

(20)

Instruction type	A	B
Cycles per Instruction (CPI)	3	2

PX2000

instruction 45%  
new instr 25%

55%

55%  $\equiv$  31-25%, 68-75%

PX3000  $\rightarrow$  clock cycle time  $\downarrow$ ,  $CPI' = 1.2(CPI)$

(Q) compiler sol is (1.11)x faster than hardware sol.

$$PX3000(\text{clock cycle time}) = \boxed{???} \times \text{of } PX2000(\text{clock cycle time})$$

Ans  $\rightarrow$  ~~original~~  $CPI(PX2000) = (0.45 \times 3) + (0.55 \times 2)$   
 $= 2.45$

compiler-optimized

$$\rightarrow A \text{ instr} = 80\% \text{ of } (45\%)$$

$$= 0.8 \times 45\%$$

$$= 36\%$$

$$\text{old Total number of instr} = (45\%) + 55\% = 100\%$$

$$\text{new Total instr (after optimization)} = (36\%) + 55\% = 91\%$$

$\rightarrow$  Old percentages / proportions:

$$\textcircled{A} \frac{45\%}{100\%} = 45\%, \textcircled{B} \frac{55\%}{100\%} = 55\%$$

$\rightarrow$  New percentages / proportions:

$$\textcircled{A} \frac{36\%}{91\%} \approx 39.56\%, \textcircled{B} \frac{55\%}{91\%} \approx 60.44\%$$

$\rightarrow$  Old CPI:

$$(0.45 \times 3) + (0.55 \times 2) = 2.45$$

$\rightarrow$  New CPI:

$$(0.3956 \times 3) + (0.6044 \times 2) = 2.3956$$

→ For PX2000 (Compiler Optimized)

$$\begin{aligned} \text{Time} &= \text{instr} \times \text{CPI} \times \text{clock time} \\ &= 0.91 N \times 2.395 \times T \\ &= (2.18)(N)(T) \end{aligned}$$

→ For PX3000 (Hardware Optimized)

$$\begin{aligned} \text{CPI}_{\text{new}} &= 2.45 \times 1.2 \\ &= 2.94 \end{aligned}$$

$$\begin{aligned} \text{Time} &= N \times 2.94 \times T' \\ &= (2.94)(N)(T') \end{aligned}$$

→ Given: Compiler is 1.11x faster than hardware solution

$$(1.11) \times (2.18)(N)(T) = (2.94)(N)(T')$$

$$T' = \frac{(1.11)(2.18)}{(2.94)} \cdot T$$

$$\left(\frac{T'}{T}\right) = 0.82306 \approx 0.8231$$

→ For clock speed ratio,

$$\text{old} : \text{new} = T : T'$$

$$= \frac{T}{T'}$$

$$= \frac{1}{\left(\frac{T'}{T}\right)}$$

$$= \frac{1}{0.8231}$$

$$= 1.21491$$

$$\approx 1.2149$$

$$\approx 1.215$$

$$\approx 1.22$$

→ So, PX3000 is (1.22)x faster than PX2000 in terms of clock cycle time.