

# AER1216 - Fundamentals of UAS Project Demonstration

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# Fixed-Wing: Performance

## Range

1000m level = **2,381.6 km**

2000m level = **2,541.5 km**

## Endurance

1000m level = **20.9 hrs**

2000m level = **23.1 hrs**



# Fixed-Wing: Model Dynamics

$$\begin{pmatrix} \dot{p}_n \\ \dot{p}_e \\ \dot{p}_d \end{pmatrix} = \begin{pmatrix} c_\theta c_\psi & s_\phi s_\theta c_\psi - c_\phi s_\psi & c_\phi s_\theta c_\psi + s_\phi s_\psi \\ c_\theta s_\psi & s_\phi s_\theta s_\psi + c_\phi c_\psi & c_\phi s_\theta s_\psi - s_\phi c_\psi \\ -s_\theta & s_\phi c_\theta & c_\phi c_\theta \end{pmatrix} \begin{pmatrix} u \\ v \\ w \end{pmatrix}$$

$$\begin{pmatrix} \dot{u} \\ \dot{v} \\ \dot{w} \end{pmatrix} = \begin{pmatrix} rv - qw \\ pw - ru \\ qu - pv \end{pmatrix} + \frac{1}{m} \begin{pmatrix} f_x \\ f_y \\ f_z \end{pmatrix},$$

$$\begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix} = \begin{pmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \frac{\sin \phi}{\cos \theta} & \frac{\cos \phi}{\cos \theta} \end{pmatrix} \begin{pmatrix} p \\ q \\ r \end{pmatrix}$$

$$\begin{pmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{pmatrix} = \begin{pmatrix} \Gamma_1 pq - \Gamma_2 qr \\ \Gamma_5 pr - \Gamma_6 (p^2 - r^2) \\ \Gamma_7 pq - \Gamma_1 qr \end{pmatrix} + \begin{pmatrix} \Gamma_3 l + \Gamma_4 n \\ \frac{1}{J_y} m \\ \Gamma_4 l + \Gamma_8 n \end{pmatrix}.$$



# Fixed-Wing: Linearization

$$\begin{bmatrix} \dot{\bar{v}} \\ \dot{\bar{p}} \\ \dot{\bar{r}} \\ \dot{\bar{\phi}} \\ \dot{\bar{\varphi}} \end{bmatrix} = \begin{bmatrix} Y_v & Y_p & Y_r & g \cos(\theta^*) \cos(\phi^*) & 0 \\ L_v & L_p & L_r & 0 & 0 \\ N_v & N_p & N_r & 0 & 0 \\ 0 & 1 & \cos(\phi^*) \tan(\phi^*) & q^* \cos(\phi^*) \tan(\phi^*) - r^* \sin(\phi^*) r^* \tan(\theta^*) & 0 \\ 0 & 0 & \cos(\phi^*) \sec(\theta^*) & p^* \cos(\phi^*) \sec(\theta^*) - r^* \sin(\phi^*) \sec(\theta^*) & 0 \end{bmatrix} \begin{bmatrix} \bar{v} \\ \bar{p} \\ \bar{r} \\ \bar{\phi} \\ \bar{\varphi} \end{bmatrix} + \begin{bmatrix} Y_{\delta_a} & Y_{\delta_r} \\ L_{\delta_a} & L_{\delta_r} \\ N_{\delta_a} & N_{\delta_r} \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \bar{\delta}_a \\ \bar{\delta}_r \end{bmatrix}$$

$$\begin{bmatrix} \dot{\bar{u}} \\ \dot{\bar{w}} \\ \dot{\bar{q}} \\ \dot{\bar{\theta}} \\ \dot{\bar{h}} \end{bmatrix} = \begin{bmatrix} X_u & X_w & X_q & -g \cos(\theta^*) & 0 \\ Z_u & Z_w & Z_q & -g \sin(\theta^*) & 0 \\ M_u & M_w & M_q & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ \sin(\theta^*) & -\cos(\theta^*) & 0 & u^* \cos(\phi^*) + w^* \sin(\theta^*) & 0 \end{bmatrix} \begin{bmatrix} \bar{u} \\ \bar{w} \\ \bar{q} \\ \bar{\theta} \\ \bar{h} \end{bmatrix} + \begin{bmatrix} X_{\delta_e} & X_{\delta_t} \\ Z_{\delta_e} & 0 \\ M_{\delta_e} & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \bar{\delta}_e \\ \bar{\delta}_t \end{bmatrix}$$

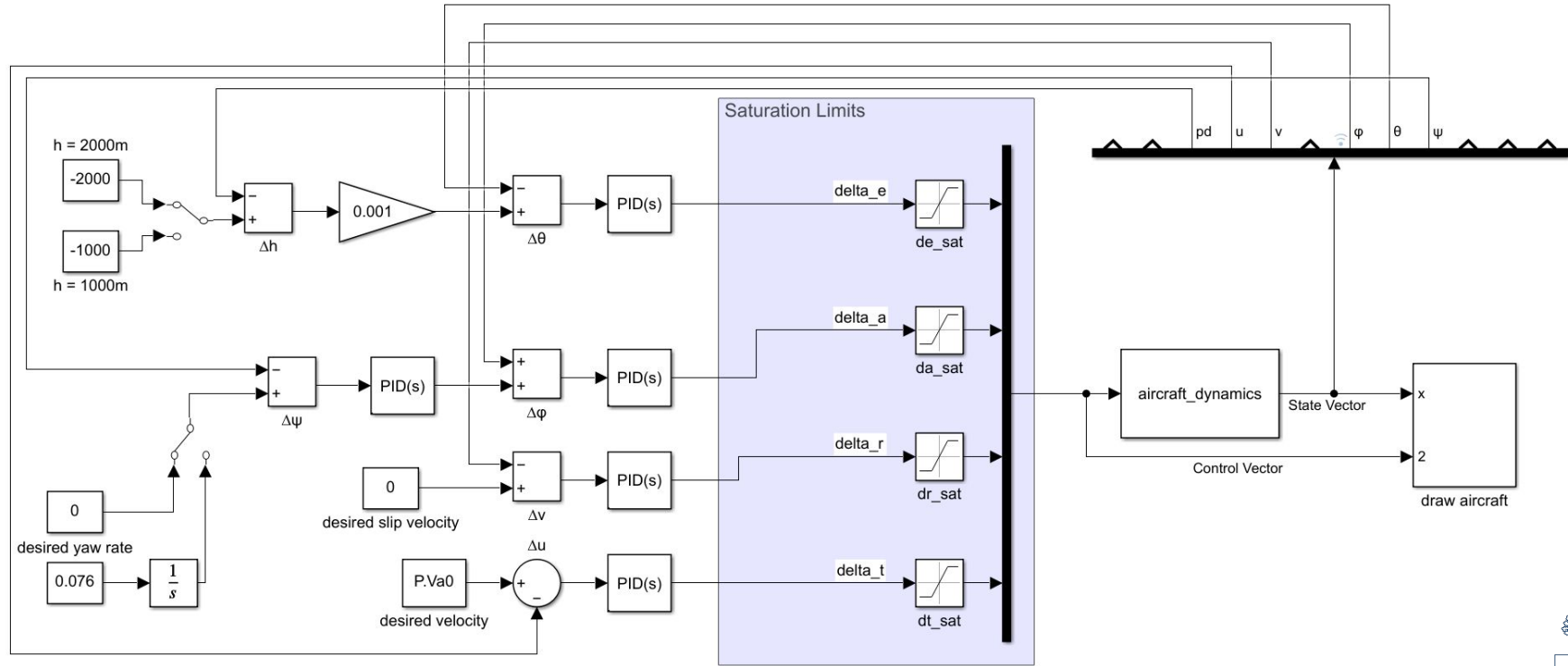
$$\begin{bmatrix} u^* \\ v^* \\ w^* \\ V_a^* \\ p^* \\ q^* \\ r^* \\ \phi^* \\ \theta^* \\ \varphi^* \\ \beta^* \\ \alpha^* \\ \delta_e^* \\ \delta_a^* \\ \delta_r^* \\ \delta_t^* \end{bmatrix} = \begin{bmatrix} 18.33 \\ 0 \\ 5.01 \\ 19 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0.2671 \\ 0 \\ 0 \\ 0.2671 \\ -0.15616 \\ 0 \\ 0 \\ 0.8311 \end{bmatrix}$$

Flight dynamics are decoupled into lateral and longitudinal dynamics

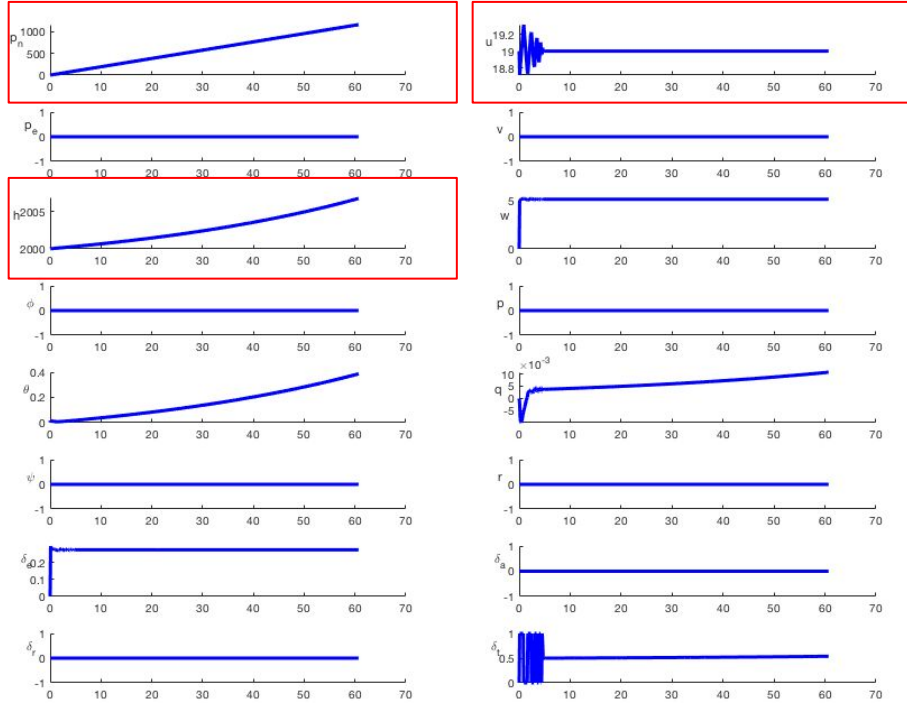
Trim States & Inputs



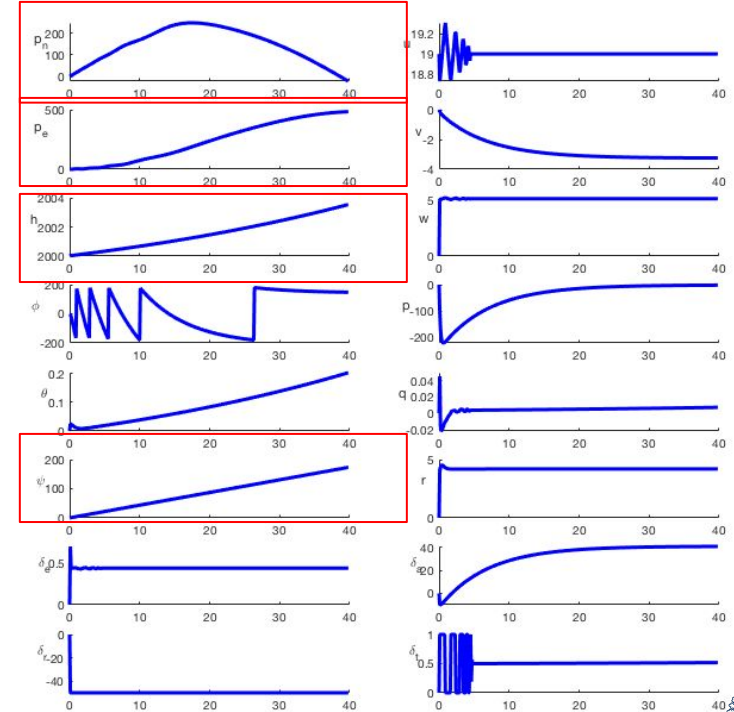
# Fixed-Wing: Controller (Alt. Hold and Coord. Turn)



# Fixed-Wing: Simulation Results



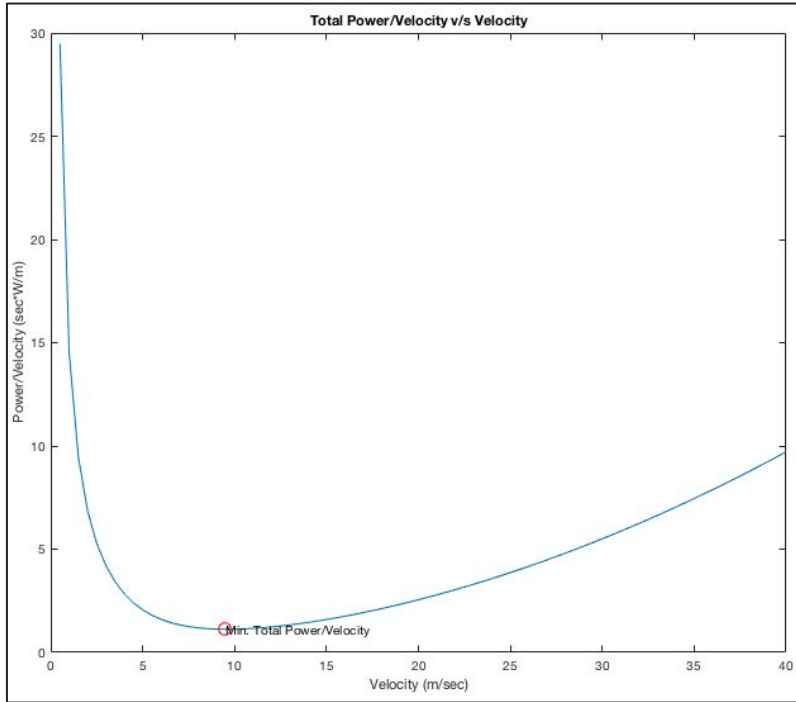
Steady-Level Flight (Altitude and Speed Control)



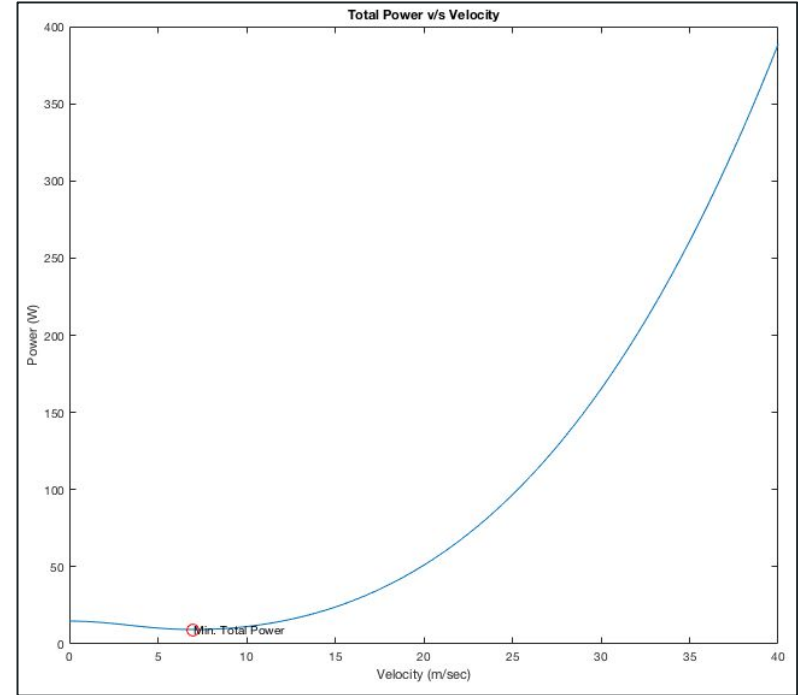
Level-Coordinated Turn



# Multi-Rotor: Performance



Max. Range: ~34 km  
Flying speed for max. range: 9.5 m/sec



Max. Endurance: ~68 minutes  
Flying speed for max. endurance: 7 m/sec



# Multi-Rotor: Model Dynamics

$$\text{Earth frame} \quad \begin{pmatrix} \dot{p}_n \\ \dot{p}_e \\ \dot{h} \end{pmatrix} = \begin{pmatrix} c\theta c\psi & s\phi s\theta c\psi - c\phi s\psi & c\phi s\theta c\psi + s\phi s\psi \\ c\theta s\psi & s\phi s\theta s\psi + c\phi c\psi & c\phi s\theta s\psi - s\phi c\psi \\ s\theta & -s\phi c\theta & -c\phi c\theta \end{pmatrix} \begin{pmatrix} u \\ v \\ w \end{pmatrix}$$

$$\text{Body frame} \quad \begin{pmatrix} \dot{u} \\ \dot{v} \\ \dot{w} \end{pmatrix} = \begin{pmatrix} rv - qw \\ pw - ru \\ qu - pv \end{pmatrix} + \begin{pmatrix} -g \sin \theta \\ g \cos \theta \sin \phi \\ g \cos \theta \cos \phi \end{pmatrix} + \frac{1}{m} \begin{pmatrix} 0 \\ 0 \\ -F \end{pmatrix},$$

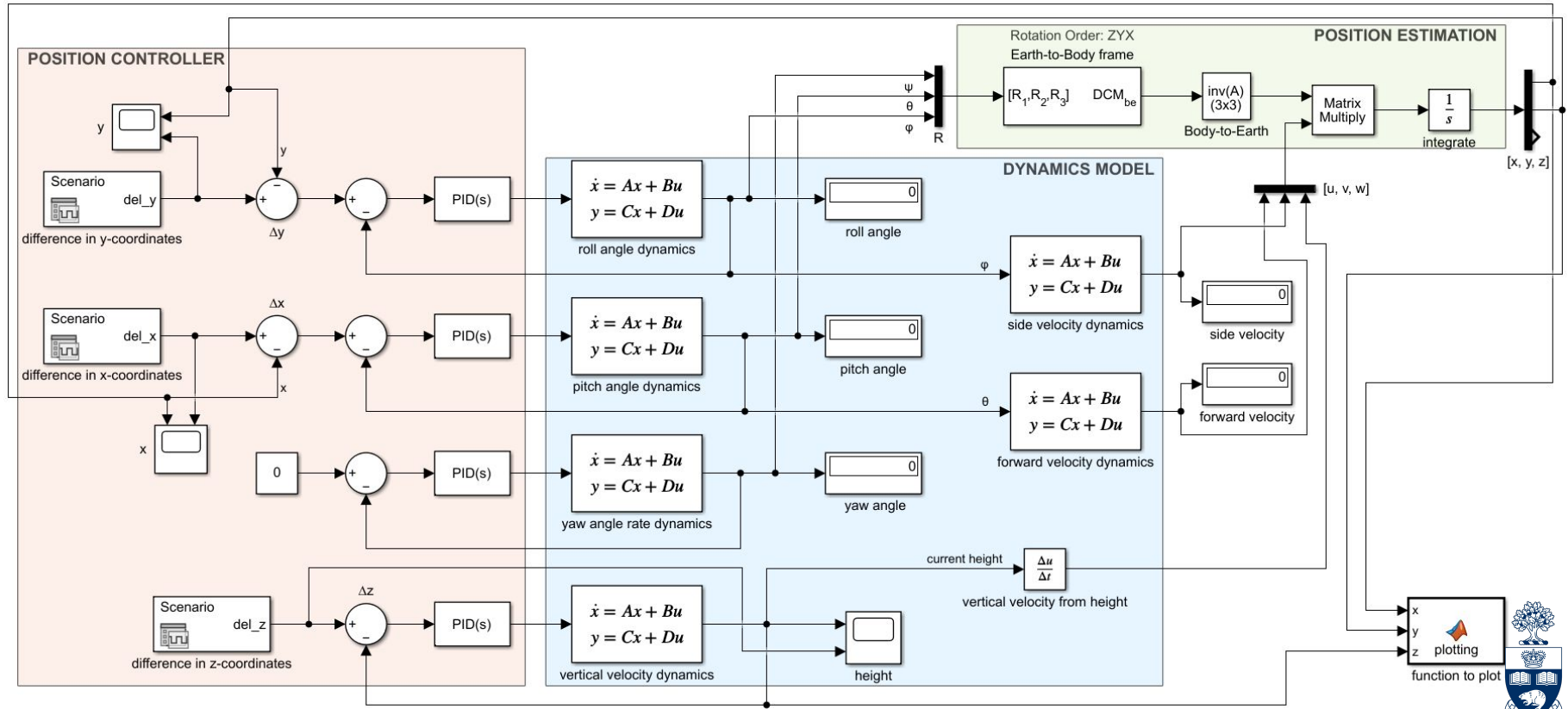
$$\text{Vehicle frames} \quad \begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix} = \begin{pmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \frac{\sin \phi}{\cos \theta} & \frac{\cos \phi}{\cos \theta} \end{pmatrix} \begin{pmatrix} p \\ q \\ r \end{pmatrix},$$

$$\text{Body frame} \quad \begin{pmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{pmatrix} = \begin{pmatrix} \frac{J_y - J_z}{J_x} qr \\ \frac{J_z - J_x}{J_y} pr \\ \frac{J_x - J_y}{J_z} pq \end{pmatrix} + \begin{pmatrix} \frac{1}{J_x} \tau_\phi \\ \frac{1}{J_y} \tau_\theta \\ \frac{1}{J_z} \tau_\psi \end{pmatrix}.$$

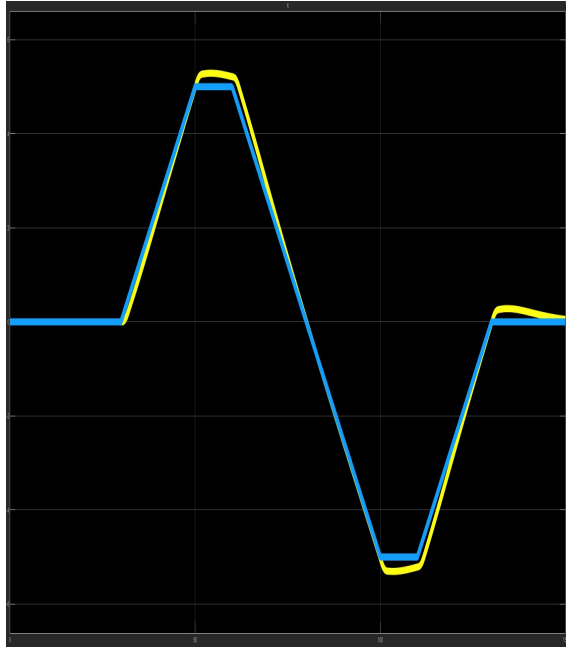




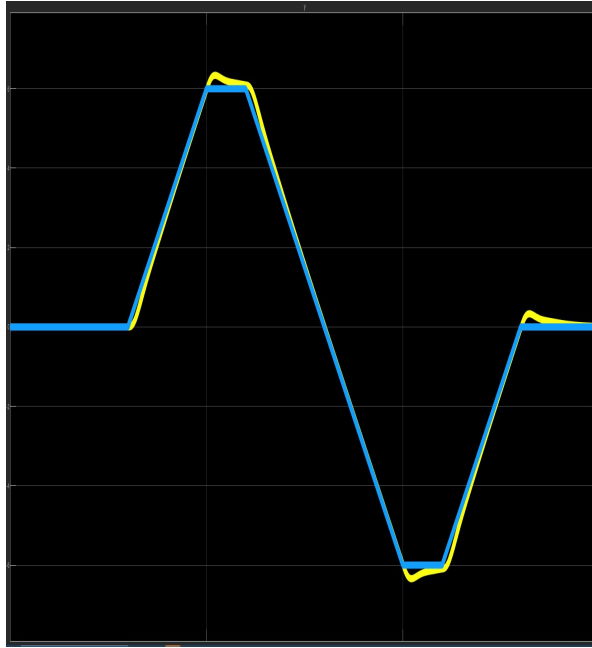
# Multi-Rotor: Controller



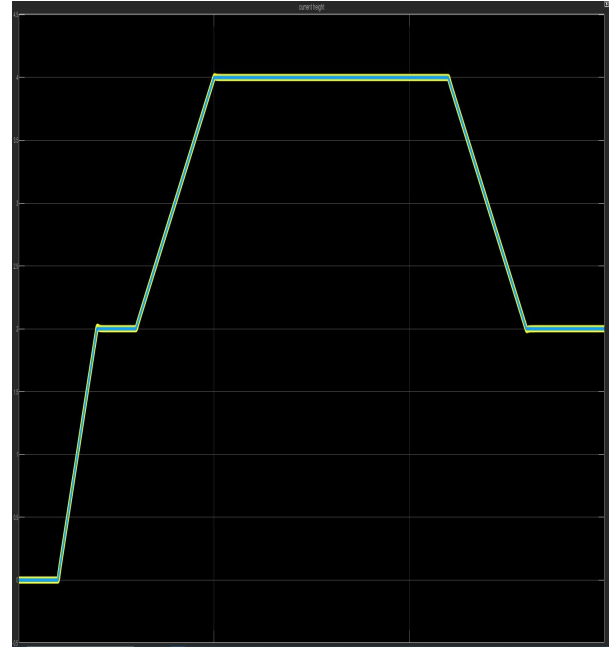
# Multi-Rotor: Simulation Results



x-coordinate

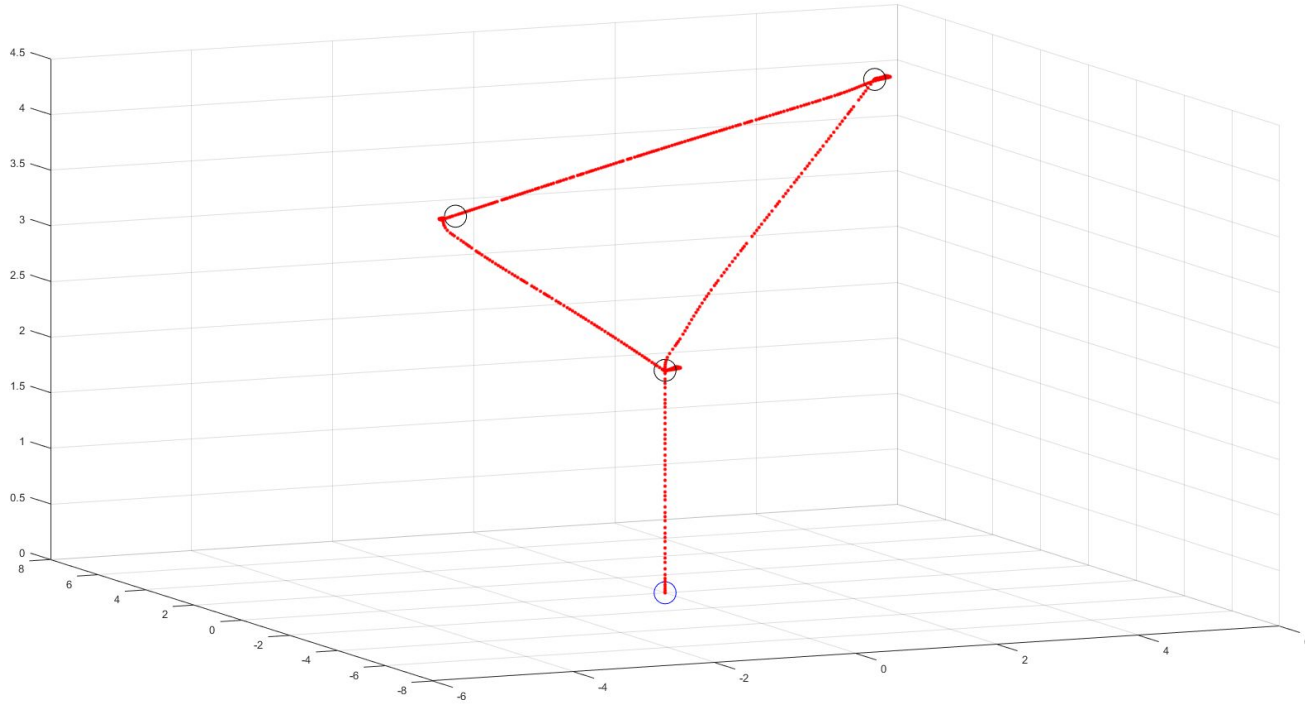


y-coordinate



z-coordinate

# Multi-Rotor: Simulation Results



# Conclusion

- It was observed that linearized system is quite sensitive to trim conditions
- Non-linear dynamics equations are easier to derive and implement; hard to design a controller for the same
- Linear dynamics are mathematically intense to derive; easier to develop a controller and debug during development
- Important to have good visualization tools

