

Predicting Machine Damage Accumulation using a Data driven Surrogate model

CSD402: Internet and Web Systems

Project Report

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Abstract

Data-driven models are one of the most popular types of surrogates due to their versatility, low evaluation cost, easy handling, and a large number of modeling techniques with ready-to-use implementations. In this work, we propose a pipe-lined architecture that implements Support Vector Regressors, Linear Regressors and LSTM based models for predicting damage accumulation based on given sensor values. Further, an ARIMA based architecture was used for forecasting individual sensor values (temperature) which can then be used by our data-driven models for predicting damage accumulation, thus enabling predictive maintenance. We also propose a novel scheduling algorithm for slot scheduling for laboratories in an academic setup that exploits predictive model for maximum utilization without causing maintenance induced interruptions.

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1 Introduction

These days, we have manufacturing machines loaded with sensors that provide critical usage data. These sensors record a variety of values such as temperature, velocity, and acceleration in regular time intervals. The sensors also provide a computed damage accumulation measure, which is helpful for predictive maintenance.

Damage accumulation in materials is a consequence of micro-defect evolution, which may lead to degradation of mechanical properties up to failure. It may also be defined with the help of Miner's rule that operates on the hypothesis that the portion of useful fatigue life used up by a number of repeated stress cycles at a particular stress is proportional to the total number of cycles in the fatigue life, if that were the only stress level applied to the part. The theory of cumulative damage assumes that a stress cycle with an alternating stress above the endurance limit inflicts a measurable permanent damage.

The objective of this problem is to create a data-driven surrogate model that makes it possible to rapidly compute the damage accumulation values based on the other measurements.

2 Background Work

2.1 Machine Learning for predictive maintenance of industrial machines using IoT sensor data (2017)

The paper [1] discusses:

Data collection was done from a slitting machine. Data generated from the Slitting machine was collected using sensors and pushed to the cloud. This data was sampled per second and collected for a period of one month. The data is stored as CSV in the system, consisting of 5 columns namely, Time Stamp, Tension, Pressure, Width and Diameter. Sliding Mean was used to replace the missing values in the data collected. The sensors send the data when the machine shows a change in state which usually is sampled per second. Hence, the data received consisted of many Null values. The first step towards preprocessing included replacing the Null values with the sliding mean values. The failure points in the data were less as compared to the data points representing good production cycles, the authors tried outlier detection using clustering and studied the outliers to gain insights. The authors used

the following models:

Naive Bayes, Support Vector Machines, CART, Deep Neural Network and ARIMA: Autoregressive integrated moving average (ARIMA) model was used to predict future points [4] in the data series. Since the data showed non-stationarity, The authors have used ARIMA. The model is fitted in the dataset and further points are predicted to find if the future states which might lead to a failure.

2.2 Predictive maintenance applications for machine learning (2017)

The key contributions of this paper [2] are listed below: The authors looked at a dataset containing a subset of maintenance inspections performed by the customer across a period of 19 years, starting in 1997 and ending in 2015. For the purpose of proof of concept engagement, to provide the most business value, the authors had agreed with the customer to focus on the asset that was most serviced, a particular type of sophisticated swivel. This swivel is used in two different settings: fracking or cementing, with different observed failure risk profiles. A number of data inconsistencies had been observed in the dataset. Working with the customer's subject matter experts, the authors dealt with these issues either by removing assets where a reconciliation could not occur, or by correcting the data where possible. The authors began building a number of Predictive Models to identify assets that are going to fail within a year of the maintenance inspection. Models used included Linear regression, Logistic Regression, Neural Networks, Decision Trees, Random Forests, Gradient Boosting Machines. When evaluating the models, the authors typically randomly split the dataset into a training set and a held-out validation set. They used the model built from the training set to predict the examples in the held out validation set and compute the metrics described above. However, with small datasets, exposure to the possibly large variance in the random selection of the validation set is inevitable. For this reason, the authors employed a method called 10 fold Cross-Validation that is estimating the performance of the final model built on a full dataset by splitting the dataset into 10 folds, then building a model on 9 folds and predicting the 10th. then rotating the folds in such a way that we end up with 10 submodels where each example in the original set appeared in exactly one validation set for a submodel. At this point the authors had collected one prediction for each example, which will ensure that their computation of the performance metrics has lower variance and is more robust than one based on a random sample of the data alone. The Champion Model was an Artificial Neural Network with 3 neuron layers, which looked at all variables in the data frame. This improvement in performance is expected as Neural Networks have the ability to uncover very complex relationships between variables.

2.3 Data-Driven methods for Predictive Maintenance of Industrial Equipment: A Survey

The contributions of this paper [3] are listed below. First, a comprehensive review of the PdM is conducted from four aspects, including the definition of the PdM, significance of the data-driven PdM, specific implementation methods of the data-driven PdM, challenges in the implementation process. Second, the PdM applications of the six algorithms are compared

from ML and DL perspectives, respectively, to provide graduate students, companies, and institutions with the preliminary understanding of the existing works recently published.

LR Model: LR is a well-known classification model in ML with the lowest algorithm complexity. It belongs to supervised learning; therefore, the collected data must have corresponding labels to be fed into the model. In addition, the LR model takes a linear combination of features as its input and applies a nonlinear function to conduct mapping, so that each output will fall within the range of $(0, 1)$ and a probabilistic interpretation can be obtained.

SVM: Typically, the SVM model is used to tackle the tasks for binary classification. In the PdM of industrial equipment, SVMs have been widely applied for identifying a specific status based on the acquired signal. Moreover, because of the diversity of fault types and the ability of mapping low dimension features to hyperplanes, the SVM model can be utilized to solve multiclass tasks.

DT and RF: DT classifiers have achieved great success in various fields such as character recognition, medical diagnosis, and speech recognition. Most significantly, a DT model has the ability to decompose a complex decision-making process into a collection of simpler decisions by recursively partitioning the covariate space into subspaces, thus providing a solution that is prone to interpretation. Furthermore, RF is an ensemble learning algorithm composed of multiple DT classifiers, and the category of its output is determined jointly by these individual trees. The RF is provided with many significant advantages. For instance, it can handle high dimensional data without feature selection; trees are independent of each other during training process, and the implementation is relatively simple; in addition, the training speed is usually fast, and at the same time the generalization ability is strong enough.

ANN: Inspired by the biological neural network, ANN is designed to address nonlinear problems. It is a massively parallel computing system consisting of an extremely large number of simple processors with many interconnections. The ability of ANN models to automatically learn from examples makes them attractive and extensively applied. Moreover, compared with traditional data-driven methods, NNs have obvious advantages in addressing fuzzy data, random data, and nonlinear data. They are especially suitable for systems with a large scale, a complex structure, and unclear information.

DNN: Compared with traditional data-driven methods, DNNs can self-adaptively extract fault features to effectively represent crucial information and realize intelligent diagnosis; they can also improve identification accuracy and are extremely effective in reducing defects in manual design features.

AE: In the PdM of industrial equipment, labeled raw sensor signals are generally difficult to obtain, requiring specific and detailed experimental settings. Obviously, unsupervised feature learning is especially suitable for handling unlabeled data; it can provide a feasible solution for fault identification and RUL estimation. In addition, the AE model belongs to the type of unsupervised learning that only requires unlabeled measurement data, and it has received extensive attention and application. Third, on the basis of the above comparison, accuracy, which is the most widely used evaluation metric, is analyzed in detail, and the corresponding conclusions are drawn. In addition, some potential research directions are provided consequently. Both ML and DL can remarkably complete the PdM task. The average prediction accuracy of the reviewed literature can reach 95.06%, and the highest accuracy

is 100%. With the great improvement of computational power and the rapid growth of data volume, AI algorithms and their variant models have increasingly demonstrated a superior advantage of performance. With the continuous innovation of algorithms, researchers will continue to focus on the data-driven methods in PdM applications.

3 Technical Details

3.1 Machine Maintenance Improving Machine Health

Machine maintenance is the process of performing upkeep on machinery to ensure continued working order. It may include maintenance that occurs as a part of a regular routine or prior to any sort of breakage or damage to things, like cleaning surfaces, lubricating gears, and checking for wear and tear on parts like belts. Poor maintenance strategies can reduce an organization's overall productive capacity. It can prove difficult to determine how often a machine should be taken offline to be serviced taking into account the weight borne by the risks of lost production time due to maintenance against those of a potential breakdown. Maintenance work, such as replacing and repairing parts and servicing equipment, can impose a large financial burden on the organization.

3.2 Maintenance Strategies

There are multiple strategies possible for maintenance.

- **Reactive Maintenance:** As the name implies, the machines are allowed to run to failure and any maintenance is carried post their failure. It is appealing because it offers the maximum utilization and in turn maximum production output, of the asset by utilising it to its limits.
- **Preventive Maintenance:** This involves preventing problems before they arise. This is also referred to as Planned Maintenance. It consists of maintenance tasks performed while the equipment is under normal operation to avoid unexpected breakdowns and the associated downtime and costs.
- **Predictive Maintenance:** This involves predicting problems to increase asset reliability. It directly monitors asset performance during normal operations to anticipate and predict failures.

3.3 Predictive Maintenance

Predictive maintenance has been enabled by advances in technology that connect the asset/machine to data analytics through sensor data. These days, we have manufacturing machines loaded with sensors that provide critical usage data. These sensors record a variety of values such as temperature velocity and acceleration in regular time intervals. These sensors may also provide a computed damage accumulation measure, which is helpful for predictive maintenance. It directly monitors asset performance during normal operation to

anticipate and predict failures. Predictive maintenance analyzes the data gathered from sensors connected to assets. This data can be used to predict when an asset will fail and in turn, allows maintenance teams to correct the issue before a failure occurs. Rather than running a part to failure, or replacing it when it still has life because of protocols, predictive maintenance helps organizations optimize their strategies by conducting maintenance only when completely necessary.

3.4 Barriers to Predictive Maintenance

- **Detection Modalities and associated datasets:** Predictive maintenance hinges on processing multiple datasets, notably those associated with different sensors and maintenance detection modalities such as vibration analysis, oil analysis, thermal imaging, acoustics and more.
- **Data Fragmentation:** Even when data from multiple sensors are available, they tend to be isolated from each other and are often represented in different formats, making their integration challenging.
- **Lack of proper analytics algorithms and tools:** The predictive analysis of large datasets requires advanced algorithms and tools beyond baseline machine learning and statistical models.
- **Complexity:** It is complex to establish than a preventive measure strategy. If the proper technology is not already established, it requires time to set up the infrastructure which involves developing equipment, technology and user adoption methods.
- **Data Collection:** Collecting the right data to enable the organization to accurately predict failures and malfunctions is crucial.

3.5 Functionality

There are multiple entities that we require, for our model of predictive maintenance to work efficiently. The entities represent different components of the structure, which will manage all the work and data flow. The majority can be alluded to as User, Admin, Analyst, Sensors, Server, Database. The **User** of the machine will be able to place requests for the slots in which different machines can be used. Based on the availability of the machine, it will be assigned to the respective slot. If the user faces any problem then, **Admin** can help him/her to troubleshoot the problems faced. **Sensors** attached to different machines will be sending information about the machine in continuous uniform time-separated intervals. All the predictive maintenance work will be done with the help of the data sent through by the sensors, on **Servers**. All this information, whether computed or general information would be stored in a **Database**, where it would possible to access that data at any time required. **Analyst** will be the one responsible for building and enhancing the damage accumulation prediction model by retrieving the data directly from the database. The Time Series data collected so far would then be used to build and enhance damage accumulation prediction model by retrieving data directly from the database. With this predictive data, alerts are

sent when maintenance is required. The Admin can then act on these alerts to halt machines and allow maintenance activities.

3.6 Dataset Description

The data is obtained from the Bernard M. Gordon Learning Factory (Penn State). The readings from a heterogeneous set of sensors used to report metrics continuously for many different machines.

3.7 Prediction Approach

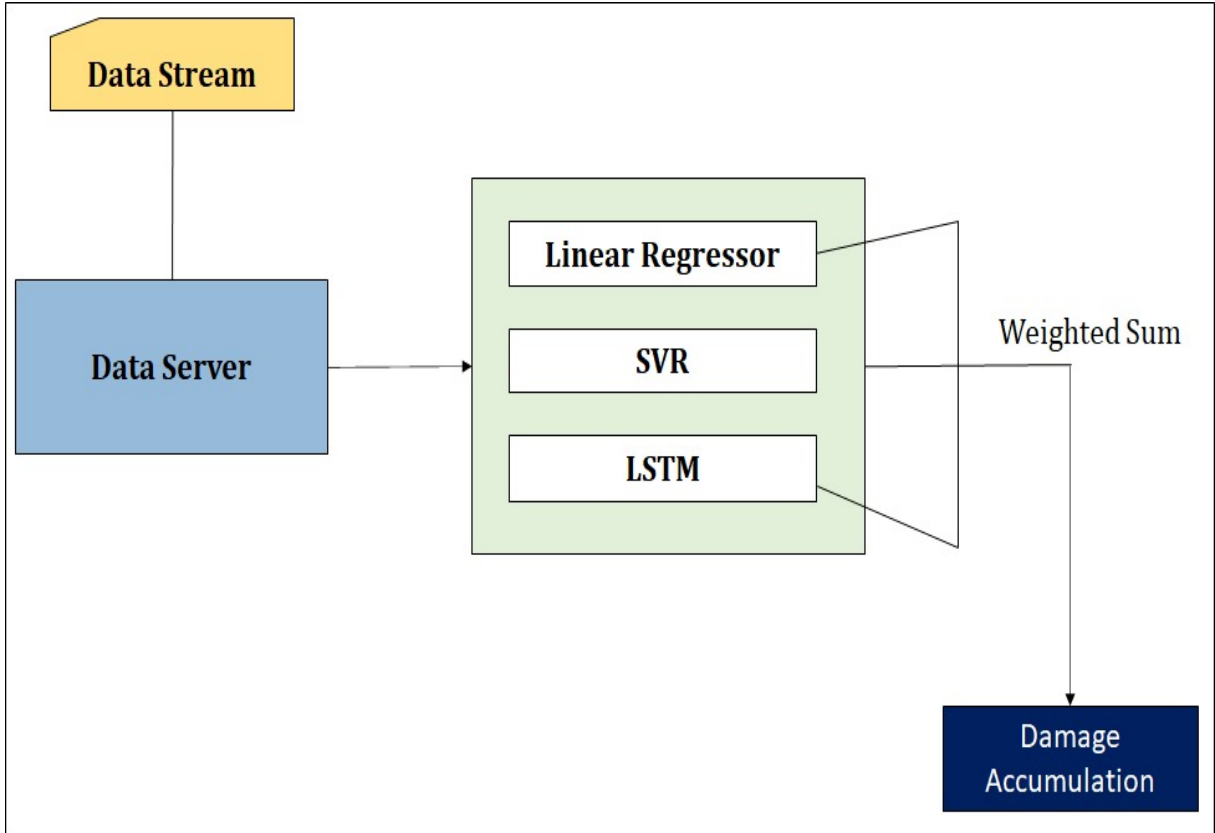


Figure 1: Proposed Model

The proposed architecture takes into account the weighted average of the Damage Accumulation DA_{model} values determined from the three models. We compute the weighted average based on the $R2$ score for Linear Regressor and SVR with the LSTM value. A higher $R2$ score implies a higher accuracy pertaining to which its weight increases, eventually having a more significant impact on the final damage accumulation value ($DA_{predicted}$).

$$DA_{LRWeighted} = R2_{score} \times (DamageAccumulation_{LR}) \quad (1)$$

$$DA_{SVRWeighted} = R2_{score} \times (DamageAccumulation_{SVR}) \quad (2)$$

$$DA_{predicted} = DA_{LRWeighted} + DA_{SVRWeighted} + DA_{LSTM} \quad (3)$$

3.8 Proposed Approaches for effective Predictive Maintenance

1. Slot-Wise Prediction

One of the methods is to analyze and predict damage accumulation before every slot is allotted, and then if the machine is in working condition then allot the slot. This approach has some disadvantages as predicting when the user has asked for a slot, has no use, as that can be figured out by the Admin only.

2. 2-Day Prediction

Analyze and predict the damage accumulation for finite number of days, so that the maintenance can be scheduled accordingly so as to minimize the reduction of working hours of the machine. This approach may also have a bottleneck when the schedule is tight for the week, and there is no time for its maintenance.

3. Chosen Approach: Weekly Prediction

Analyze and predict damage accumulation for a week in advance, which would allow us to have increased buffer time for machine repair including out of office times and weekends. There are some benefits for this approach as we can have Day-Wise analysis, Weekly average, Month-wise analysis.

3.9 SAM - Scheduling Algorithm

Given the data about different tasks required to be completed by different users(students/staff) on machines which have predictive maintenance model enabled. The data presumably consists of the duration of each task requires, and the deadlines for each of them, suggesting the urgency of it. We propose an algorithm which takes into account the slots available for the machine over the week, and the data given to it by the users, to assign slots to the respective projects.

The basic implementation of the program is to first sort the data according to the deadlines, then assign higher priority to the deadlines. It might be possible that multiple of them may have the same deadline, when a weighted value is taken to give more priority to the tasks requiring more time to complete than others. It also checks whether the duration and deadlines specified are feasible or not, comparing the total hours of the tasks to the total slots available, and also comparing the total hours of similar deadline tasks to the total slots available for them. **Pseudo Code:** The Basic implementation of the algorithm [5](#)

4 Experiments

The dataset consists of information provided by the sensors attached to different machine collected from (cite). The task at hand is to predict damage accumulation for predictive maintenance of machines, to enable a higher performance, and reduced off time. 80% of the values from the Dataset were considered as the training set for different machine learning models, 10% for the testing set and the rest 10% for the validation set. The models used for this experimentation were, Linear Regression, Support Vector Regression and LSTM.

Support Vector Regression (SVR): We had trained the model on varying ratios of training and test data before finding most suitable ratio. SVR involves hyper-parameters and their tuning is key to rendering a good accuracy. We have employed auto-tuning to find the best suited hyper-parameters.

5 Results

Both the training and validation loss for the LSTM based model converge as shown in figure 2, showing effective learning. The accuracy has not been plotted as the target variables here are float values which may give incorrect insight on the model performance. Alternatively, a rounded-off approach for determining the accuracy may be employed.

Figure 3 shows comparison for the three employed approaches Linear Regression (LR), Support Vector Regression (SVR) and LSTM with the ground truth values. The LR and SVR are more accurate in predicting the ground truth variables while the LSTM fails to predict the peak values for the samples in range (100-150) and (200-250). One possible reason for this could be the small volume of points with such high values. Correspondingly, the LSTM is supposed the that the LSTM

Metric Scores		
Metrics	Linear Regression	SVR
Mean Squared Error 0.4263	0.1031	0.3332
$R2_{score}$ 0.898	0.9803	0.909

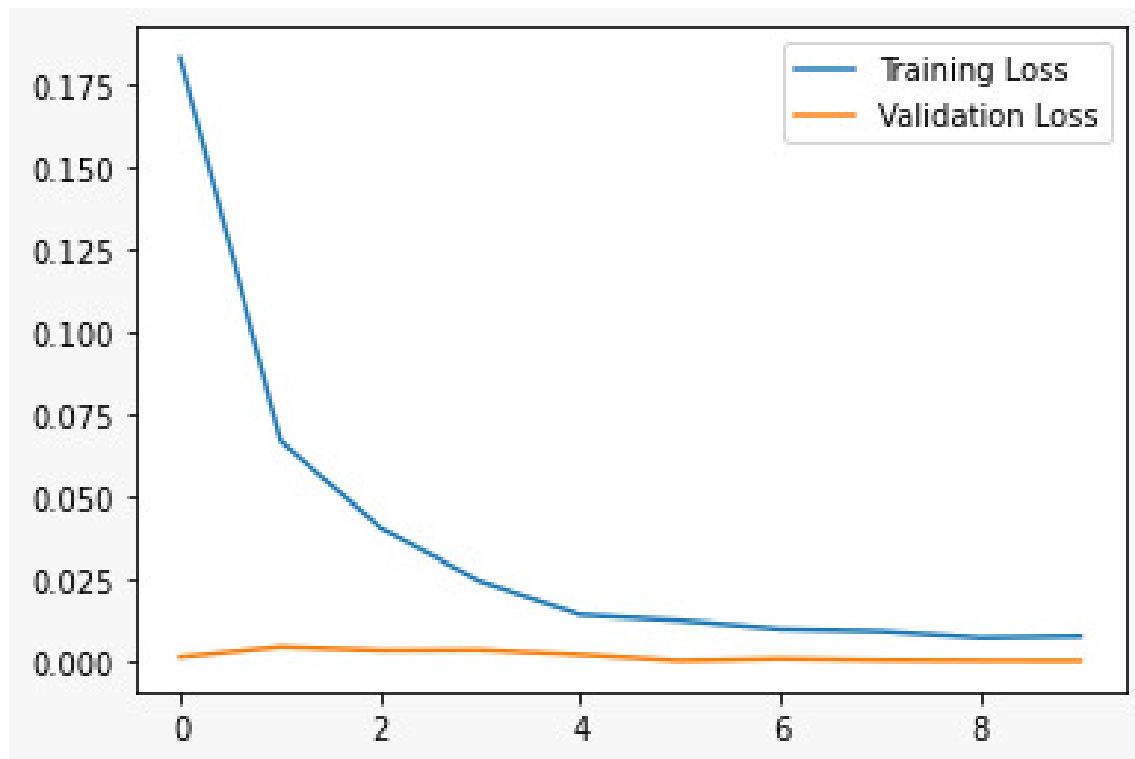


Figure 2: Training Loss and Validation Loss for LSTM

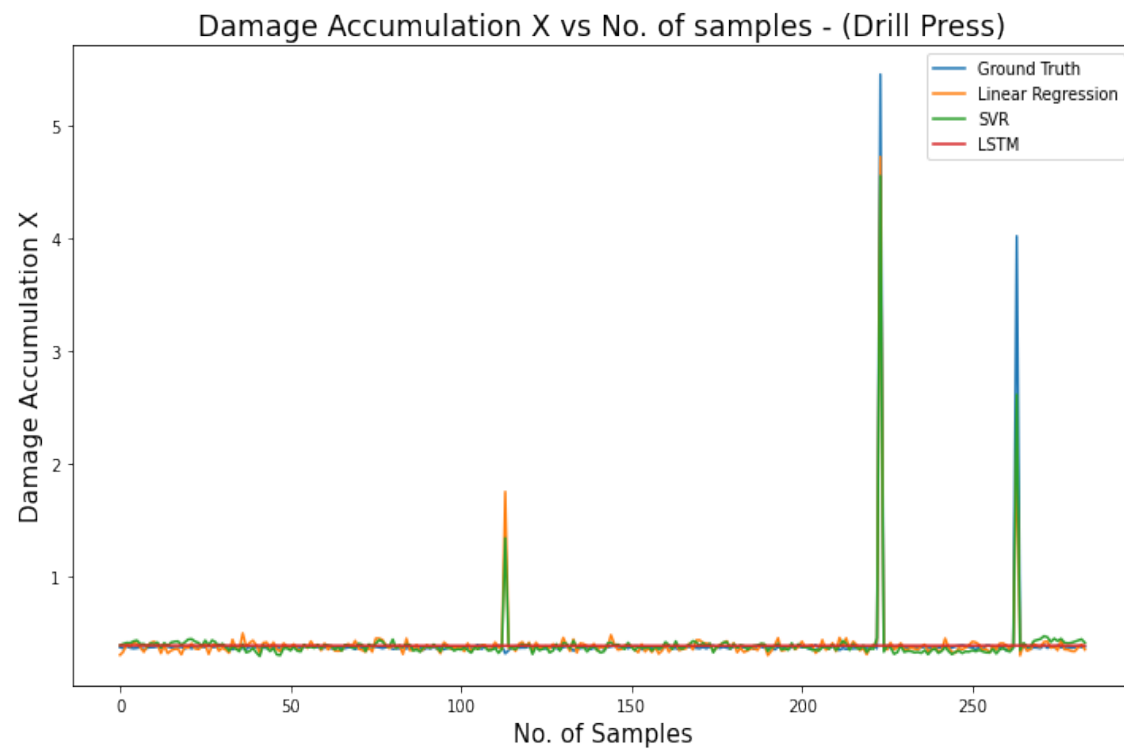


Figure 3: Prediction comparison of different Models

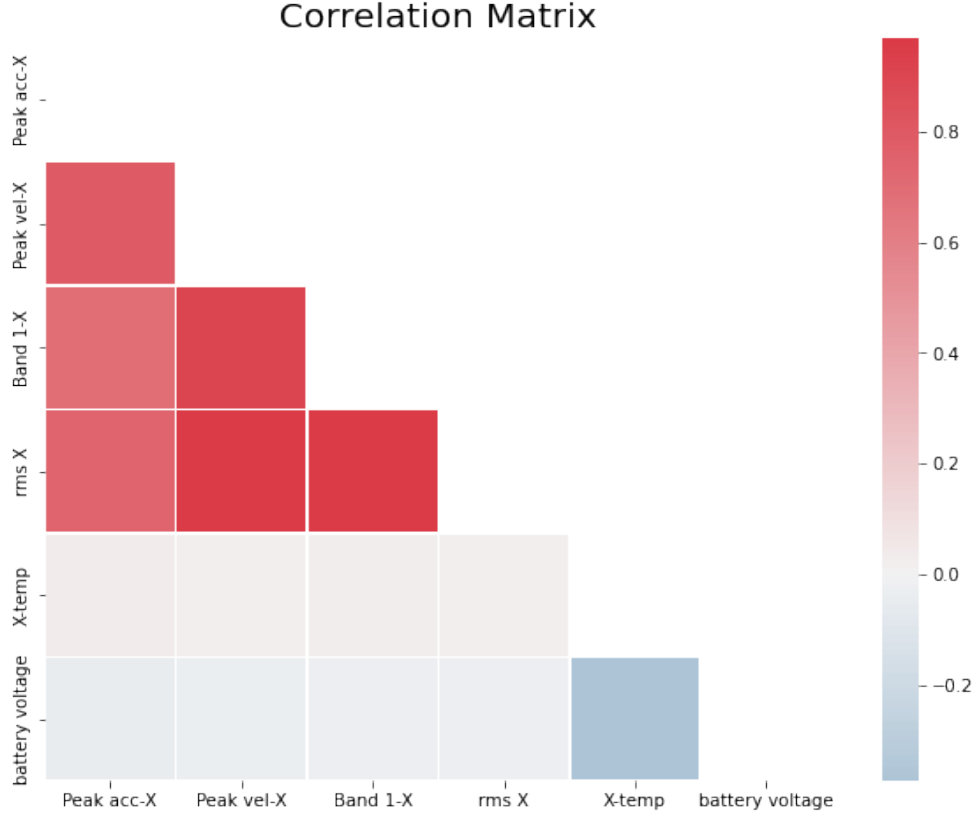


Figure 4: Correlation Matrix

6 Conclusion and Future Scope

The results are encouraging and show that the proposed architecture can be useful in the predictive maintenance use case that we have targeted. Damage accumulation value and its relation with machine breakdown is an active research problem as it varies for every machine based on its mechanical parts and their corresponding usage. For instance, a machine with a high speed motor may break down more frequently than a low speed one for most cases. However, this may also vary depending on the material and the weight of the components for the motor. So, in such cases, it is recommended to experimentally determine the relationship between damage accumulation and machine breakdown, following which the relationship can be used to effective implementation of predictive maintenance.

The SAM - scheduler is a promising algorithm and has the potential for successful implementation in manufacturing laboratories in an academic setup. The scheduler also takes into account a buffer time to incorporate cases wherein the user may end up consuming more time for the given task or the machine breaks down during the operational hours. It is though noteworthy that the latter can occur only in the case of a Predictive Maintenance failure when the model incorrectly predicts the possible time to breakdown.

The experiments currently were done on the data collected before hand, but in future the data would be continuously be sent to the server in a stream, with a uniform interval.

Algorithm 1 SAM Scheduler

```
1: duration  $\leftarrow$  List of all project duration (in hours)
2: deadline  $\leftarrow$  List of number duration duration array
3: procedure High_Level_Feasibility_Check(params)
4:   if projectHrs > available * days then
5:     feasible  $\leftarrow$  False
6:   end if
7: end procedure
8: procedure Low_Level_Feasibility_Check(params)
9:   i  $\leftarrow$  0
10:  while i < len(project) do
11:    count  $\leftarrow$  1
12:    c  $\leftarrow$  project[i][1]
13:    s  $\leftarrow$  project[i][0]
14:    for j = i + 1, i + 2 ... len(project) do
15:      if project[j][1] == c then
16:        count  $\leftarrow$  count + 1
17:        s  $\leftarrow$  s + project[j][0]
18:      else
19:        break
20:      end if
21:    end for
22:    if s > available * count then
23:      feasible  $\leftarrow$  False
24:      while project[i][1] == c do
25:        nfp.append(i)
26:        i  $\leftarrow$  i + 1
27:      end while
28:    end if
29:  end while
30:  if not feasible then
31:    print("The following projects are not feasible : ")
32:    for i = 1, 2 ... len(nfp) do
33:      print("Project" + nfp[i] + 1)
34:    end for
35:  end if
36:  assert feasible
37: end procedure
```

```

1: procedure AllotSlots(params)
2:   High_Level_Feasibility_Check()
3:   setup_project_matrix()
4:   Low_Level_Feasibility_Check()
5:   available_slots_per_day  $\leftarrow$  Number and type of Daily slots available
6:   week_slots  $\leftarrow$  Weekly Slots to be filled
7:   i, start  $\leftarrow$  0
8:   while i < len(project) do
9:     c  $\leftarrow$  project[i][1]
10:    Append (i) to group
11:    for j = i + 1, i + 2 ... len(project) do
12:      if project[j][i] == c then Append (i) to group, i  $\leftarrow$  i + 1
13:      else break
14:    end if
15:  end for
16:  hrs, tday  $\leftarrow$  0
17:  for g in group do hrs  $\leftarrow$  hrs + project[g][0]
18:  end for
19:  while hrs > 0 do
20:    division  $\leftarrow$  ceil(hrs/c), s  $\leftarrow$  0
21:    for g = 1, 2 ... len(group) do
22:      if g! = len(group) - 1 then
23:        calc = ceil(project[group[g][0]]/hrs * division)
24:        s  $\leftarrow$  s + calc, Append (group[g], calc) to temp
25:      else Append (group[g], division - s) to temp
26:      end if
27:    end for
28:    flag  $\leftarrow$  True
29:    for t in temp do
30:      x  $\leftarrow$  available - availableslotsperday[tday], e  $\leftarrow$  x
31:      while e < available and e < x + t[1] do
32:        weekslots[tday][e]  $\leftarrow$  project[t[0]][2], e  $\leftarrow$  e + 1
33:      end while
34:      if x + t[1] <= available then
35:        availableslotsperday[tday]  $\leftarrow$  availableslotsperday - t[1]
36:        hrs  $\leftarrow$  hrs - t[1]
37:        project[t[0]][0]  $\leftarrow$  project[t[0]][0] - t[1]
38:      else
39:        availableslotsperday[tday]  $\leftarrow$  0
40:        hrs  $\leftarrow$  hrs - (available - x)
41:        project[t[0]][0]  $\leftarrow$  project[t[0]][0] - (available - x)
42:      end if
43:      project[t[0]][1]  $\leftarrow$  project[t[0]][1] - 1
44:    end for
45:    c  $\leftarrow$  c - 1, tday  $\leftarrow$  tday + 1
46:  end while
47:  i  $\leftarrow$  i + 1
48: end while
49: end procedure

```

As we have seen from previous data, there might be possibility of not receiving any signal at a particular timestamp, so we can use a rolling average to determine the missing stream values. We can further experiment by increasing the window size for non null values for the rolling average, to get more accurate results.

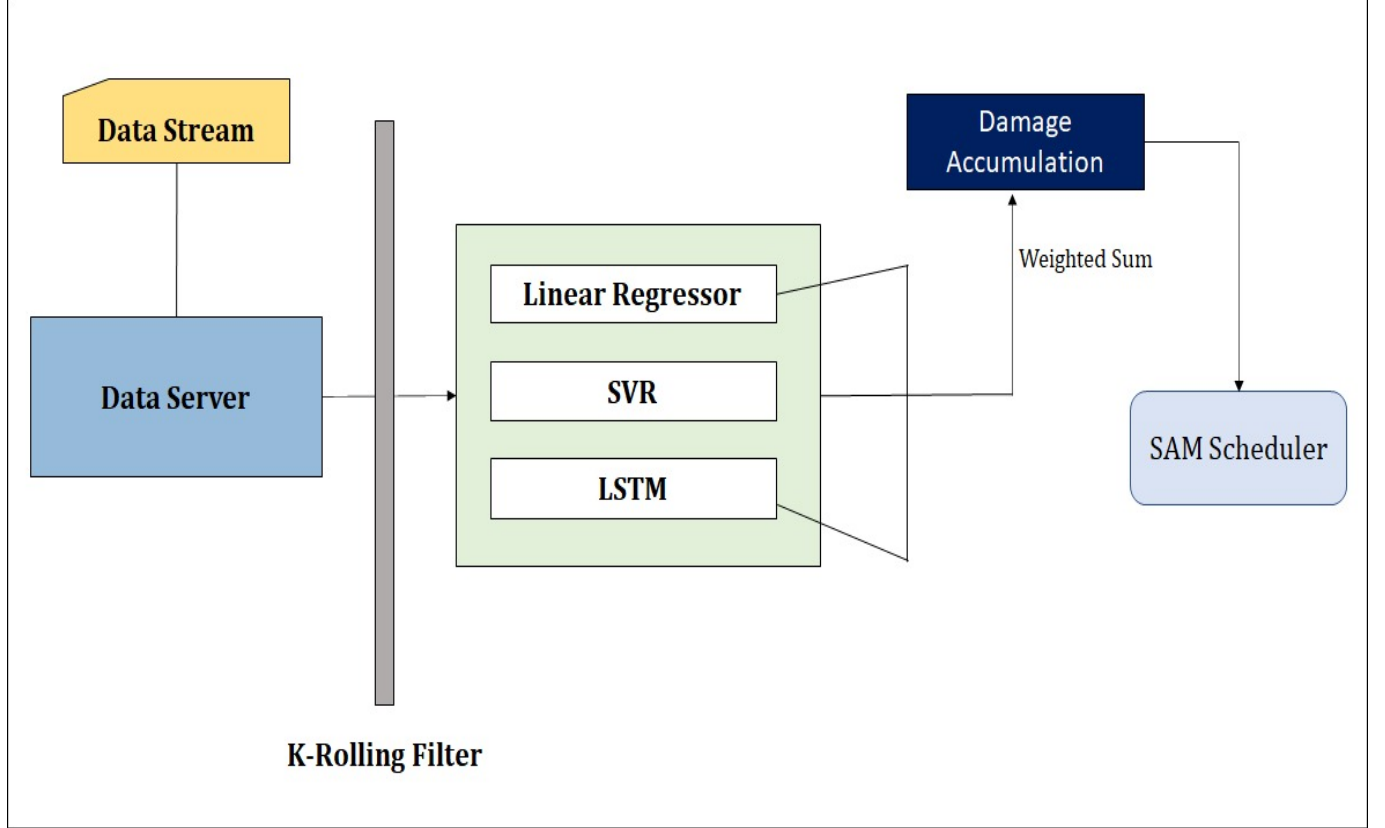


Figure 5: Proposed Model

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