

Compiler Design

Syntax Analysis



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Syllabus: Unit 01

Syntax Analysis:

The role of the parser,

Review of context-free grammar for syntax analysis.

Top-down Parsing:

Recursive descent parsing,

Predictive parsers,

Transition diagrams for predictive parsers,

Non-recursive predictive parsing,

FIRST and FOLLOW,

Construction of predictive parsing tables, LL (1) grammars.

Non-recursive predictive parsing, Error recovery in predictive parsing.



THE ROLE OF THE PARSER

The parser or syntactic analyzer obtains a string of tokens from the lexical analyzer and verifies that the string can be generated by the grammar for the source language. It reports any syntax errors in the program. It also recovers from commonly occurring errors so that it can continue processing its input.

A parser is a compiler that is used to break the data into smaller elements coming from the lexical analysis phase.

A parser takes input in the form of a sequence of tokens and produces output in the form of a parse tree.

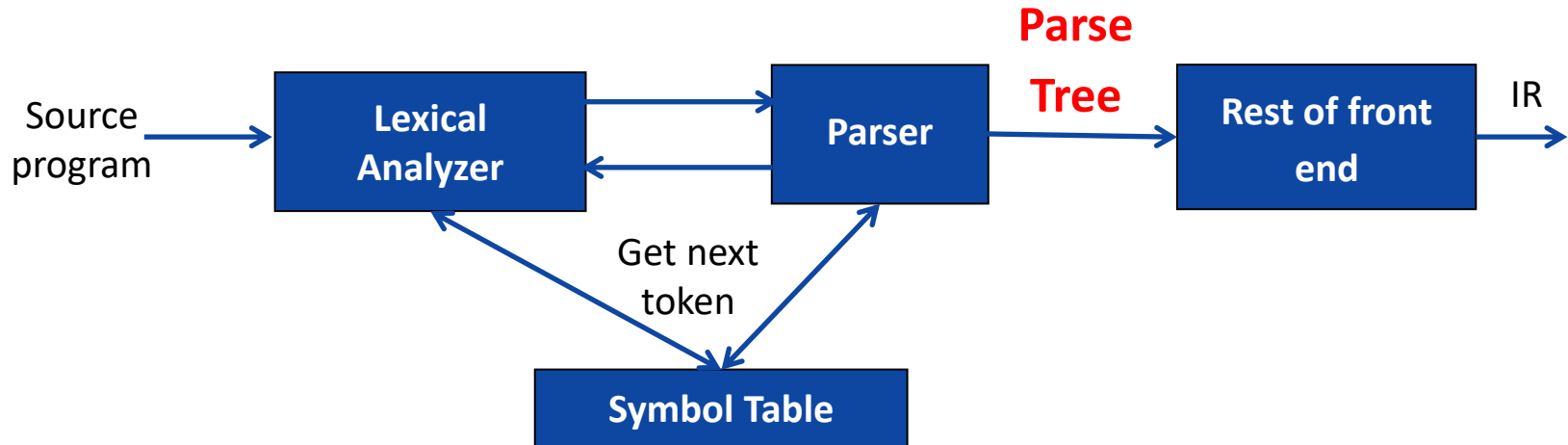


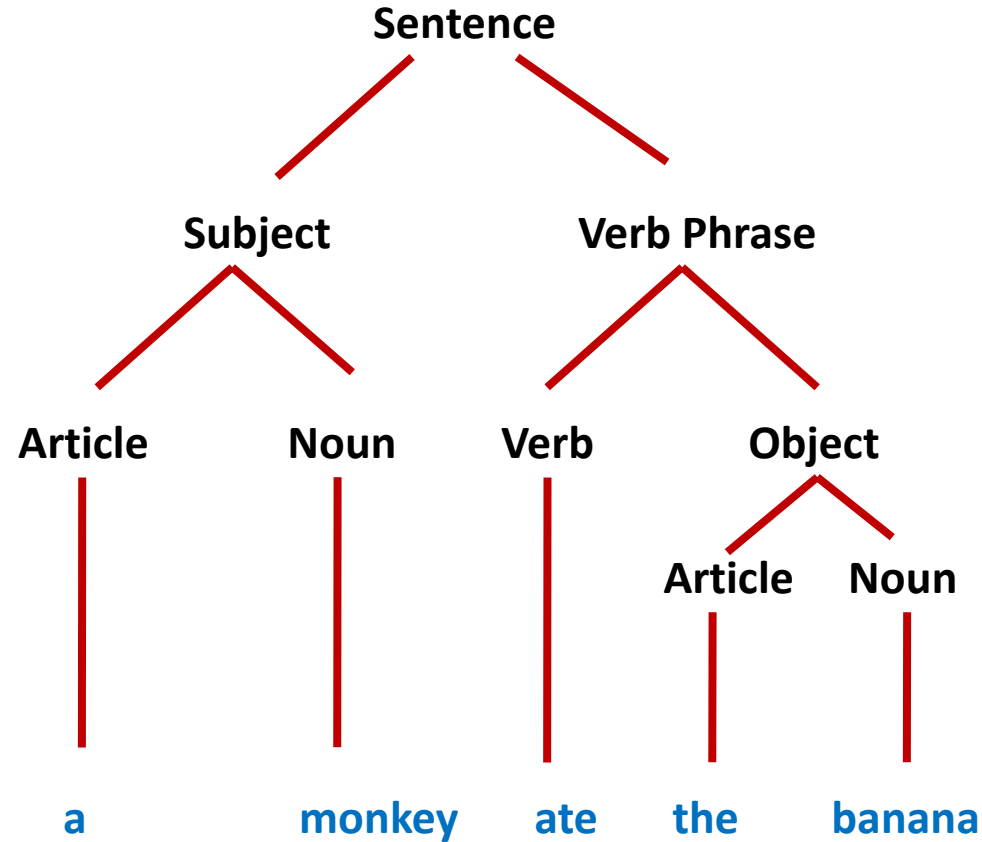
THE ROLE OF THE PARSER

Parser obtains a string of tokens from the lexical analyzer and reports **syntax error** if any otherwise generates **syntax tree**.

There are two types of parser:

1. Top-down parser
2. Bottom-up parser





CONTEXT-FREE GRAMMAR

A grammar is defined by a four-tuple:

$$G = \langle V_N, V_T, S, \emptyset \rangle$$

Where

V_N is a set of non-terminals

V_T is a set of terminals

S is starting symbol

\emptyset is finite subset

▶ Nonterminal Symbols:

- The name of the syntax category of a language, e.g., noun, verb, etc.
- It is written as a **single capital letter**, or as a **name enclosed between < ... >**, e.g.,
A or <Noun>

<Noun Phrase> → <Article><Noun>

<Article> → a | the

<Noun> → monkey | banana



CONTEXT-FREE GRAMMAR

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▶ Terminal Symbols:

- ↳ A symbol in the alphabet.
- ↳ It is denoted by lower case letters and punctuation marks used in language.

<Noun Phrase> \rightarrow <Article><Noun>

<Article> \rightarrow a | the

<Noun> \rightarrow monkey | banana



CONTEXT-FREE GRAMMAR

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▶ Starting Symbol:

↳ First nonterminal symbol of grammar is called the start symbol.

<Noun Phrase> \rightarrow <Article><Noun>

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<Noun> \rightarrow monkey | banana



CONTEXT-FREE GRAMMAR

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► Production:

→ A production, also called a rewriting rule, is a rule of grammar. It has the form of

A nonterminal symbol → String of terminal and nonterminal symbols

$\langle \text{Noun Phrase} \rangle \rightarrow \langle \text{Article} \rangle \langle \text{Noun} \rangle$

$\langle \text{Article} \rangle \rightarrow a \mid the$

$\langle \text{Noun} \rangle \rightarrow monkey \mid banana$



CONTEXT-FREE GRAMMAR

Problem: Let $G_2 = \langle \{E, T, F\}, \{a, +, *, (,)\}, S, \emptyset \rangle$

Where \emptyset consists of the productions

$$S \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow a$$

Obtain the expression $a * a + a$

Terminals, non terminals, start symbol, and productions for given grammar are:

Terminals: $+, *, (,)$

Non terminals: $S, E, T,$

Start symbol: S

Productions: $S \rightarrow E + T$

$E \rightarrow T$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow a$



CONTEXT-FREE GRAMMAR

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Obtain the expression $a * a + a$

Solution: Therefore the generation or derivation of a sentence is:

$$S \rightarrow E + T$$

$$S \rightarrow T + T$$

$$S \rightarrow T * F + T$$

$$S \rightarrow F * F + T$$

$$S \rightarrow a * F + T$$

$$S \rightarrow a * a + T$$

$$S \rightarrow a * a + F$$

$$S \rightarrow a * a + a$$



DERIVATION & AMBIGUITY

DERIVATION

Derivation is used to find whether the string belongs to a given grammar or not.

Types of derivations are:

1. Leftmost derivation
2. Rightmost derivation



DERIVATION & AMBIGUITY

LEFTMOST DERIVATION

A derivation of a string W in a grammar G is a left most derivation if at every step the **left most non terminal** is replaced.

Grammar: $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$

Output string: $a*a-a$

$S \rightarrow S - S$

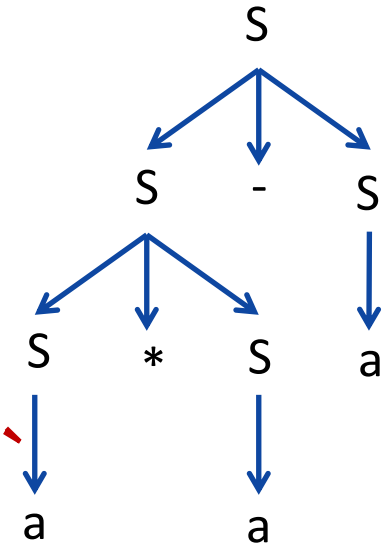
$S \rightarrow S * S - S$

$S \rightarrow a * S - S$

$S \rightarrow a * a - S$

$S \rightarrow a * a - a$

Parse tree represents the structure of derivation



Leftmost Derivation

Parse tree



DERIVATION & AMBIGUITY

RIGHTMOST DERIVATION

A derivation of a string W in a grammar G is a right most derivation if at every step the **right most non terminal** is replaced. It is also called canonical derivation.

Grammar: $S \rightarrow S+S \mid S-S \mid S*S \mid S/S \mid a$

Output string: $a*a-a$

$$S \rightarrow S * S$$

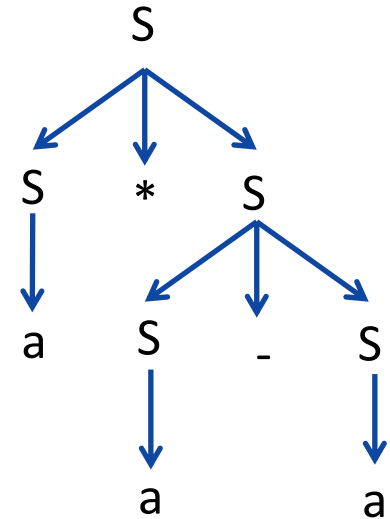
$$S \rightarrow S * S - S$$

$$S \rightarrow S * S - a$$

$$S \rightarrow S * a - a$$

$$S \rightarrow a * a - a$$

Parse tree represents
the structure of
derivation



Rightmost Derivation

Parse tree



DERIVATION & AMBIGUITY

1. Perform leftmost derivation and draw parse tree.

$$S \rightarrow A1B$$

$$A \rightarrow 0A \mid \epsilon$$

$$B \rightarrow 0B \mid 1B \mid \epsilon$$

Output string: 1001

2. Perform leftmost derivation and draw parse tree.

$$S \rightarrow 0S1 \mid 01$$

Output string: 000111

3. Perform rightmost derivation and draw parse tree.

$$E \rightarrow E+E \mid E * E \mid \text{id} \mid (E) \mid -E$$

Output string: id + id * id



DERIVATION & AMBIGUITY

AMBIGUITY

Ambiguity, is a word, phrase, or statement which contains **more than one meaning**.

Chip

A long thin piece of potato



A small piece of silicon



DERIVATION & AMBIGUITY

• AMBIGUITY

In formal language grammar, ambiguity would arise if identical string can occur on the RHS of two or more productions.

Grammar:

$$N_1 \rightarrow \alpha$$

$$N_2 \rightarrow \alpha$$

 N_1 N_2 α

Replaced by
 N_1 or N_2 ?

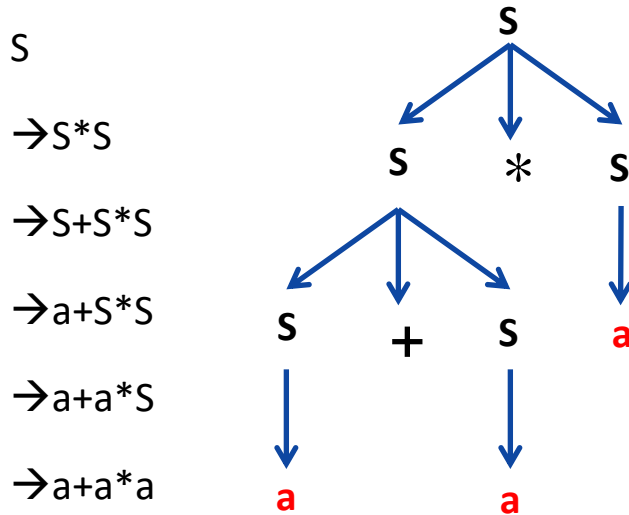


DERIVATION & AMBIGUITY

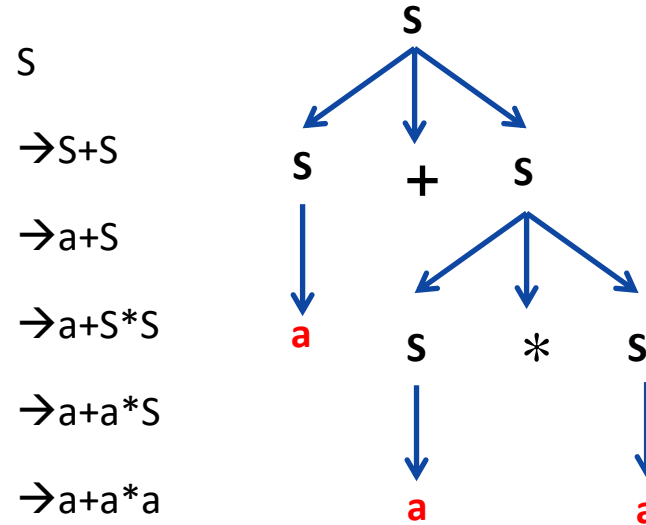
AMBIGUITY

Ambiguous grammar is one that produces more than one leftmost or more than one rightmost derivation for the same sentence.

Grammar: $S \rightarrow S+S \mid S*S \mid (S) \mid a$



Output string: $a+a*a$



Here, Two leftmost derivation for $a+a*a$ is possible hence, above grammar is ambiguous.



DERIVATION & AMBIGUITY

AMBIGUITY

Check Ambiguity in following grammars:

1) $S \rightarrow aS \mid Sa \mid \epsilon$ (output string: aaaa)

2) $S \rightarrow aSbS \mid bSaS \mid \epsilon$ (output string: abab)

3) $S \rightarrow SS^+ \mid SS^* \mid a$ (output string: aa+a*)

4) $\langle \text{exp} \rangle \rightarrow \langle \text{exp} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{letter} \rangle \mid \langle \text{letter} \rangle$

$\langle \text{letter} \rangle \rightarrow a \mid b \mid c \mid \dots \mid z$ (output string: a+b*c)

5) Prove that the CFG with productions: $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$ is ambiguous

(output string: aaaabb)



LEFT RECURSION

A grammar is said to be **left recursive** if it has a non terminal A such that there is a derivation $A \rightarrow A\alpha$ for some string α .

$$\begin{aligned} A &\rightarrow A\alpha \\ &\rightarrow A\alpha\alpha \\ &\rightarrow A\alpha\alpha\alpha \\ &\rightarrow A\alpha\alpha\alpha\alpha \\ &\rightarrow A\alpha\alpha\alpha\alpha\alpha \\ &\rightarrow A\alpha\alpha\alpha\alpha\alpha\alpha \end{aligned}$$


LEFT RECURSION

Algorithm to eliminate left recursion

1. Arrange the non terminals in some order A_1, \dots, A_n
2. for $i := 1$ to n **do begin**
 - for $j := 1$ to $i - 1$ **do begin**
 - replace each production of the form $A_i \rightarrow A_i \gamma$
 - by the productions $A_i \rightarrow \delta_1 \gamma \mid \delta_2 \gamma \mid \dots \mid \delta_k \gamma$,
 - where $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$ are all the current A_j
 - productions;
- end**
- eliminate the immediate left recursion among the A_i – productions
- end**

$$A \rightarrow A\alpha \mid \beta \quad \longrightarrow \quad \begin{array}{l} A \rightarrow A' \\ A' \rightarrow A' \mid \epsilon \end{array}$$



LEFT RECURSION

$$E \rightarrow E+T \mid T$$
$$E \rightarrow TE'$$
$$E' \rightarrow +TE' \mid \epsilon$$
$$T \rightarrow T*F \mid F$$
$$T \rightarrow FT'$$
$$T' \rightarrow *FT' \mid \epsilon$$
$$X \rightarrow X\%Y \mid Z$$
$$X \rightarrow ZX'$$
$$X' \rightarrow \%YX' \mid \epsilon$$


LEFT RECURSION

Exercise:

$$1) \quad A \rightarrow Abd \mid Aa \mid a$$

$$B \rightarrow Be \mid b$$

$$2) \quad A \rightarrow AB \mid AC \mid a \mid b$$

$$3) \quad S \rightarrow A \mid B$$

$$A \rightarrow ABC \mid Acd \mid a \mid aa$$

$$B \rightarrow Bee \mid b$$

$$4) \quad \text{Exp} \rightarrow \text{Exp} + \text{term} \mid \text{Exp} - \text{term} \mid \text{term}$$



LEFT FACTORING

$$A \rightarrow \alpha \beta \mid \alpha \delta \longrightarrow \begin{array}{l} A \rightarrow A' \\ A' \rightarrow \mid \end{array}$$



Thank You



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