4	5	6

Budget \rightarrow	0	1	2	3	4	5
Item \downarrow						
0	0	0	0	0	0	0
1	0	0	3	3	3	3
2	0	0	3	4	4	$3+4=7$
3	0	0	3	4	5	7
4	0	0	3	4	5	7

Cost

PROBLEM : edit distance

how similar is 'horse' and 'course'?

h o r s e } for a program these words
c o u r s e } are quite different

if we ignore the column with u when writing horse

c o u r s e
h o r s e

now only two cols dont match out
of six

Levenshtein (Edit) distance

given: 2 strings

edit distance \rightarrow # of operations needed
to transform one string to another

operations: add
delete
replace

minimize #
of operations

eg: horse and rose

rose \rightarrow horse

①	oose	②	orse	③	horse
	R		R		A

horse \rightarrow rose

①	rorse	②	rose
	R		D

$\text{Edist}(A, B, i, j) \rightarrow$ # of operations needed
to transform $A[0:i] \rightarrow B[0:j]$

if $(A[i] == B[j]) \{$

$\text{Edist}(A, B, i, j) = \text{Edist}(A, B, i-1, j-1);$

$\} \text{ else } \{$

$\text{Edist}(A, B, i, j) = 1 + \min \{$

$\text{Edist}(A, B, i, j-1),$

$\text{Edist}(A, B, i-1, j),$

$\text{Edist}(A, B, i-1, j-1)$

$\}$

$\}$

1	2	3	4	5	6	7
	"	h	o	r	s	e
2	"	o	1	2	3	4
3	r	1	¹⁺⁰ 1	¹⁺¹ 2	2	3
4	o	2	2	1	2	3
5	s	3	3	2	2	2
6	e	4	4	3	3	2

The first col and row of cost array should be the base case

Running time: $m \times n$
(size of cost matrix)

↖ replace
← delete
↖ nothing

Optimization: for taking space less than $(m \times n)$ we can just keep track of current row and the row above

if we also want the steps taken, we can have an arr of max $(m+n)$ size to do back keeping

KT \rightarrow Chp 6.6

Jeff \rightarrow Chp 3.7