Project - STAT 151A

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```
load(url("http://www.stat.berkeley.edu/users/nolan/data/baseball2012.rda"))
baseball = as_tibble(baseball)
```

Data Exploration and Feature Creation

1)

The first step is to clean the baseball data by removing unecessary explanatory variables and entries missing a salary (observed Yi) value.

```
baseball = baseball %>% dplyr::select(-c("ID", "yearID", "teamID", "lgID", "nameFirst", "nameLast", "G_" baseball = baseball %>% drop_na(salary) # remove units with no salary values
```

Next, I followed the author's process in creating new features as decribed in the textbook.

Finally, I cleaned the Position and Years explanatory variables through reimpementing them as dummy variables.

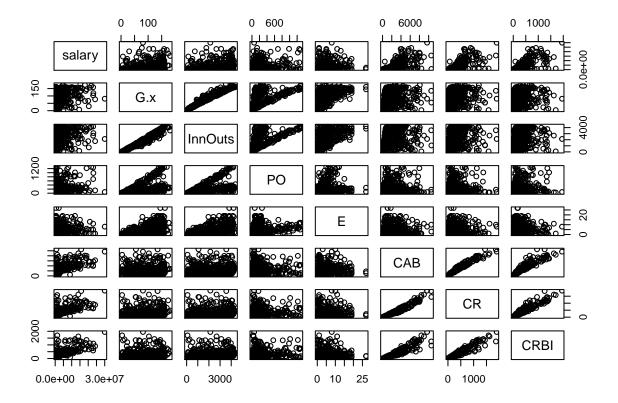
According to Fox's description of his analysis, he mentions **middle infielders** as players who consistently played second base or shortstop so I classified all individuals with either position as such.

```
lm.fit = lm(salary ~ ., data = baseball)
new.baseball = as_tibble(model.matrix(lm.fit)[,-1])
new.baseball$salary = baseball$salary
```

Now that we have completed the feature creation process, the next step is to analyze the data itself.

Firstly, I'll look at the structure of the data itself and how the different variables are associated with each other. Since there are a lot of explanatory variables within the data, I will select a few key variables I believe to be the most influential in the model and investigate the structure.

Note: -G.x = Position played at specified position - InnOut = Time played in the field expressed as outs - PO = Putouts - E = Errors - CAB = Career at bats - CR = Career runs - CRBI = Career runs batted in



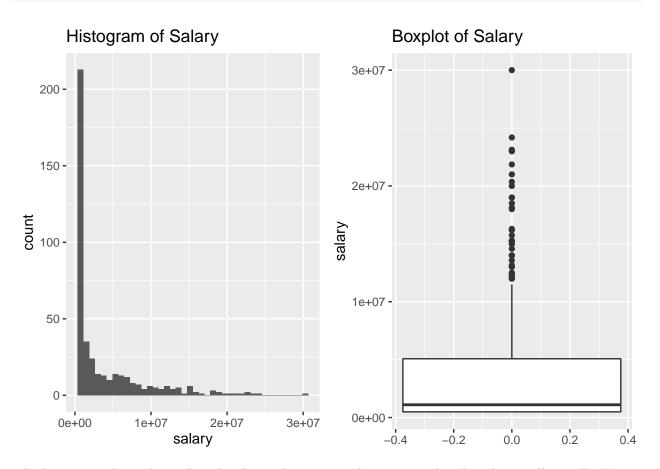
From observing the paired structures of data it is evident that some features are uncorrelated whereas others are strongly correlated. However, this is mostly expected as certain features relate to one another. For example, a player's career at bats would be associated with his career runs or career runs batted in since all tie into a players capability of scoring bases.

This indicates a possible issue in inference of coefficients through linear modeling since the standard error calculation will be grossly inflated.

In addition, I noticed some of the variables have a stronger correlation with the salary than that of other variables. For example, G.x and InnOuts do not seem to have a strong association with salary whereas CAB, CR, and CRBI have comparitively stronger correlations with salary. This indicates some sort of variable selection and model pruning may be of benefit.

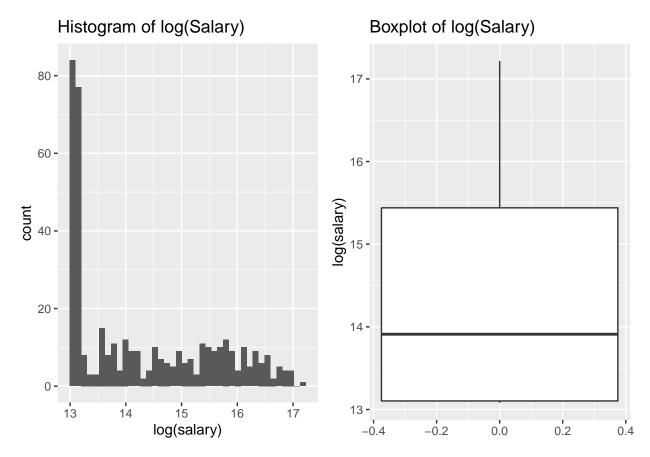
Next, I'd like to look into whether the data is distributed normally as per an assumption of guassian distributed errors in linear modelling.

```
sal1 = ggplot(data=new.baseball, aes(x=salary)) + geom_histogram(bins=40) + ggtitle("Histogram of Salary
sal2 = ggplot(data=new.baseball, aes(y=salary)) + geom_boxplot() + ggtitle("Boxplot of Salary")
grid.arrange(sal1, sal2, nrow=1)
```



The histogram above shows that the observed outcome values are not distributed normally at all. Hence, some sort of transformation of the data is necessary in order to use linear modelling.

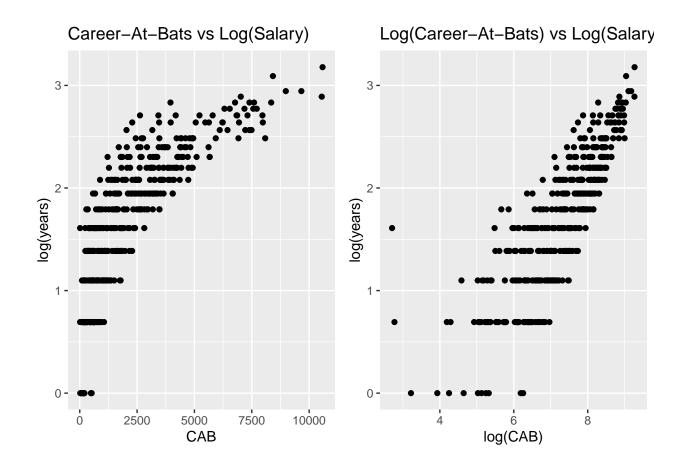
```
log.sal1 = ggplot(data=new.baseball, aes(x=log(salary))) + geom_histogram(bins=40) + ggtitle("Histogram
log.sal2 = ggplot(data=new.baseball, aes(y=log(salary))) + geom_boxplot() + ggtitle("Boxplot of log(Sa
grid.arrange(log.sal1, log.sal2, nrow=1)
```



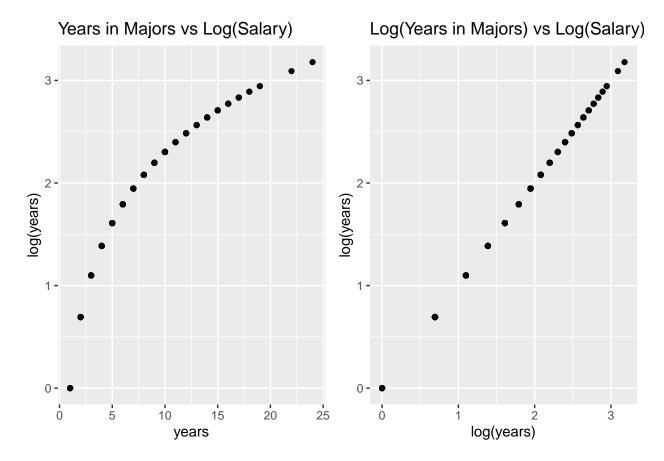
Fox mentions log transforming the salary data in his linear modelling analysis and this is in line with the observed histograms above. The histogram of the original salaries is right skewed whereas the histogram of the log transformed salaries is somewhat more stabilized and appears more so normally distributed in some sense.

Fox also suggests log transforming some feature variables (years in the majors, career-at-bats) through preliminary examination and so I will do the same to carry forward analysis in a similar manner. An argument for why this may be benefificial is that it might garner a stronger linear relationship between the seemingly most influential explanatory variables and the salary and thus improving the model's predictive capability overall.

```
cab.plot1 = ggplot(data=new.baseball, aes(x=CAB, y=log(years))) + geom_point() + ggtitle(label = "Caree.
cab.plot2 = ggplot(data=new.baseball, aes(x=log(CAB), y=log(years))) + geom_point() + ggtitle(label = ".
grid.arrange(cab.plot1, cab.plot2, nrow=1)
```



yrs.plot1 = ggplot(data=new.baseball, aes(x=years, y=log(years))) + geom_point() + ggtitle(label = "Years.plot2 = ggplot(data=new.baseball, aes(x=log(years), y=log(years))) + geom_point() + ggtitle(label = grid.arrange(yrs.plot1, yrs.plot2, nrow=1)



```
new.baseball$log.CAB = log(new.baseball$CAB)
new.baseball$log.years = log(new.baseball$years)
new.baseball$log.salary = log(new.baseball$salary)
new.baseball = new.baseball %>% dplyr::select(-c(CAB, years, salary))
```

Data Analysis

1)

For the first of the project, I will be fitting a simple model that predicts log(salary) from the dummy variables for years in majors and log(career runs), allowing for an interactio between the feature variables.

```
dat1 = new.baseball %>% dplyr::select(log.salary, CR, neg.sal, neg.cont)
simple.model = lm(log.salary ~ log(1+CR)*(neg.cont + neg.sal), data=dat1)
simple.model
Call:
lm(formula = log.salary ~ log(1 + CR) * (neg.cont + neg.sal),
    data = dat1)
Coefficients:
         (Intercept)
                               log(1 + CR)
                                                        neg.cont
            12.88064
                                   0.08743
                                                        -3.96431
                                            log(1 + CR):neg.sal
            neg.sal log(1 + CR):neg.cont
            -1.06871
                                   0.94036
                                                         0.24940
```

Although I have fitted the simple model above, I want to check for any outliers, high leverage points, and influential observations for further evaluation of the simple model. All criterions in determining such observations will be in line with what Fox suggests using.

```
hat.vals = hatvalues(simple.model)
stud.res = studres(simple.model)
cook.dis = cooks.distance(simple.model)
measures = tibble(Hat.Values=hat.vals, Studentized.Residuals=stud.res, Cooks.Distance=cook.dis)
```

First, I'd like to take a look at the **high leverage** points, which are observations with explanatory variables markedly different from that of the average. In terms of numerical cutoffs for diagnostic statistics, *hat values* exceeding **twice** the average hat value (k+1)/n are noteworthy.

```
h.3 = 3*length(simple.model$coefficients)/nrow(new.baseball)
high.leverage = measures[hat.vals > h.3,]
high.leverage
```

A tibble: 17 x 3

	Hat.Values	${\tt Studentized.Residuals}$	Cooks.Distance			
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>			
1	0.0477	1.87	0.0289			
2	0.0486	0.525	0.00235			
3	0.0565	0.0299	0.00000898			
4	0.0428	-0.305	0.000695			
5	0.0733	0.0664	0.0000582			
6	0.0507	-0.267	0.000637			
7	0.0428	-0.305	0.000694			
8	0.0733	0.0664	0.0000582			
9	0.0437	0.475	0.00172			
10	0.0554	0.606	0.00359			
11	0.126	0.163	0.000643			
12	0.0565	0.0284	0.0000807			
13	0.0489	0.533	0.00244			
14	0.0462	0.504	0.00206			
15	0.0573	0.564	0.00323			
16	0.245	0.334	0.00606			
17	0.148	1.51	0.0663			

There appears to be 17 data points which have a relatively high leverage.

In addition to high leverage points, I'll analyze discrepant observations to detect outliers within the data through utilizing studentized residuals with a numerical cutoff of |t-test statistic| > 2

```
outliers = measures[abs(stud.res) > 2,]
outliers %>% head(n=5)
```

```
# A tibble: 5 x 3
```

2	0.00468	-2.18	0.00370
3	0.0274	4.12	0.0768
4	0.00804	-3.01	0.0120
5	0.00476	-2.54	0.00510

There are **26** observations which are determined to be outliers.

Although I have determined observations that have high leverage or are outliers, what I am most conerned about are the subset of these points which have an influence on the determined coefficients of the model. Such points greatly alter the predictive capability of the simple model and thus cannot be overlooked.

Through recommendation by Fox, the criterion I will be using to determine highly influential points is D_i > 4/(n-k-1)

```
cook.cutoff = 4/(nrow(new.baseball)-length(simple.model$coefficients))
influential.points = measures[cook.dis > cook.cutoff,]
influential.points %>% arrange(desc(Cooks.Distance))
```

A tibble: 16 x 3

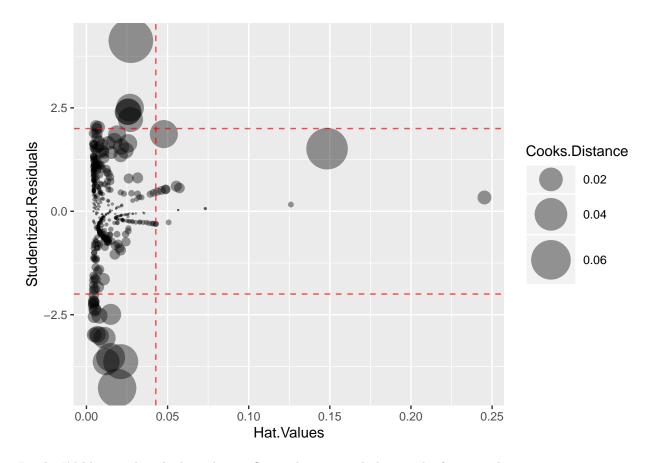
<dbl></dbl>	/JL75
	<dbl></dbl>
4.12	0.0768
1.51	0.0663
-4.27	0.0563
-3.63	0.0462
-3.53	0.0306
1.87	0.0289
2.50	0.0285
-3.64	0.0264
2.41	0.0254
2.40	0.0249
2.22	0.0227
-3.06	0.0173
-2.49	0.0155
-3.01	0.0120
1.64	0.0118
1.86	0.0111
	1.51 -4.27 -3.63 -3.53 1.87 2.50 -3.64 2.41 2.40 2.22 -3.06 -2.49 -3.01 1.64

It appears there are 16 influential points within the dataset. I'm not very surprised as players' baseball data is incredibly varied and prone to uniquely performing individuals, thus causing there to be influential observations.

To better grasp the idea behind the information produced above, the following is a plot of the hat values representing the leverage with relation to the studentized residuals. Each circle represents an obervation with it's area proportional to it's calculated Cook's Distance.

Note: The horizontal line represents 3 times the average hat value and the 2 vertical lines mark t-test statistics of -2 and 2.

```
measures = tibble(Hat.Values=hat.vals, Studentized.Residuals=stud.res, Cooks.Distance=cook.dis)
ggplot(aes(x=Hat.Values, y=Studentized.Residuals, size=Cooks.Distance), data=measures) +
   geom_point(alpha=0.4) + scale_size(range=c(0, 15)) +
   geom_vline(xintercept = 3*6/421, color='red', alpha=.7, linetype = "dashed") +
   geom_hline(yintercept = -2, color='red', alpha=.7, linetype = "dashed") +
   geom_hline(yintercept = 2, color='red', alpha=.7, linetype = "dashed")
```



Lastly, I'd like to take a look at these influential points and observe the feature values.

new.baseball[cook.dis > cook.cutoff,]

# A	tibble	: 16	x 44										
	POSC P	OSCF	POSMI	G.x	GS	${\tt InnOuts}$	PO	Α	E	DP	G.y	AB	
	<dbl> <</dbl>	dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	
1	0	0	1	153	147	3953	289	398	8	96	153	607	
2	0	0	0	154	149	4030	297	8	6	1	155	560	
3	0	0	0	104	102	2702	221	9	3	0	129	487	
4	0	0	0	74	56	1523	85	91	6	7	113	278	
5	0	0	0	13	12	269	86	3	0	7	60	89	
6	0	0	0	131	131	3383	207	7	4	0	135	518	
7	0	0	0	93	76	1953	131	2	0	0	130	384	
8	0	0	0	70	55	1358	81	3	1	2	94	233	
9	0	0	0	50	49	1239	37	81	8	7	74	273	
10	0	0	0	107	98	2399	156	1	1	0	130	394	
11	0	0	1	158	157	4176	227	434	12	93	158	593	
12	0	0	0	105	103	2562	73	208	13	14	108	396	
13	0	1	0	125	122	3220	339	6	4	3	128	516	
14	0	0	0	4	4	81	35	2	1	4	58	163	
15	0	0	1	55	37	1063	58	103	3	19	60	153	
16	0	0	0	1	0	0	0	0	0	0	78	2	
#	i+h	20 ~		omioble	D	/4k1\ U	/dh1\	VOD .	/JL1\	VOD /	มนาง ย	ואג ס	

[#] ... with 32 more variables: R <dbl>, H <dbl>, X2B <dbl>, X3B <dbl>, HR <dbl>,

[#] RBI <dbl>, SB <dbl>, CS <dbl>, BB <dbl>, SO <dbl>, IBB <dbl>, HBP <dbl>,

[#] SH <dbl>, SF <dbl>, GIDP <dbl>, CH <dbl>, CHR <dbl>, CR <dbl>, CR dbl>, CRBI <dbl>,

```
# CBB <dbl>, AVG <dbl>, OBP <dbl>, CAB.avg <dbl>, CH.avg <dbl>,
# CHR.avg <dbl>, CR.avg <dbl>, CRBI.avg <dbl>, neg.cont <dbl>, neg.sal <dbl>,
# log.CAB <dbl>, log.years <dbl>, log.salary <dbl>
```

Through manual obervation of the feature vaues of these influential points it appears that these observation have much higher or lower values for certain features such as G.x, InnOuts, PO compared to those of non-influential points. The table of encompassing Cook's Distance with Leverage Hat Value and Studentized Residuals do a much better job providing insight into why a point is influential, however.

CAB.avg

CH.avg

CHR.avg

CR.avg

-0.0042031

-0.0133749

-0.0709547

0.0030973

0.0133111

0.0361205

0.0534385 0.0151076

```
all.fit = lm(log.salary ~ ., data = new.baseball)
summary(all.fit)
Call:
lm(formula = log.salary ~ ., data = new.baseball)
Residuals:
     Min
               1Q
                    Median
                                  3Q
                                          Max
-1.63762 -0.31246  0.06423  0.31947  1.51943
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 14.2702482 0.5240182
                                   27.232 < 2e-16 ***
POSC
            -0.0426637
                        0.1518434
                                   -0.281 0.778886
POSCF
            -0.0268705 0.1494435
                                   -0.180 0.857403
POSMI
                        0.1027617
                                    0.760 0.447882
             0.0780726
G.x
             0.0039647
                        0.0046887
                                    0.846 0.398321
GS
            -0.0062069
                        0.0109901
                                   -0.565 0.572567
                        0.0004900
                                    0.296 0.767175
InnOuts
             0.0001452
PO
             0.0002185
                        0.0003197
                                    0.683 0.494768
Α
             0.0003503
                        0.0008990
                                    0.390 0.697023
Ε
             0.0026430
                        0.0104617
                                    0.253 0.800687
DP
            -0.0042697
                        0.0029331
                                   -1.456 0.146306
G.y
            -0.0118007
                        0.0033350
                                   -3.538 0.000453 ***
AB
             0.0065267
                        0.0016068
                                    4.062 5.92e-05 ***
R
            -0.0093742
                        0.0063621
                                   -1.473 0.141465
Η
            -0.0065391
                        0.0048988
                                   -1.335 0.182729
X2B
            -0.0063059
                        0.0070018
                                   -0.901 0.368367
ХЗВ
             0.0006723
                        0.0184037
                                    0.037 0.970877
HR
            -0.0102874
                        0.0121474
                                   -0.847 0.397599
RBI
             0.0039993
                        0.0057956
                                    0.690 0.490580
SB
                        0.0058889
                                   -0.223 0.823382
            -0.0013153
CS
            -0.0276728
                        0.0185481
                                   -1.492 0.136549
BB
             0.0056713 0.0039142
                                    1.449 0.148192
                        0.0019363
SO
            -0.0012819
                                   -0.662 0.508337
                        0.0136217
                                    0.688 0.491937
IBB
             0.0093704
HBP
             0.0036525
                        0.0110282
                                    0.331 0.740680
SH
             0.0093553 0.0161609
                                    0.579 0.563012
SF
             0.0014463
                        0.0204969
                                    0.071 0.943783
GIDP
            -0.0086423
                        0.0093884
                                   -0.921 0.357889
CH
                        0.0010424
                                     2.091 0.037157 *
             0.0021802
CHR
             0.0076434
                        0.0038205
                                     2.001 0.046147 *
CR
            -0.0022325
                        0.0016753
                                   -1.333 0.183480
CRBI
            -0.0026771
                        0.0018308
                                   -1.462 0.144502
CBB
                        0.0005733
                                   -2.065 0.039609 *
            -0.0011839
AVG
             0.5156185
                        3.3598388
                                    0.153 0.878113
OBP
            -0.0025942
                        0.0291738
                                   -0.089 0.929190
```

3.537 0.000455 ***

-1.357 0.175589

-1.005 0.315641

-1.964 0.050219 .

```
CRBI.avg
             0.0469204
                        0.0166307
                                    2.821 0.005036 **
neg.cont
             1.2416258
                        0.2315305
                                    5.363 1.43e-07 ***
             0.0541843
                                    0.356 0.722168
neg.sal
                        0.1522766
log.CAB
            -0.3434284
                        0.1713702
                                   -2.004 0.045783 *
log.years
             0.2802810
                        0.2404271
                                    1.166 0.244447
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 0.5807 on 377 degrees of freedom Multiple R-squared: 0.8082, Adjusted R-squared: 0.7863 F-statistic: 36.95 on 43 and 377 DF, p-value: < 2.2e-16

From former analysis I am aware of collinearity within the explanatory variables and hence inflated standard errors. However, it appears several of the coefficients are statistically significant and that the omnibus F-statistic for all explanatory variables in the model having coefficients of 0 is also statistically significant. In addition, the adjusted R-squared value is a bit lower than the R-squared of the model. This all leans toward the argument of the model requiring the explanatory variables but with possible variable selection that may improve the model's regression ability.

Next, I'll be finding the best 10 models for each model size using **forward selection**. I won't output the results of the summary as they are a bit extensive and in anyways I will select 5 specific models from all of these models in the next part.

```
best10 = regsubsets(log.salary ~ ., data=new.baseball, nvmax=43, nbest=10, method="forward")
# summary(best10)
```

```
lowest5.bic = sort(summary(best10)$bic)[1:5]
top5.bic.loc = order(summary(best10)$bic)[1:5]
top5.models = summary(best10)$which[top5.bic.loc,]
models = c()
for(i in 1:nrow(top5.models)){
  cat(sprintf("Model %d:", i))
  cat(sprintf("\nBIC: %f", lowest5.bic[i]))
  models = c(models, list(names(which(top5.models[i,]))[-1]))
  cat(sprintf("\nFeatures: %s", paste(models[[i]], collapse = ", ")))
  cat("\n\n")
}
Model 1:
BIC: -586.225215
Features: GS, G.y, AB, R, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
Model 2:
BIC: -583.405937
Features: GS, R, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
Model 3:
BIC: -582.502074
Features: G.x, GS, G.y, AB, R, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
Model 4:
BIC: -582.402615
Features: GS, G.y, AB, R, X2B, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
Model 5:
BIC: -582.248168
Features: GS, G.y, AB, R, H, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
```

Using BIC as a criterion may not be sufficient and hence I will use 10-fold cross validation to re-rank the 5 models determined above. Rather than hard-code the k-fold procedure, I will be using built-in functions available in the caret package.

The output will show the features of each model for clarity as well as the previously determined BIC value and the newly determined mean-MSE (through 10-fold CV).

```
# 10-fold cross validation setup
train.control = trainControl(method = "cv", number = 10)
mean.mse = c()
for (i in 1:5){
  model.to.train.test = as.formula(paste("log.salary ~", paste(models[[i]], collapse=" + ")))
  model.trained.tested = train(model.to.train.test, data = new.baseball, method = "lm", trControl = tra
  mean.mse = c(mean.mse, model.trained.tested$results[[2]]**2)
  cat(sprintf("Model %d:", i))
  cat(sprintf("\nBIC: %f", lowest5.bic[i]))
  cat(sprintf("\nFeatures: %s", paste(models[[i]], collapse = ", ")))
  cat(sprintf("\n--> MSE: %f", mean.mse[i]))
  cat(sprintf("\n\n"))
}
Model 1:
BIC: -586.225215
Features: GS, G.y, AB, R, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
--> MSE: 0.344688
Model 2:
BIC: -583.405937
Features: GS, R, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
--> MSE: 0.356297
Model 3:
BIC: -582.502074
Features: G.x, GS, G.y, AB, R, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
--> MSE: 0.341484
Model 4:
BIC: -582.402615
Features: GS, G.y, AB, R, X2B, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
--> MSE: 0.343067
Model 5:
BIC: -582.248168
Features: GS, G.y, AB, R, H, BB, CH, CBB, CAB.avg, CR.avg, CRBI.avg, neg.cont, log.CAB, log.years
--> MSE: 0.349388
```

From the values above, it is evident the following is the model with the lowest mean-MSE:

```
i = which.min(mean.mse)
cat(sprintf("Model %d:", i))
Model 3:
cat(sprintf("\nBIC: %f", lowest5.bic[i]))
BIC: -582.502074
cat(sprintf("\nFeature: %s", models[[i]]))
Feature: G.x
Feature: GS
Feature: G.y
Feature: AB
Feature: R
Feature: BB
Feature: CH
Feature: CBB
Feature: CAB.avg
Feature: CR.avg
Feature: CRBI.avg
Feature: neg.cont
Feature: log.CAB
Feature: log.years
cat(sprintf("\n--> MSE: %f", mean.mse[i]))
```

--> MSE: 0.341484

Through many repetitions it appears that the choice of model changes (stemming from the variability in how data is partitioned in 10-fold CV). It appears that it isn't always the case the model with lowest BIC has the lowest mean-MSE.

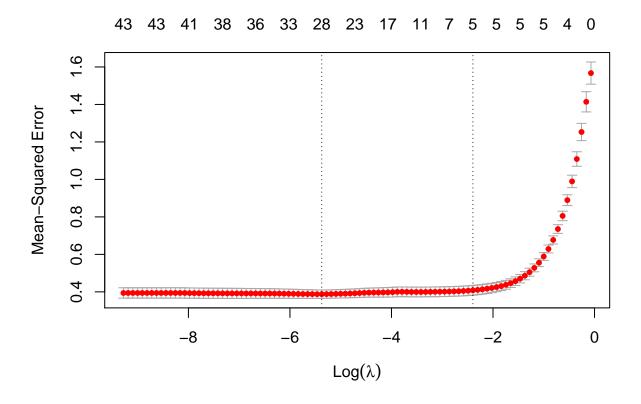
In determining the value of the hyperparameter lambda to use for the LASSO model (original feature variables), I will be using 10-fold cross validation with an average MSE for the criterion.

```
X = new.baseball %>% dplyr::select(-c(log.salary)) %>% as.matrix()
y = new.baseball$log.salary

lasso.model = glmnet(x = X, y = y, alpha = 1)
cv.lasso.model = cv.glmnet(x = X, y = y, alpha = 1, nfolds = 10)
```

The following is the plot of the log of the hyperparameter lambda with respect to the resulting average MSE.

```
plot(cv.lasso.model)
```



The left-most dashed vertical line in the plot represents the lambda corresponding to the minimum MSE whereas the right-most dashed vertical line represents the lambda 1 standard error away from the min lambda.

I believe the data intrinsically contains a lot of collinear explanatory variables and would like to reduce the number of features used in model prediction. I believe the lambda corresponding to the minimum MSE would be suitable as it not only performs variable selection through utilizing just 28 feature variables for regression rather than all 43, it also has the lowest MSE out of all other possible lambda hyperparameter values and thus seems to be the best choice in prediction.

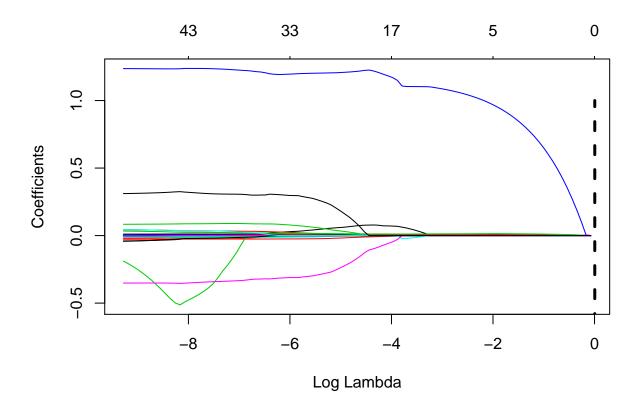
The value of lambda I will use for the LASSO model is the following:

```
best.lasso.lambda = cv.lasso.model$lambda.min
best.lasso.lambda
```

[1] 0.00464043

The following is a visualization of how different values of lambda influence the coefficient values of the regression model:

```
plot(lasso.model, xvar = "lambda", )
lines(c(best.lasso.lambda, best.lasso.lambda), c(-1, 1), lty = "dashed", lwd = 3)
```



Lastly, using the hyperparameter value of lambda specified above, I'd like to analyze which coefficients are retained through implicit variable selection of LASSO.

```
best.lasso.coefs = predict(lasso.model, type = 'coefficients', s = best.lasso.lambda)
best.lasso.coefs
```

```
44 x 1 sparse Matrix of class "dgCMatrix"

1
(Intercept) 1.392036e+01
POSC 4.819060e-02
POSCF .
POSMI 5.389061e-02
G.x 7.148762e-04
```

```
GS
InnOuts
             8.253821e-05
PO
             2.248210e-05
Α
Ε
DP
            -1.477442e-03
            -6.109311e-03
G.y
              1.353649e-03
AB
R
Η
X2B
            -2.861447e-03
ХЗВ
HR
            -8.452375e-03
             1.503657e-03
RBI
SB
            -2.788658e-04
CS
            -2.260273e-02
ВВ
             4.007321e-03
SO
IBB
             8.545359e-03
HBP
             1.690402e-03
SH
             7.327374e-03
SF
             1.045290e-02
GIDP
CH
             1.384542e-05
             9.327663e-04
CHR
CR
             8.514916e-04
CRBI
CBB
            -1.026886e-03
AVG
OBP
CAB.avg
            -3.898353e-04
CH.avg
CHR.avg
              1.469175e-02
CR.avg
CRBI.avg
              1.560951e-02
neg.cont
              1.203511e+00
neg.sal
log.CAB
            -2.850154e-01
log.years
             2.542452e-01
```

From analyzing the output summary of the LASSO model coefficients, it appears 28 explanatory variables have non-zero coefficients.

I chose the lambda value corresponding to the minimum MSE value for the LASSO model, which is the following value:

```
min(cv.lasso.model$cvm)
```

[1] 0.3875681

In the previous part, I found the top 5 models with the lowest BIC and then used 10-fold cross validation with a mean-MSE criterion to find the lowest MSE model. I'd like compare the that result with the model I determined though LASSO by examining the MSE values.

min(cv.lasso.model\$cvm) <= mean.mse</pre>

[1] FALSE FALSE FALSE FALSE

The expression above compared the MSE of the LASSO model to the other 5 models but it turns out LASSO produces a regression with a higher MSE compared to all.