

MOSFET

LEC-12

18/03/25

↓
metal oxide semiconductor field effect transistor

4 terminal

↳ Gate

→ Drain

→ Source

→ Body

NMOS MOSFET

↳ S and D

are heavily doped

n type

↳ p type substrate
(body)

NFET → NMOS

PFET → PMOS

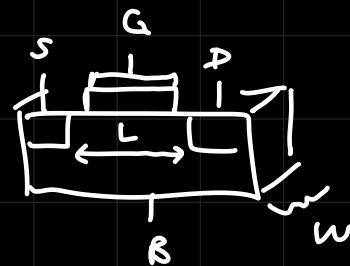
Gate: metal / p-crystalline

2 regions: p type substrate and S, D n type doped

SiO_2 : gate oxide

channel length: L

width: w

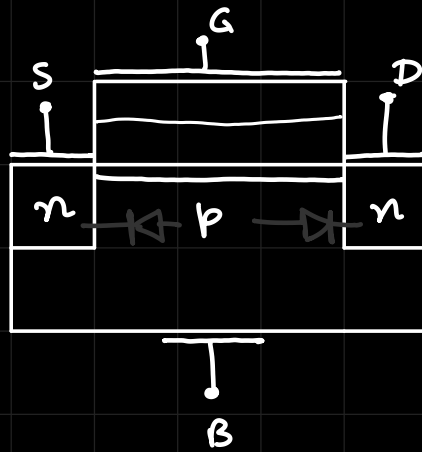


L : 0.1 - 3 μm

8 nm

w : 0.2 - 100 μm

0.2 - 100 nm



at equilibrium, no current flows between S and D

for inducing a channel btw S and D

a positive voltage is applied at gate terminal: V_{GS}

but still no current flows unless there is a potential difference between S and D

Inversion Layer

for NMOS \rightarrow free e^- due to p type substrate

$V_{GS} > V_T$: threshold voltage for current flow btw S and D

$V_{GS} \uparrow \rightarrow$ inversion layer width \uparrow

overdrive voltage : $V_o = V_{GS} - V_T$

enhancement type MOSFET

① Cutoff mode :

$$0 < V_{GS} < V_T$$

$$\sim 0.2 - 0.5V$$

assumption: $V_{SB} = 0$

② $0 < V_{GS}$, $V_{GS} > V_T$, $V_{DS} = 0$

enhancement type MOSFET

no current flow

channel created

③ $0 < V_{GS}$, $V_{GS} > V_T$, $0 < V_{DS} < (V_{GS} - V_T)$

I_D current from D \rightarrow S flows

proportional to V_{DS}

$$I_D \propto V_{DS}$$

drain
current

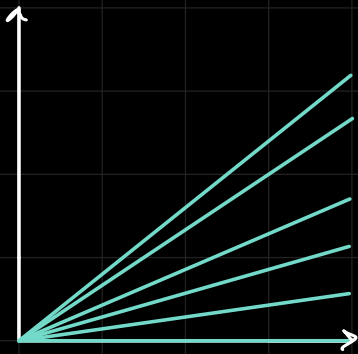
voltage controlled resistance

triode mode / linear mode

because of SiO_2 gate oxide $\rightarrow I_G = 0$

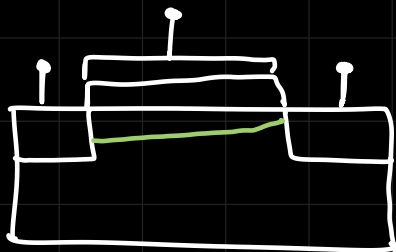
$$R_D = \frac{V_{DS}}{I_D}$$

Characteristic



for small $V_{DS} \rightarrow V_{DS} < V_{GS} - V_T$
triode mode / linear mode
 $I_D \approx 0$

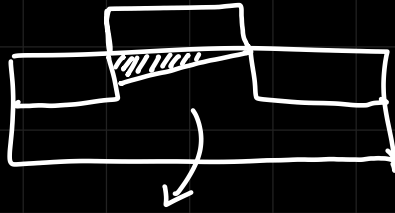
but for $V_{DS} > V_{GS} - V_T$
the Gate will attract free e^-
alongside Drain
 $I_D \neq 0$



The channel/
inversion layer's
width tapers

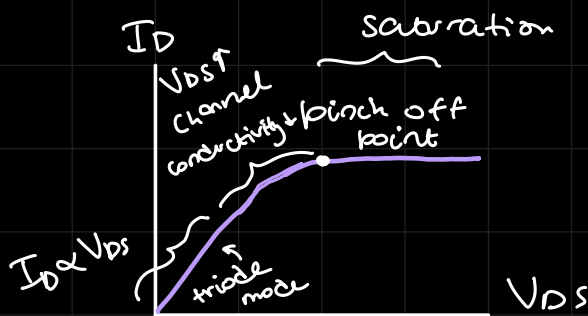
at very high V_{DS} ,
 I_D becomes constant

pinch off situation



pinch off region

no more increase in I_D with V_{DS}



cutoff mode

$$I_D = 0$$

$$V_{GS} - V_T < 0$$

$V_C(x)$: channel voltage wrt source
at position x

effective voltage inducing the channel

$$\text{at } x \rightarrow V_{GS} - V_T - V_C(x)$$

V_0

V_0

net charge within narrow dx strip:

$q = CV$

$$dq = \overset{\text{fm}^{-2}}{\underbrace{-C_{ox}(Wdx)}_{\substack{\text{e}^- \\ \text{charge} \\ \text{(NMOS)}}}} \underbrace{(V_{GS} - V_T - V_c(x))}_{\substack{\text{net capacitance} \\ \text{net potential}}}$$

\vec{E} by V_{DS} is in $-x$ direction

$$\vec{E}(x) = -\frac{dV_c(x)}{dx}$$

net mobility constant: μ_n
of charge carriers

$$\text{Velocity } \left(\frac{dx}{dt} \right) = \mu_n E(x)$$

$$-\frac{dq}{dt} = \left(-\frac{dq}{dx} \right) \times \left(\frac{dx}{dt} \right)$$

$$I_D(x) = W C_{ox} [V_{GS} - V_T - V_c(x)] \mu_n \frac{dv}{dx}$$

at a point x

for the entire channel \rightarrow integrate from $0 \rightarrow L$

$$\int_0^L I_d dx = \int_{v=0}^{v=V_{DS}} W C_{ox} [V_{GS} - V_T - V_c(x)] \mu_n \frac{dV_c(x)}{dx} dx$$

$$I_D \cdot L = \mu_n \cdot C_{ox} \cdot W \left([V_{GS} - V_T] V_{DS} - \frac{V_{DS}^2}{2} \right)$$

$$I_D = \mu_n \cdot C_{ox} \cdot \frac{W}{L} \left[(V_{GS} - V_T) V_{DS} - \frac{V_{DS}^2}{2} \right]$$

→ At pinch off → $V_{DS} = V_{GS} - V_T$

$$I_{D_{max}} = \frac{1}{2} \mu_n \cdot C_{ox} \cdot \frac{W}{L} [V_{GS} - V_T]^2$$

→ for triode mode: $V_{DS} \ll$

$$\text{So, } I_D = \mu_n \cdot C_{ox} \cdot \frac{W}{L} [(V_{GS} - V_T) V_{DS}]$$

So, $I_D \propto V_{DS}$ ← V_{DS}^2 term goes away

Ref → Sedra Smith 5th edition
not 7th edition

for small V_{DS} , we see a linear
relation btw I_D and V_{DS}

Saturation mode: $V_{DS} \geq V_{GS} - V_T$
 $V_{GS} \geq V_T$

MOSFET \equiv Voltage controlled
current source
AND
Voltage controlled
resistance