

## Experiment - 6

### Fourier Transform

#### Aim:

To observe the effect of amplitude and frequency variation of fourier transform of following waveforms;

- ↳ sine wave, cosine wave,
- ↳ triangular wave,
- ↳ sawtooth wave,
- ↳ square wave.

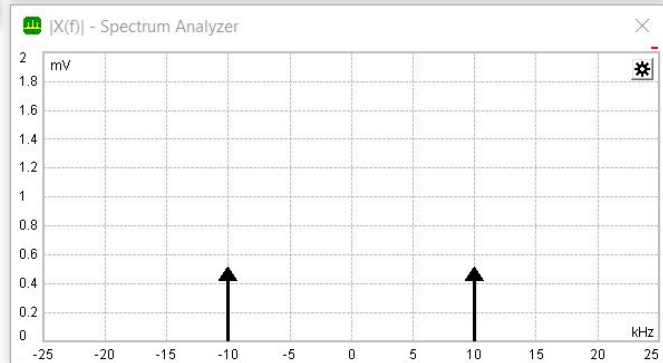
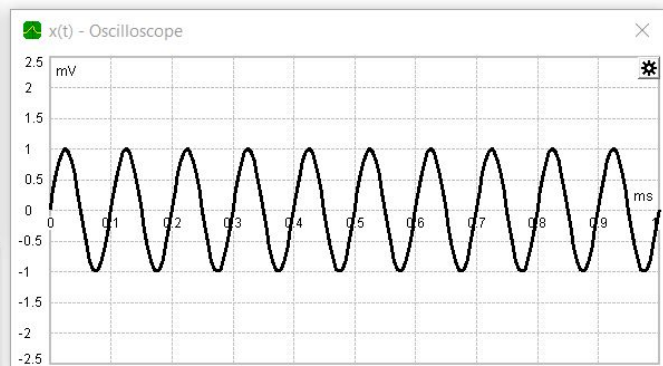
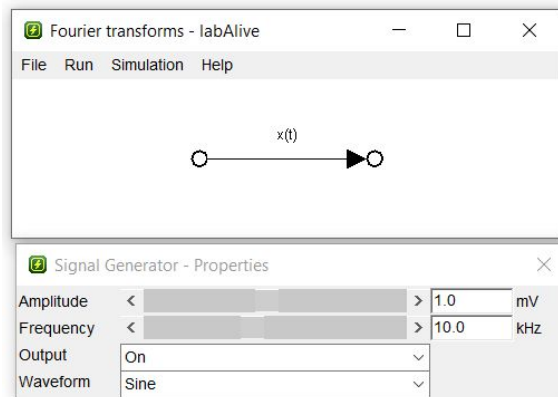
#### Theory:

Fourier transform is simply a method of expressing a function in terms of the sum of its projections onto a set of basis functions. Since an image is only defined on a closed and bounded domain, it is integrable over real line.

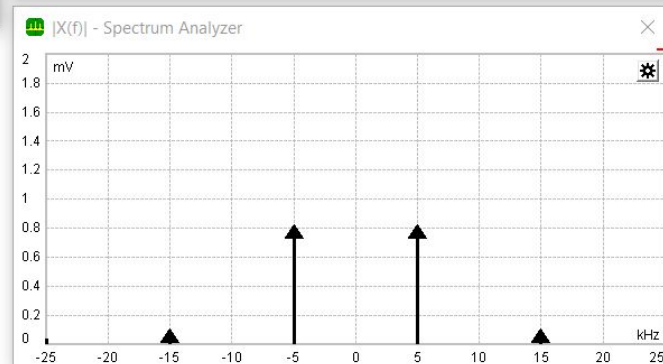
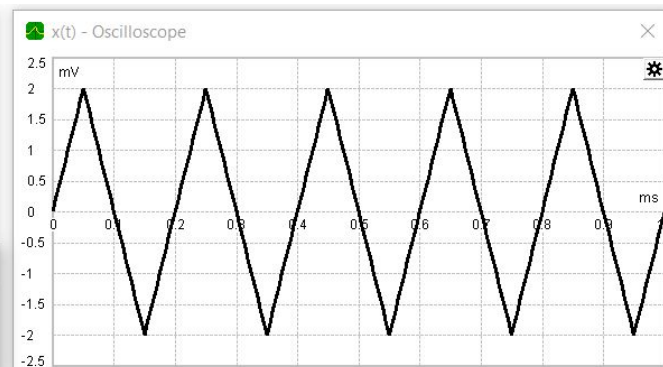
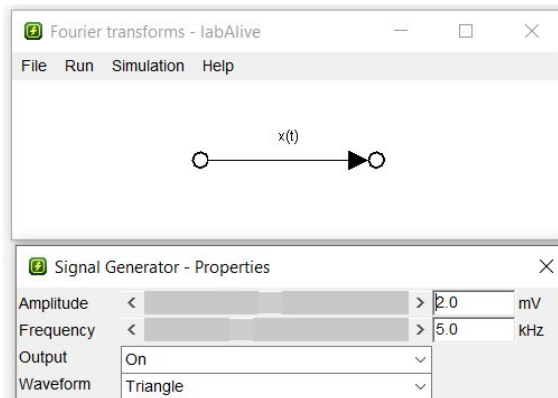
$$\hat{f}(\xi) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i x \xi} dx.$$

The result is a Dirac Delta function at  $\xi = \xi_0$ , which is the only frequency component of the sinusoidal signal  $e^{2\pi i \xi_0 x}$ .

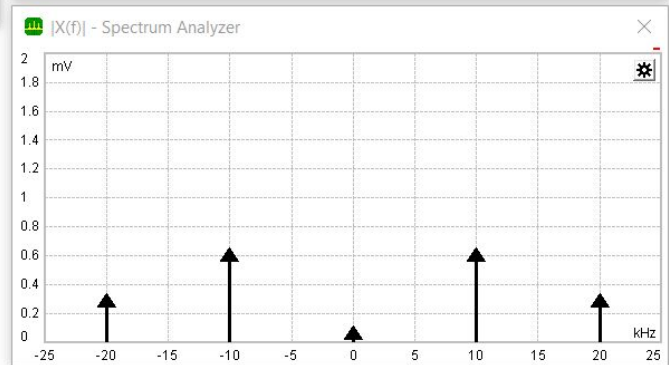
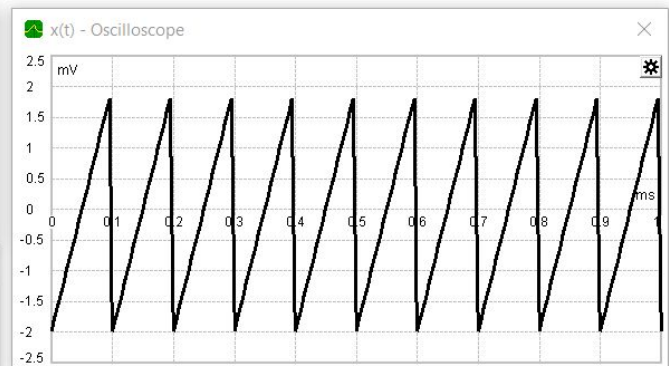
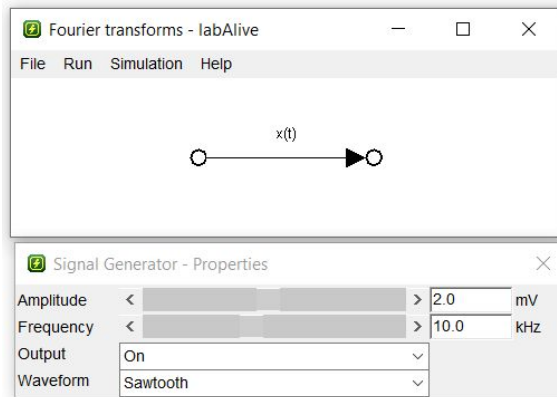
## Sine, Cosine Wave



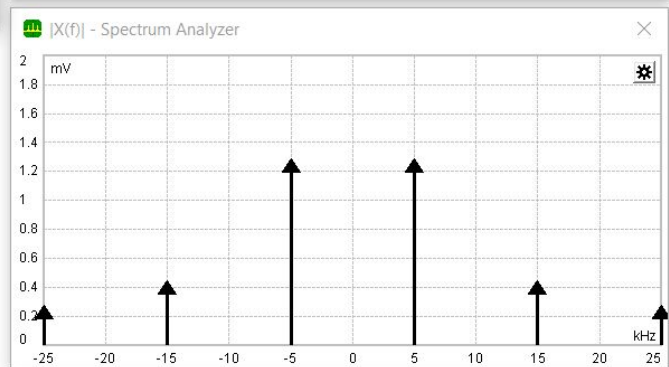
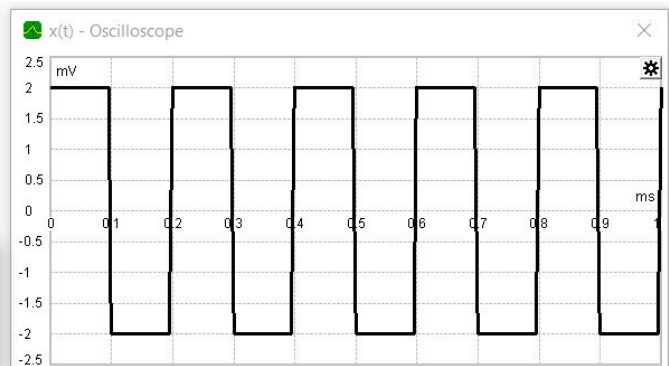
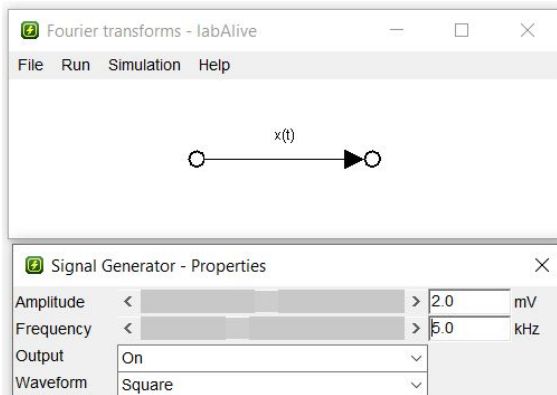
## Triangular Wave



## Sawtooth Wave



## Square Wave



Procedure :

- 1) Start the simulator.
- 2) Vary frequency and amplitude, and take the readings for sine, cosine, sawtooth, triangular and square wave.

Observations :

- 1) The spectrum was observed for different values of amplitude and frequency for different waveforms.
- 2) for sine wave, the value of amplitude was reduced to half, spectrum shows both extremes.
- 3) for cosine wave, result were same as sine wave.
- 4) for triangular wave, the value of amplitude reduces by 0.4, spectrum will appear one after skipping other.
- 5) Sawtooth wave will transform as

$$x_{\text{sawtooth}} = \frac{1}{2} - \frac{1}{\pi} \sum \left( \frac{\sin(2\pi k f(t))}{k} \right)$$

- 6) Square wave will follow

$$a_n = \frac{2A}{n\pi} \sin\left(\frac{n\pi}{2}\right).$$