Value-sensitive product (content) recommendation

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- 1 Abstract
- 2 Introduction
- 3 Formulation

For each article A_i in our database we know its 3 properties:

1. v_i^1 is a vector of its graph-representation:

Let (V^1, E^1) be the coviewership graph. Here V^1 represents the set of graph-embeddings of all nodes (articles) v^1 , and E^1 represents set of all edges connecting those nodes. d_{ij}^1 's be the distance between v_i^1 and v_i^1 .

2. v_i^2 is a vector of its sentence embedding:

Let (V^2, E^2) be the similarity graph. As above, d_{ij}^2 's be the distance between v_i^2 and v_j^2 .

3. c_i is the value associated with that article

So, each article A_i is represented by this triad $\{v_i^1, v_i^2, c_i\}$. Although, this is a very general formulation. For the sake of simplicity, for now we will just assume that each the article is characterized by its sentence embedding and its value.

Problem Statement:

Now, the problem statement is:

Given that a user is reading an article A_i , what article must be recommended next so that we

- 1. maximize the content relevance to the user
- 2. maximize the ad-monetary value.

Mathematically, given A_i , we seek A_j such that:

$$j = \arg\max_{J} \phi(A_i, A_J),$$

where ϕ is the utility function. This above formulation is mainly for our *Read Next* pages, but it could be easily extended to *Infinite scroll*.

How do we choose the utility function ϕ ?

Each article A_J is attributed with its sentence-embedding and its value. So we must design a utility function ϕ that maps its attributes to a real value:

$$\phi: \mathbb{R}^D \times \mathbb{R}^D \times \mathbb{R} \to \mathbb{R}$$

• ϕ must be directly proportional to the value of the article A_J being recommended

$$\phi(A_i, A_J) \propto c_J$$

• ϕ must be inversely proportional to the distance of the article A_J from the current article A_i

$$\phi(A_i, A_J) \propto \frac{1}{|d_i - d_J|} = \frac{1}{d_{iJ}}$$

Hence, we choose

$$\phi(A_p, A_q) := \frac{(c_q)^{r_1}}{(d_{pq})^{r_2}}.$$

Here r_1 and r_2 are the parameters that control the contribution of the value and the distance, on the utility term ϕ respectively.

Note: The special case of $\{r_1 = 0, r_2 = 1\}$ reduces the method back to the BAU.

Assumptions made:

- 1. The value of an article \approx its $\left(\frac{\text{total revenue}}{\text{total impressions}}\right)$ from the past
- 2. The article value remains almost unchanged for 1 week
- 3. Each article is characterized by the universal sentence embedding vector of its:
 - post_title
 - meta_title
 - summary

Formulation for Infinite scroll:

Quite often, we recommend more than just one article, either in the form of infinite-scroll or the 'Next Page' option.

So a more general form of the problem is: Given an article A_i , we seek (N-1) articles $\{A_{a_1}, A_{a_2}, \dots A_{a_{N-1}}\}$ such that:

$$\{a_1 \cdots a_{N-1}\} = \underset{\{b_1 \cdots b_{N-1}\}}{\arg \max} \sum_{i=1}^{N-1} \gamma^{k-1} \phi(A_i, A_{b_k}),$$

where $0 < \gamma < 1$ is called the discount factor.

Finally, after we know the 'optimal' recommendations, we evaluate the discounted value as

$$\mathcal{V}_{disc} := \sum_{k=1}^{N-1} \gamma^{k-1} c_{a_k}$$

We use the discounted-value instead of actual value to account for the fact that the likelihood of a user reading an article decreases with increasing scroll depth.

4 Results

Simulation results for infinite scroll:

- in BAU: 0.709

We used $r_1 = 0.8, r_2 = 15, \gamma = 0.09, N = 6$, and ran 30,000 random simulations.

• We observe a lift of 14.76% in the discounted value

$$\left(\frac{\mathcal{V}_{disc}^{VAL} - \mathcal{V}_{disc}^{BAU}}{\mathcal{V}_{disc}^{BAU}}\right) \times 100 = 14.76\%$$

• We observe a reduction in relevance of 0.4%

I.e., Mean cosine-similarity between the recommended articles and the article being read:

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- in VAL: 0.706.

Rand-expt #5/25000

Current article being read:-
['21 Chilled Soups That Are So Hot Right Now']

Recommended using distance-based:-
1. [disc_val=0.00135, cossim=0.7454] 9 Soups to Meal-Prep Now That It's Chilly Out and Salads Aren't Cutting It
2. [disc_val=0.00018, cossim=0.7386] 5-Ingredient Fall Soups That Don't Require Hours of Chopping
3. [disc_val=0.00002, cossim=0.7214] 19 Whole30 Soup Recipes That Make January Way More Tolerable
4. [disc_val=0.00000, cossim=0.7157] 19 Breakfast Soups (Yes, Really!) for Cold Mornings
5. [disc_val=0.00000, cossim=0.6856] 21 Noodle Soup Recipes That Prove It's Not All About Chicken

Recommended using value-based:-
1. [disc_val=0.00195, cossim=0.7386] 5-Ingredient Fall Soups That Don't Require Hours of Chopping
2. [disc_val=0.00012, cossim=0.7454] 9 Soups to Meal-Prep Now That It's Chilly Out and Salads Aren't Cutting It
```

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    [disc_val=0.00002, cossim=0.7214]
    Whole30 Soup Recipes That Make January Way More Tolerable
    [disc_val=0.00000, cossim=0.7157]
    Breakfast Soups (Yes, Really!) for Cold Mornings
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5. [disc_val=0.00000, cossim=0.6856] 21 Noodle Soup Recipes That Prove It's Not All About Chicken

Figure 1: Example recommendations showing a lift in the value for the same set of articles.

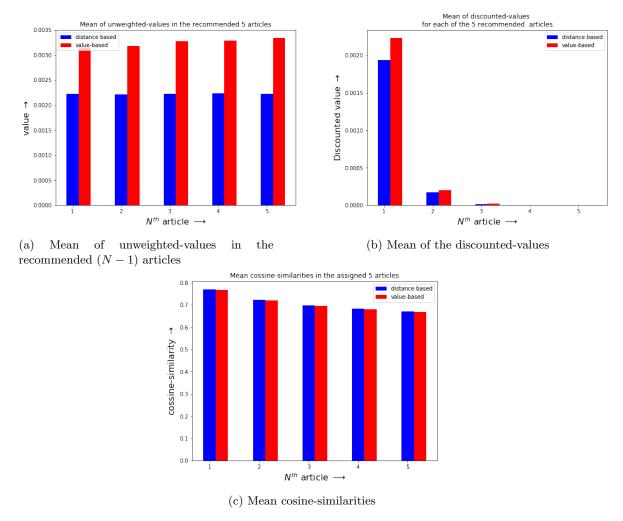


Figure 2: Conglomerated results of the recommended articles after doing the random simulations.

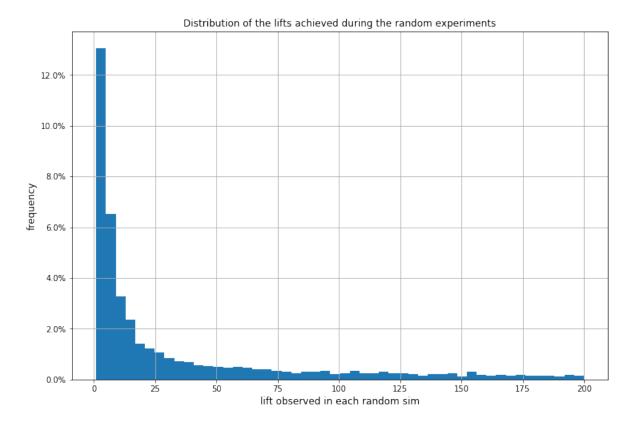


Figure 3: Distribution of the observed lift in each random simulation.

5 Conclusion

As seen from Fig. (2c), by achieving an almost equal cosine similarity score as the BAU, we are achieving a higher value (Fig. (2b)) using the value-based method.

Hence we think that it is worth implementing this value-based recommendation method into a live A/B test with the BAU.

6 Miscellaneous

Some questions:

- 1. Any reason why the articles are so differently valued?
 - I.e., why are there different articles which are quite similar to a given current article, but with so much variance in the values? So much so that we see a big value lift?
- 2. Do we have any idea how seasonality affects the volatility of article value? Do we have enough confidence on the value being stable over time?
 - Is there a way we can get the c-values within a desired time window, instead of an all time historical value? Yes. But can we also get to plot the values over time?
 - ullet Can we somehow test these c-values to ascertain our attribution of an article to a value?
- 3. In the process of showing article an A instead of article B, I hope that we aren't just transferring money from one pocket to another?
- 4. [Do analysis] It would be good to know how often "high-value" pages are recommended with this approach vs the similarity based approach.