

OS1 – CS3510

Report: Programming Assignment 2 - Finding Perfect numbers using threads.

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Problem Statement:

Our problem is to find all perfect numbers between 1 and the number "n". This is done by partitioning the work amongst "k" threads created by the main thread, such that no two threads work on the same number (by work, we mean finding whether the numbers assigned to that thread are perfect or not). "k" and "n" are input variables.

Brief Summary:

The k threads were allocated the numbers from 1 to n as follows:

Thread 1 – {1, $k + 1$, $2k + 1$, $3k + 1$, ..., $k \lfloor n/k \rfloor + 1$ }

Thread 2 – {2, $k + 2$, $2k + 2$, $3k + 2$, ..., $k \lfloor n/k \rfloor + 2$ }

Thread 3 – {3, $k + 3$, $2k + 3$, $3k + 3$, ..., $k \lfloor n/k \rfloor + 3$ }, etc

This would be the allocation, provided none of these numbers exceed n. This makes sure that each thread, to some extent, while not doing the work of any other thread, does around the equal amount of work as the other threads due to near-equal distribution.

Detailed Description of Algorithm:

- We first open the input file that contains the values of n and k. We take this file as a command line argument.
- In the occurrence that k is greater than n, we require only n threads (each thread will take care of one number). In this case, all threads between n + 1 and k are not required. This is printed in the OutMain.txt
- We now create a pointer-"parameters", which stores the values of n, k, and i (i is the counter variable for the threads). Since pthread_create takes a (void *) parameter, this (int *) pointer is typecasted to (void *) and then passed to the function threadAlloc_perfCheck.

- Function **threadAlloc_perfCheck**:
 - This function does the following – using the passed parameters n , k and i (this is unique for each thread), the function computes all numbers it has to check for whether it is perfect or not. **(Math. 1)**
 - The thread checks whether the number is perfect or not using the function `ifPerf`. **(Math. 2)**
 - These perfect numbers are stored in an array `isPerf`. This array has a maximum length of $\lfloor n/k \rfloor$. The number of elements in the array is also stored in an integer variable – `numOfPerf`.
 - All numbers assigned to `Threadi` are stored in a file `OutFilei` – This file will store whether each number is a perfect number or not.
 - To the main file `OutMain.txt`, we append all the newly found perfect numbers by that thread. After the completion of all threads, `OutMain.txt` will contain each thread, followed by all the perfect numbers they found among the numbers they were assigned.

Math.1:

The algorithm for allocating the numbers amongst the threads is pretty straight-forward.

Thread_i will have an “adder” assigned to it. This will be equal to i (i ranging from 1 to k). To get the numbers for each thread described in the **Brief Summary**, we go in a loop, taking j as the looping variable.

We can see that **the last term in all the numbers assigned to Thread_i is the adder**. Hence, the numbers will be $j*k + \text{adder}$, j ranging from 0 to $\lfloor n/k \rfloor$, including 0 and $\lfloor n/k \rfloor$.

In every iteration, we make sure that the number it is checking is less than n . If not, it goes to the next number.

This way, we **near-equally distribute** all numbers 1 to n amongst k threads.

Math. 2:

The algorithm to check whether a given number is a perfect number is fairly simple. We find out all factors of the number and add them to the variable `sumOfFact`. In the end, if the sum of its factors (excluding itself) is equal to the number itself, the function returns 1; if not, it returns 0.

Analysis of Output:

1. Input: $n = 100$, $k = 7$

Output:

```
OutFile1.txt x +
1 1 : Is not a perfect Number
2 8 : Is not a perfect Number
3 15 : Is not a perfect Number
4 22 : Is not a perfect Number
5 29 : Is not a perfect Number
6 36 : Is not a perfect Number
7 43 : Is not a perfect Number
8 50 : Is not a perfect Number
9 57 : Is not a perfect Number
10 64 : Is not a perfect Number
11 71 : Is not a perfect Number
12 78 : Is not a perfect Number
13 85 : Is not a perfect Number
14 92 : Is not a perfect Number
15 99 : Is not a perfect Number

OutFile2.txt x +
1 2 : Is not a perfect Number
2 9 : Is not a perfect Number
3 16 : Is not a perfect Number
4 23 : Is not a perfect Number
5 30 : Is not a perfect Number
6 37 : Is not a perfect Number
7 44 : Is not a perfect Number
8 51 : Is not a perfect Number
9 58 : Is not a perfect Number
10 65 : Is not a perfect Number
11 72 : Is not a perfect Number
12 79 : Is not a perfect Number
13 86 : Is not a perfect Number
14 93 : Is not a perfect Number
15 100 : Is not a perfect Number

OutFile3.txt x +
1 3 : Is not a perfect Number
2 10 : Is not a perfect Number
3 17 : Is not a perfect Number
4 24 : Is not a perfect Number
5 31 : Is not a perfect Number
6 38 : Is not a perfect Number
7 45 : Is not a perfect Number
8 52 : Is not a perfect Number
9 59 : Is not a perfect Number
10 66 : Is not a perfect Number
11 73 : Is not a perfect Number
12 80 : Is not a perfect Number
13 87 : Is not a perfect Number
14 94 : Is not a perfect Number

OutFile4.txt x +
1 4 : Is not a perfect Number
2 11 : Is not a perfect Number
3 18 : Is not a perfect Number
4 25 : Is not a perfect Number
5 32 : Is not a perfect Number
6 39 : Is not a perfect Number
7 46 : Is not a perfect Number
8 53 : Is not a perfect Number
9 60 : Is not a perfect Number
10 67 : Is not a perfect Number
11 74 : Is not a perfect Number
12 81 : Is not a perfect Number
13 88 : Is not a perfect Number
14 95 : Is not a perfect Number

OutFile5.txt x +
1 5 : Is not a perfect Number
2 12 : Is not a perfect Number
3 19 : Is not a perfect Number
4 26 : Is not a perfect Number
5 33 : Is not a perfect Number
6 40 : Is not a perfect Number
7 47 : Is not a perfect Number
8 54 : Is not a perfect Number
9 61 : Is not a perfect Number
10 68 : Is not a perfect Number
11 75 : Is not a perfect Number
12 82 : Is not a perfect Number
13 89 : Is not a perfect Number
14 96 : Is not a perfect Number

OutFile6.txt x +
1 6 : Is a perfect Number
2 13 : Is not a perfect Number
3 20 : Is not a perfect Number
4 27 : Is not a perfect Number
5 34 : Is not a perfect Number
6 41 : Is not a perfect Number
7 48 : Is not a perfect Number
8 55 : Is not a perfect Number
9 62 : Is not a perfect Number
10 69 : Is not a perfect Number
11 76 : Is not a perfect Number
12 83 : Is not a perfect Number
13 90 : Is not a perfect Number
14 97 : Is not a perfect Number

OutFile7.txt x +
1 7 : Is not a perfect Number
2 14 : Is not a perfect Number
3 21 : Is not a perfect Number
4 28 : Is a perfect Number
5 35 : Is not a perfect Number
6 42 : Is not a perfect Number
7 49 : Is not a perfect Number
8 56 : Is not a perfect Number
9 63 : Is not a perfect Number
10 70 : Is not a perfect Number
11 77 : Is not a perfect Number
12 84 : Is not a perfect Number
13 91 : Is not a perfect Number
14 98 : Is not a perfect Number

OutMain.txt x +
1
2 Thread 1.
3 Thread 2.
4 Thread 3.
5 Thread 4.
6 Thread 5.
7 Thread 6.6
8 Thread 7.28
```

Analysis:

- We know that the only perfect numbers between 1 and 100 are 6 and 28. Hence, that computation has been done properly (Math. 2).
- We see that Threads 1 and 2 have computed 99 and 100. However, the subsequent threads have **NOT computed 101, 102, and so on**. Hence, that condition has been applied properly.
- The allocation has also been done properly. According to our algorithm,
Thread₆: {6, 13, 20, 27, ...}
Thread₇: {7, 14, 21, **28**, 35, ...}
- As expected, Threads 6 and 7 have detected 6 and 28 to be perfect numbers, respectively.

2. Input: n = 7, k = 9

Output:

```
OutFile1.txt × +
1 1 : Is not a perfect Number

OutFile2.txt × +
1 2 : Is not a perfect Number

OutFile3.txt × +
1 3 : Is not a perfect Number

OutFile4.txt × +
1 4 : Is not a perfect Number

OutFile5.txt × +
1 5 : Is not a perfect Number

OutFile6.txt × +
1 6 : Is a perfect Number

OutFile7.txt × +
1 7 : Is not a perfect Number

OutMain.txt × +
1
2 Thread 1.
3 Thread 2.
4 Thread 3.
5 Thread 4.
6 Thread 5.
7 Thread 6.6
8 Thread 7. Threads 8, 9, were not required to perform operations
```

Analysis:

- The only perfect number between 1 and 7 is 6. This is detected by Thread₆.
- The allocation has been done properly. According to our algorithm,
Thread₁: {1}
Thread₂: {2}
Thread₆: {6}
- Also, as per our code, threads 7, 8, and 9 are **not required and are hence not used**. This is also printed in the OutMain.txt file.