

Lab 3 (24 Jan 2019)

Problem 1 [Counting Inversions]: An *inversion* in a sequence A of numbers is a pair of indices (i, j) such that $i < j$ and $A[i] > A[j]$. Write a program to count the total number of inversions in an input sequence. For e.g. the number of inversions in 1,3,9,8,5 is 3 while that in 4,10,8,2,1 is 8. [Write a simple naive algorithm to do this. Write a program to implement the divide-and-conquer algorithm to count inversions.

Problem 2 [Maximum sum sub-array]: Given an array A of integers write a program to return indices (i, j) ($0 \leq i < j \leq n-1$) such that the sum $A[i] + A[i+1] + \dots + A[j]$ is maximum for all sub-arrays. For e.g. if $A = [-2, 10, -4, 12, -9]$, then $i=1, j=3$ would give the maximal sum ($10 + (-4) + 12 = 18$). Your algorithm should run in $O(n \log n)$ time.

Hint: Think of a divide-and-conquer strategy. You can implement a naive $O(n^2)$ algorithm to check the correctness of your divide-and-conquer algorithm. Do you think you can solve this problem in $O(n)$ time?