

Experiment-3

Aim :

- To determine the number of lines per millimeter of the grating using the green line of the mercury spectrum.
- To calculate the wavelength of the other prominent lines of mercury by normal incidence method.

Apparatus :

Spectrometer, diffraction grating element, mercury vapor lamp.

Virtual Lab Simulator

Theory :

Diffraction Grating - arrangement of large number of equidistant and parallel slits which splits and diffracts light into several beams travelling in different directions. At normal incidence,

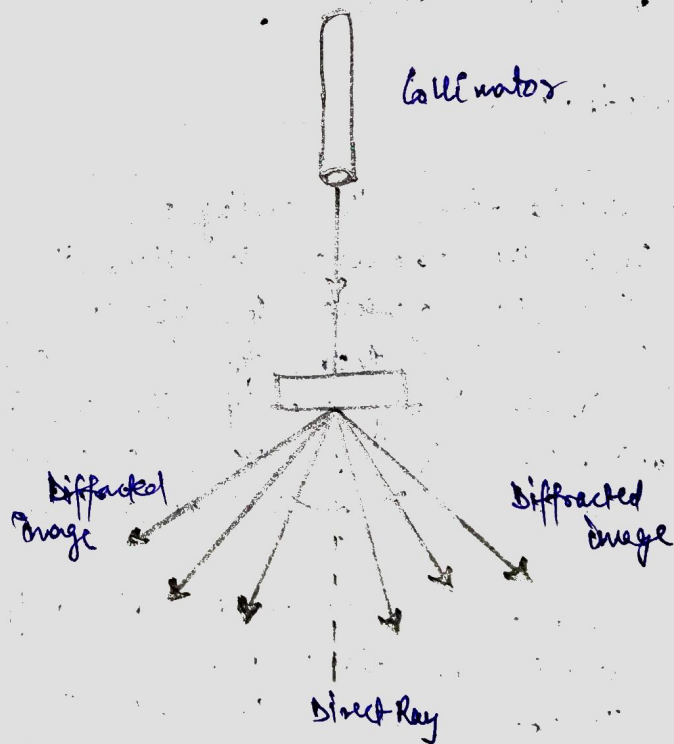
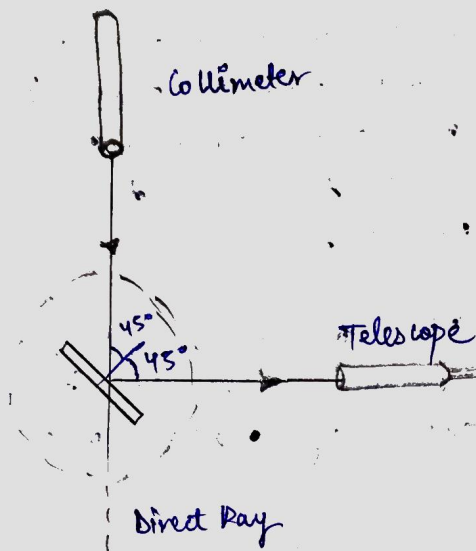
$$\sin(\theta) = N n \lambda$$

where, $N \rightarrow$ no. of lines per unit length of the grating.

$n \rightarrow$ order of spectrum.

$\lambda \rightarrow$ wavelength of light.

$\theta \rightarrow$ diffraction angle.



When waves pass through a gap, which is about as wide as the wavelength they spread out into the region beyond the gap. Huygens considered each point along a wave front to be the source of a secondary disturbance that forms a semi-circular wavelet.

Diffraction is due to the superposition of such secondary wavelets. These spreads and overlap each other interfering with each other to form a pattern of maximum and minimum intensity.

Procedure :

→ To standardize the grating :

- 1) Turn the telescope to obtain the image of the slit.
- 2) Turn the telescope to left and right side, note the readings ~~from~~ for green color.
- 3) Calculate difference in the reading to obtain diffraction angle. Hence calculate no. of lines per unit length of the grating can be calculated.

→ To calculate the wavelength of different lines :

- 1) Obtain the direct image.
- 2) Telescope is moved to make the cross-wire coincide with each line of the spectrum.
- 3) Note the readings on the vernier and calculate

Green colour :

	V_1			V_2		
	MS	VS	Total	MS	VS	Total
Left	340.5	8	340.633	160.5	27	160.95
Right	19	2	19.033	199	10	199.166
Difference (20)			321.6			38.216

$$V_1 - V_1' = 360 - 321.6 = 38.4$$

$$V_2 - V_2' = 38.216$$

$$\theta_{\text{mean}} = \frac{19.2 + 19.108}{2} = 19.154$$

no. of lines per millimeter,

$$N = \frac{\sin \theta}{n \lambda}$$

$$n = 1, \lambda_{\text{green}} = 546.1 \text{ nm}$$

$$N = \frac{0.328108}{1 \times 546.1} = 600.82$$

the diffraction angle.

4) Then calculate the wavelength of each colour.

Calculation :

Yellow :

$$V_1 - V_1' = 360 - (339.566 - 20.1) = 20.267$$

$$V_2 - V_2' = 200.066 - 159.533 = 20.2665$$

$$\theta_{\text{mean}} = 20.26675$$

$$\lambda = \frac{\sin \theta_{\text{mean}}}{nN} = \frac{0.346391}{600.82} = 576.53$$

Blue :

$$V_1 - V_1' = 360 - (342.6 - 172.533) = 34.433$$

$$V_2 - V_2' = 197.166 - 162.583 = 34.583$$

$$\theta_{\text{mean}} = 17.254$$

$$\lambda = \frac{0.296608}{600.82} = 493.67$$

Violet :

$$V_1 - V_1' = 360 - (345.6 - 14.033) = 28.433$$

$$V_2 - V_2' = 194.166 - 165.566 = 28.6$$

$$\theta_{\text{mean}} = 14.258$$

$$\lambda = \frac{0.246293}{600.82} = 409.92$$

Result :

Wavelength of yellow, blue, and violet line comes out to be 576.53 nm, 493.67 nm, and 409.92 nm respectively.

e. Determination of wavelength of prominent lines

color	left V_1 V_2		Right V_1 V_2		ϕ_{mean}	λ
Yellow	339.566	159.53	20.1	20.06	20.26	576.53
Blue	342.6	162.58	17.03	197.16	17.25	493.67
Violet	345.6	165.56	14.03	194.16	14.26	409.92

Least Count of Spectrometer = $\left(\frac{N}{V}\right) = \left(\frac{1}{60}\right)^\circ$

Total Reading = $MS + VS \times \text{Least Count}$