ADITYA CHAUTAM

MACHINE LEARNING

agautam1@ordrew

AS KINMENT #3

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Ques 1) Kernel Poature Mapping $x = (1, x_2)^T$ P(x) = (x12, 52x, x2, x2) $K(x,z) = \emptyset(x). \emptyset(z)$ $=(x_1^2, \sqrt{2}x_1x_2, x_2^2), (z_1^2, \sqrt{2}z_1z_2, z_2^2)$ = (x, z, +x, zz)2 = (xz)2 [(x, z+x, zz)2]

Corresponding Kernel functions = [(x, z+x, zz)2]

- K(1,2) 242ER2
 - a) mapping into teature space.

 $(x_1,x_2) \rightarrow x(x) = (x_1^2, \sqrt{2}x_1x_2, x_2^2)$

Total no. of multiplication needed for above feature mapping = 3 multiplication wapping, we would noted 3 multiplication similarly, for z mapping, we would noted 3 multiplication

to multiply in feature space

we would need 3 multiplication (dot product) Thus total multiplication = 3+3+3= | Multiplication

Total Acidition = 2

b) computing through kerner function.

(x,Z,+x2Z2)2 -> 2+1 - 3 Multiplication reduition = 1

$$y = \emptyset (\leq n, w, +b)$$
 $\emptyset (z) = \{0, \sqrt{2} \leq 0\}$

(2) AND.

$$(0.821 \times 10^{-1}) \times 10^{-1} \Rightarrow y = 0 \Rightarrow y = 0 \Rightarrow y = 0 \Rightarrow y = 0$$

 $\Rightarrow x_1 \times 10^{-1} \times 10^$

(aue 2)
$$x_1=0$$
, $x_2=1$ AND $\rightarrow 0$
 $\Rightarrow 0.\omega_1+1.\omega_2+b \leq 0$ $\omega_2+b \leq 0$

Boiling about 4 inequalities we get, be0, w, 50, w,

AND table

| n, 1 | 2 | AND |
|------|---|-----|
| 0 | 0 | 0 |
| 0 | \ | 0 |
| 1 | O | 0 |
| 1 | 1 | 1 |

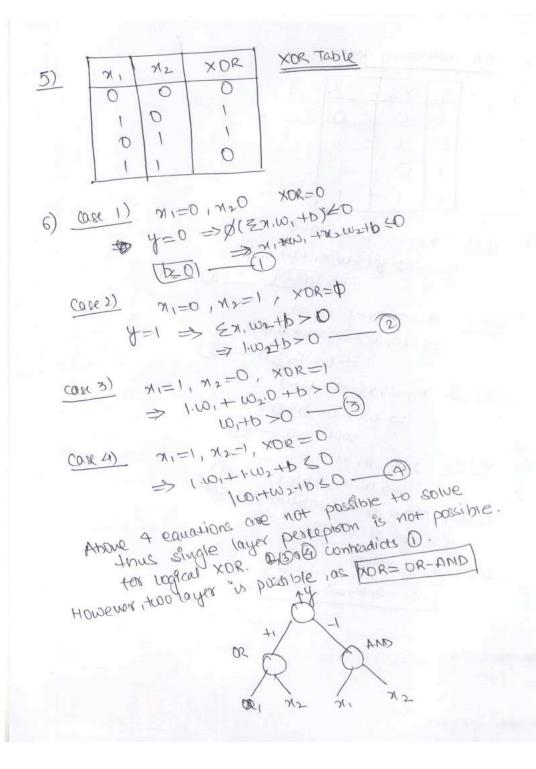
| · | 71, | × 2 | OR |
|---|-----|-----|-----|
| | 0 | 0 | 0 |
| | 0 | 1 | - \ |
| | 1 | 0 | 1 |

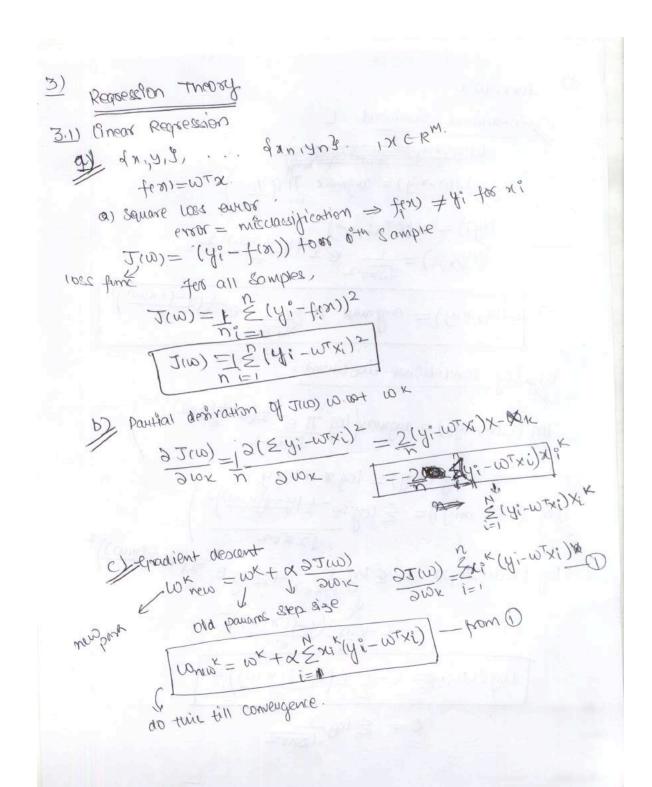
4)
$$(0.01)$$
 (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01) (0.01)

$$\frac{(ase 3)}{\Rightarrow \omega_{1} \cdot 0 + \omega_{2} \cdot n_{2} + b \Rightarrow 0}$$

$$\Rightarrow b + \omega_{2} \approx 0 - 0$$

Soluting above 4 inequalities, we get a range of values.





2)
$$f(x) = \omega^{T}x$$

a) Conditional Cholinood L

 $f(x) = \omega^{T}x$
 $f(x) =$

3)
$$y = f(x) + E$$
. E ; when $E = 0$

Note of the point $E = 0$

b)
$$Eo[(y-h(n))^2]$$
 $I = Eo[(h(n))$
 $I = Eo[(h(n))]$
 $I = Eo[(h(n))]$
 $I = E[(y-1)^2] = E[(y-1+1-y')^2]$
 $I = E[(y-1)^2 + (1-9)^2 + 2[(y-1)][x-9]]$
 $I = E[(y-1)^2] + E[(h-9)^2] + 2[(y-1)^2] - E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(h-9)^2] + 2[E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(h-9)^2] + 2[E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(h-9)^2] + 2[E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(h-9)^2] + 2[E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(y-1)^2] + 2[E[(y-1)^2] - E[(y-1)^2] - E[(y-1)^2]$
 $I = E[(y-1)^2] + E[(y-1)^2] + 2[(y-1)^2] + 2[(y-1)^2] - E[(y-1)^2] - E[(y-1)^2] + 2[(y-1)^2] - E[(y-1)^2] -$

3.2) Regularization.

L =
$$\frac{1}{2} \stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularization}}{\stackrel{\text{Regularizati$$

Regularization.
$$L = \frac{1}{2} \sum_{i=1}^{N} (y_i - wTx_i)^2 \quad (original loss function)$$

$$L = \frac{1}{2} \sum_{i=1}^{N} (y_i - wTx_i)^2 + \frac{1}{2} ||w||^2 \quad (loss function with regularization)$$

$$\alpha) \quad L = \frac{1}{2} \sum_{i=1}^{N} (y_i - wTx_i)^2 + \frac{1}{2} ||w||^2 \quad (loss function)$$

$$\frac{\partial L}{\partial w_{K}} = \frac{2}{2} \left[\frac{1}{2} (y - w^{T} \times i) \times k + \frac{2}{2} \times \lambda ||w_{k}|| \right]$$

$$\frac{\partial L}{\partial w_{K}} = \frac{2}{2} \left[\frac{1}{2} (y - w^{T} \times i) \times k + \lambda ||w_{k}|| \right]$$

b) first Agonthm is more cibely to give a sparse wards as it penalises the weight swith high weightige of white.

In second algo, to will reduce by A. Ahowever in other reduces white)

with more wis set to zoro

(1) togletic function.

$$f(x_1 w) = \frac{1}{1 + e^{-\alpha}}$$
, where $\alpha = \sum_{k=1}^{N} w_k w_k^2 + m_k w_k^2 = m_k w_k^2$

2) conditional liberhood

 $P(y = y_k) = \frac{1}{1 + e^{-\alpha}} = \frac{1}{1 + e^{-\alpha} +$

5) epradient decent

$$\omega_{\text{New}} = \omega_{\text{K}} + \chi_{\frac{\partial L}{\partial \omega_{\text{K}}}}$$
 $[\omega_{\text{New}} = \omega_{\text{K}} + \chi_{\frac{\partial L}{\partial \omega_{\text{K}}}}]$

$$\frac{\partial(0b)(ct)}{\partial wi} = -\frac{\partial(l(w), x_1y)}{\partial wi} + \frac{1}{1}x_1x_2(wi)$$

Gradient with a
$$= -2(lw; x_1y) + \frac{\lambda}{\lambda} \times (w; \frac{\lambda}{\lambda})$$

Gradient with $= -\frac{\lambda}{\lambda} \times (\frac{\lambda}{\lambda}) + \frac{\lambda}{\lambda} \times (w; \frac{\lambda}{\lambda})$

Gradient with $= -\frac{\lambda}{\lambda} \times (\frac{\lambda}{\lambda}) + \frac{\lambda}{\lambda} \times (w; \frac{\lambda}{\lambda})$

Gradient with $= -\frac{\lambda}{\lambda} \times (\frac{\lambda}{\lambda}) + \frac{\lambda}{\lambda} \times (w; \frac{\lambda}{\lambda})$

$$P_{\text{NeM}} = P_{\text{K}} + X \frac{910poject}{900!}$$

$$= P_{\text{K}} + X \frac{910poject}{100!}$$

$$= P_{\text{K}} + X \frac{910poject}{100!}$$

4.3 Analyse of results (Programming logistic regression)

1) The Accuracy of the training set increased with the application of Regularization (combdo = 25).

acturacy = 98.5075] without regularization # MB classified Image = 15]

accuracy = 98.7065 HMis classified Image = 13 Juith Lz regularization

This is expected as penatizing the high weight features based on the training set would make the hypothesis much better i.e reduce overfitting. Liberaice, we see that L2 regularization improves the overall accuracy of any training set. However on test data, accuracy improved a little bit.

2) Mis classified Image count = 13 (with L2 regularization)
Higure attached

T-Y/GX & COWINDON

