

Probabilistic Skin Detection

CSE 6367 – Computer Vision
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Probabilistic Skin Detection

- Maximum likelihood approach:
 - given training data:
 - Estimate $P(\text{RGB} \mid \text{skin})$, $P(\text{RGB} \mid \text{non-skin})$
 - given test data:
 - For every pixel, compute $P(\text{skin} \mid \text{RGB})$, using Bayes rule.
- $P(\text{RGB} \mid \text{skin})$:
 - probability that we will observe rgb , when we know that the pixel is a skin pixel.

Obtaining Training Data



frame2



frame2(80:120, 137:172, :)

```
% finding a training sample
```

```
figure(2); imshow(frame2(80:120, 137:172, :) / 255);
```

```
sample = frame2(80:120, 137:172, :);
```

- Find subwindows that only contain skin pixels.
 - For good results, collect data from many images.
 - Here, for simplicity, we only use data from one image.

A Simple Gaussian Model

- All we need: mean and std.
- Assumption: colors are mutually independent.

```
sample_red = sample(:, :, 1);  
sample_green = sample(:, :, 2);  
sample_blue = sample(:, :, 3);
```

```
sample_red = sample_red(:);  
sample_green = sample_green(:);  
sample_blue = sample_blue(:);
```

```
red_mean = mean(sample_red);  
green_mean = mean(sample_green);  
blue_mean = mean(sample_blue);
```

```
red_std = std(sample_red);  
green_std = std(sample_green);  
blue_std = std(sample_blue);
```

Probability of a Color

- Given the means and stds for each color:
 - What is $P(\text{RGB} \mid \text{skin})$?
 - How can it be decomposed?

Probability of a Color

- Given the means and stds for each color:
 - What is $P(\text{RGB} \mid \text{skin})$?
 - How can it be decomposed?
 - Assuming that colors are independent:
 - $P(\text{RGB} \mid \text{skin}) =$
 - $= P(R \mid \text{skin}) * P(G \mid \text{skin}) * P(B \mid \text{skin})$
 - $= N(R, \text{red_mean}, \text{red_std}) *$
 - $N(G, \text{green_mean}, \text{green_std}) *$
 - $N(B, \text{blue_mean}, \text{blue_std})$
- % N is the normal (Gaussian) distribution

Applying the Skin Model

```
frame20 = double(imread('frame20.bmp'));  
[rows,cols, bands] = size(frame20);  
  
skin_detection = zeros(rows, cols);  
  
for row = 1:rows  
    for col = 1:cols  
        red = frame20(row, col, 1);  
        green = frame20(row, col, 2);  
        blue = frame20(row, col, 3);  
  
        red_pr = gaussian_probability(red_mean, red_std, red);  
        green_pr = gaussian_probability(green_mean, green_std, green);  
        blue_pr = gaussian_probability(blue_mean, blue_std, blue);  
        prob = red_pr * green_pr * blue_pr;  
        skin_detection(row, col) = prob;  
    end  
end
```

Results



frame20



skin_detection



skin_detection > 0.0000001

Switching to Normalized rg Space

- $r = R / (R+G+B);$
- $g = G / (R+G+B);$
- Intuition: intensity does not matter.

```
sample_total = sample_red + sample_green + sample_blue;  
sample_red2 = sample_red ./ sample_total;  
sample_red2(isnan(sample_red2)) = 0;  
sample_green2 = sample_green ./ sample_total;  
sample_green2(isnan(sample_green2)) = 0;
```

```
r_mean = mean(sample_red2);  
g_mean = mean(sample_green2);  
r_std = std(sample_red2);  
g_std = std(sample_green2);
```

Probability of a Color in rg Space

- Given the means and stds for each color:
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Probability of a Color

- Given the means and stds for each color:
 - What is $P(\text{RGB} \mid \text{skin})$?
 - How can it be decomposed?
- Assuming that colors are independent:
 - $r = R / (R+G+B)$;
 - $g = G / (R+G+B)$;
 - $P(\text{RGB} \mid \text{skin}) = P(rg \mid \text{skin})$
 $= P(r \mid \text{skin}) * P(g \mid \text{skin})$
 $= N(r, r_mean, r_std) * N(g, g_mean, g_std)$

Results



frame20



skin_detection2



skin_detection2 > 10

Compare to Results Using RGB



frame20



skin_detection



skin_detection > 0.0000001

Probability Question

- Why are some values > 1 ?
- Why does $P(\text{rg} \mid \text{skin}) > 1$ for some rg ?
 - Why is it not violating the rule of probability theory that probabilities always ≤ 1 ?

Probability Question

- Why are some values > 1 ?
- Why does $P(\text{rg} \mid \text{skin}) > 1$ for some rg ?
 - Why is it not violating the rule of probability theory that probabilities always ≤ 1 ?
- Answer: because $P(\text{rg} \mid \text{skin})$ is a *density* function, not a discrete probability function.

Towards a Nonparametric Model

- How many colors are there?
 - Assuming we use 8 bits per color.

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- $256 * 256 * 256 = 16.777$ million colors
- How can we overcome the Gaussian assumption?
 - Assume we have lots of training data.

Towards a Nonparametric Model

- How many colors are there?
 - Assuming we use 8 bits per color.
- $256 * 256 * 256 = 16.777$ million colors
- How can we overcome the Gaussian assumption?
 - Assume we have lots of training data.
- By estimating explicitly $P(\text{RGB} \mid \text{skin})$ for each RGB.

Color Histograms

- Simplest form:
 - A $256 \times 256 \times 256$ array.
- Given training samples of skin:
 - For each bin (R, G, B) of histogram:
 - Count how many pixels have color RGB in the training samples.
- What is $P(\text{RGB} \mid \text{skin})$ according to the histogram?

Color Histograms

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 - Count how many pixels have color RGB in the training samples.
- What is $P(\text{RGB} \mid \text{skin})$ according to the histogram?
 - $\text{histogram}(\text{R}, \text{G}, \text{B}) / \text{sum of all histogram bins.}$

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Practical Considerations

- Estimating 16.8 million numbers requires too much training data.
 - How much?
- If we want 10 more pixels than the number of bins:
 - 168 million skin pixels.
 - 67200 50x50 skin patches.
- Remedy: make a coarser histogram.

A 32x32x32 Histogram

- A 32x32x32 array.
 - 32,768 entries.
- If we want 10 more pixels than the number of bins:
 - 327,680 million skin pixels.
 - 131 50x50 skin patches.
- Color (R,G,B) maps to bin:
 - $\text{floor}(R/8, G/8, B/8)$.
 - Assuming bins are numbered starting at 0.
 - Matlab formula: $\text{floor}(R/8, G/8, B/8) + 1$.


```
function result = detect_skin2(image, positive_histogram)

% function result = detect_skin2(image, positive_histogram)

vertical_size = size(image, 1);
horizontal_size = size(image, 2);
histogram_bins = size(positive_histogram, 1);
factor = 256 / histogram_bins;

result = zeros(vertical_size, horizontal_size);

for vertical = 1: vertical_size
    for horizontal = 1: horizontal_size
        red = image(vertical, horizontal, 1);
        green = image(vertical, horizontal, 2);
        blue = image(vertical, horizontal, 3);

        r_index = floor(red / factor) + 1;
        g_index = floor(green / factor) + 1;
        b_index = floor(blue / factor) + 1;

        skin_value = positive_histogram(r_index, g_index, b_index);
        result(vertical, horizontal) = skin_value;
    end
end
```

Results



frame20



result



result > 0.0002

Compared to Gaussian rg Model



frame20



skin_detection2



skin_detection2 > 10

Parametric and Non-parametric Models

- Parametric models:
 - We assume type of distribution.
 - We compute parameters.
- Gaussians are parametric distributions.
 - Parameters are mean and std.
- Histograms are *non-parametric* distributions.
 - No assumption about how values are distributed.
 - Plus: Fewer assumptions → more robust system.
 - Minus: Must estimate a lot more numbers → we need a lot more training data.

What Is Missing?

- We have tried three skin color models:
 - A Gaussian RGB distribution.
 - A Gaussian rg distribution.
 - A histogram-based distribution.
- Using each of them, we compute for each pixel:

What Is Missing?

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 - A Gaussian RGB distribution.
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- Using each of them, we compute for each pixel:
 - $P(\text{RGB} \mid \text{skin})$.
- What do we *really* want to compute?

What Is Missing?

- We have tried three skin color models:
 - A Gaussian RGB distribution.
 - A Gaussian rg distribution.
 - A histogram-based distribution.
- Using each of them, we compute for each pixel:
 - $P(\text{RGB} \mid \text{skin})$.
- What do we *really* want to compute?
 - $P(\text{skin} \mid \text{RGB})$.
- What is the difference?

Review of Bayes Rule

- Relating $P(\text{skin} \mid \text{RGB})$ to $P(\text{RGB} \mid \text{skin})$:

Review of Bayes Rule

- Relating $P(\text{skin} \mid \text{RGB})$ to $P(\text{RGB} \mid \text{skin})$:

$$P(\text{skin} \mid \text{RGB}) = P(\text{RGB} \mid \text{skin}) * P(\text{skin}) / P(\text{RGB}).$$

- What is $P(\text{RGB})$?

Review of Bayes Rule

- Relating $P(\text{skin} \mid \text{RGB})$ to $P(\text{RGB} \mid \text{skin})$:

$$P(\text{skin} \mid \text{RGB}) = P(\text{RGB} \mid \text{skin}) * P(\text{skin}) / P(\text{RGB}).$$

- What is $P(\text{RGB})$?

$$P(\text{RGB}) = P(\text{RGB} \mid \text{skin}) * P(\text{skin}) + P(\text{RGB} \mid \text{non_skin}) * P(\text{non_skin})$$

- We need $P(\text{RGB} \mid \text{non_skin})$ and $P(\text{skin})$.
 - How do we get $P(\text{RGB} \mid \text{non_skin})$?

Review of Bayes Rule

- Relating $P(\text{skin} \mid \text{RGB})$ to $P(\text{RGB} \mid \text{skin})$:

$$P(\text{skin} \mid \text{RGB}) = P(\text{RGB} \mid \text{skin}) * P(\text{skin}) / P(\text{RGB}).$$

- What is $P(\text{RGB})$?

$$P(\text{RGB}) = P(\text{RGB} \mid \text{skin}) * P(\text{skin}) + P(\text{RGB} \mid \text{non_skin}) * P(\text{non_skin})$$

- We need $P(\text{RGB} \mid \text{non_skin})$ and $P(\text{skin})$.
 - How do we get $P(\text{RGB} \mid \text{non_skin})$?

Non-skin Color Histogram

- A skin histogram estimates $P(\text{RGB} \mid \text{skin})$.
 - Based on skin samples.
- A non-skin histogram estimates $P(\text{RGB} \mid \text{non-skin})$.
 - Based on non-skin samples.

Implementation

- Pick manually $P(\text{skin})$.
 - I always use 0.5.
 - It is clearly too high.
 - Results are good.
- Then, $P(\text{skin} \mid \text{RGB}) =$
$$\frac{P(\text{RGB} \mid \text{skin}) * 0.5}{(0.5 * P(\text{RGB} \mid \text{skin}) + 0.5 * P(\text{RGB} \mid \text{non_skin}))} =$$
$$\frac{P(\text{RGB} \mid \text{skin})}{(P(\text{RGB} \mid \text{skin}) + P(\text{RGB} \mid \text{non_skin}))}$$
- Full implementation: `code/detect_skin.m`

Calling detect_skin.m

```
% read histograms
clear;
negative_histogram = read_double_image('negatives.bin');
positive_histogram = read_double_image('positives.bin');

frame20 = double(imread('frame20.bmp'));
%figure(1); imshow(frame2 / 255);

result = detect_skin(frame20, positive_histogram, negative_histogram);
figure (5); imshow(result, []);
```

Results



frame20



result



result > 0.2

Compare to Using Only Skin Histogram



frame20



result



result > 0.0002

Results



frame20



result

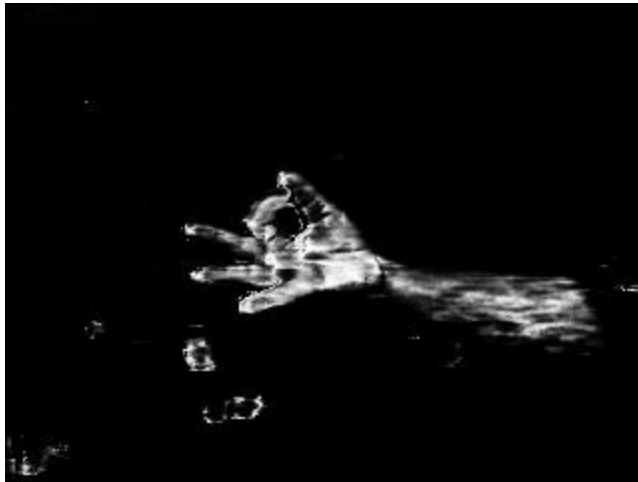


result > 0.2

Compared to Gaussian rg Model



frame20



skin_detection2



skin_detection2 > 10