

EXPERIMENT - 1

Aim :

Determination of Stefan - Boltzmann constant σ .

Apparatus :

Heater, temperature-indicators, metallic hemisphere with water-flow, copper-disk as a black body.

Theory :

A black body is an ideal body which absorbs or emits all types of electromagnetic radiation. Acc. to Stefan's law, energy radiated per unit area per unit time is,

$$R = \epsilon \sigma T^4.$$

ϵ = emissivity of material

σ = Stefan's constant ($5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$)

$$\text{net Heat Transfer, } \frac{\Delta Q}{\Delta t} = \sigma A (T_h^4 - T_d^4) = m C_p \frac{dT}{dt}$$

$$\text{Hence, } \sigma = \frac{m C_p}{A (T_h^4 - T_d^4)} \times \frac{dT}{dt}$$

Procedure :

- Remove the disc from the bottom of the hemisphere and switch on the heater and allow the water to flow through it.
- Allow the hemisphere to reach the steady state and note down the temperature T_1, T_2, T_3 .

- Fit the disc at bottom of hemisphere and note down its rise in temperature with respect to time till steady state is reached.
- A graph is plotted with temperature of disc along Y-axis and time along X-axis.
- Find out the slope dT/dt from the graph.
- For simulator :
 - choose desirable values of water temperature, surrounding temperature, mass and radius of disc using sliders.
 - Power on wait till T_1, T_2, T_3 reach steady state.
 - Plot temperature - time and determine its slope dT/dt , after pulling T_1 button and fit the disk.
 - Note down T_1 at different intervals of time till it reaches steady state.

Calculation :

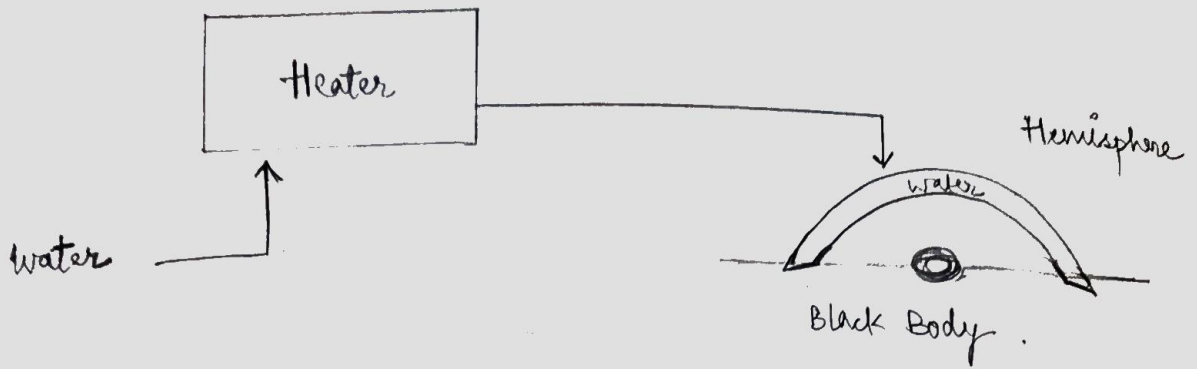
Mass of copper disk = $m = 0.007 \text{ kg}$.

Radius of the disk = 0.03 m .

Area of disk = 0.002826 m^2

Specific heat of copper = 385 J/kg .

$$\sigma = \frac{m C_p \frac{dT}{dt}}{A (T_h^4 - T_c^4)} \quad \text{W m}^{-2} \text{ K}^{-4}$$



Observation

①

S.No.	T (°C)	t (sec)
1	34	30
2	41	60
3	48	90
4	55	120
5	63	150
6	64.33	160

Temp. of hemisphere = 67°

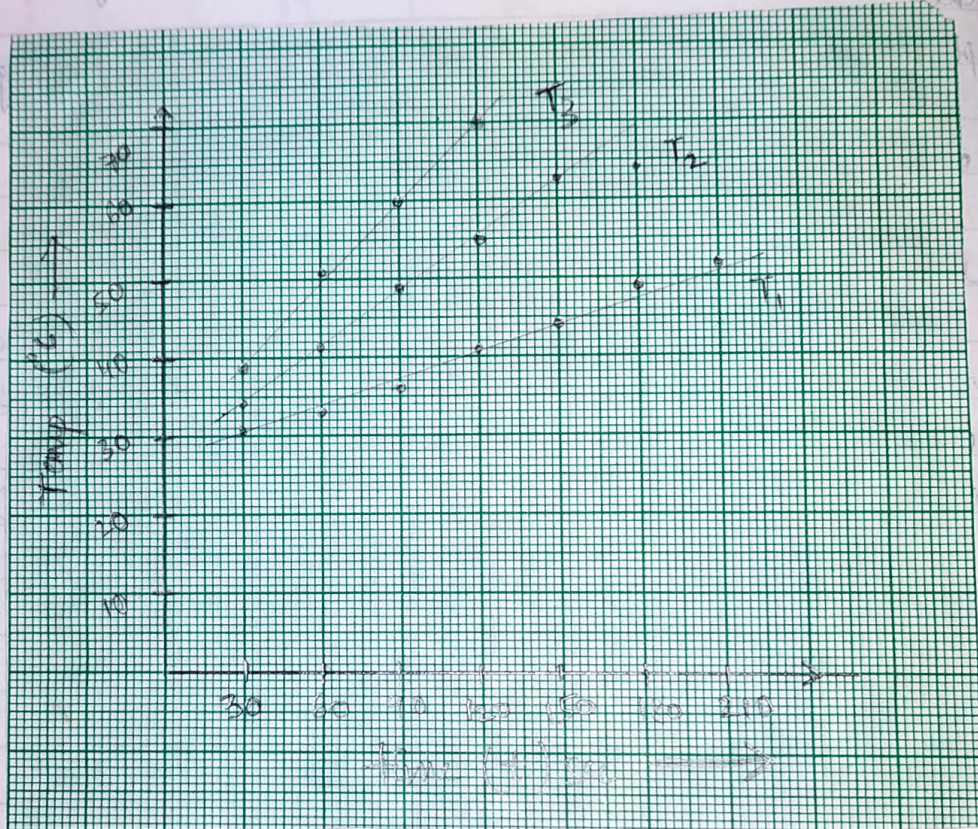
Temp. of disk = 27°

- ② Temp. of hemisphere = 77°
 Temp. of disk = 27° .

S.No.	T ($^{\circ}\text{C}$)	t (sec)
1.	39	30
2.	51	60
3	60	90
4	76.4	120
5	76.4	150

- ③ Temp. of hemisphere = 57° , disk = 27° .

S.No.	T ($^{\circ}\text{C}$)	t (sec)
1	30.58	30
2	33	60
3	37	90
4	41	120
5	44.8	150
6	48.46	180
7	52.03	210
8	54.42	235



Graph:

Temp v/s time

$$(P_1 T_1 - P_2 T_2) A$$

$$① \quad T_h = 330 \text{ K}, \quad T_d = 300 \text{ K}, \quad \frac{dT}{dt} = \frac{5}{30}$$

$$\sigma_1 = \frac{0.007 \times 385 \times 5}{2826 \times 10^{-6} \times (330^4 - 300^4) \times 30} = 4.228 \times 10^{-8}$$

$$② \quad T_h = 340 \text{ K}, \quad T_d = 300 \text{ K}, \quad \frac{dT}{dt} = \frac{9}{30}$$

$$\sigma_2 = \frac{0.007 \times 385 \times 9}{2826 \times 10^{-6} \times 30 (340^4 - 300^4)} = 5.435 \times 10^{-8}$$

$$③ \quad T_h = 350 \text{ K}, \quad T_d = 300 \text{ K}, \quad \frac{dT}{dt} = \frac{12}{30}$$

$$\sigma_3 = \frac{0.007 \times 385 \times 12}{2826 \times 10^{-6} \times 30 \times (350^4 - 300^4)} = 5.523 \times 10^{-8}$$

$$\text{Mean } \sigma = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3} = 5.062 \times 10^{-8}$$

Percent Error :

$$\frac{5.67 \times 10^{-8} - 5.062 \times 10^{-8}}{5.67 \times 10^{-8}} = 10.7 \%$$

Result :

Stefan-Boltzmann's constant $\sigma = 5.062 \times 10^{-8}$.