

Q1  $(p \rightarrow q) \wedge q \rightarrow p$

ans. c) contingency.

Q2 ans. a)  $(p \leftrightarrow q) \leftrightarrow (p \rightarrow q) \wedge (q \rightarrow p)$ .

Q3 ans. a) Mathematical induction.

Q4  $a_n = (2.4) 3^n + 0.6 (-2^n)$ .

Q5 Direct proof is a sequence of statements which one either gives or deductions from previous statements, & whose last statement is the conclusion to be proved.

if  $x > y$ ,  $\max(x, y) = x$ ,  $\min(x, y) = y$

$\therefore \max(x, y) + \min(x, y) = x + y$

if  $x < y$ ,  $\max(x, y) = y$ ,  $\min(x, y) = x$

$\therefore \max(x, y) + \min(x, y) = y + x$ .

Q6 if  $P$  is a set of integers such that  
i)  $a$  is in  $P$ , ii) if all integers  $k$ ,  $a \leq k \leq n$  are in  $P$ ,  
then  $n+1$  is also in  $P$ .

then  $P = \{x \in \mathbb{Z} \mid x \geq a\}$  that is,  $P$  is the set of all integers greater than or equal to  $a$ .



Let  $M(n) \Rightarrow$  "You can run  $n^{\text{th}}$  mile",

Base Step :  $n=1, n=2$ ,

$M(1)$  and  $M(2)$  are true, according to question.

Inductive :

Assume  $M(1), M(2) \dots M(k)$  are all true,  
then you can run first  $k$  miles.

Since,  $M(k-1)$  is true, then  $M(k+1)$  is true,  
as you can run 2 miles more after a specific mile.

Conclusion :

By the principle of strong induction,  
 $M(n)$  is true for all positive  $n$  integers.

Q.7. Proof with example.

$$a_n = 6a_{n-1} - 9a_{n-2}, \quad a_0 = 1, a_1 = 6.$$

$\therefore x^2 - 6x + 9 = 0$  has only 3 as root.

Solution format:  $\alpha_1 3^n + \alpha_2 n 3^n$ ,

$$a_0 = 1 = \alpha_1, \quad a_1 = 6 = \alpha_1 3 + \alpha_2 3$$

$$\Rightarrow \boxed{\alpha_1 = 1, \alpha_2 = 1}$$

$$\therefore \underline{a_n = 3^n + n 3^n}$$