

**THIRD SEMESTER**

**B.Tech. IEP**

**Class Test-2**

**September-2020**

**EP-203: MATHEMATICAL PHYSICS**

**Time: 1.5 Hours**

**Max. Marks: 20**

**Note :** Answer **ALL** questions.  
Assume suitable missing data, if any.

1. A vector field given by  $\vec{A} = (x^2 + xy^2)\hat{i} + (y^2 + x^2y)\hat{j}$ . Show that the field is irrotational. (3)
2. Use Green's theorem in a plane to evaluate the integral  $\oint_C [(2x^2 - y^2)dx + (x^2 + y^2)dy]$  where C is the boundary in the xy-plane of the area enclosed by the x-axis and the semi-circle  $x^2 + y^2 = 1$  in the upper half xy-plane. (5)
3. Derive the various possible solutions to Laplace's equation in Cartesian coordinates by the method of separation of variables. (5)
4. Derive the solution of the equation for the vibrating rectangular membrane. (7)