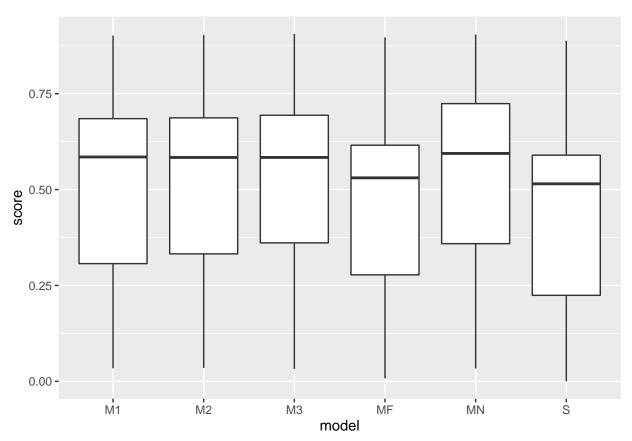
# Research Question 2

Question: What is the effect of different strategies to simultaneously learn one model from multiple TrD's?

For answering this question we need to evaluate the effect of the transfer lerning methods (MN, M1, M2, M3, MF) and the simple model (S) on the score. We will then perform significance tests to see if there is a significant difference between the methods. We will also see how the Methods perform on specific tasks/TeD.

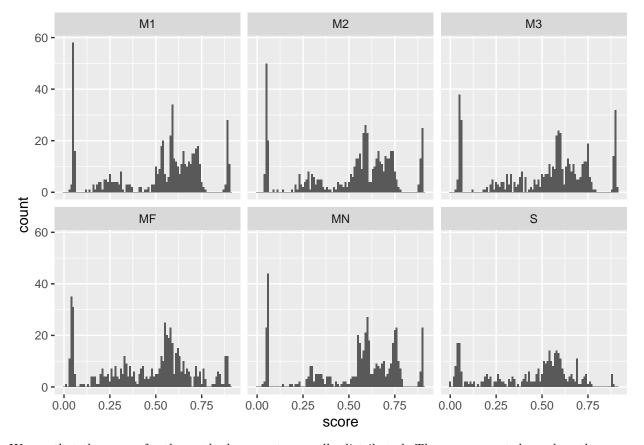
# Observing the distribution of scores by models





We can see that transfer learning methods' mean performance is better over the simple model (disregarding all the other independent variables and the interaction effects). But we need stronger tests than this.

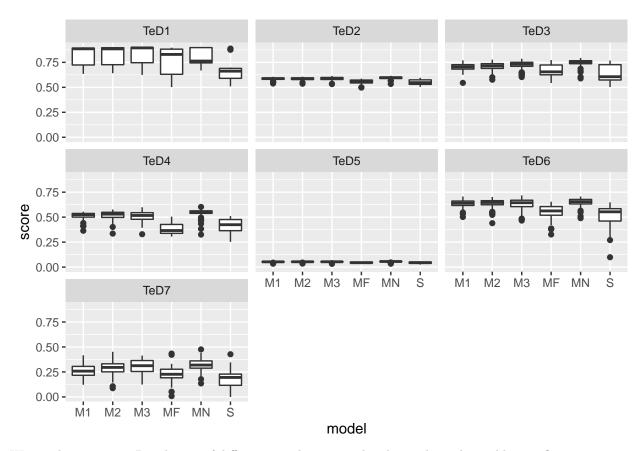
```
ggplot(d, aes(score)) + geom_histogram(binwidth = 0.01) + facet_wrap(~model)
```



We see that the scores for the methods are not normally distributed. Thus, we cannot depend on the mean alone.

Let us observe the effect of other independent variables (test dataset) on the score

```
ggplot(d, aes(model, score)) + geom_boxplot(notch = FALSE) + facet_wrap(~TeD)
```



We see that except TeD5, the use of different test datasets and tasks result in observably significant variations in performance in different models.

## Simple Significance Tests

Because the 5 Mx methods were implimented using randamization in selection of training set we are not considering the effect of selection of the training set here. Our purpose here is to **only compare methods** against each other considering consistent testing strategy for evaluation on the same test set/task and consistent (emperically comparable) scoring method.

Lets create a simple linear model and observe the coefficients and confidence intervals.

```
m = lm(score \sim model + TeD, d)
summary(m)
##
## lm(formula = score ~ model + TeD, data = d)
##
## Residuals:
##
        Min
                       Median
                                     3Q
                                              Max
                   1Q
   -0.44115 -0.02813 -0.00022 0.03989
                                         0.22644
##
## Coefficients:
                                      t value Pr(>|t|)
##
                Estimate Std. Error
## (Intercept)
                0.802059
                            0.003828
                                      209.528
                                               < 2e-16 ***
## modelM2
                0.005737
                            0.003747
                                         1.531 0.12585
```

```
## modelM3
                0.011600
                           0.003812
                                       3.043 0.00236 **
## modelMF
               -0.054194
                                    -14.603 < 2e-16 ***
                           0.003711
## modelMN
                0.022119
                           0.003840
                                       5.760 9.26e-09 ***
## modelS
               -0.080192
                           0.004279
                                     -18.743
                                              < 2e-16 ***
## TeDTeD2
               -0.212136
                           0.004233
                                     -50.115
                                              < 2e-16 ***
## TeDTeD3
               -0.089711
                           0.004233
                                     -21.193
                                              < 2e-16 ***
## TeDTeD4
               -0.308013
                           0.004233
                                     -72.765
                                              < 2e-16 ***
## TeDTeD5
               -0.739268
                           0.004233 - 174.643
                                              < 2e-16 ***
## TeDTeD6
               -0.182050
                           0.004233
                                     -43.007
                                              < 2e-16 ***
## TeDTeD7
               -0.520991
                           0.004233 -123.078 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.06171 on 2963 degrees of freedom
## Multiple R-squared: 0.9386, Adjusted R-squared: 0.9384
## F-statistic: 4120 on 11 and 2963 DF, p-value: < 2.2e-16
confint(m)
                      2.5 %
                                 97.5 %
## (Intercept)
                0.794553364
                             0.80956472
## modelM2
               -0.001609790
                             0.01308316
## modelM3
                0.004126552
                             0.01907403
## modelMF
               -0.061470820 -0.04691716
## modelMN
                0.014589781 0.02964789
## modelS
               -0.088581303 -0.07180280
## TeDTeD2
               -0.220435645 -0.20383575
## TeDTeD3
               -0.098010994 -0.08141110
## TeDTeD4
               -0.316313333 -0.29971343
               -0.747567696 -0.73096780
## TeDTeD5
## TeDTeD6
               -0.190349527 -0.17374963
## TeDTeD7
               -0.529290562 -0.51269066
```

We see that the both Method of training and choice of TeD have a significant effect on the score. Therefore it is also wise to perform an interaction analysis.

## Interaction Effect

Let us observe the interaction effect of the TeD and method on the score.

```
m = lm(score \sim model*TeD, d)
summary(m)
##
## Call:
## lm(formula = score ~ model * TeD, data = d)
##
## Residuals:
##
        Min
                  1Q
                        Median
                                     3Q
                                              Max
## -0.41416 -0.02131 0.00255 0.02837
                                         0.24426
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                                0.006583 123.562 < 2e-16 ***
## (Intercept)
                    0.813362
## modelM2
                   -0.001235
                                0.009339
                                          -0.132 0.894768
## modelM3
                    0.024685
                                0.009501
                                           2.598 0.009420 **
```

```
## modelMF
                   -0.055233
                                0.009251
                                          -5.971 2.65e-09 ***
## modelMN
                   -0.002631
                                          -0.275 0.783398
                                0.009571
## modelS
                   -0.150884
                                0.010665 -14.148
## TeDTeD2
                   -0.228385
                                0.009309 -24.533
                                                  < 2e-16 ***
## TeDTeD3
                   -0.111086
                                0.009309 -11.933
                                                  < 2e-16 ***
                   -0.300258
                                0.009309 -32.254
## TeDTeD4
                                                  < 2e-16 ***
## TeDTeD5
                                0.009309 -81.790
                   -0.761399
                                                  < 2e-16 ***
## TeDTeD6
                   -0.176892
                                0.009309 - 19.002
                                                  < 2e-16 ***
## TeDTeD7
                   -0.553264
                                0.009309 -59.432
                                                  < 2e-16 ***
## modelM2:TeDTeD2
                    0.001042
                                0.013208
                                           0.079 0.937102
## modelM3:TeDTeD2 -0.022875
                                0.013437
                                          -1.702 0.088787
## modelMF:TeDTeD2
                                           1.905 0.056899
                    0.024920
                                0.013083
## modelMN:TeDTeD2
                    0.012305
                                0.013536
                                           0.909 0.363392
## modelS:TeDTeD2
                    0.117038
                                0.015083
                                           7.760 1.17e-14 ***
## modelM2:TeDTeD3
                    0.008719
                                           0.660 0.509219
                                0.013208
## modelM3:TeDTeD3 -0.007320
                                0.013437
                                          -0.545 0.585951
## modelMF:TeDTeD3
                    0.020738
                                0.013083
                                           1.585 0.113032
## modelMN:TeDTeD3
                    0.045473
                                0.013536
                                           3.359 0.000791 ***
## modelS:TeDTeD3
                    0.085371
                                0.015083
                                           5.660 1.66e-08 ***
## modelM2:TeDTeD4
                    0.004270
                                0.013208
                                           0.323 0.746497
## modelM3:TeDTeD4 -0.029303
                                0.013437
                                          -2.181 0.029273 *
## modelMF:TeDTeD4 -0.075271
                                0.013083
                                          -5.754 9.64e-09 ***
## modelMN:TeDTeD4
                    0.030419
                                0.013536
                                           2.247 0.024698 *
## modelS:TeDTeD4
                    0.049532
                                0.015083
                                           3.284 0.001035 **
## modelM2:TeDTeD5
                    0.001597
                                0.013208
                                           0.121 0.903760
## modelM3:TeDTeD5 -0.024242
                                0.013437
                                          -1.804 0.071306
## modelMF:TeDTeD5
                    0.047596
                                0.013083
                                           3.638 0.000279
## modelMN:TeDTeD5
                    0.005911
                                0.013536
                                           0.437 0.662349
## modelS:TeDTeD5
                    0.141808
                                0.015083
                                           9.402 < 2e-16 ***
## modelM2:TeDTeD6
                    0.001360
                                0.013208
                                           0.103 0.917966
## modelM3:TeDTeD6 -0.028562
                                0.013437
                                          -2.126 0.033612 *
## modelMF:TeDTeD6 -0.032200
                                0.013083
                                          -2.461 0.013901 *
## modelMN:TeDTeD6
                    0.014689
                                0.013536
                                           1.085 0.277938
## modelS:TeDTeD6
                    0.027243
                                0.015083
                                           1.806 0.070986
## modelM2:TeDTeD7
                    0.031816
                                0.013208
                                           2.409 0.016063
## modelM3:TeDTeD7
                    0.020707
                                0.013437
                                           1.541 0.123407
## modelMF:TeDTeD7
                    0.021487
                                0.013083
                                           1.642 0.100612
## modelMN:TeDTeD7
                    0.064454
                                0.013536
                                           4.762 2.01e-06 ***
  modelS:TeDTeD7
                    0.073851
                                0.015083
                                           4.896 1.03e-06 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.05814 on 2933 degrees of freedom
## Multiple R-squared: 0.9461, Adjusted R-squared: 0.9453
## F-statistic: 1255 on 41 and 2933 DF, p-value: < 2.2e-16
```

We can see that indeed there is significant interaction effect. We cannot do further analysis just using coefficients. We need to separate instances depending on TeD and see how the models comparatively perform.

# Pairwise comparisons for Models

We need to perform pairwise comparisons while making adjustments for experiment design issues (interaction effects of TeD).

```
m = lm (score ~model*TeD, d)
emmeans(m, ~model)
```

## NOTE: Results may be misleading due to involvement in interactions

```
model emmean
                       SE
                            df lower.CL upper.CL
           0.509 0.00249 2933
##
   M1
                                   0.504
                                            0.514
##
   M2
           0.515 0.00250 2933
                                   0.510
                                            0.520
##
   МЗ
           0.520 0.00259 2933
                                   0.515
                                            0.526
##
   MF
           0.455 0.00246 2933
                                   0.450
                                            0.460
##
   MN
           0.531 0.00263 2933
                                   0.526
                                            0.536
##
    S
           0.429 0.00317 2933
                                   0.422
                                            0.435
##
```

## Results are averaged over the levels of: TeD

## Confidence level used: 0.95

The estimated marginal means (EMMs) tell us that the mean method performance, averaged over the test dataset used, is in the order:

We can check pairwise comparison of the methods for understanding how significant these rankings are.

```
emmeans(m, pairwise~model)
```

```
## NOTE: Results may be misleading due to involvement in interactions
## $emmeans
   model emmean
##
                       SE
                            df lower.CL upper.CL
##
   M1
           0.509 0.00249 2933
                                  0.504
                                            0.514
##
   M2
           0.515 0.00250 2933
                                  0.510
                                            0.520
##
    МЗ
           0.520 0.00259 2933
                                  0.515
                                            0.526
##
   MF
           0.455 0.00246 2933
                                  0.450
                                            0.460
##
   MN
           0.531 0.00263 2933
                                  0.526
                                            0.536
           0.429 0.00317 2933
##
    S
                                  0.422
                                            0.435
##
```

## Results are averaged over the levels of: TeD

## Confidence level used: 0.95

##

## \$contrasts

```
##
    contrast estimate
                            SE
                                 df t.ratio p.value
   M1 - M2
             -0.00574 0.00353 2933
                                     -1.625 0.5818
##
   M1 - M3
             -0.01160 0.00359 2933
                                     -3.230 0.0158
##
   M1 - MF
              0.05419 0.00350 2933
                                     15.500 < .0001
##
   M1 - MN
             -0.02212 0.00362 2933
                                     -6.114 < .0001
   M1 - S
              0.08019 0.00403 2933
                                     19.894 < .0001
##
   M2 - M3
             -0.00586 0.00360 2933
                                     -1.628 0.5801
##
   M2 - MF
              0.05993 0.00351 2933
                                     17.084 < .0001
##
   M2 - MN
             -0.01638 0.00363 2933
                                     -4.515 0.0001
   M2 - S
##
              0.08593 0.00404 2933
                                     21.264 < .0001
##
    M3 - MF
              0.06579 0.00357 2933
                                     18.432 < .0001
##
   M3 - MN
             -0.01052 0.00369 2933
                                     -2.852 \ 0.0500
   M3 - S
              0.09179 0.00409 2933
                                     22.419 < .0001
   MF - MN
##
             -0.07631 0.00360 2933 -21.220 <.0001
##
    MF - S
              0.02600 0.00401 2933
                                      6.480 < .0001
##
    MN - S
              0.10231 0.00412 2933
                                     24.846 < .0001
##
```

## Results are averaged over the levels of: TeD

## P value adjustment: tukey method for comparing a family of 6 estimates

We observe the following:

- Using any transfer learning method (Mx) is better than using the simple model (S) i.e. (obs. p < 0.0001).
- Changing method between M1 to M2 (obs. p=0.5818) OR M2 to M3 (obs. p=0.5801) only gives slight improvements.
- Using MN over M3 gives marginally significant (obs. p = 0.0500) performance improvement.
- Using MN over {M1, M2, MF, S} gives highly significant (obs. p < 0.0001) performance improvement.

## Pairwise comparison for Models per TeD

Lets also account for the performance of models depending on different tasks (TeD) the models have to perform.

#### Means for particular TeDs:

```
emmeans(m, pairwise~model|TeD)$emmeans
## TeD = TeD1:
##
    model emmean
                       SE
                            df lower.CL upper.CL
##
    M1
          0.8134 0.00658 2933
                                  0.8005
                                           0.8263
##
    M2
          0.8121 0.00663 2933
                                  0.7991
                                           0.8251
##
    МЗ
          0.8380 0.00685 2933
                                  0.8246
                                           0.8515
          0.7581 0.00650 2933
                                           0.7709
##
    MF
                                  0.7454
##
    MN
          0.8107 0.00695 2933
                                  0.7971
                                           0.8244
          0.6625 0.00839 2933
##
    S
                                  0.6460
                                           0.6789
##
## TeD = TeD2:
                            df lower.CL upper.CL
    model emmean
                       SE
          0.5850 0.00658 2933
                                           0.5979
##
    M1
                                  0.5721
                                  0.5718
##
    M2
          0.5848 0.00663 2933
                                           0.5978
    МЗ
##
          0.5868 0.00685 2933
                                  0.5734
                                           0.6002
##
    MF
          0.5547 0.00650 2933
                                  0.5419
                                           0.5674
    MN
          0.5946 0.00695 2933
                                  0.5810
                                           0.6083
##
##
    S
          0.5511 0.00839 2933
                                  0.5347
                                           0.5676
##
##
  TeD = TeD3:
##
    model emmean
                       SE
                            df lower.CL upper.CL
##
    M1
          0.7023 0.00658 2933
                                  0.6894
                                           0.7152
##
    M2
          0.7098 0.00663 2933
                                  0.6968
                                           0.7227
                                  0.7062
                                           0.7331
##
    МЗ
          0.7196 0.00685 2933
##
    MF
          0.6678 0.00650 2933
                                  0.6550
                                           0.6805
    MN
##
          0.7451 0.00695 2933
                                  0.7315
                                           0.7587
##
    S
          0.6368 0.00839 2933
                                  0.6203
                                           0.6532
##
  TeD = TeD4:
##
##
    model emmean
                       SE
                            df lower.CL upper.CL
##
    M1
          0.5131 0.00658 2933
                                  0.5002
                                           0.5260
##
    M2
          0.5161 0.00663 2933
                                  0.5031
                                           0.5291
##
    МЗ
          0.5085 0.00685 2933
                                  0.4951
                                           0.5219
##
    MF
          0.3826 0.00650 2933
                                  0.3699
                                           0.3953
##
    MN
          0.5409 0.00695 2933
                                  0.5273
                                           0.5545
##
    S
          0.4118 0.00839 2933
                                  0.3953
                                           0.4282
##
```

```
## TeD = TeD5:
    model emmean
                      SE
                            df lower.CL upper.CL
          0.0520 0.00658 2933
                                 0.0391
                                           0.0649
##
          0.0523 0.00663 2933
                                 0.0393
                                           0.0653
   M2
##
    МЗ
          0.0524 0.00685 2933
                                 0.0390
                                           0.0658
##
   MF
          0.0443 0.00650 2933
                                 0.0316
                                           0.0571
          0.0552 0.00695 2933
                                 0.0416
                                           0.0689
          0.0429 0.00839 2933
##
    S
                                 0.0264
                                           0.0593
##
## TeD = TeD6:
    model emmean
                       SE
                            df lower.CL upper.CL
##
          0.6365 0.00658 2933
                                 0.6236
                                           0.6494
    M1
##
    M2
          0.6366 0.00663 2933
                                 0.6236
                                           0.6496
##
          0.6326 0.00685 2933
    МЗ
                                 0.6192
                                           0.6460
##
    MF
          0.5490 0.00650 2933
                                 0.5363
                                           0.5618
##
    MN
          0.6485 0.00695 2933
                                 0.6349
                                           0.6622
##
    S
          0.5128 0.00839 2933
                                 0.4964
                                           0.5293
##
## TeD = TeD7:
##
    model emmean
                      SE
                            df lower.CL upper.CL
##
    M1
          0.2601 0.00658 2933
                                 0.2472
                                           0.2730
          0.2907 0.00663 2933
                                 0.2777
                                           0.3037
##
##
   МЗ
          0.3055 0.00685 2933
                                 0.2921
                                           0.3189
   MF
##
          0.2264 0.00650 2933
                                 0.2136
                                           0.2391
##
   MN
          0.3219 0.00695 2933
                                 0.3083
                                           0.3355
##
    S
          0.1831 0.00839 2933
                                 0.1666
                                           0.1995
##
## Confidence level used: 0.95
```

## Comtrasts for particular TeDs:

#### emmeans(m, pairwise~model|TeD)\$contrasts

```
## TeD = TeD1:
    contrast estimate
##
                                  df t.ratio p.value
                             SE
    M1 - M2
              1.24e-03 0.00934 2933
                                       0.132 1.0000
   M1 - M3
             -2.47e-02 0.00950 2933
                                      -2.598 0.0980
##
    M1 - MF
              5.52e-02 0.00925 2933
                                       5.971 < .0001
##
   M1 - MN
              2.63e-03 0.00957 2933
                                       0.275 0.9998
##
   M1 - S
              1.51e-01 0.01067 2933
                                     14.148 < .0001
   M2 - M3
##
             -2.59e-02 0.00953 2933
                                      -2.720 0.0717
##
    M2 - MF
              5.40e-02 0.00928 2933
                                       5.818 < .0001
##
    M2 - MN
              1.40e-03 0.00960 2933
                                       0.145 1.0000
   M2 - S
              1.50e-01 0.01069 2933
##
                                      13.997 < .0001
##
   M3 - MF
              7.99e-02 0.00944 2933
                                       8.462 < .0001
##
    M3 - MN
              2.73e-02 0.00976 2933
                                       2.799 0.0578
##
    M3 - S
              1.76e-01 0.01083 2933
                                     16.207 < .0001
##
    MF - MN
             -5.26e-02 0.00951 2933
                                      -5.528 < .0001
   MF - S
##
              9.57e-02 0.01061 2933
                                       9.012 <.0001
              1.48e-01 0.01089 2933
##
    MN - S
                                     13.608 < .0001
##
## TeD = TeD2:
##
    contrast
              estimate
                             SE
                                  df t.ratio p.value
              1.93e-04 0.00934 2933
    M1 - M2
                                       0.021 1.0000
   M1 - M3 -1.81e-03 0.00950 2933
                                     -0.191 1.0000
```

```
M1 - MF
              3.03e-02 0.00925 2933
                                      3.277 0.0136
            -9.67e-03 0.00957 2933
##
   M1 - MN
                                     -1.011 0.9145
    M1 - S
              3.38e-02 0.01067 2933
                                      3.174 0.0190
             -2.00e-03 0.00953 2933
                                     -0.210 0.9999
##
    M2 - M3
##
    M2 - MF
              3.01e-02 0.00928 2933
                                      3.245 0.0150
##
    M2 - MN
            -9.87e-03 0.00960 2933
                                     -1.028 0.9087
    M2 - S
              3.37e-02 0.01069 2933
                                      3.148 0.0206
   M3 - MF
##
              3.21e-02 0.00944 2933
                                      3.401 0.0089
##
    M3 - MN
             -7.86e-03 0.00976 2933
                                     -0.806 0.9665
##
    M3 - S
              3.57e-02 0.01083 2933
                                      3.291 0.0129
    MF - MN
            -4.00e-02 0.00951 2933
                                     -4.203 0.0004
##
    MF - S
              3.53e-03 0.01061 2933
                                      0.333 0.9995
##
    MN - S
              4.35e-02 0.01089 2933
                                      3.995 0.0009
##
## TeD = TeD3:
##
                            SE
                                 df t.ratio p.value
    contrast estimate
##
            -7.48e-03 0.00934 2933
                                     -0.801 0.9673
    M1 - M2
             -1.74e-02 0.00950 2933
                                     -1.828 0.4479
    M1 - M3
              3.45e-02 0.00925 2933
##
    M1 - MF
                                      3.729 0.0027
##
    M1 - MN
            -4.28e-02 0.00957 2933
                                     -4.476 0.0001
##
   M1 - S
              6.55e-02 0.01067 2933
                                      6.143 < .0001
    M2 - M3
             -9.88e-03 0.00953 2933
                                     -1.037 0.9055
    M2 - MF
##
              4.20e-02 0.00928 2933
                                      4.523 0.0001
    M2 - MN
             -3.54e-02 0.00960 2933
##
                                     -3.683 0.0032
                                      6.828 < .0001
##
    M2 - S
              7.30e-02 0.01069 2933
    M3 - MF
              5.19e-02 0.00944 2933
                                      5.491 < .0001
   M3 - MN
            -2.55e-02 0.00976 2933
                                     -2.611 0.0949
##
##
    M3 - S
              8.29e-02 0.01083 2933
                                      7.650 < .0001
    MF - MN
            -7.73e-02 0.00951 2933
##
                                     -8.128 <.0001
    MF - S
              3.10e-02 0.01061 2933
                                      2.922 0.0409
##
    MN - S
              1.08e-01 0.01089 2933
                                      9.946 < .0001
##
## TeD = TeD4:
                            SE
                                 df t.ratio p.value
##
    contrast estimate
             -3.03e-03 0.00934 2933
                                     -0.325 0.9995
    M1 - M2
              4.62e-03 0.00950 2933
##
   M1 - M3
                                      0.486 0.9967
   M1 - MF
              1.31e-01 0.00925 2933
                                    14.107 < .0001
   M1 - MN
             -2.78e-02 0.00957 2933
                                     -2.903 0.0432
##
   M1 - S
              1.01e-01 0.01067 2933
                                      9.503 < .0001
##
              7.65e-03 0.00953 2933
##
    M2 - M3
                                      0.803 0.9670
              1.34e-01 0.00928 2933
    M2 - MF
                                     14.388 < .0001
   M2 - MN
            -2.48e-02 0.00960 2933
                                     -2.578 0.1029
##
##
    M2 - S
              1.04e-01 0.01069 2933
                                      9.764 < .0001
##
    M3 - MF
              1.26e-01 0.00944 2933
                                     13.330 <.0001
    M3 - MN
             -3.24e-02 0.00976 2933
                                     -3.321 0.0117
   M3 - S
              9.67e-02 0.01083 2933
##
                                      8.930 <.0001
##
    MF - MN
            -1.58e-01 0.00951 2933 -16.636 <.0001
##
    MF - S
             -2.92e-02 0.01061 2933
                                    -2.747 0.0667
##
    MN - S
              1.29e-01 0.01089 2933 11.853 <.0001
##
## TeD = TeD5:
   contrast estimate
                            SE
                                 df t.ratio p.value
## M1 - M2 -3.62e-04 0.00934 2933 -0.039 1.0000
## M1 - M3 -4.43e-04 0.00950 2933 -0.047 1.0000
```

```
M1 - MF
              7.64e-03 0.00925 2933
                                       0.825 0.9629
             -3.28e-03 0.00957 2933
##
    M1 - MN
                                     -0.343 0.9994
    M1 - S
              9.08e-03 0.01067 2933
                                       0.851 0.9577
             -8.15e-05 0.00953 2933
   M2 - M3
                                      -0.009 1.0000
##
##
    M2 - MF
              8.00e-03 0.00928 2933
                                       0.862 0.9555
             -2.92e-03 0.00960 2933
##
    M2 - MN
                                      -0.304 0.9997
    M2 - S
              9.44e-03 0.01069 2933
                                       0.883 0.9507
   M3 - MF
##
              8.08e-03 0.00944 2933
                                       0.856 0.9568
##
    M3 - MN
             -2.84e-03 0.00976 2933
                                      -0.291 0.9997
##
    M3 - S
              9.52e-03 0.01083 2933
                                       0.879 0.9516
    MF - MN
            -1.09e-02 0.00951 2933
                                      -1.147 0.8614
              1.44e-03 0.01061 2933
##
    MF - S
                                       0.136 1.0000
##
    MN - S
              1.24e-02 0.01089 2933
                                       1.134 0.8672
##
## TeD = TeD6:
##
    contrast
             estimate
                             SE
                                  df t.ratio p.value
##
            -1.25e-04 0.00934 2933
                                     -0.013 1.0000
    M1 - M2
    M1 - M3
              3.88e-03 0.00950 2933
                                       0.408 0.9986
              8.74e-02 0.00925 2933
##
   M1 - MF
                                       9.451 < .0001
##
    M1 - MN
             -1.21e-02 0.00957 2933
                                      -1.260 0.8069
##
   M1 - S
              1.24e-01 0.01067 2933
                                     11.593 <.0001
    M2 - M3
              4.00e-03 0.00953 2933
                                       0.420 0.9983
    M2 - MF
              8.76e-02 0.00928 2933
##
                                       9.434 < .0001
             -1.19e-02 0.00960 2933
##
    M2 - MN
                                      -1.243 0.8157
##
   M2 - S
              1.24e-01 0.01069 2933
                                      11.576 < .0001
   M3 - MF
              8.36e-02 0.00944 2933
                                       8.848 < .0001
   M3 - MN
            -1.59e-02 0.00976 2933
                                      -1.633 0.5767
##
              1.20e-01 0.01083 2933
##
    M3 - S
                                      11.056 < .0001
    MF - MN
            -9.95e-02 0.00951 2933 -10.456 <.0001
##
    MF - S
              3.62e-02 0.01061 2933
                                       3.411 0.0086
##
    MN - S
              1.36e-01 0.01089 2933 12.455 <.0001
##
## TeD = TeD7:
##
    contrast
             estimate
                             SE
                                  df t.ratio p.value
    M1 - M2
             -3.06e-02 0.00934 2933
                                      -3.274 0.0137
             -4.54e-02 0.00950 2933
##
   M1 - M3
                                     -4.778 < .0001
   M1 - MF
              3.37e-02 0.00925 2933
                                       3.648 0.0037
   M1 - MN
             -6.18e-02 0.00957 2933
                                      -6.459 < .0001
##
    M1 - S
              7.70e-02 0.01067 2933
                                       7.223 < .0001
##
             -1.48e-02 0.00953 2933
                                      -1.554 0.6290
##
    M2 - M3
              6.43e-02 0.00928 2933
   M2 - MF
                                       6.931 < .0001
             -3.12e-02 0.00960 2933
                                      -3.254 0.0146
##
   M2 - MN
##
    M2 - S
              1.08e-01 0.01069 2933
                                      10.065 < .0001
##
   M3 - MF
              7.91e-02 0.00944 2933
                                       8.380 < .0001
   M3 - MN
             -1.64e-02 0.00976 2933
                                      -1.684 0.5427
   M3 - S
              1.22e-01 0.01083 2933
                                      11.301 < .0001
##
##
    MF - MN
             -9.56e-02 0.00951 2933 -10.044 <.0001
##
    MF - S
              4.33e-02 0.01061 2933
                                       4.078 0.0007
##
    MN - S
              1.39e-01 0.01089 2933 12.745 <.0001
##
## P value adjustment: tukey method for comparing a family of 6 estimates
```

## For TeD1 (Classification task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- There is significant difference on moving from S to Mx (obs. p < 0.0001)
- $\{MN, M1, M2, M3\}$  result in similar performance  $(obs.p \in [0.0578, 1.0])$
- Only for this task MN performs worse than {M1, M2, M3}. But judging by previous point this is not too significant.

## For TeD2 (Classification task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- {MN, M1, M2, M3} do not show much performance difference  $obs.p \in [0.9087, 1.0]$ )
- MF and MS perform similarly (obs. p = 0.9995)
- There is significant difference between  $\{MN, M1, M2, M3\}$  and  $\{MF, MS\}$   $(obs.p \in [0.0089, 0.01])$

## For TeD3 (Classification task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- In the above, going from MN to M1 with 1 step jump there isn't too much score change (obs. p > 0.09)
- There is a significant difference with a jump from M1 to MF (obs. p = 0.0027)
- Again, all Mx are better than S (obs. p < 0.0409)

#### For TeD4 (Classification task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- $\{M1, M2, M3\}$  perform similarly (obs. p > 0.9)
- MN performs significantly better than any other method (obs. p < 0.04)
- An oddity where S performs better than MF, but with marginal insignificance (obs. p = 0.0667).

## For TeD5 (Recommendation task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- $\{M1, M2, M3, MF, MN, S\}$  all perform very similarly (obs. p > 0.86).
- Overall no significant different in score based on learning method used.
- This meets our prior expectation from observing the data graphically.

## For TeD6 (Regression task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- $\{MN, M1, M2, M3\}$  perform sililarly (obs. p > 0.57)
- There is a stark degradation when juping from M3 to MF (obs. p < 0.001)
- Again, S is significantly inferior to all Mx (obs. p < 0.008)

#### For TeD7 (Regression task)

Looking simply at means:

After looking at contrasts, with reference to the ranking above:

- $\{MN, M2, M3\}$  perform sililarly (obs. p > 0.54)
- Stark degredation in score on going from M2 to M1 (obs. p = 0.0137), showing thats tuning parts refined is give better performance.
- Again, S is significantly inferior (obs. p < 0.0007).

## **RQ-2** Conclusion

In general, transfer learning is better than a simple model trained with a single dataset (obs. p < 0.0001). No retraining for the specific TeD (MN) performed significantly better (obs. p < 0.05) than the simple model or any form of refininf.

For particular testsets and tasks transfer learning significantly was better in most cases (6 out of 7). For one recommendation task (TeD5) the choice of the methods did not show any significant difference in performance. For the regresion tasks no refinement (MN) worked very similarly (obs. p > 0.86) as refining 2 and 3 parts(M2, M3).