

# Getting Started

CS771: Introduction to Machine Learning

Purushottam Kar

# Announcements

Course has reached capacity – no more adds unless drops take place

Please sign-up on Piazza – we will discontinue use of emails soon

All discussions/queries only on Piazza – none over email

Class polls on whether to hold extra discussions also only over Piazza

Do not worry about Gradescope – I will signup all registered students

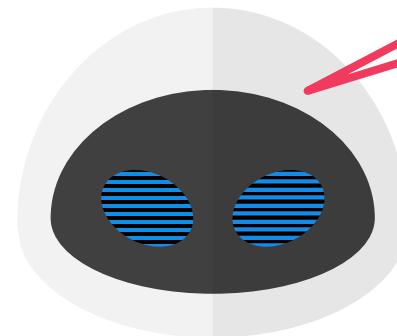
Reference list updated – more organized, math for ML resources



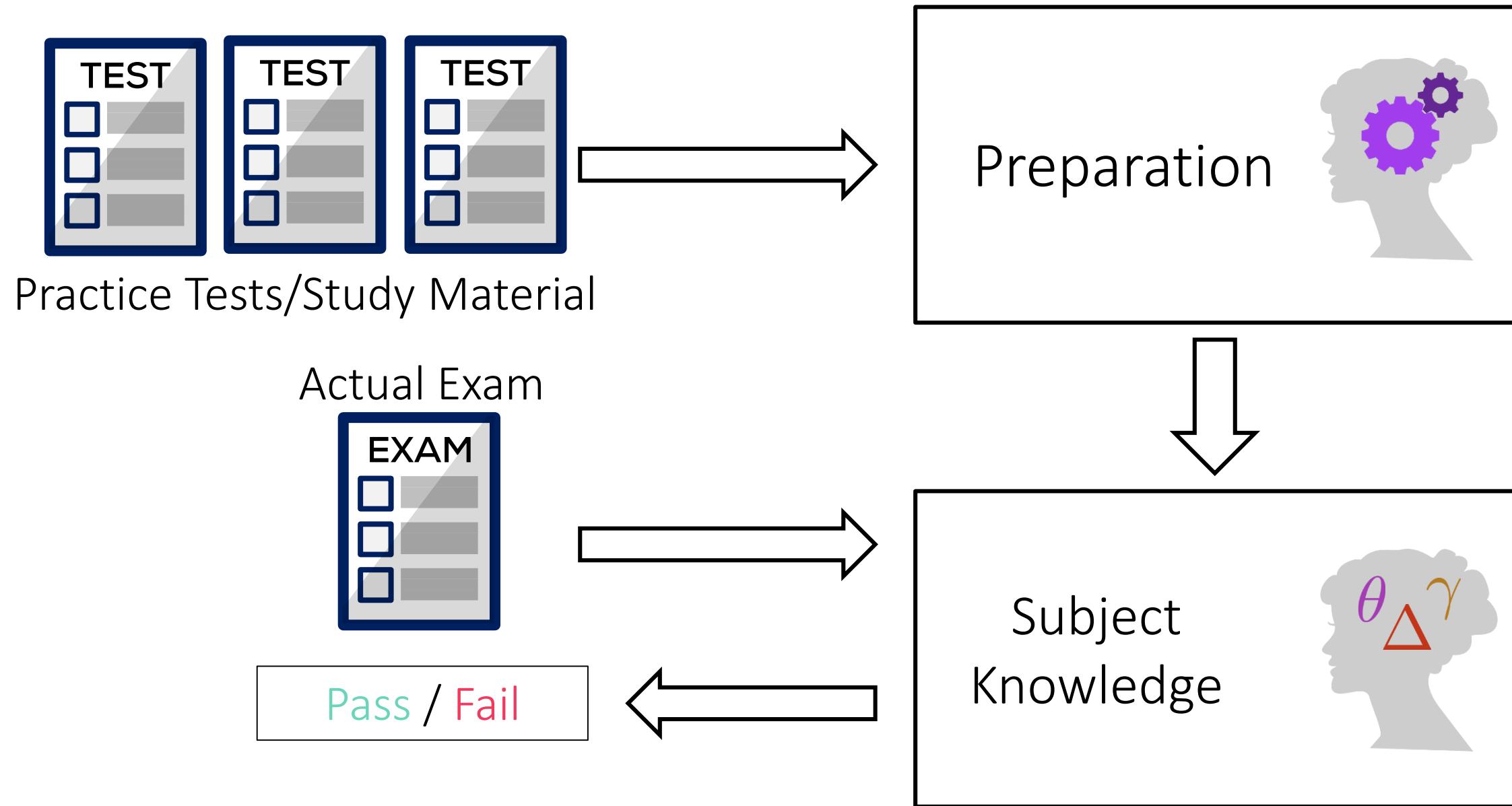
# An overview of ML

- Study similarity of ML with a student preparing for an exam
- Look at a toy ML problem
- Learn what is training data, test data?
- Learn what is a model?

Warning: lots of oversimplifications ahead!

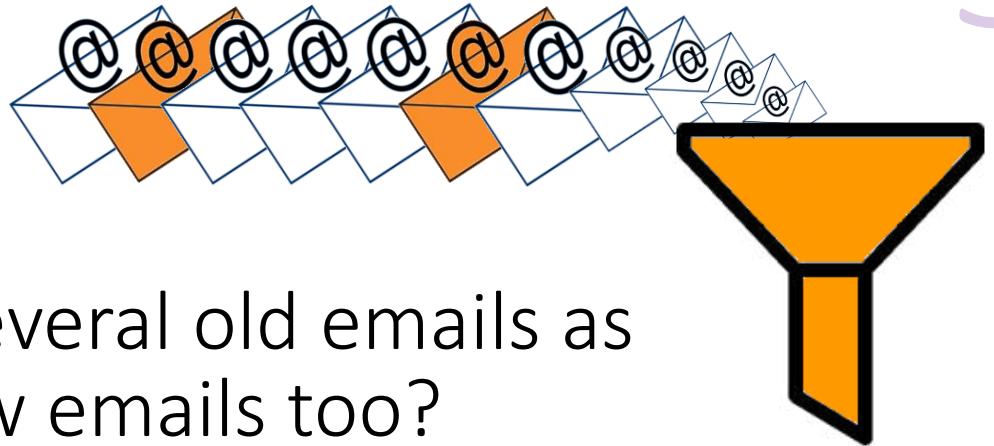


# A typical study cycle (e.g. in a course)



# Spam Filtering

- Suppose Mary has already tagged several old emails as spam/non-spam, can we tag her new emails too?
- Trick: use the old tagged emails to try and understand what sort of emails does Mary think of as spam and which as non-spam!
- E.g. may find that emails about shopping always tagged as spam
- E.g. may find that emails from Jill are never tagged as spam
- These insights/patterns are what are stored in the spam filter
- Our spam filter helps us make predictions on new emails



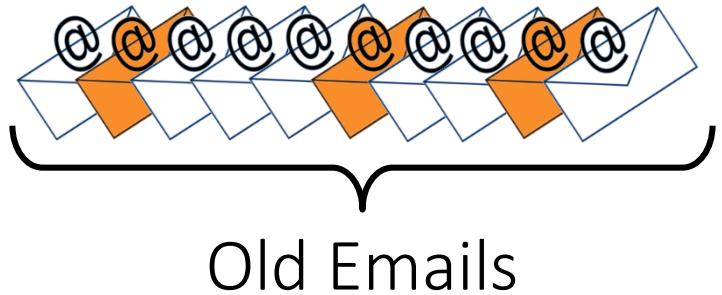
# A typical ML workflow

6

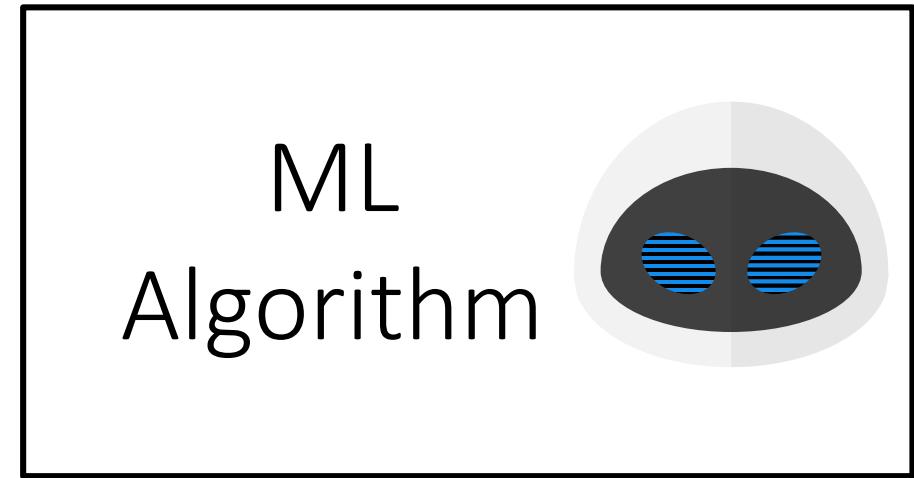
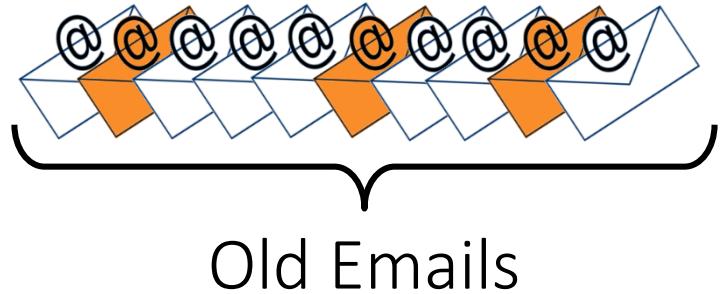


CS771: Intro to ML

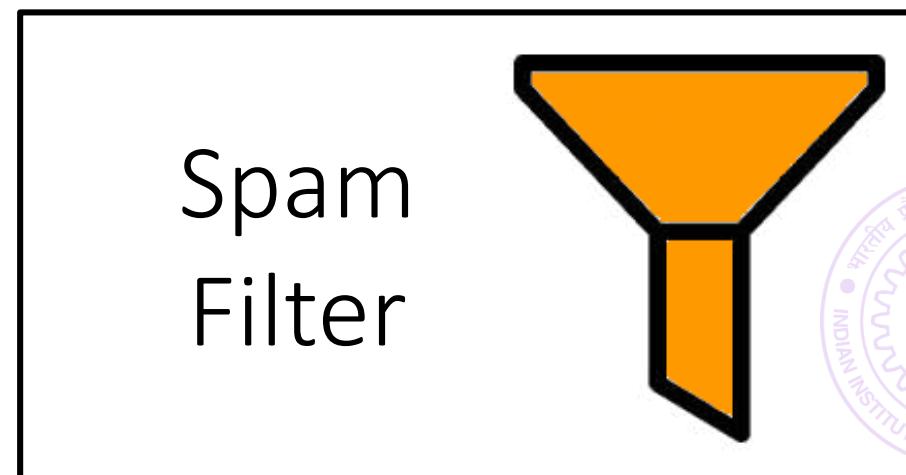
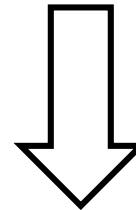
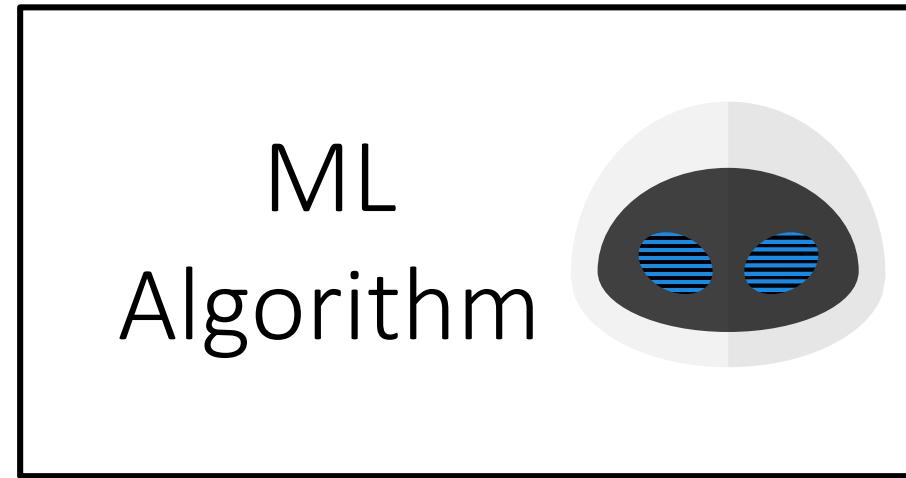
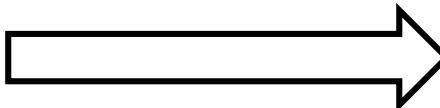
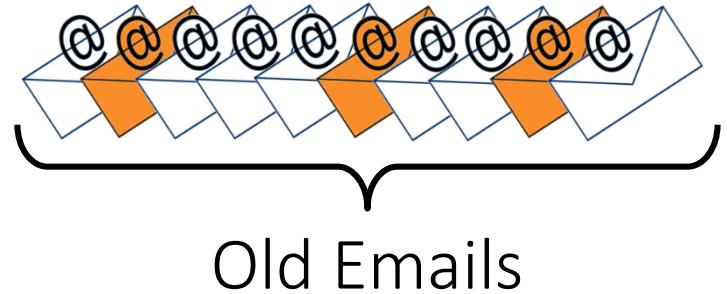
# A typical ML workflow



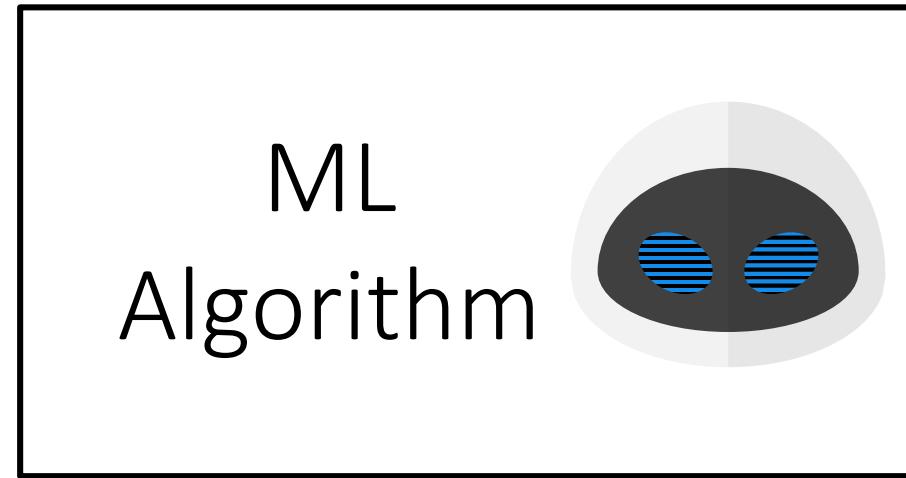
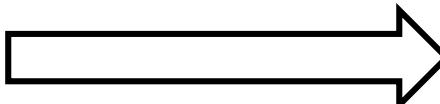
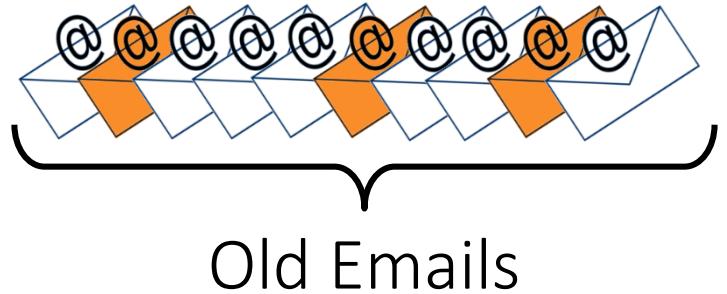
# A typical ML workflow



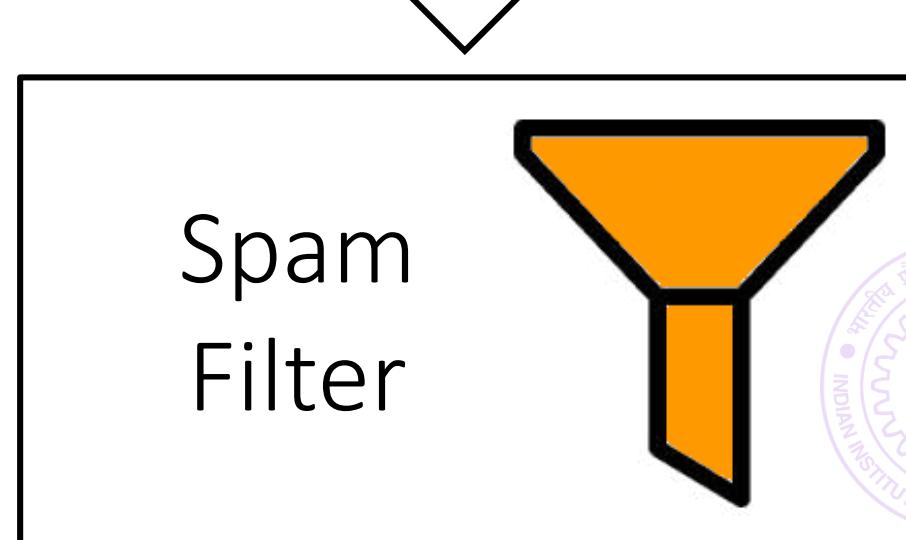
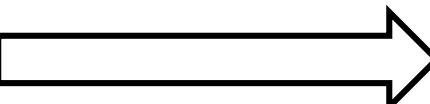
# A typical ML workflow



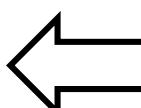
# A typical ML workflow



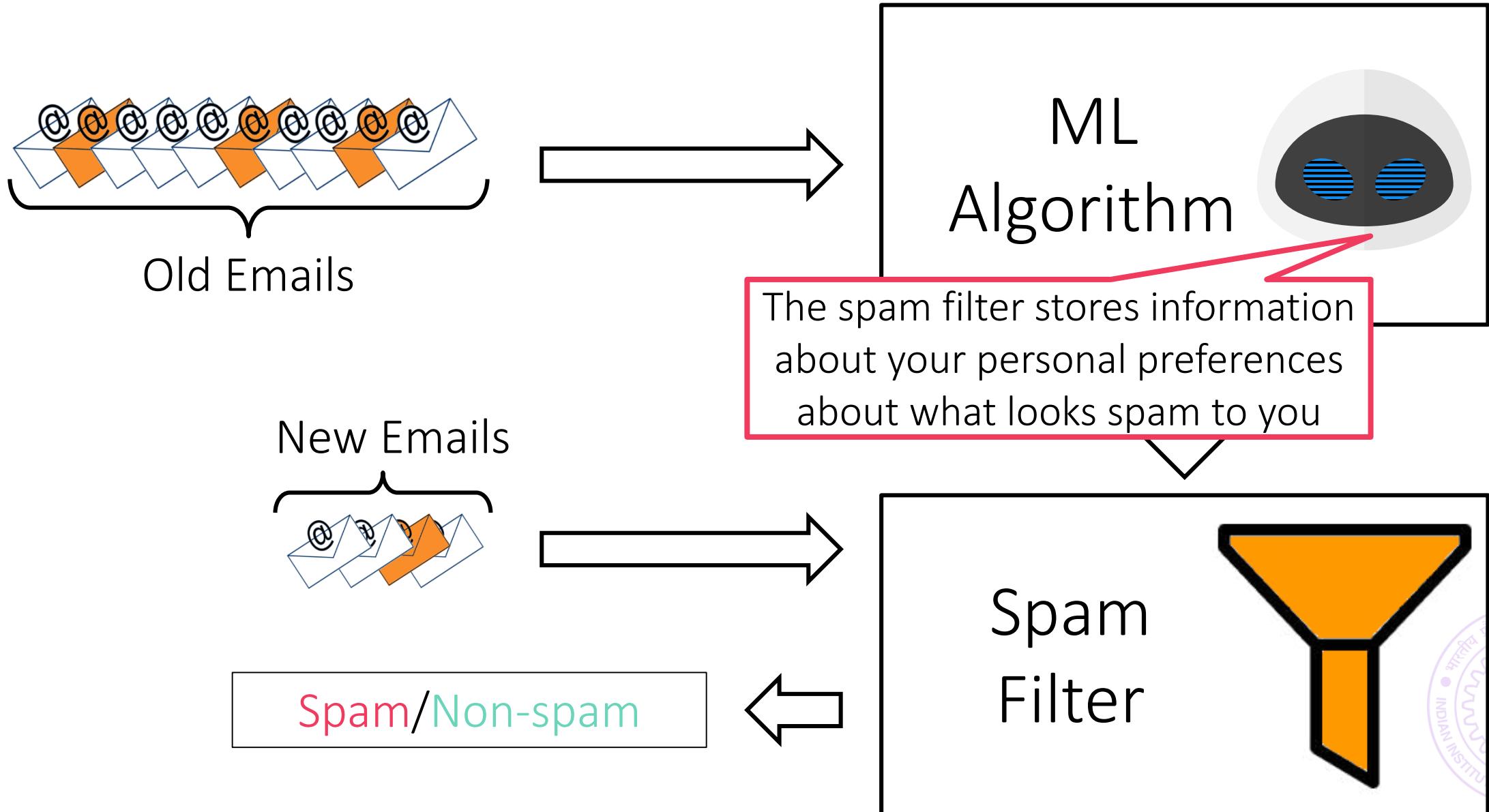
New Emails



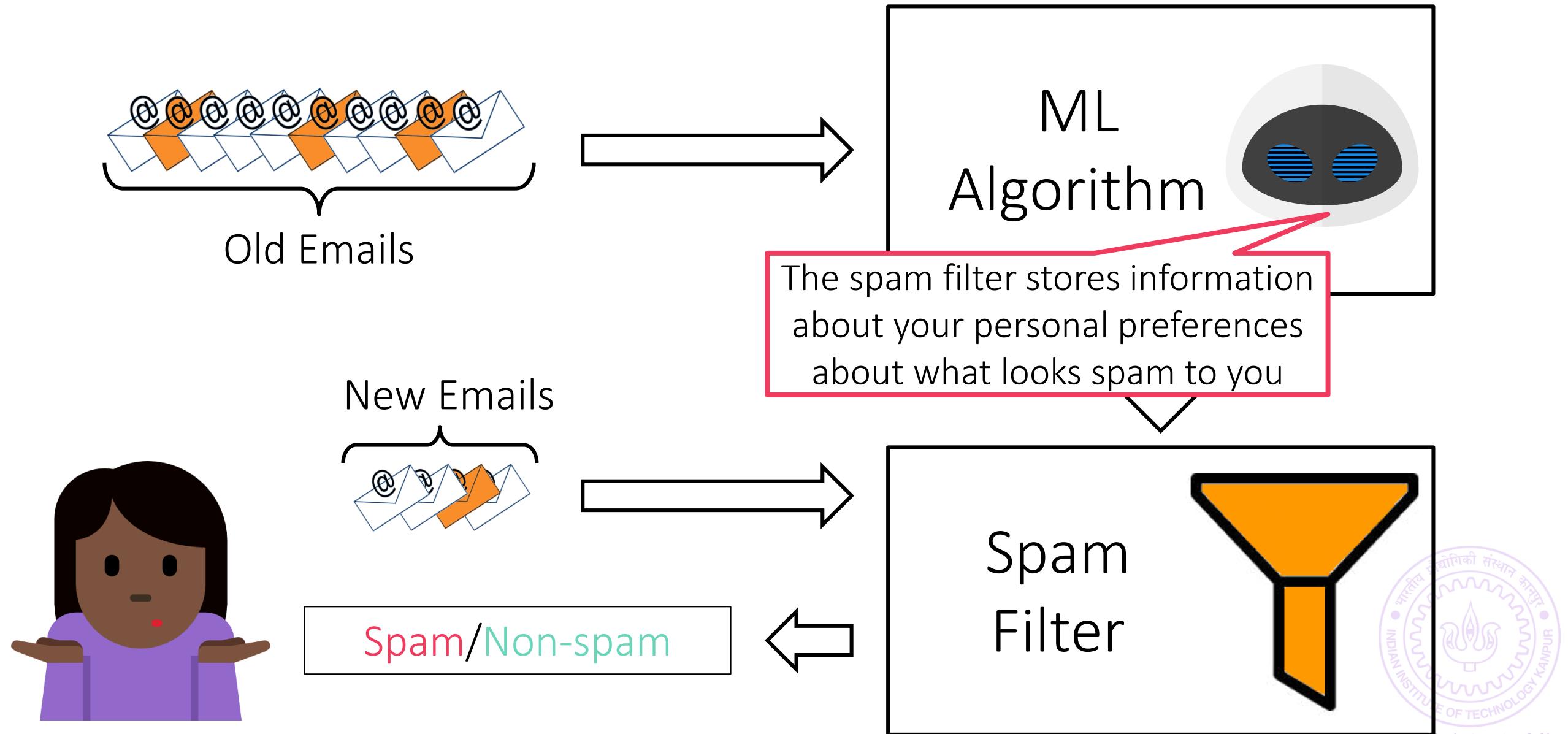
Spam/Non-spam



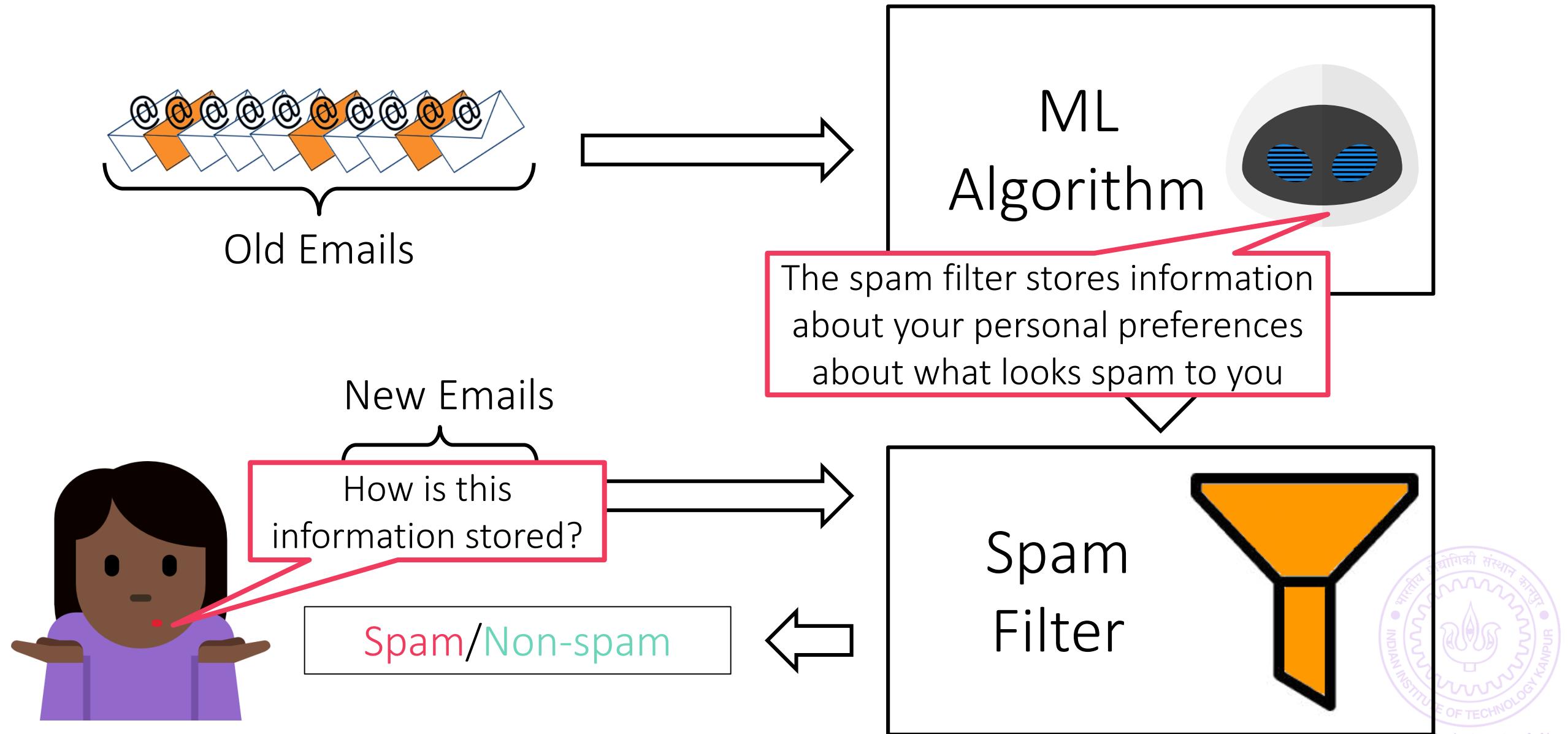
# A typical ML workflow



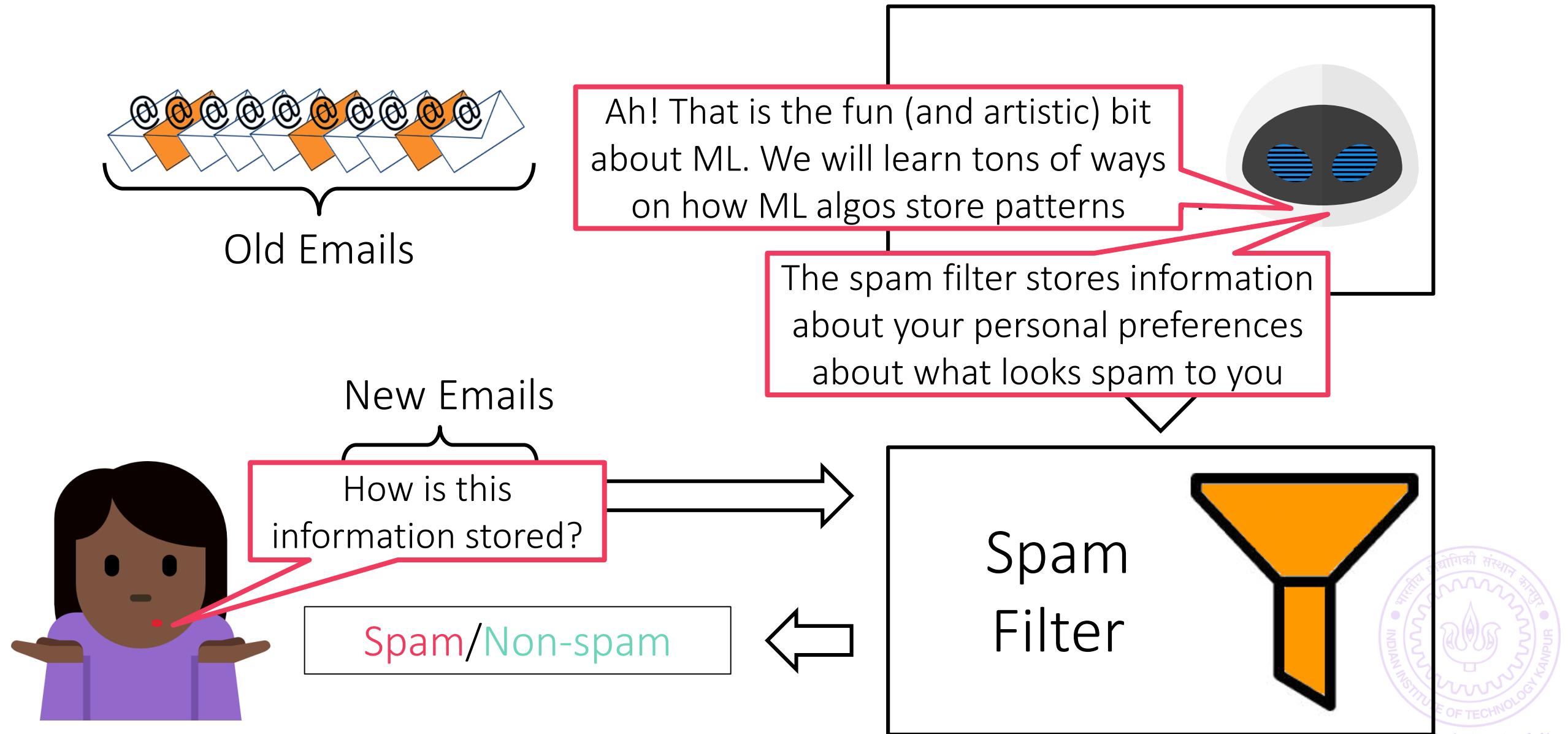
# A typical ML workflow



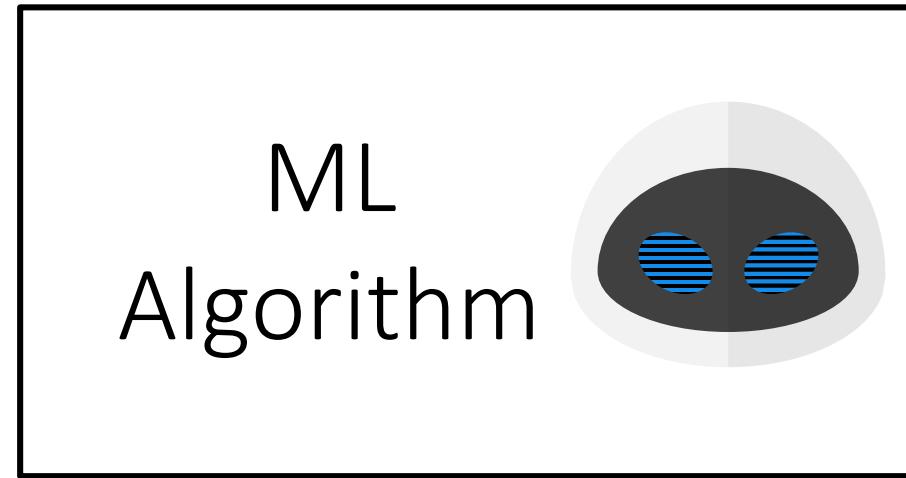
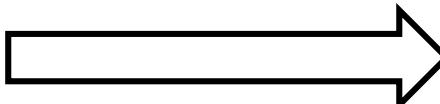
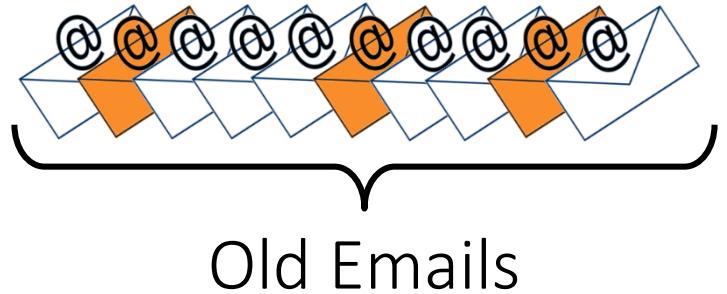
# A typical ML workflow



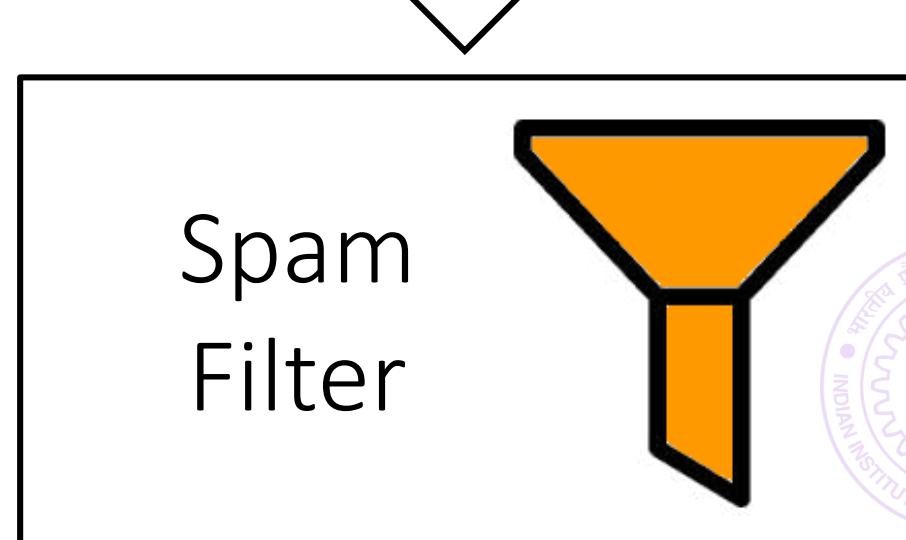
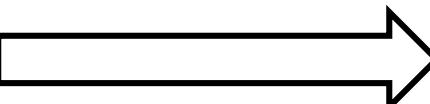
# A typical ML workflow



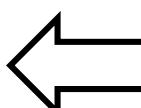
# A typical ML workflow



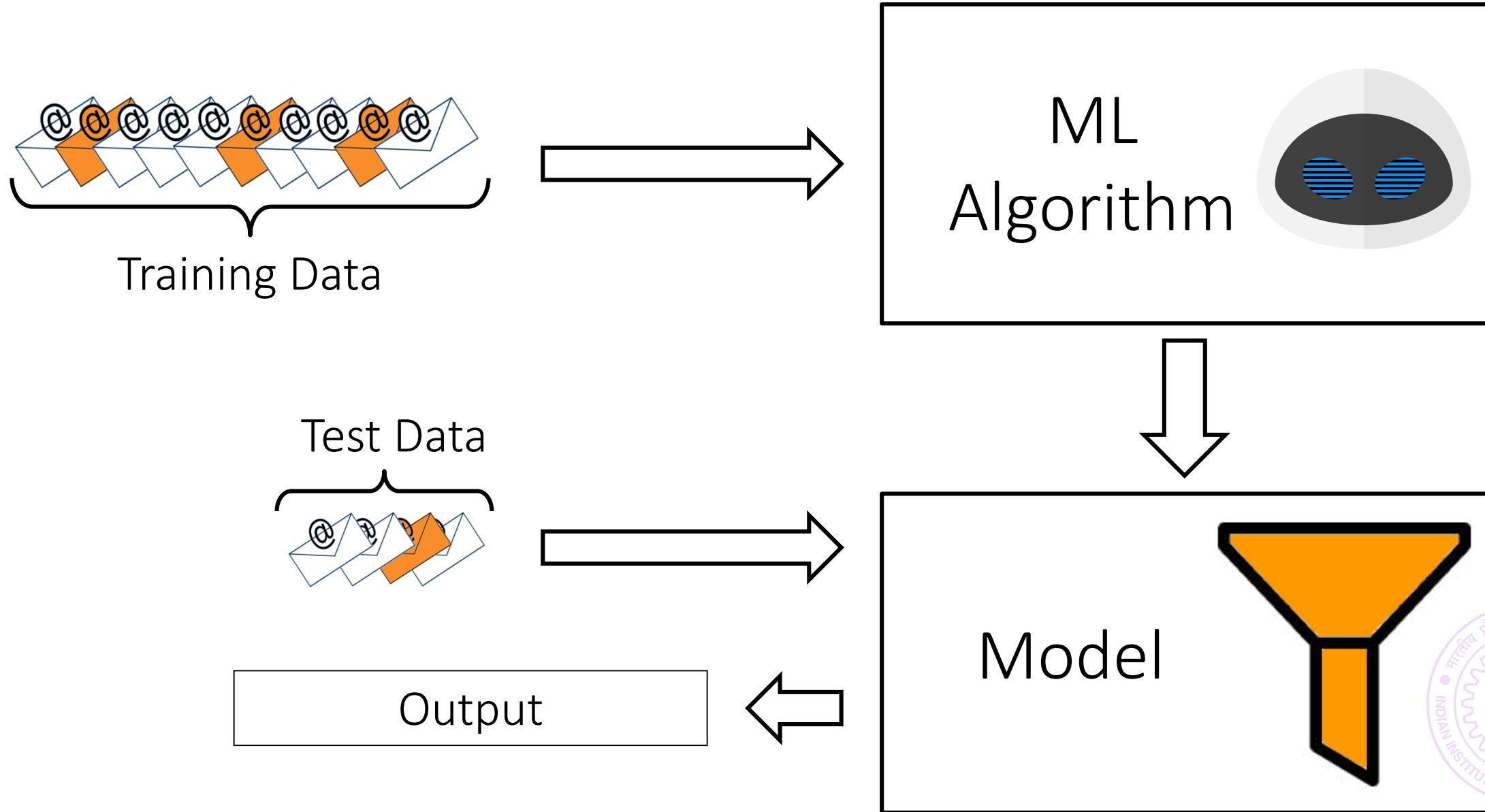
New Emails



Spam/Non-spam

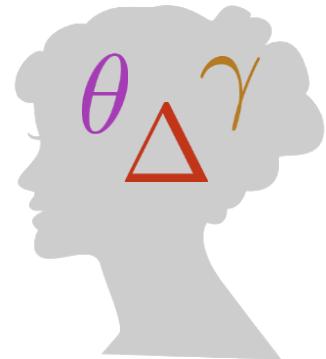


# A typical ML workflow

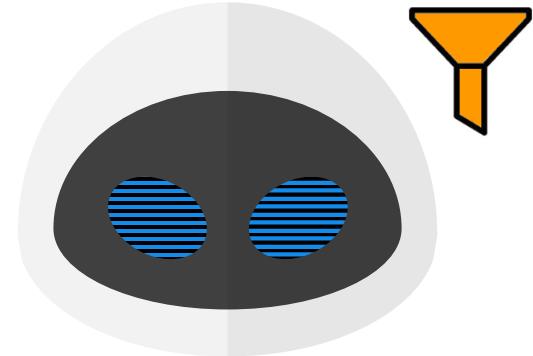


# ML as an “examination”

17



Our brain stores subject matter  
Use subject matter to solve exam  
Critical to do well on exam-day  
Mock test results indicative  
No out-of syllabus questions  
Should not leak exam paper before exam



The model stores data patterns  
Use model to predict on test data  
Critical to do well on test data  
Training accuracies indicative  
Training/test data are similar  
Should not look at test data while training

# ML can do lots of cool things with test data

Test Data



# ML can do lots of cool things with test data

18

Test Data



## Regression

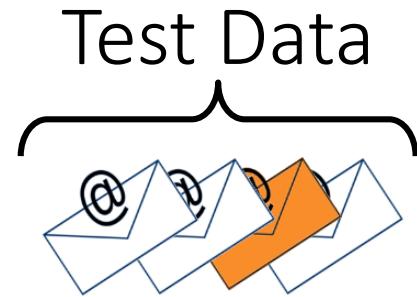
**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89



# ML can do lots of cool things with test data

18



## Regression

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes



# ML can do lots of cool things with test data

18

Test Data

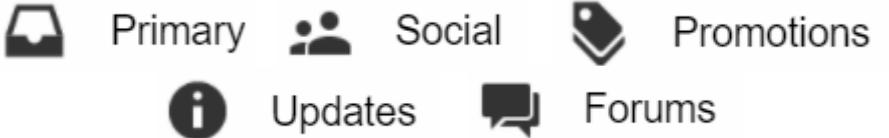


## Regression

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

## Multi-classification



## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes



# ML can do lots of cool things with test data

18

Test Data

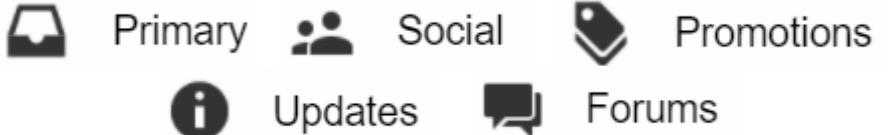


## Regression

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

## Multi-classification

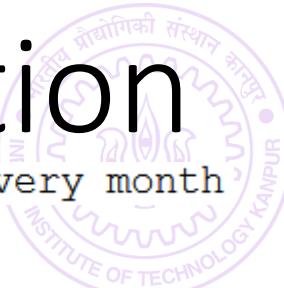


## Tagging



## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes



# ML can do lots of cool things with test data

18

Test Data

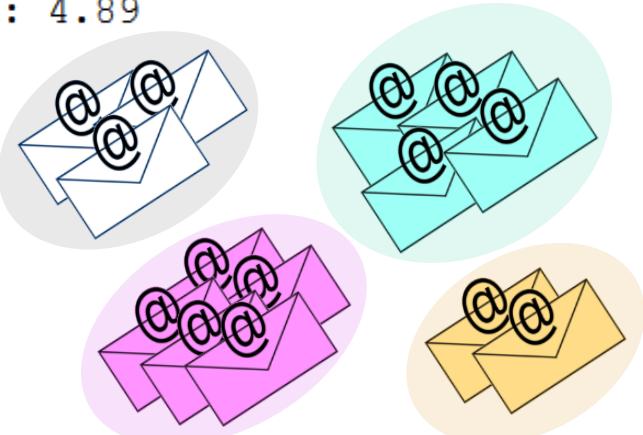


## Regression

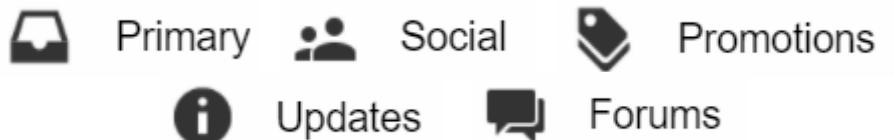
**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

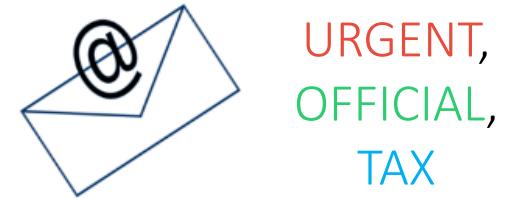
## Clustering



## Multi-classification

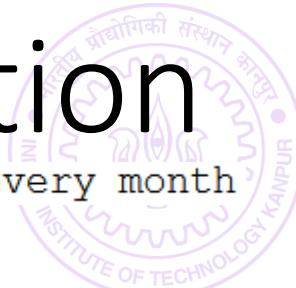


## Tagging



## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes



# ML can do lots of cool things with test data

18

Test Data

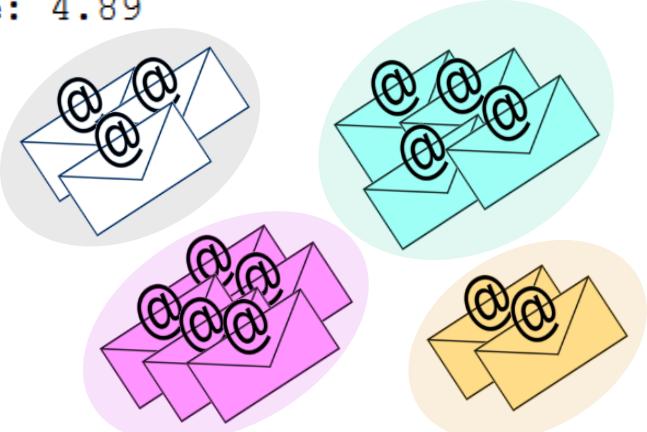


## Regression

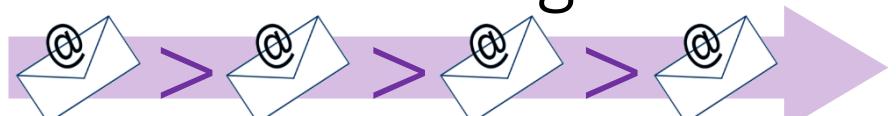
**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

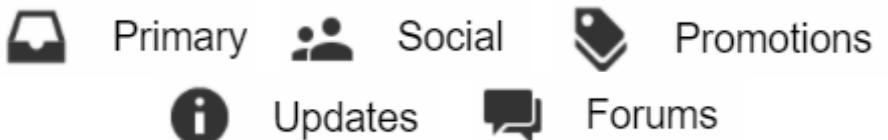
## Clustering



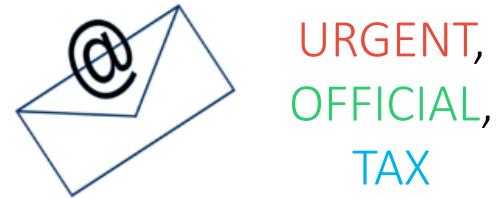
## Ranking



## Multi-classification



## Tagging

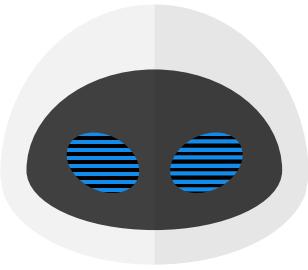
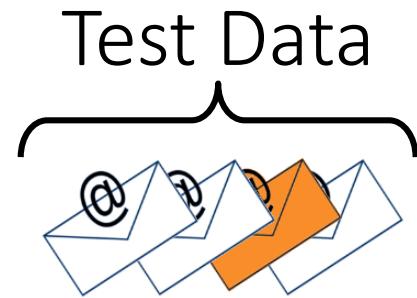


## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes

# ML can do lots of cool things with test data

18

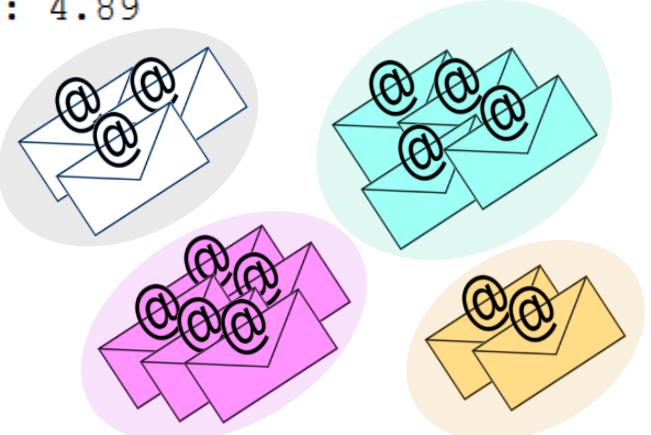


## Regression

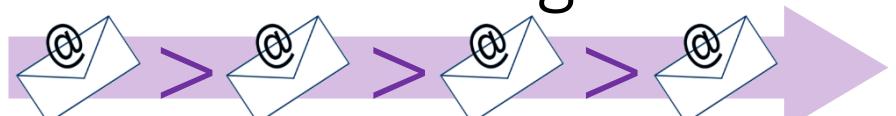
**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

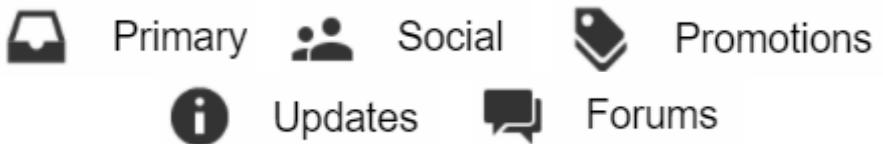
## Clustering



## Ranking



## Multi-classification



## Tagging



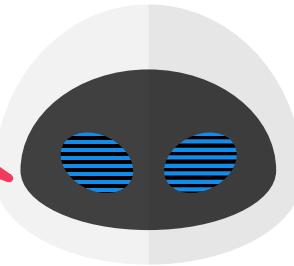
## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes

# ML can do lots of cool things with test data

18

In this course, we will learn how to do most of these operations with test data

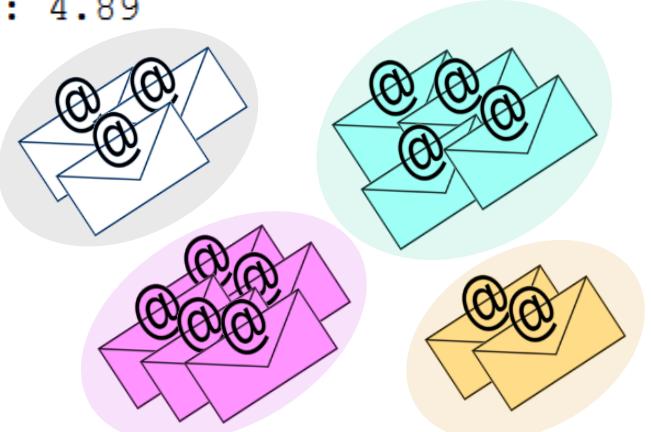


## Regression

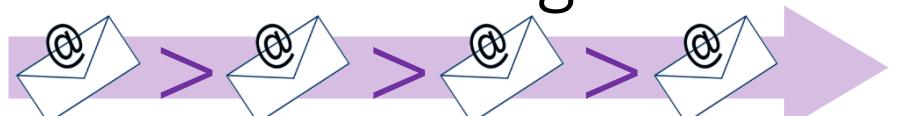
**Subject:** [\*\*SPAM\*\*] Free movie tickets every month

**X-Barracuda-Spam-Score:** 4.89

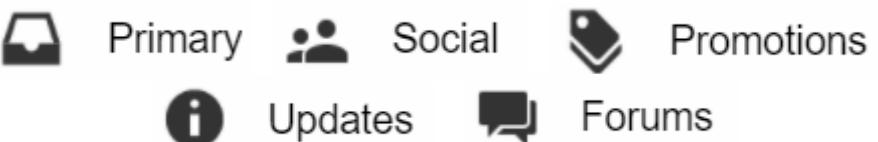
## Clustering



## Ranking



## Multi-classification



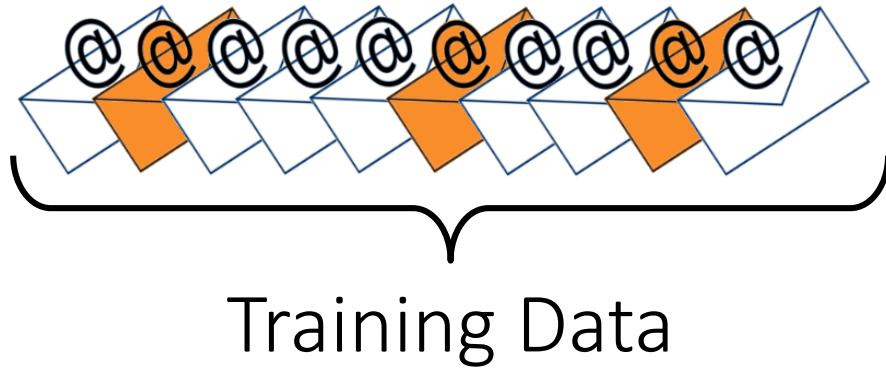
## Tagging



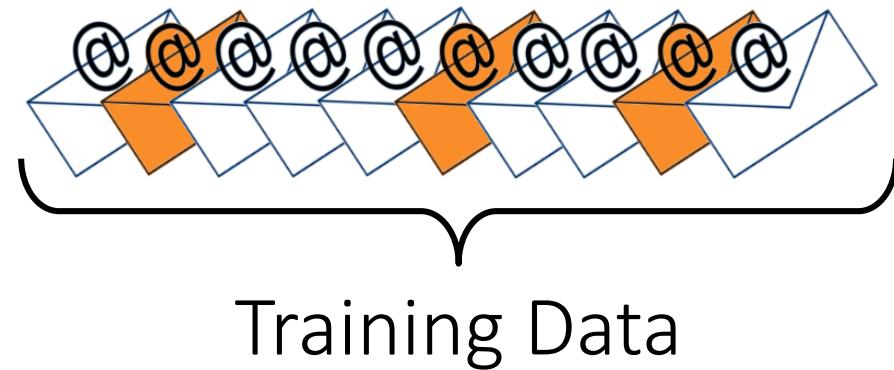
## Binary Classification

**Subject:** [\*\*SPAM\*\*] Free movie tickets every month  
**X-Barracuda-Spam-Status:** Yes

# ML can take in lots of kinds of training data



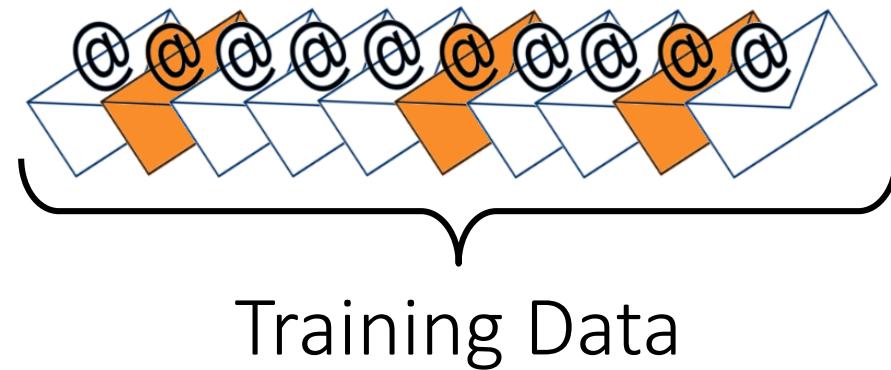
# ML can take in lots of kinds of training data



## Batch Learning



# ML can take in lots of kinds of training data

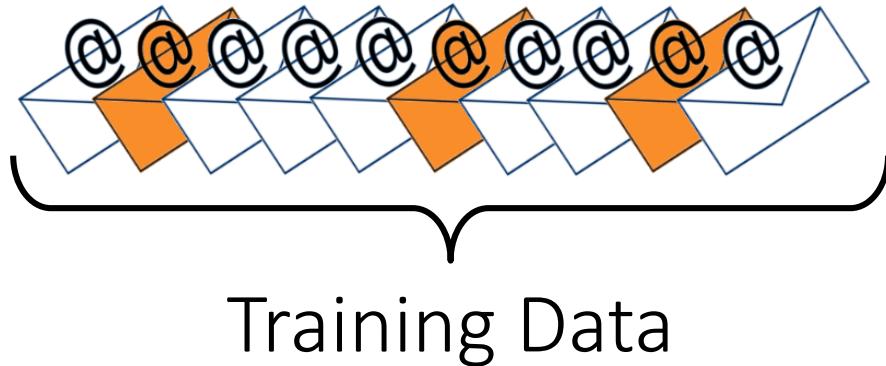


## Batch Learning

## Online Learning



# ML can take in lots of kinds of training data



---

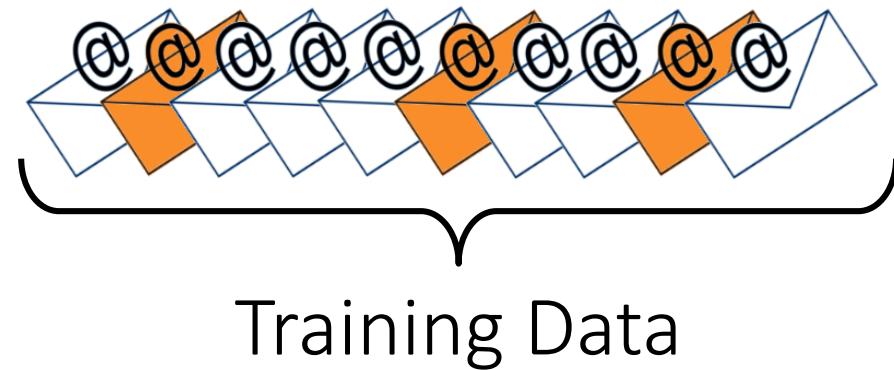
# Batch Learning

# Supervised Learning

# Online Learning



# ML can take in lots of kinds of training data



---

## Batch Learning

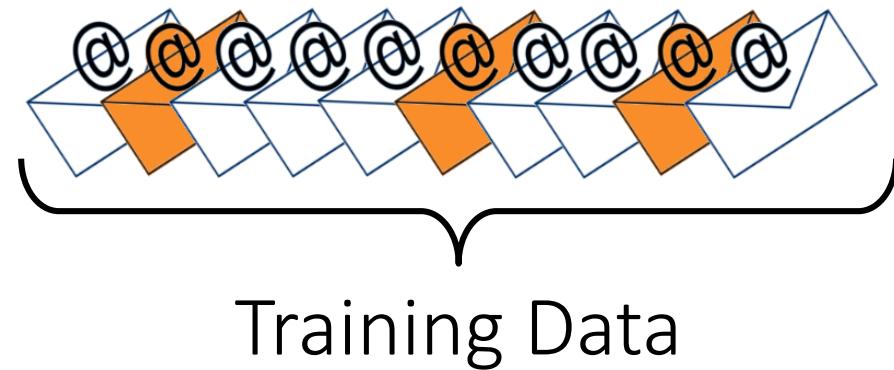
## Supervised Learning

### Online Learning

## Unsupervised Learning



# ML can take in lots of kinds of training data



## Batch Learning

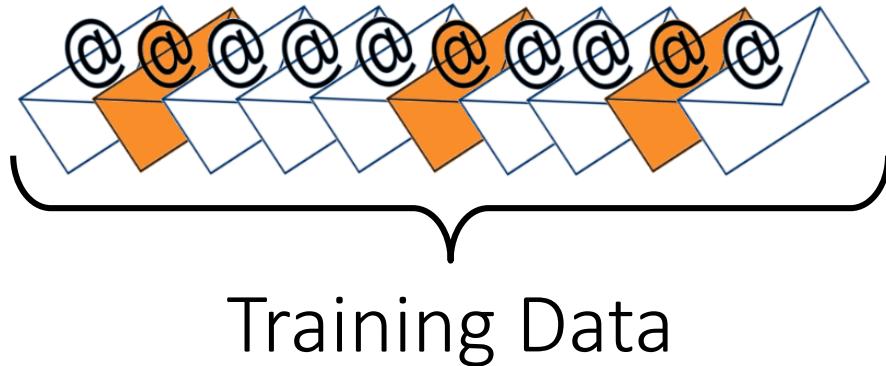
Semi-supervised  
Learning

Unsupervised Learning

Supervised Learning  
Online Learning



# ML can take in lots of kinds of training data



## Batch Learning

Semi-supervised  
Learning

## Unsupervised Learning

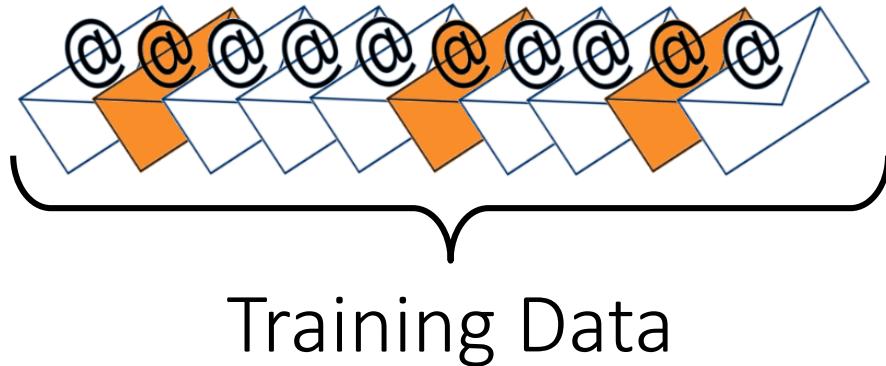
## Active Learning

## Supervised Learning

Online Learning



# ML can take in lots of kinds of training data



## Batch Learning

Semi-supervised  
Learning

## Unsupervised Learning

## Supervised Learning

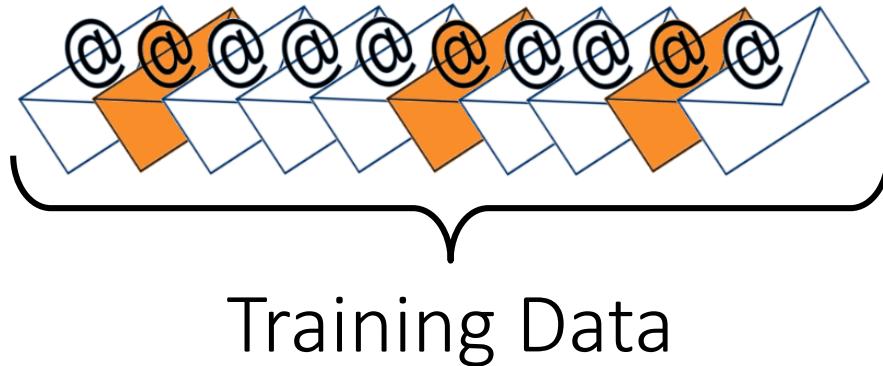
Robust Learning

Active Learning

Online Learning



# ML can take in lots of kinds of training data



## Batch Learning

Semi-supervised  
Learning

## Unsupervised Learning

## Supervised Learning

Online Learning

Active Learning

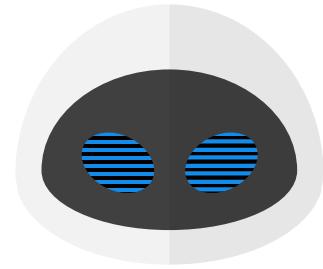
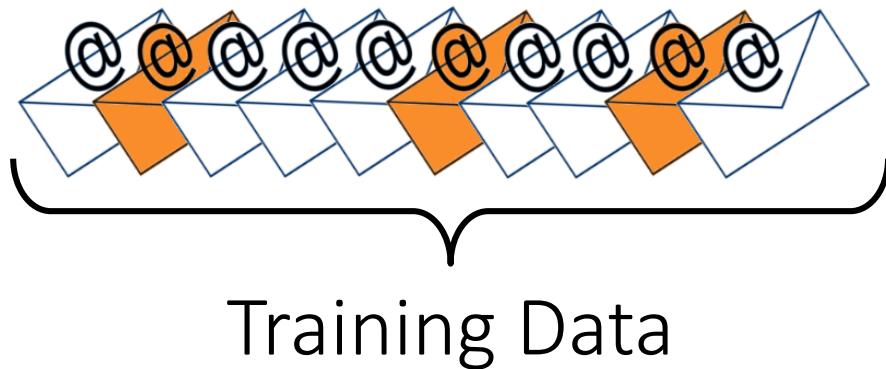
Robust Learning

Reinforcement Learning



# ML can take in lots of kinds of training data

19



## Batch Learning

Semi-supervised  
Learning

## Unsupervised Learning

## Supervised Learning

Robust Learning

Online Learning

Active Learning

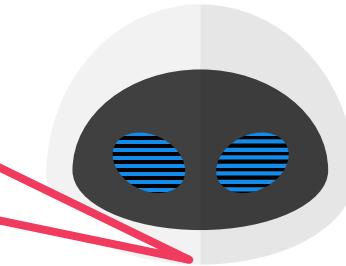
Reinforcement Learning



# ML can take in lots of kinds of training data

We won't be able to cover all these training settings in this course – there are entire courses devoted to specific training settings e.g. CS773 (Online Learning)

Training Data



## Batch Learning

Semi-supervised  
Learning

## Unsupervised Learning

## Supervised Learning

Robust Learning

Online Learning

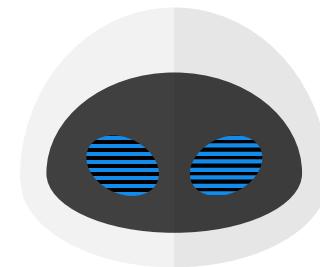
Active Learning

Reinforcement Learning



## ML Models and Algorithms

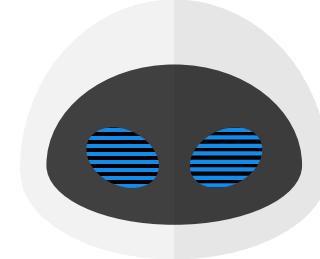
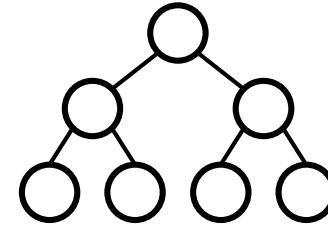
---



## ML Models and Algorithms

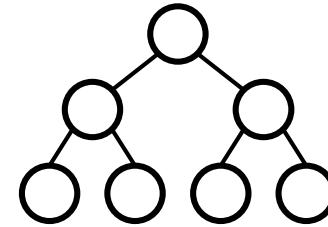
---

Local

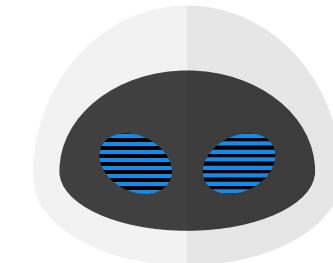
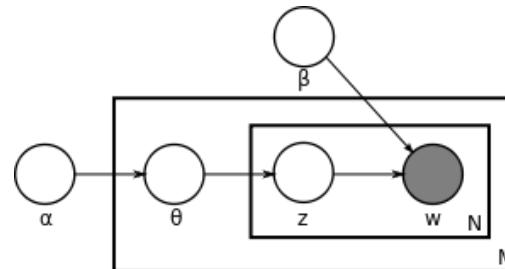


## ML Models and Algorithms

Local

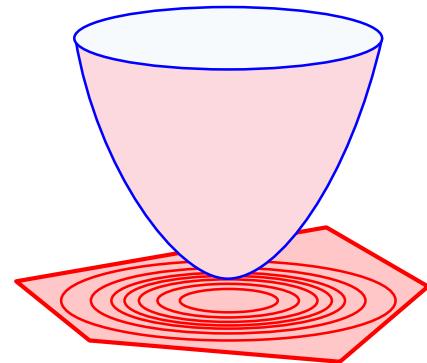


Probabilistic/Bayesian

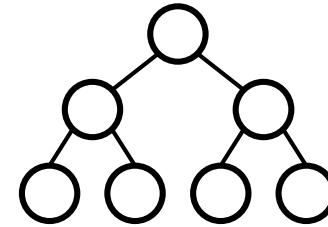


## ML Models and Algorithms

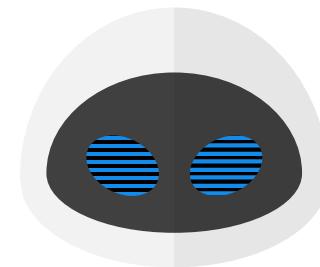
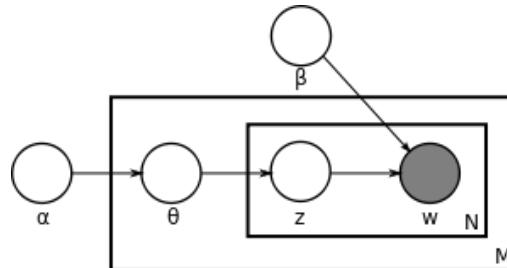
Linear/Opt



Local

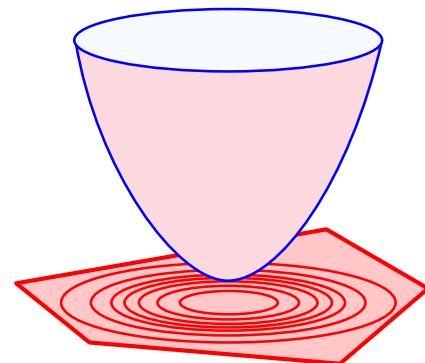


Probabilistic/Bayesian

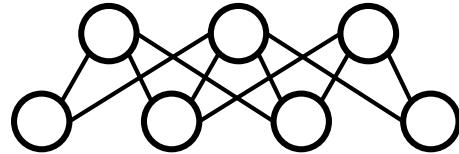


## ML Models and Algorithms

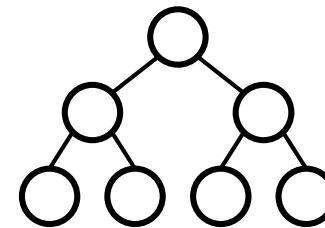
Linear/Opt



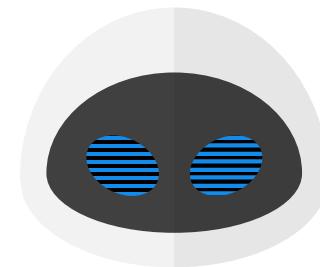
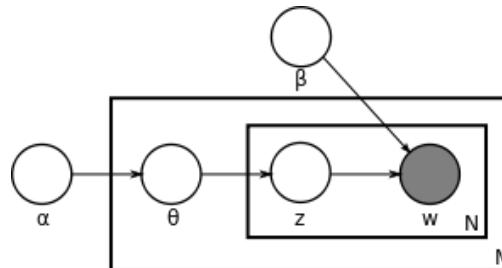
Neural/Deep



Local



Probabilistic/Bayesian

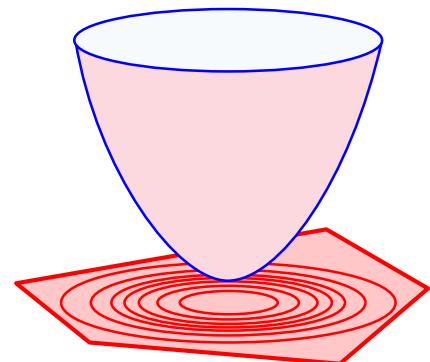


# ML can store info in lots of innovative ways

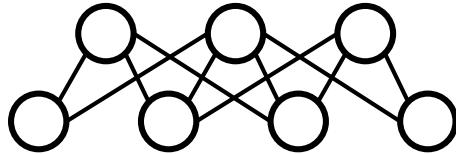
38

## ML Models and Algorithms

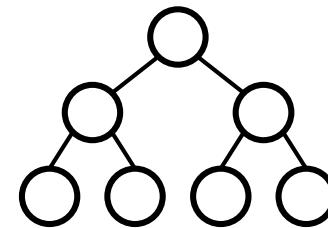
Linear/Opt



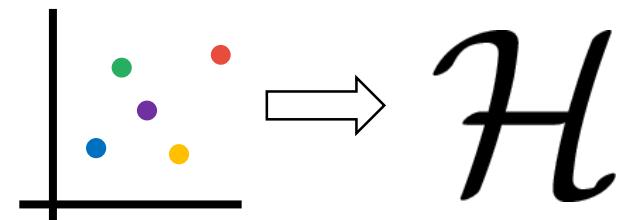
Neural/Deep



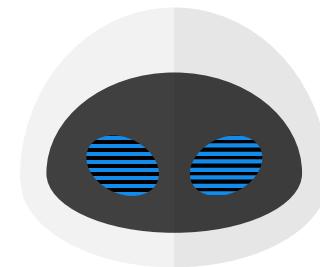
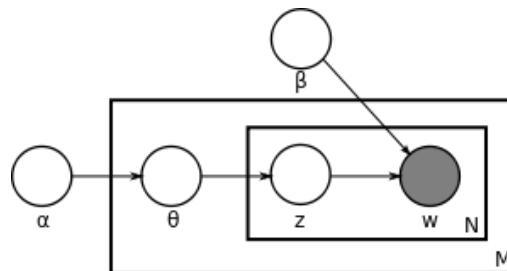
Local



Kernel

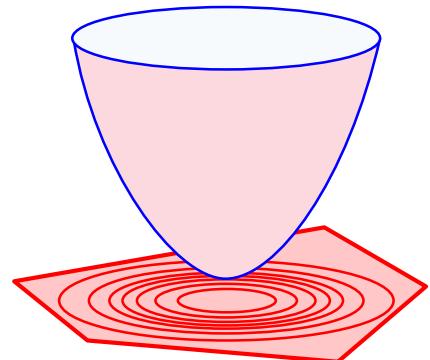


Probabilistic/Bayesian

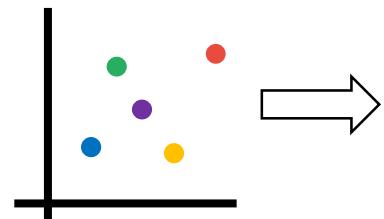


## ML Models and Algorithms

Linear/Opt



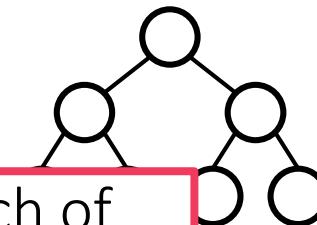
Kernel



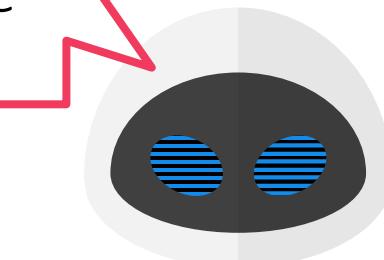
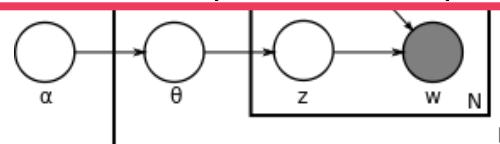
Neural/Deep



Local



We will learn how to use each of these techniques in the course, but a bit briefly. As before, there are entire courses devoted to each technique e.g. CS772 (Prob ML), CS774 (Opt)

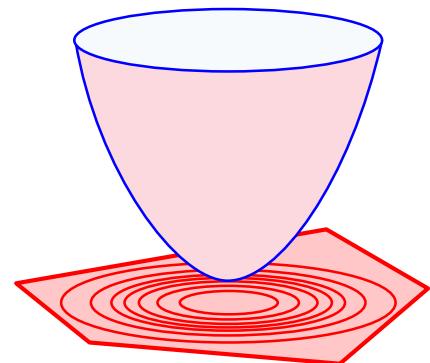


# ML can store info in lots of innovative ways

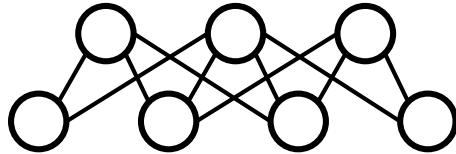
38

## ML Models and Algorithms

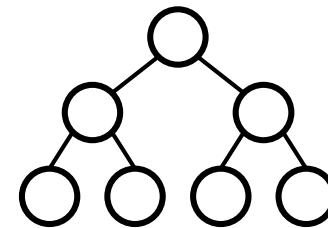
Linear/Opt



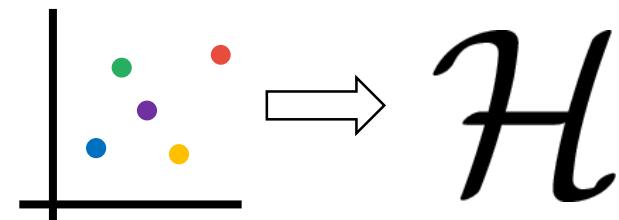
Neural/Deep



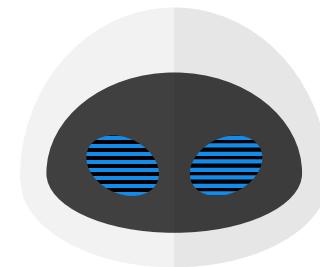
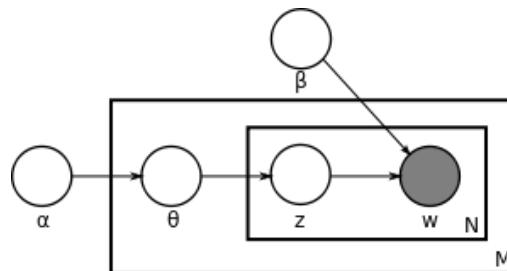
Local



Kernel



Probabilistic/Bayesian



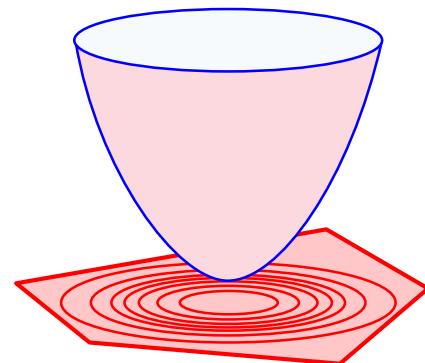
# ML can store info in lots of innovative ways

38

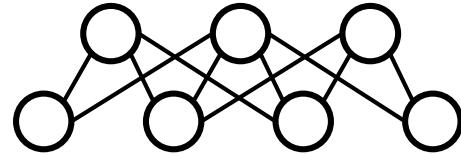


## ML Models and Algorithms

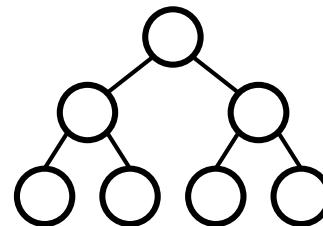
Linear/Opt



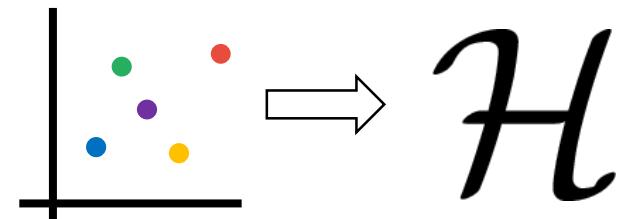
Neural/Deep



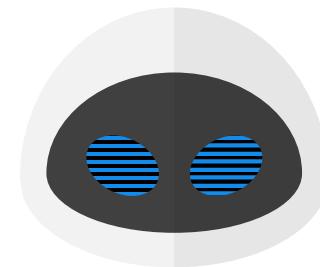
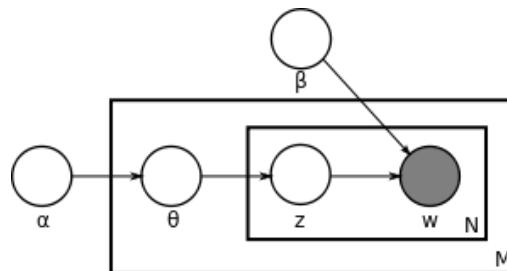
Local



Kernel

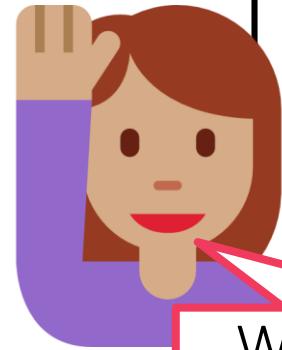


Probabilistic/Bayesian



# ML can store info in lots of innovative ways

38

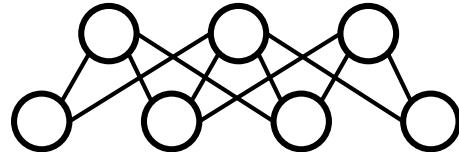


## ML Models and Algorithms

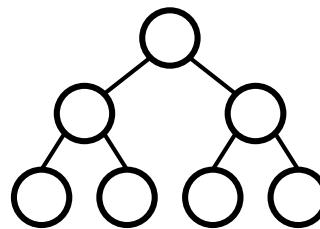
### Linear/Opt

We can mix-n-match these methods too e.g. Bayesian Deep Learning or Kernel Nearest Neighbours (Local)

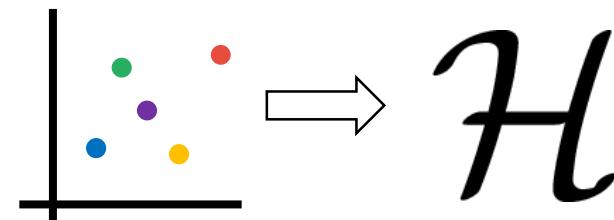
### Neural/Deep



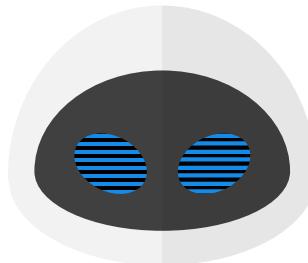
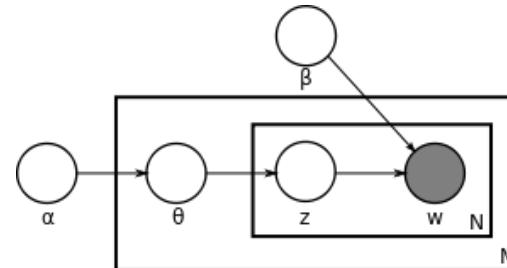
### Local



### Kernel

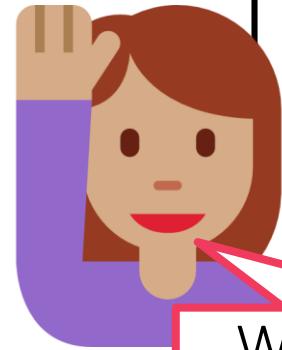


### Probabilistic/Bayesian



# ML can store info in lots of innovative ways

38

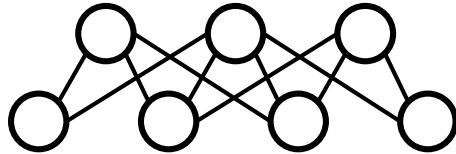


## ML Models and Algorithms

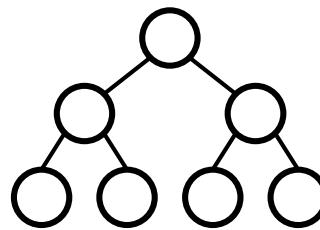
### Linear/Opt

We can mix-n-match these methods too e.g. Bayesian Deep Learning or Kernel Nearest Neighbours (Local)

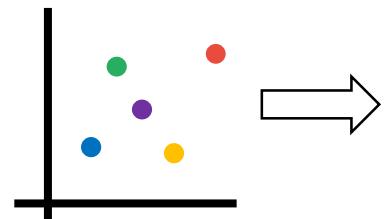
### Neural/Deep



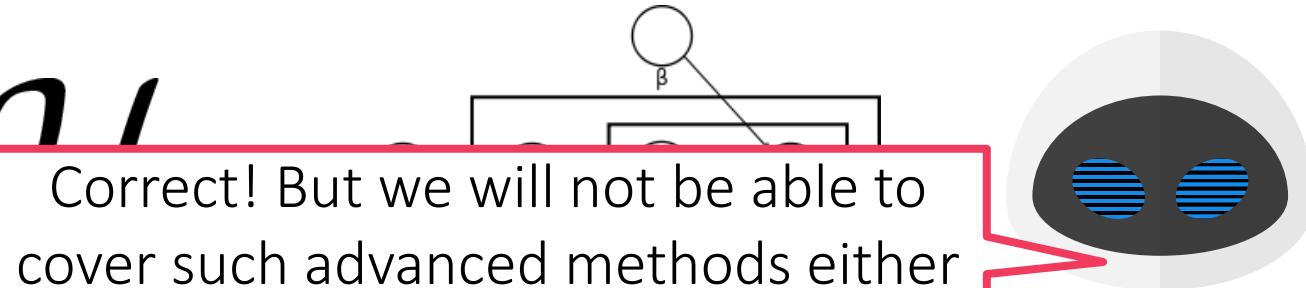
### Local



### Kernel



### Probabilistic/Bayesian



Correct! But we will not be able to cover such advanced methods either

# Fantastic Features

- ... and how to find them
- What are vectors
- How are vectors used in ML
- Useful operations on vectors



# What are features

50



CS771: Intro to ML

# What are features

Features are a way for us to give input to ML algorithms



# What are features

Features are a way for us to give input to ML algorithms



# What are features

Features are a way for us to give input to ML algorithms

Since I am basically a computer program, I need you to convert your data into a nice set of numbers

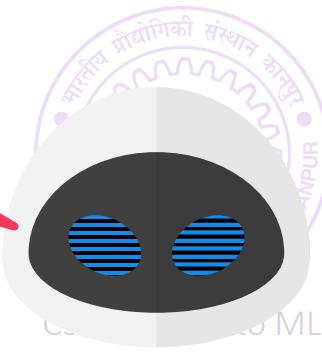


# What are features

Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



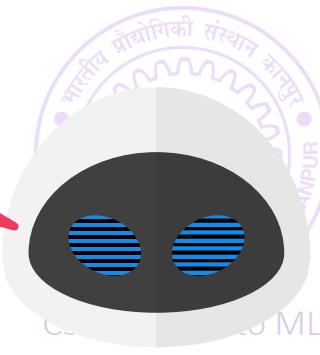
# What are features

Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Features are a way for us to give input to ML algorithms

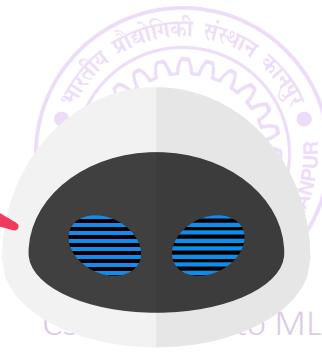
Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector



Do you want to go for dinner?

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector

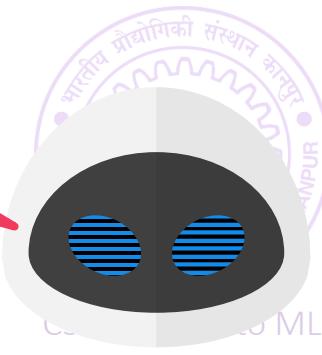


Do you want to go for dinner?



Do you want to win a million dollars?

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector



Do you want to go for dinner?



Do you want to win a million dollars?



I have a million things to do today!

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector

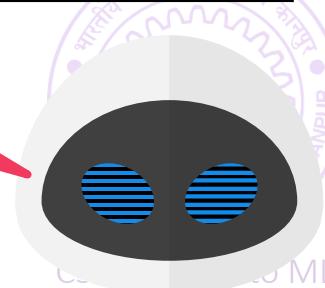
 Do you want to go for dinner?

 Do you want to win a million dollars?

 I have a million things to do today!

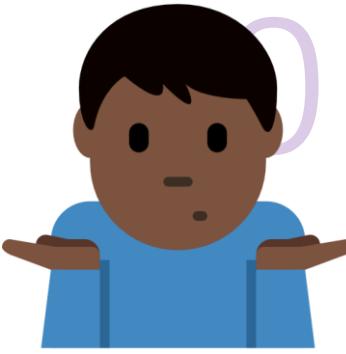
Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Features are a way for us to give input to ML algorithms



Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector

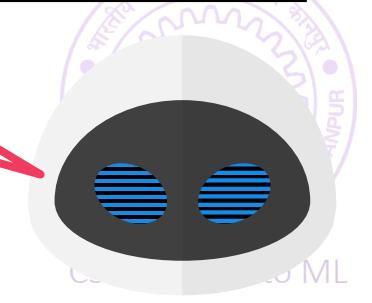
 Do you want to go for dinner?

 Do you want to win a million dollars?

 I have a million things to do today!

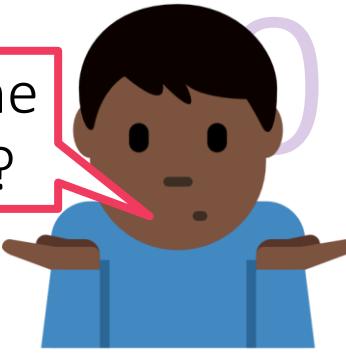
Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Why did we not keep the word “to” as a feature?



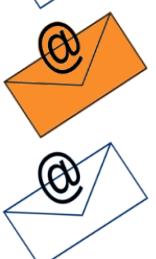
Features are a way for us to give input to ML algorithms

Most ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector



Do you want to go for dinner?



Do you want to win a million dollars?



I have a million things to do today!

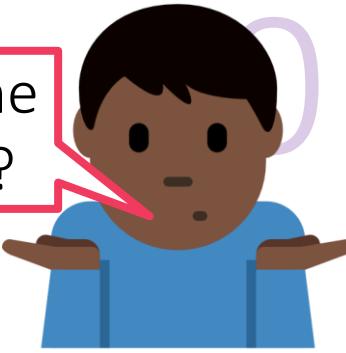
Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features

Why did we not keep the word “to” as a feature?



Features are a way for us to give input to ML algorithms



ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector

Do you want to go for dinner?



Do you want to win a million dollars?



I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features



Feature

We could have – but it does not carry much information about spam/non-spam since it is such a common word!

ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) as well as every new email (test data) must be converted into a vector



Do you want to go for dinner?



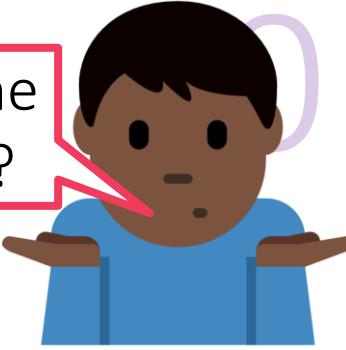
Do you want to win a million dollars?



I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Why did we not keep the word “to” as a feature?



Since I am basically a computer program, I need you to convert your data into a nice set of numbers



COMPUTER VISION ML

# What are features



Feature

We could have – but it does not carry much information about spam/non-spam since it is such a common word!

ML algorithms use numerical vectors to represent features

For example, in spam classification, every old email (training data) and every new email (test data) must be converted into a vector.



Do you want to go for dinner?



Do you want to win a million dollars?

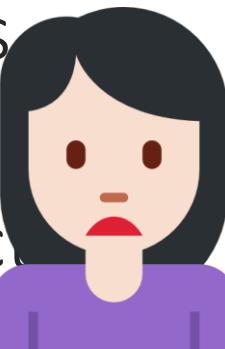
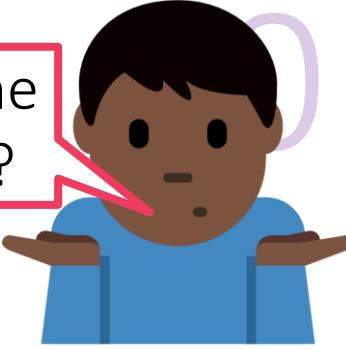


I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers

Why did we not keep the word “to” as a feature?



# What are features

Feature

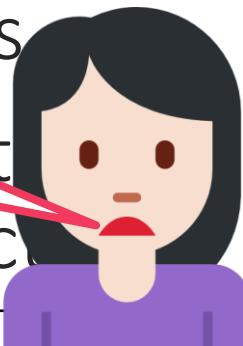
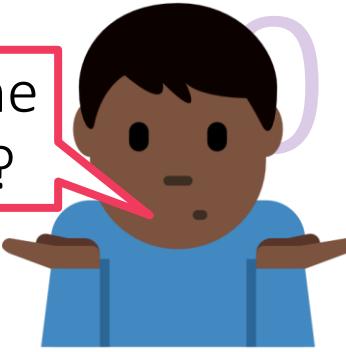
We could have – but it does not carry much information about spam/non-spam since it is such a common word!



ML algorithms use numerical vectors to represent features  
example, in spam classification

every new email (test data) must be converted into a vector

Why did we not keep the word “to” as a feature?



@ Do you want to go for dinner?



@ Do you want to win a million dollars?



@ I have a million things to do today!



Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers



# What are features



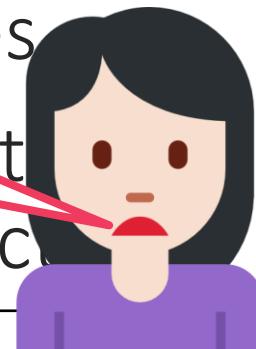
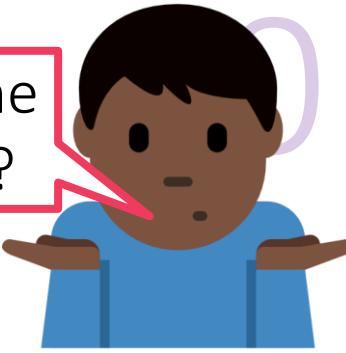
Feature

We could have – but it does not carry much information about spam/non-spam since it is such a common word!

ML algorithms use numerical vectors to represent features  
example, in spam classification

every new email (test data) must be converted into a vector

Why did we not keep the word “to” as a feature?



@ Do you want to go for dinner?



@ Do you want to win a million dollars?



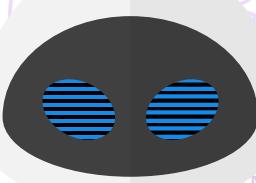
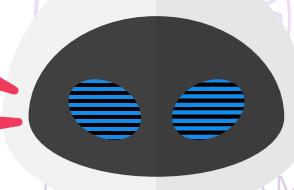
@ I have a million things to do today!



Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

Since I am basically a computer program, I need you to convert your data into a nice set of numbers

Good catch – this may not be the best feature representation!



# What are features

67



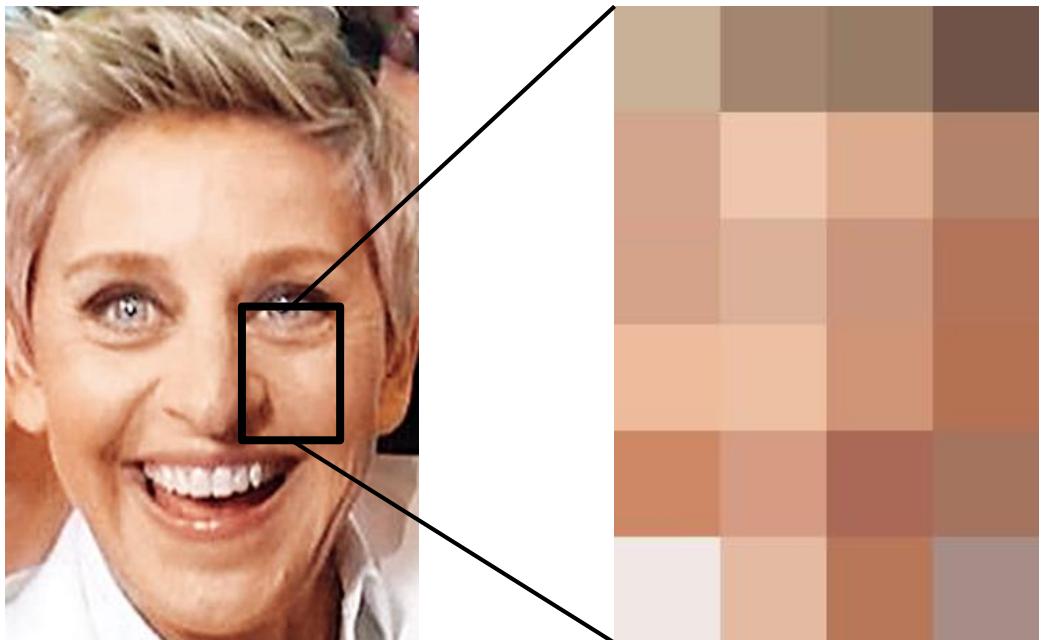
CS771: Intro to ML

# What are features

67

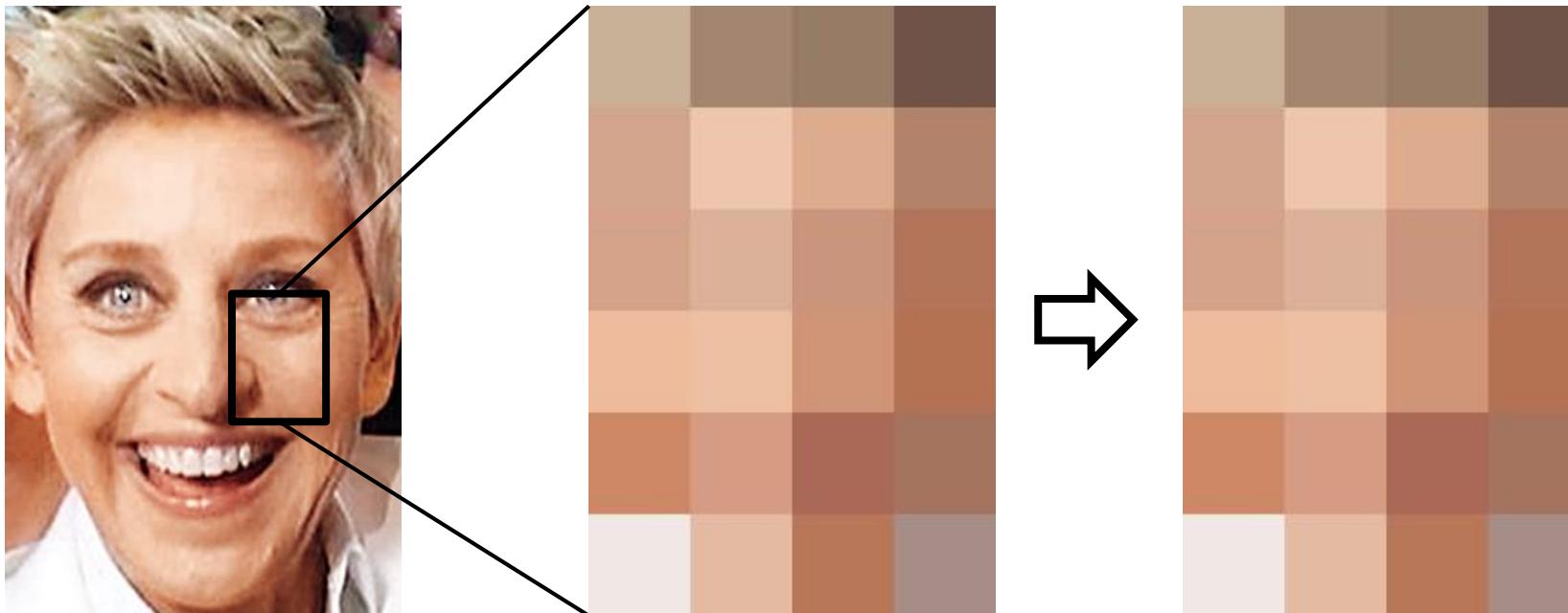


# What are features



May represent images  
as a vector/matrix of  
pixel RGB values

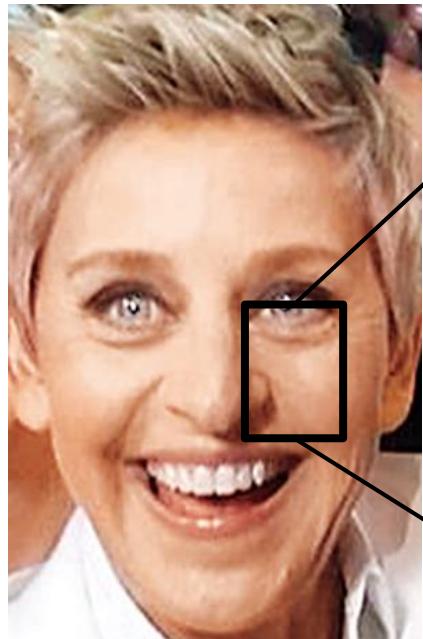
# What are features



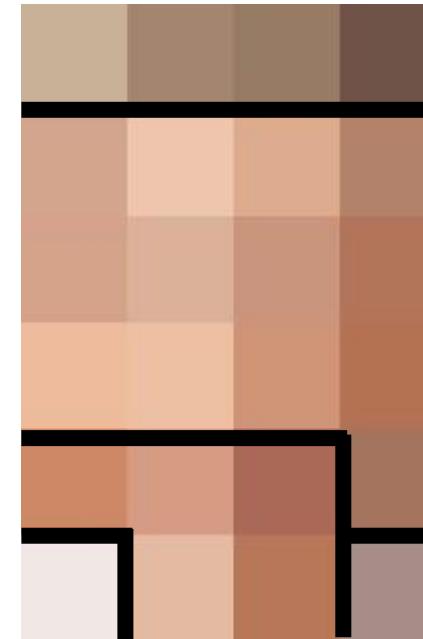
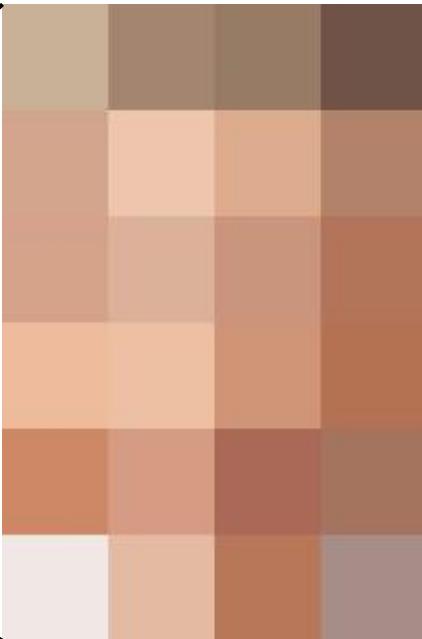
May represent images  
as a vector/matrix of  
pixel RGB values



# What are features

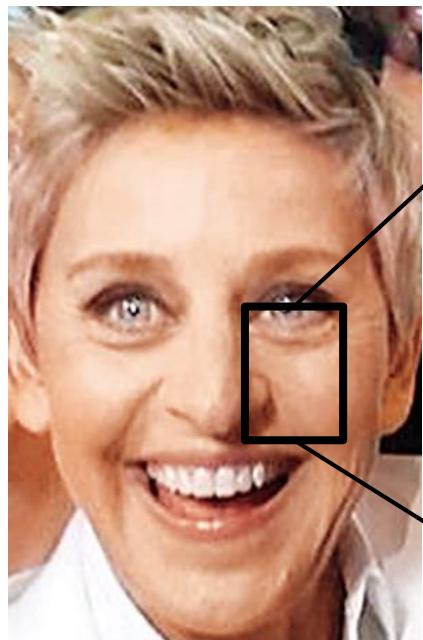


May represent images  
as a vector/matrix of  
pixel RGB values

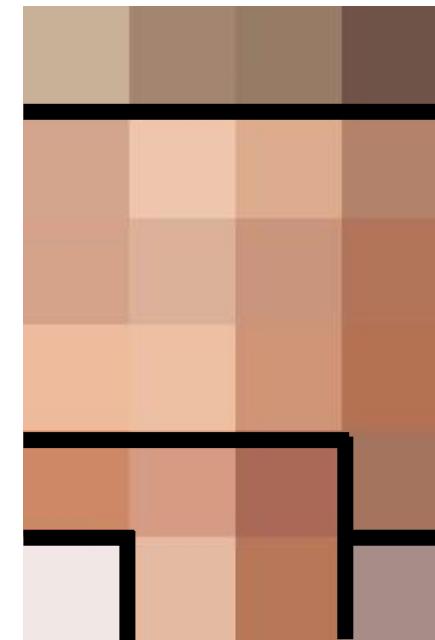
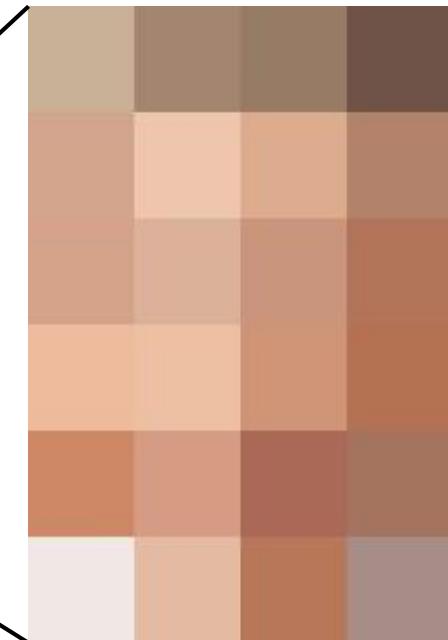


May instead encode  
images using edges  
present in them

# What are features



May represent images  
as a vector/matrix of  
pixel RGB values

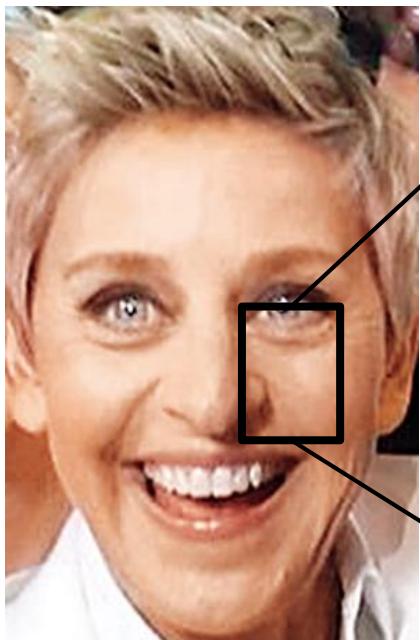


May instead encode  
images using edges  
present in them

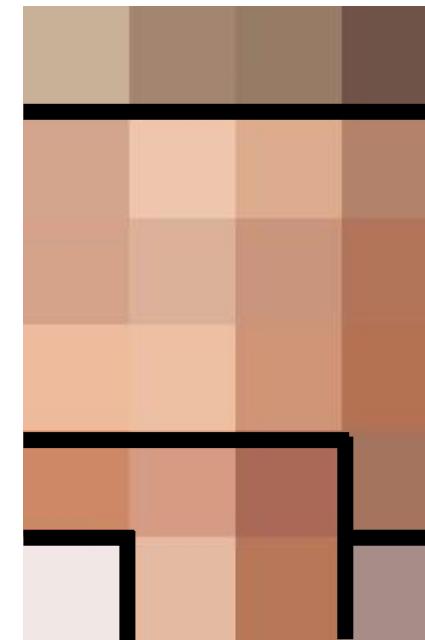
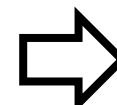
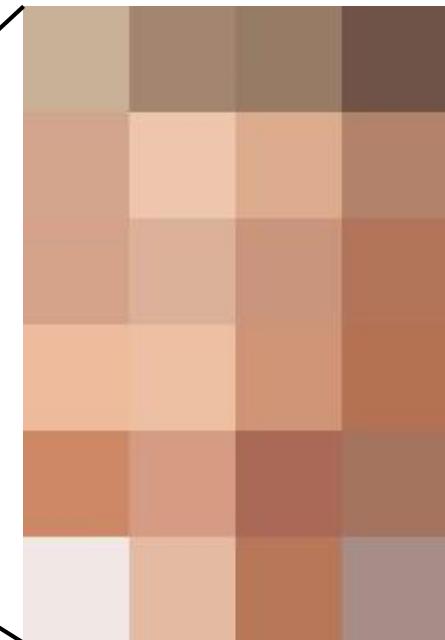


May instead encode  
images using presence  
of eyes/noses/ears

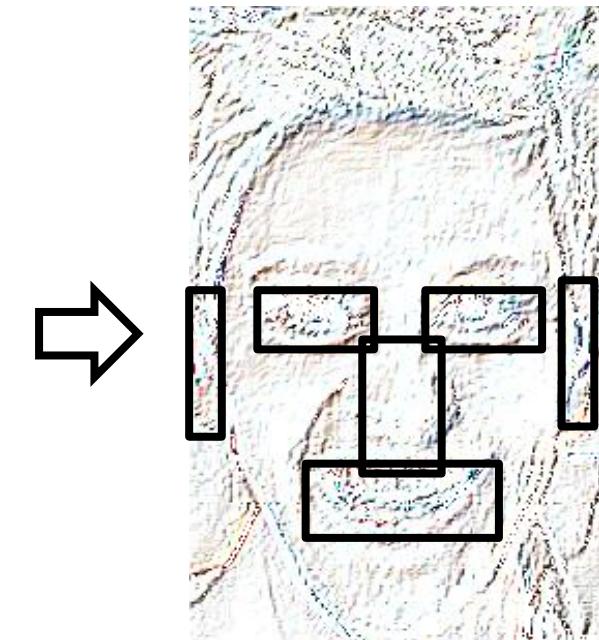
# What are features



May represent images  
as a vector/matrix of  
pixel RGB values

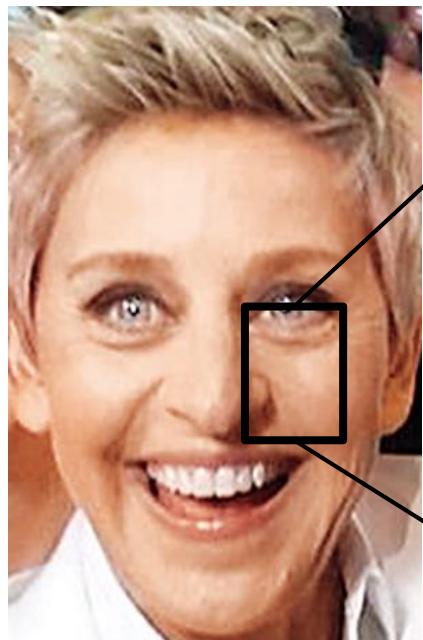


May instead encode  
images using edges  
present in them

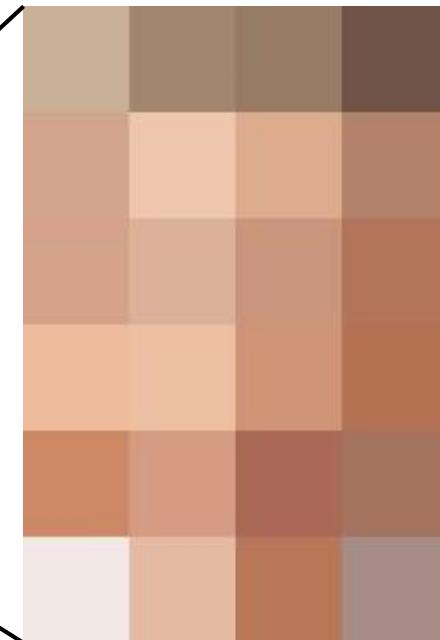


May instead encode  
images using presence  
of eyes/noses/ears

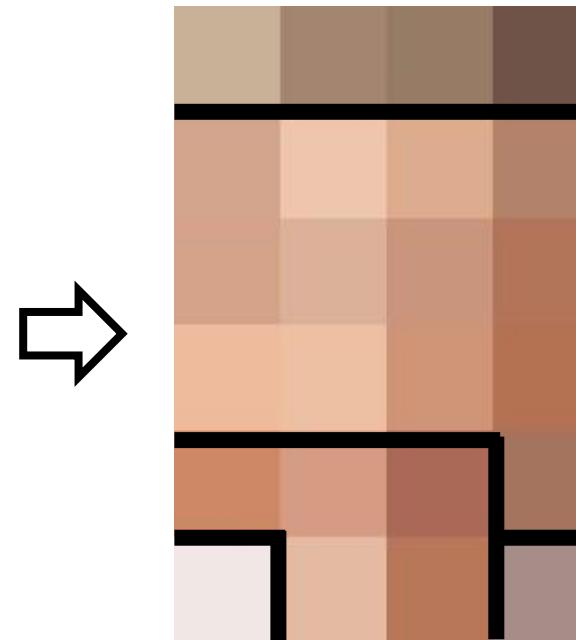
# What are features



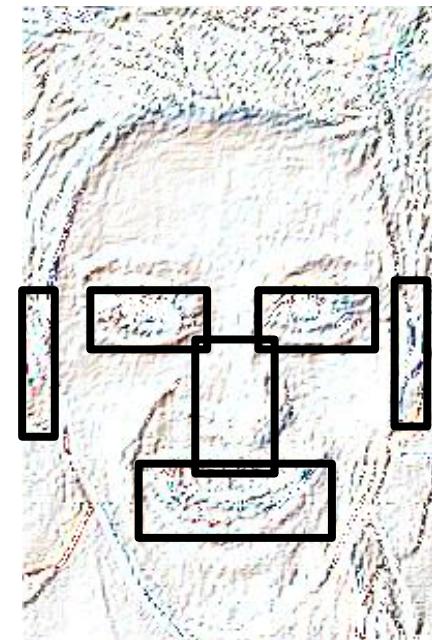
Raw/ Low-level  
features



May represent images  
as a vector/matrix of  
pixel RGB values

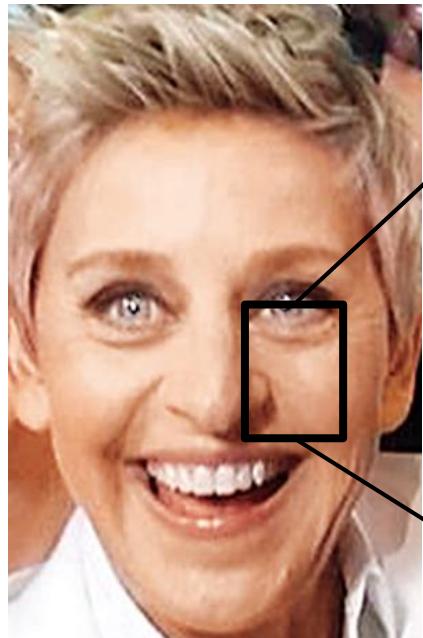


May instead encode  
images using edges  
present in them

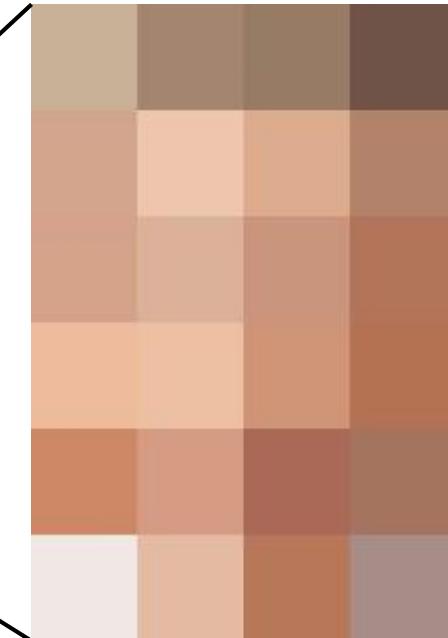


May instead encode  
images using presence  
of eyes/noses/ears

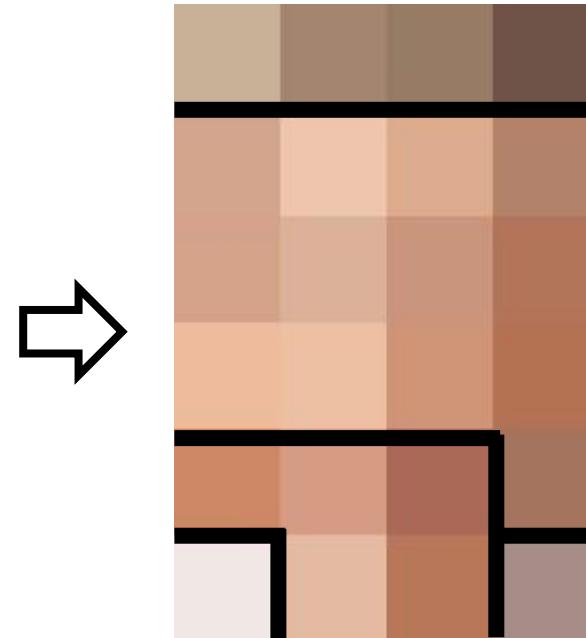
# What are features



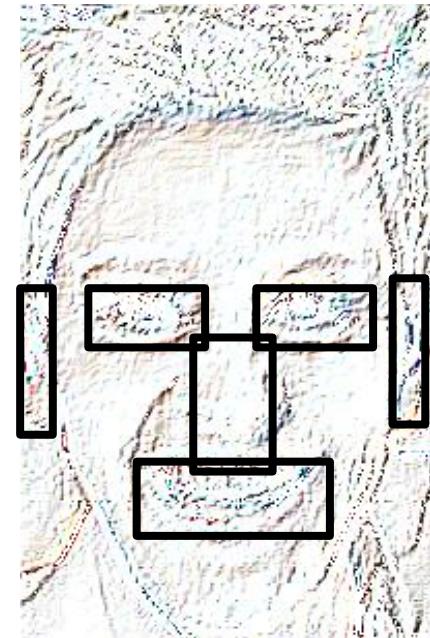
Raw/ Low-level  
features



May represent images  
as a vector/matrix of  
pixel RGB values



May instead encode  
images using edges  
present in them

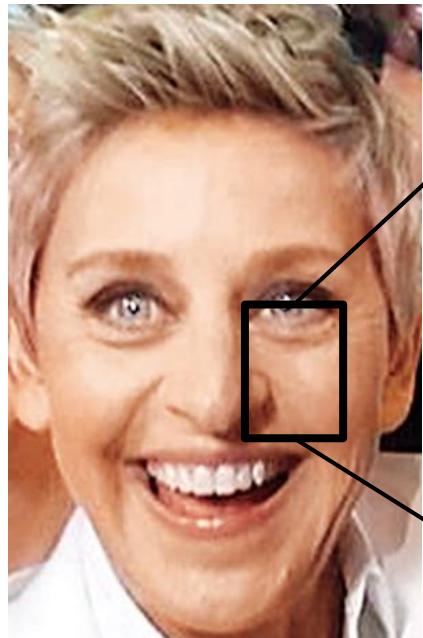


May instead encode  
images using presence  
of eyes/noses/ears

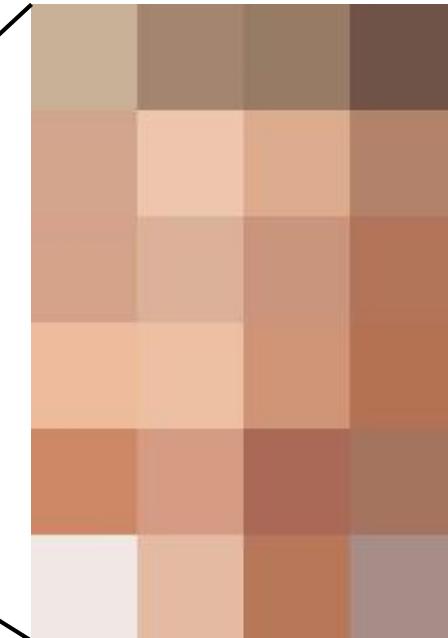


Derived/ High-  
level features

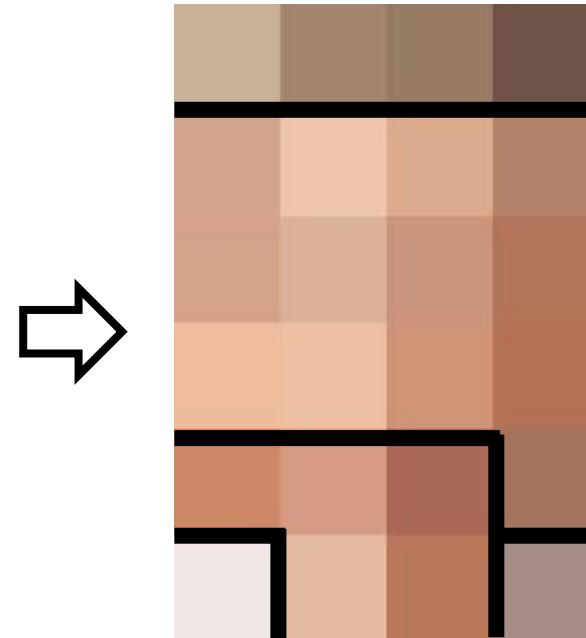
# What are features



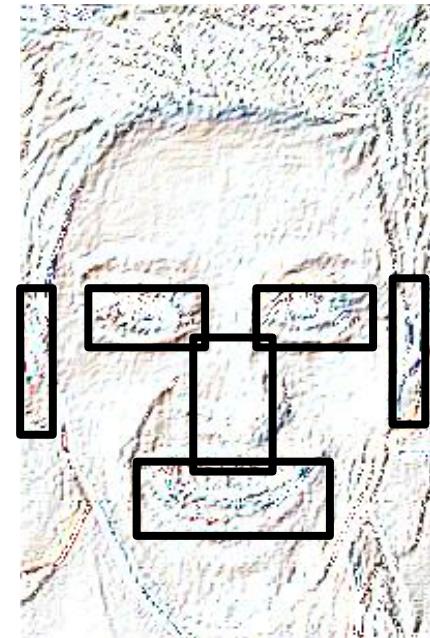
Raw/ Low-level  
features



May represent images  
as a vector/matrix of  
pixel RGB values



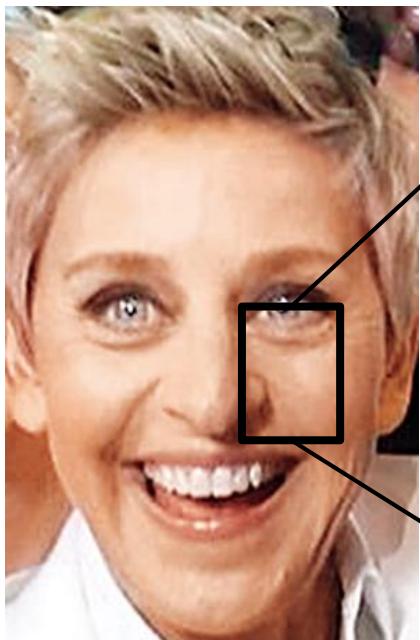
May instead encode  
images using edges  
present in them



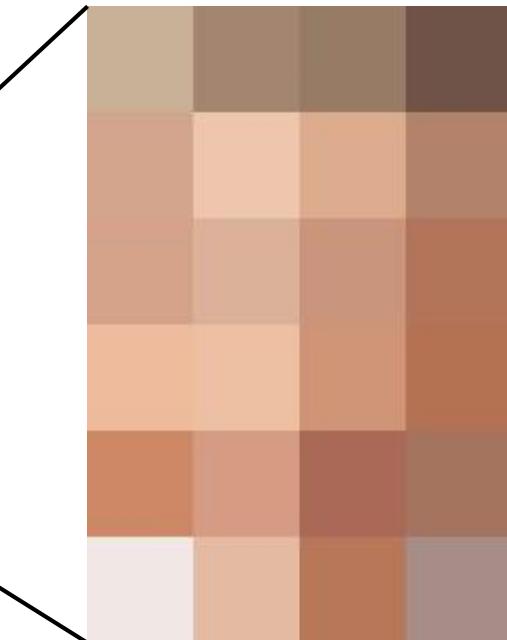
Derived/ High-  
level features



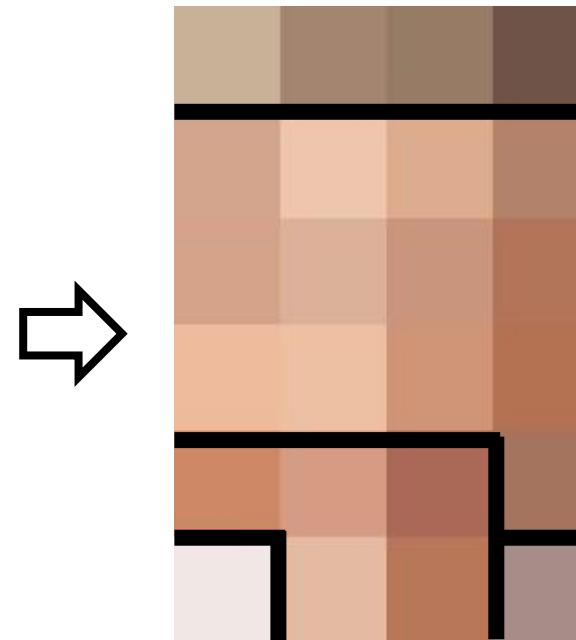
# What are features



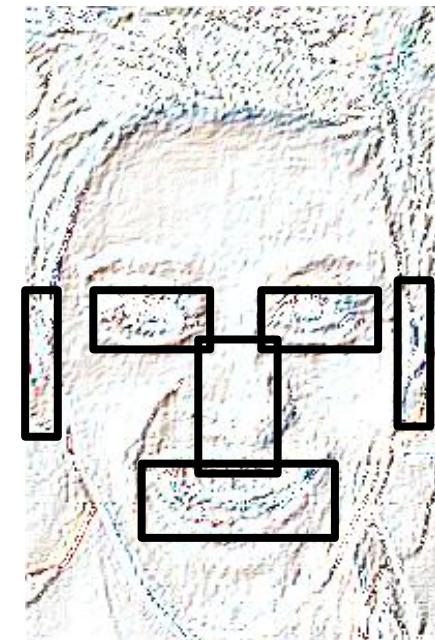
Raw/ Low-level  
features



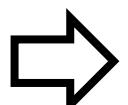
May represent images  
as a vector/matrix of  
pixel RGB values



May instead encode  
images using edges  
present in them

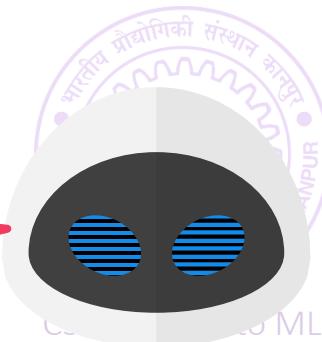


May instead encode  
images using presence  
of eyes/noses/ears

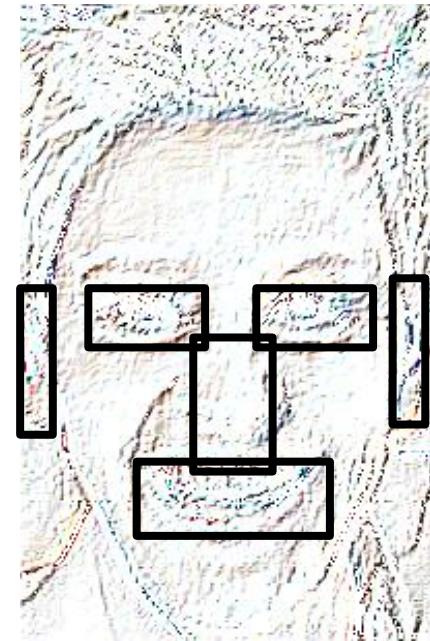
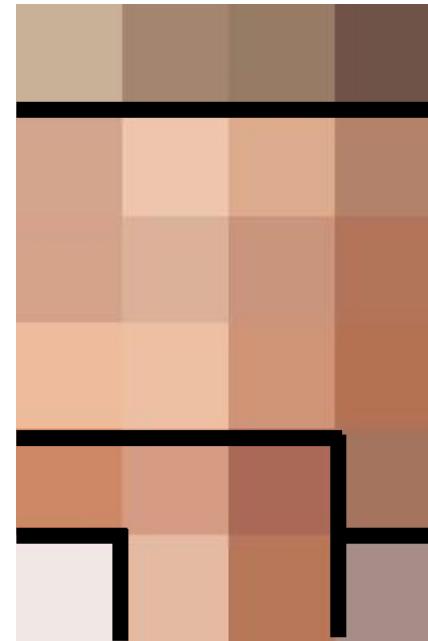
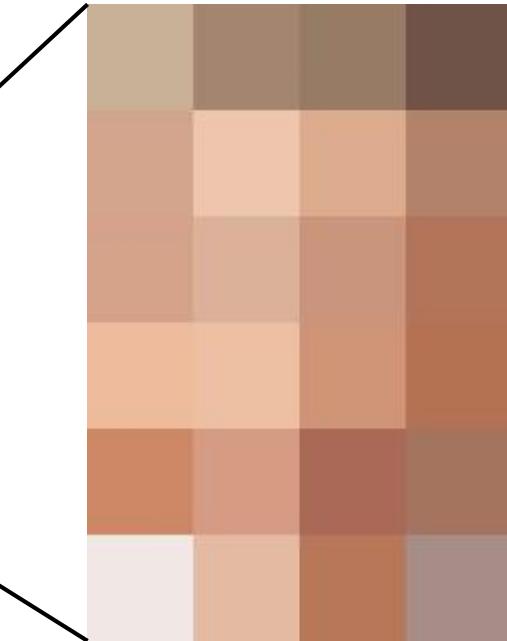
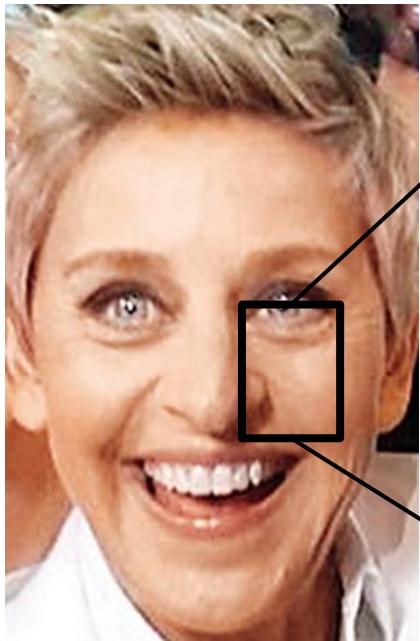


Derived/ High-  
level features

If your features are good, my job becomes twice as easy.  
If not, then doing any ML may become impossible!



# What are features



May represent images as a vector/matrix of pixel RGB values

May instead encode images using edges present in them

May instead encode images using presence of eyes/noses/ears

Raw/ Low-level features

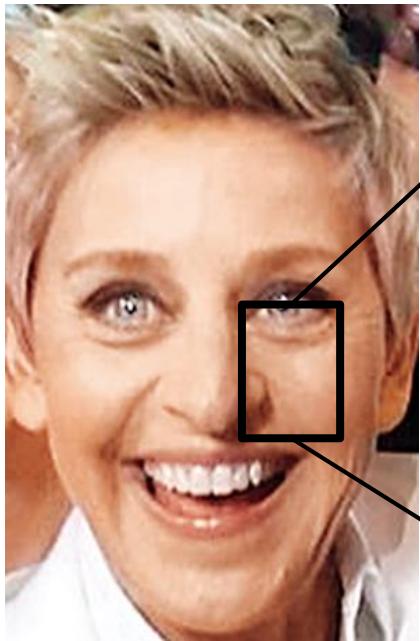


Derived/ High-level features

If your features are good, my job becomes twice as easy.  
If not, then doing any ML may become impossible!



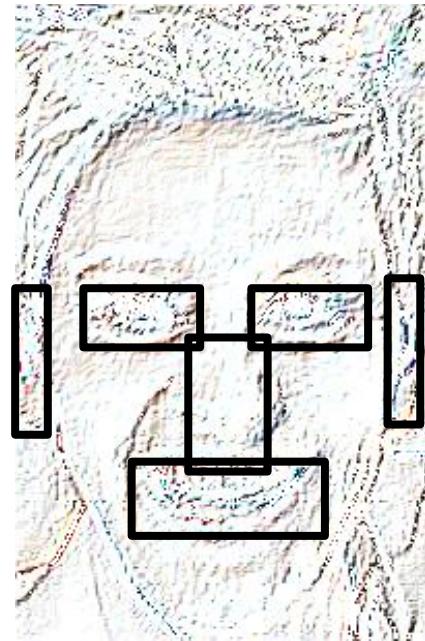
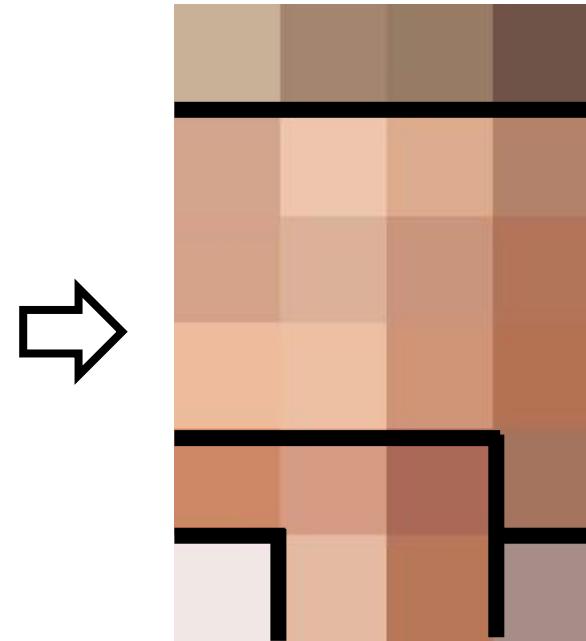
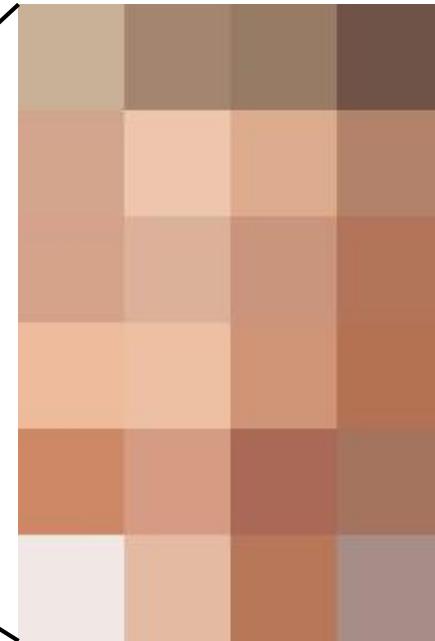
# What are features



May represent images as a vector/matrix of pixel RGB values

Makes sense. Features are also a way for us to store what we know about data. If we throw away data, naturally doing anything becomes hard!

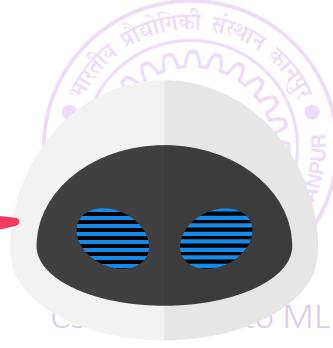
If your features are good, my job becomes twice as easy.  
If not, then doing any ML may become impossible!



May instead encode images using edges present in them

NEVER RECREATE

May instead encode images using presence of eyes/noses/ears

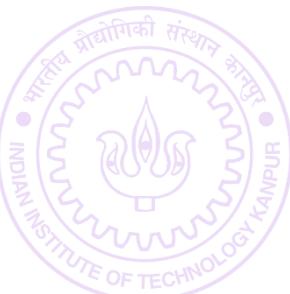


# Types of Features



# Types of Features

## Numerical Features



# Types of Features

Numerical Features

Dangal ★★★★☆

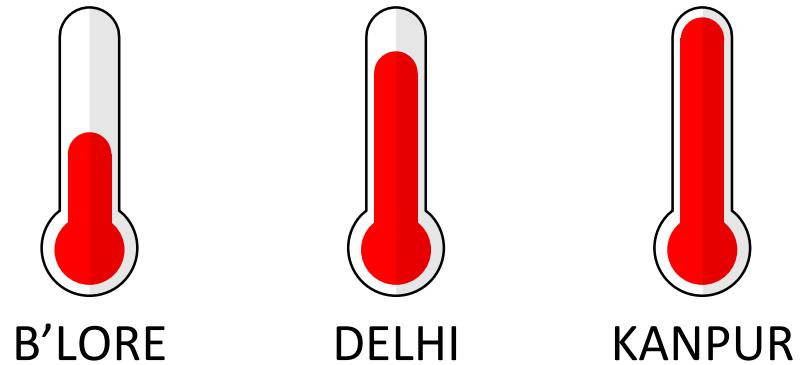
Dhoom 3 ★★★



# Types of Features

Numerical Features

Dangal      
Dhoom 3    



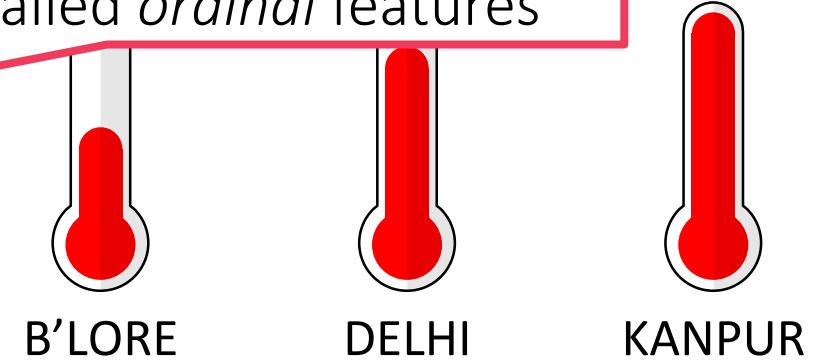
# Types of Features

## Numerical Features

Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



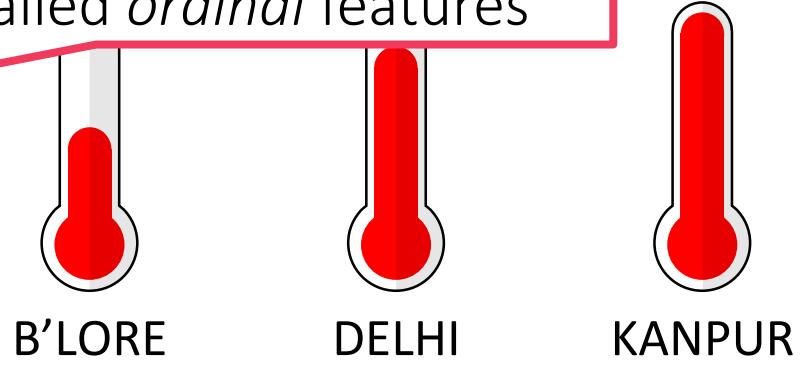
# Types of Features

## Numerical Features

Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



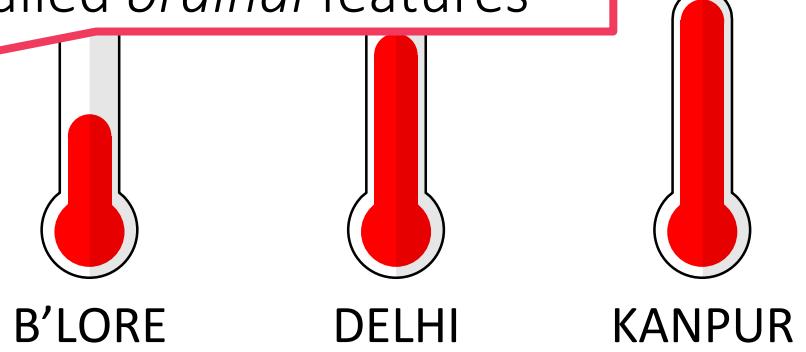
# Types of Features

## Numerical Features

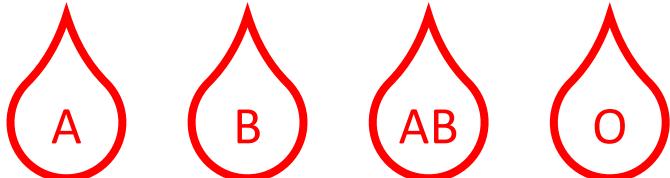
Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



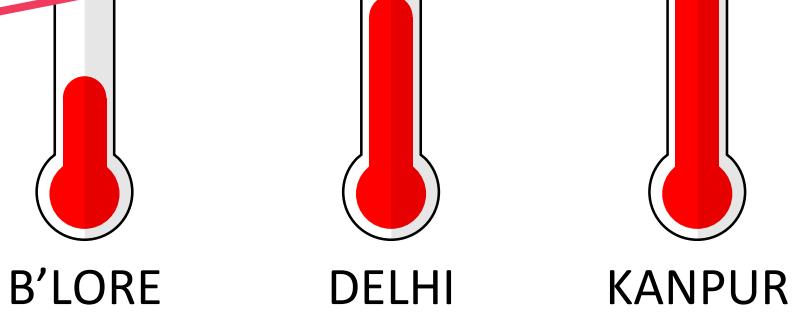
# Types of Features

## Numerical Features

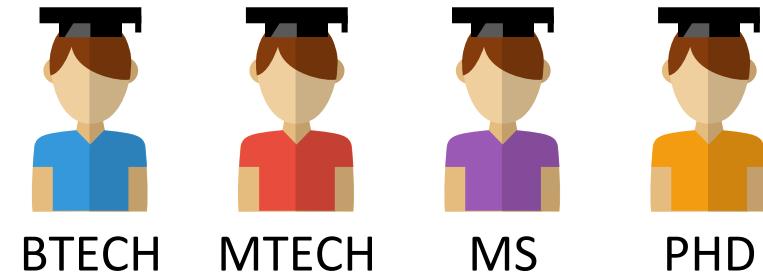
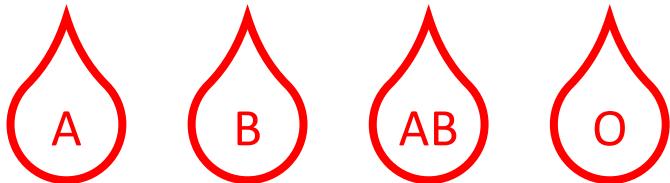
Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



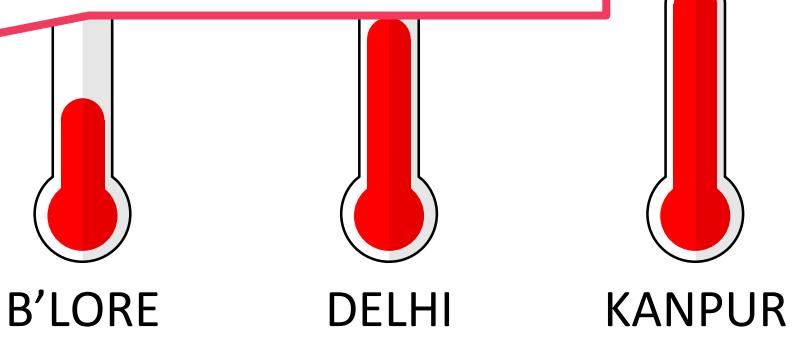
# Types of Features

## Numerical Features

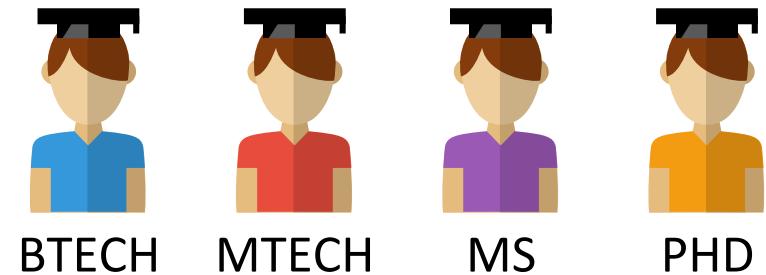
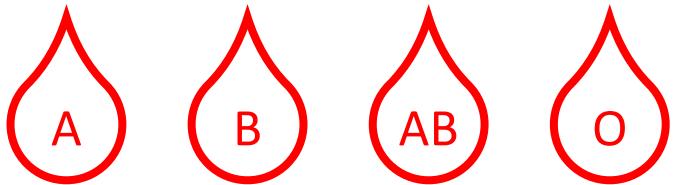
Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



## Relational Features

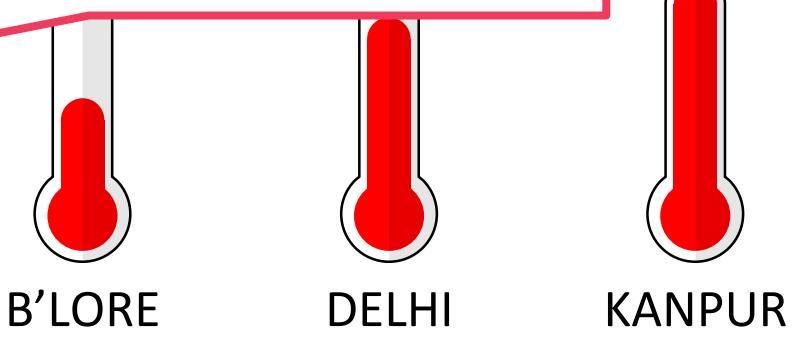
# Types of Features

## Numerical Features

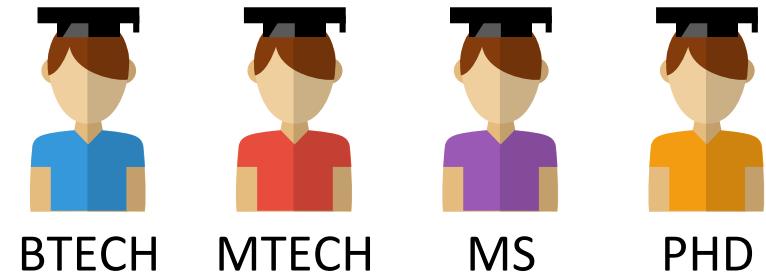
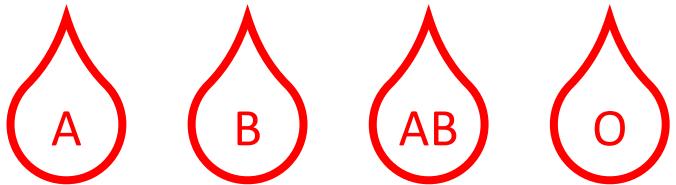
Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



## Relational Features



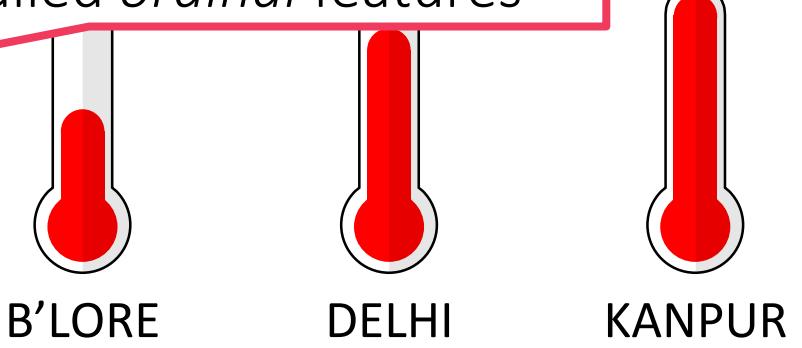
# Types of Features

## Numerical Features

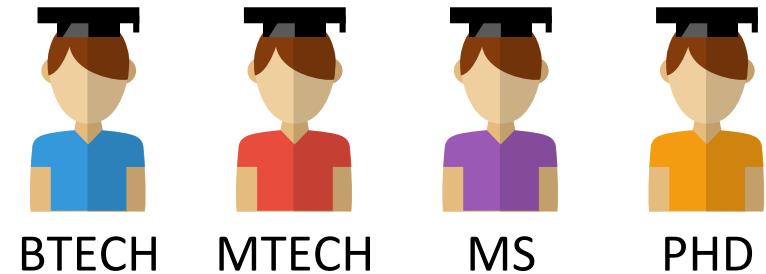
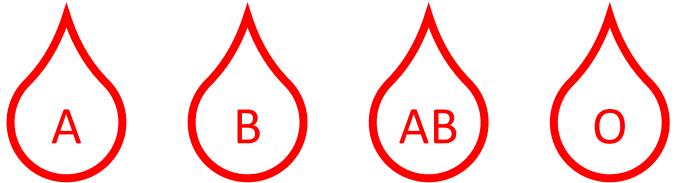
Dangal 

Dhoom 3 

Discrete numerical features  
often called *ordinal* features



## Categorical Features



## Relational Features



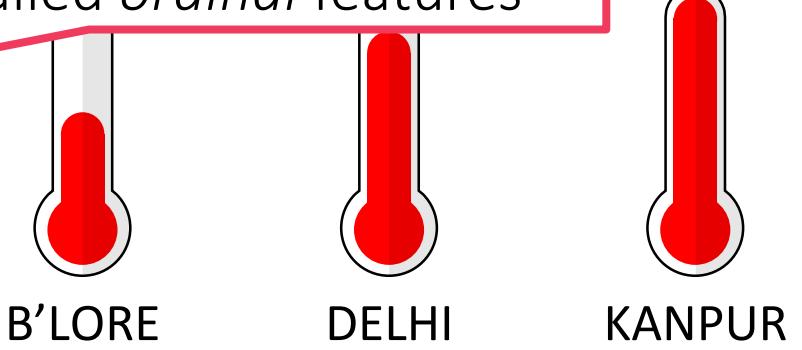
# Types of Features

## Numerical Features

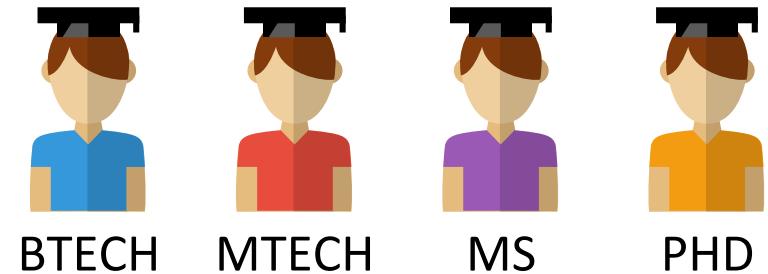
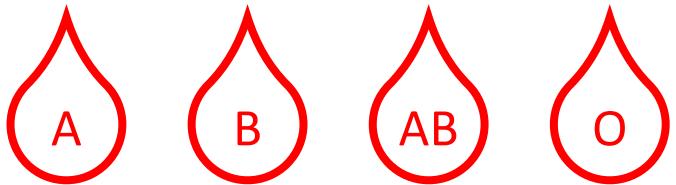
Dangal 

Dhoom 3 

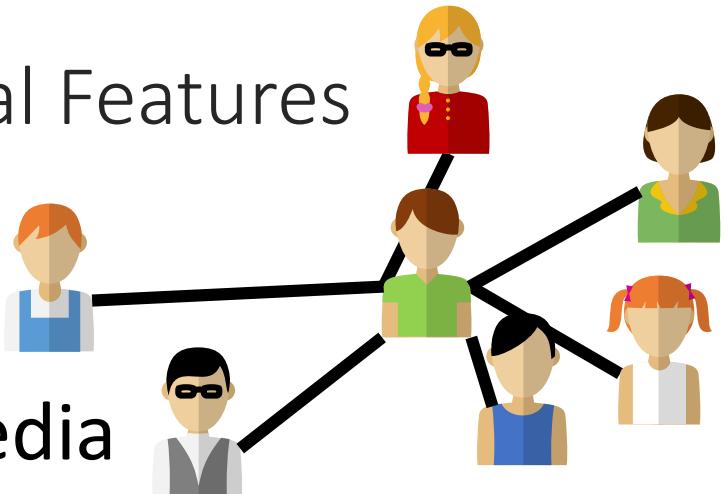
Discrete numerical features  
often called *ordinal* features



## Categorical Features



## Relational Features



## Social Media

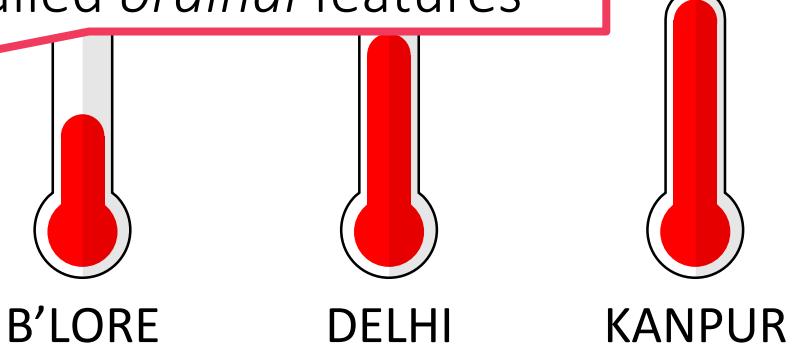
# Types of Features

## Numerical Features

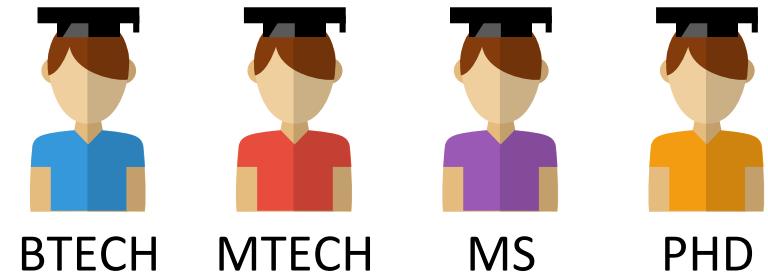
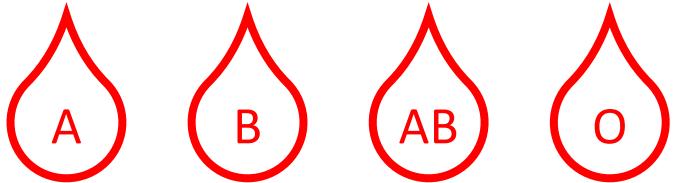
Dangal 

Dhoom 3 

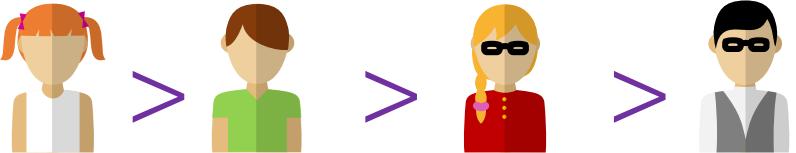
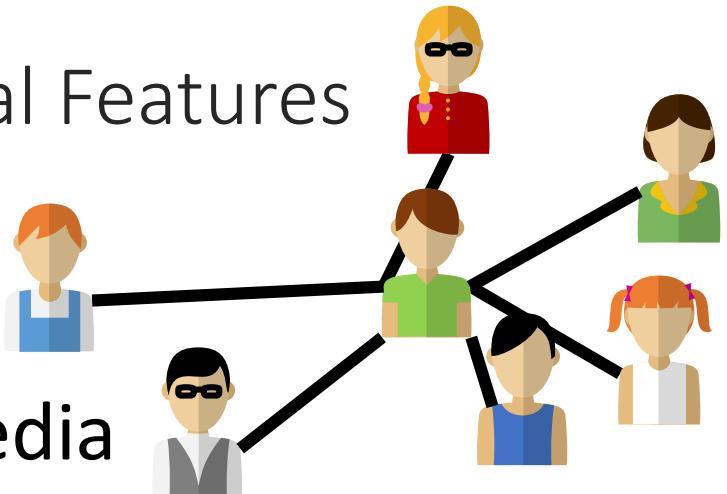
Discrete numerical features  
often called *ordinal* features



## Categorical Features



## Relational Features



## Social Media

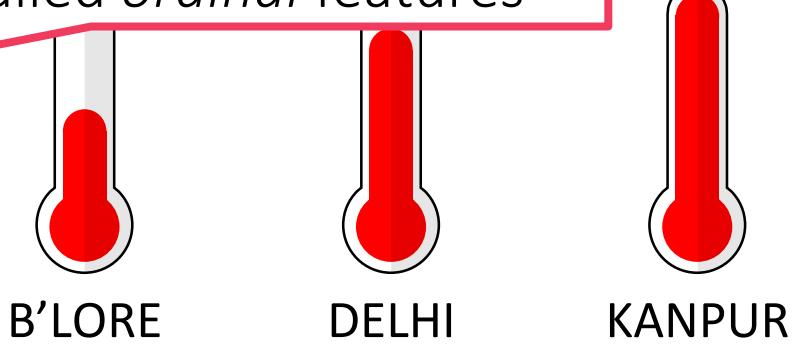
# Types of Features

## Numerical Features

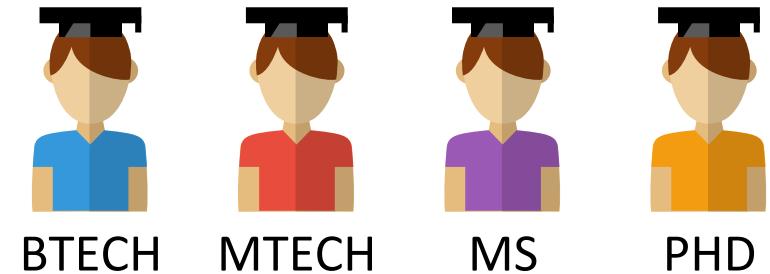
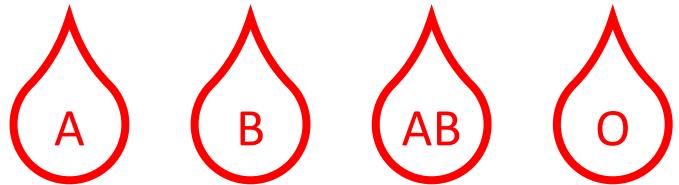
Dangal 

Dhoom 3 

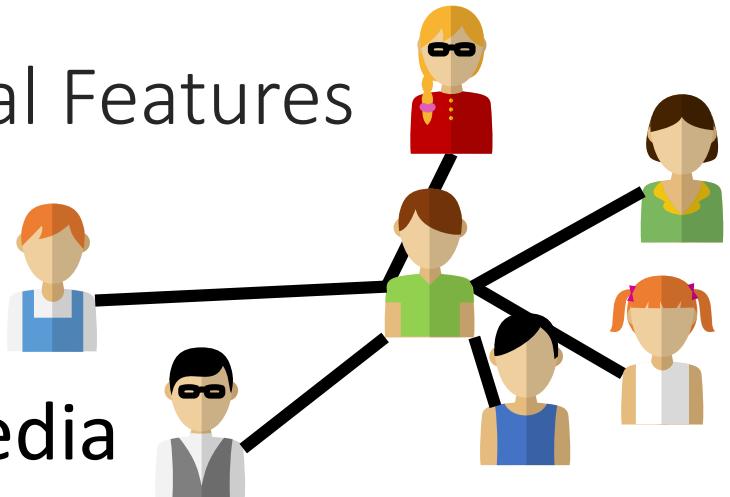
Discrete numerical features  
often called *ordinal* features



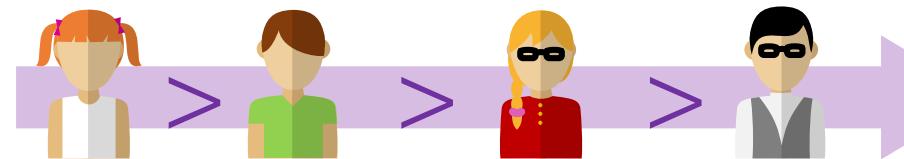
## Categorical Features



## Relational Features



## Social Media



Ranking in Class

# Derived Features

81



CS771: Intro to ML

# Derived Features

81

Bagged/binned features



CS771: Intro to ML

# Derived Features

81

## Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



CS771: Intro to ML

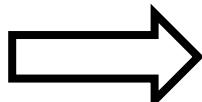
# Derived Features

81

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



A B C D E F



CS771: Intro to ML

# Derived Features

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)

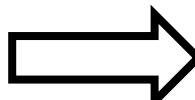


# Derived Features

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



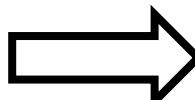
Pooled/aggregated features

# Derived Features

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)

# Derived Features

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)

# Derived Features

Bagged/binned features



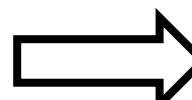
ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)



Do you want to go for dinner?

Do you want to win a million dollars?

I have a million things to do today!

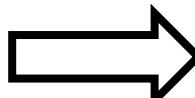
Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1

# Derived Features

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)



Do you want to go for dinner?

Do you want to win a million dollars?

I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1



# Derived Features

Bagged/binned features



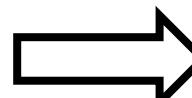
ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)

The way we represented  
emails in the spam  
problem is called the  
*bag-of-words* feature



Do you want to go for dinner?



Do you want to win a million dollars?



I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1



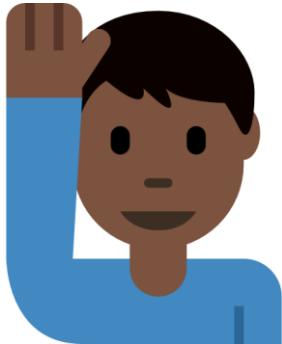
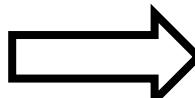
# Derived Features

81

Bagged/binned features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)

The way we represented  
emails in the spam  
problem is called the  
*bag-of-words* feature



Do you want to go for dinner?



Do you want to win a million dollars?



I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1



# Derived Features

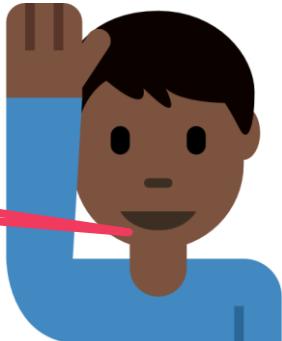
81

## Bagged/binned features



ESC101 (A), ESO207 (B), CS2  
CS340 (C), MSO201 (A), CS7

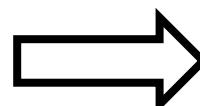
As we saw, the bag-of-words (also called BoW) is not always a very good feature (it confuses polysemous words). However, it is still extremely popular due to its simplicity



## Pooled/aggregated features



ESC101 (A), ESO207 (B), CS220 (B),  
CS340 (C), MSO201 (A), CS771 (A)



10 (max), 8.67 (avg)

The way we represented emails in the spam problem is called the *bag-of-words* feature



Do you want to go for dinner?

Do you want to win a million dollars?

I have a million things to do today!

Do	You	Want	Go	Million	Dollars	Dinner	Today
1	1	1	1	0	0	1	0
1	1	1	0	1	1	0	0
1	0	0	0	1	0	0	1



# Feature Selection??

107



CS771: Intro to ML

# Feature Selection??

107



CS771: Intro to ML

# Feature Selection??

107

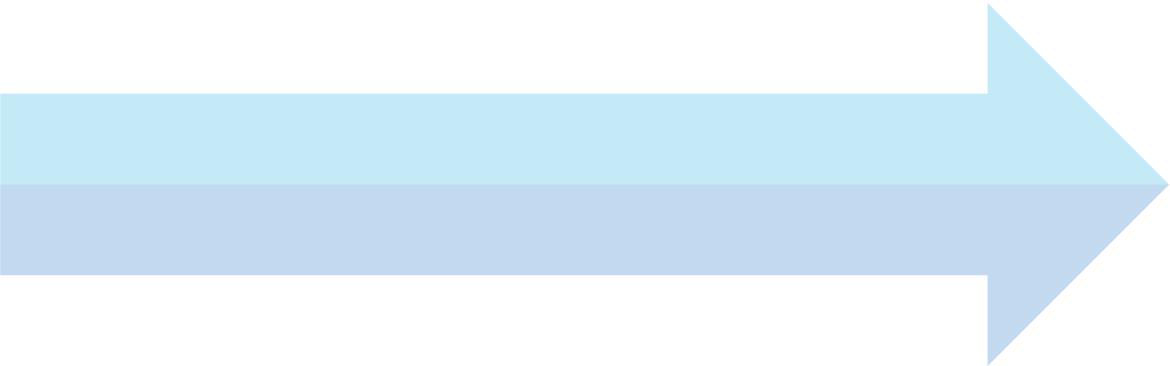


(EXPENDITURE)



# Feature Selection??

107



(EXPENDITURE)



# Feature Selection??

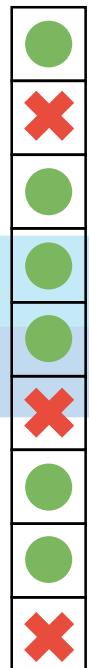


DIET (VEG/NON-VEG)  
EYE COLOR  
TOTAL INCOME  
EDUCATION LEVEL  
**FAMILY SIZE**  
HOUSE NO (ODD/EVEN)  
NO OF CHILDREN  
RENTED/SELF OWNED  
SURNAME LENGTH



(EXPENDITURE)

# Feature Selection??

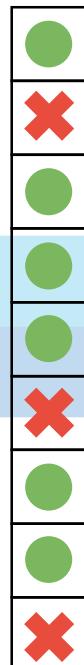


- DIET (VEG/NON-VEG)
- ✗ EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- ✗ HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- ✗ SURNAME LENGTH



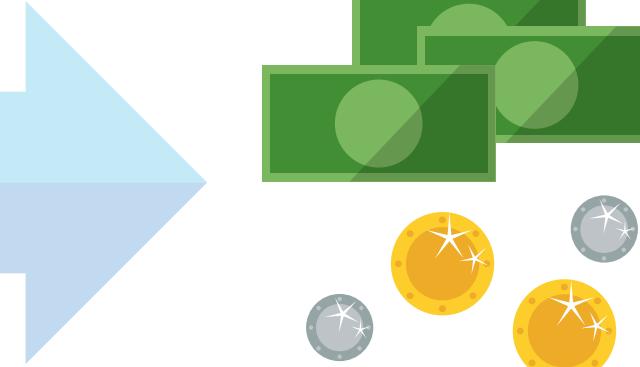
(EXPENDITURE)

# Feature Selection??



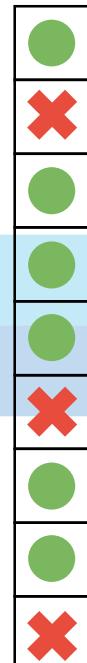
- DIET (VEG/NON-VEG)
- EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- SURNAME LENGTH

Useful for predicting expenditure



(EXPENDITURE)

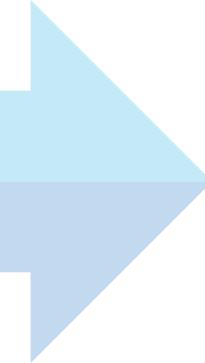
# Feature Selection??



- DIET (VEG/NON-VEG)
- EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- SURNAME LENGTH

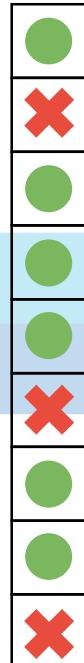
Useful for predicting expenditure

Not useful for predicting expenditure



(EXPENDITURE)

# Feature Selection??



Useful for predicting expenditure

Not useful for predicting expenditure

DIET (VEG/NON-VEG)

EYE COLOR

TOTAL INCOME

EDUCATION LEVEL

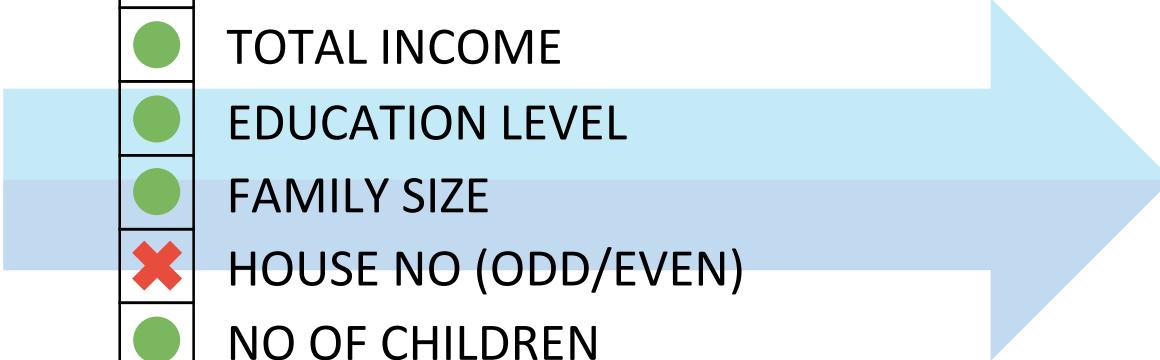
FAMILY SIZE

HOUSE NO (ODD/EVEN)

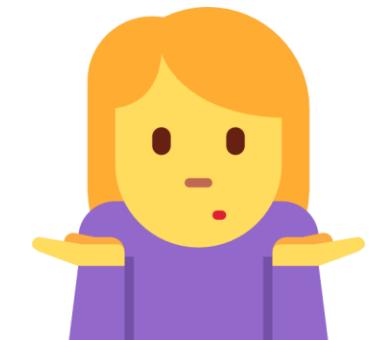
NO OF CHILDREN

RENTED/SELF OWNED

SURNAME LENGTH



(EXPENDITURE)



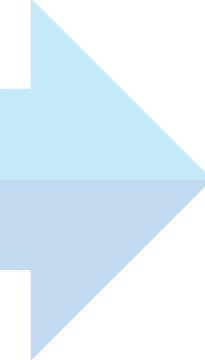
# Feature Selection??



- DIET (VEG/NON-VEG)
- ✖ EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- ✖ HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- ✖ SURNAME LENGTH

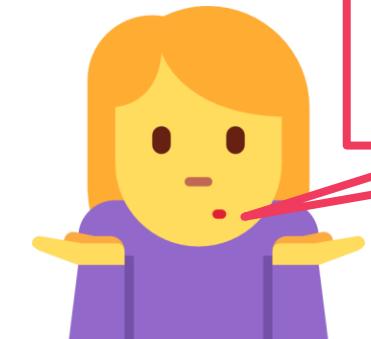
Useful for predicting expenditure

Not useful for predicting expenditure

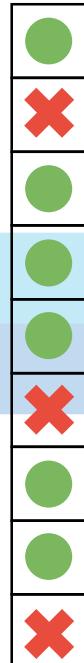


(EXPENDITURE)

Can we perform automatic  
feature selection?



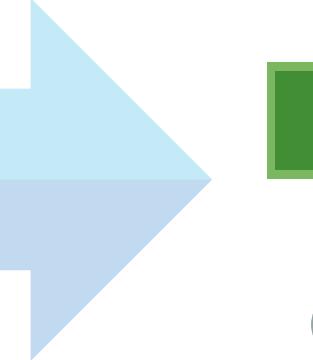
# Feature Selection??



- DIET (VEG/NON-VEG)
- EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- SURNAME LENGTH

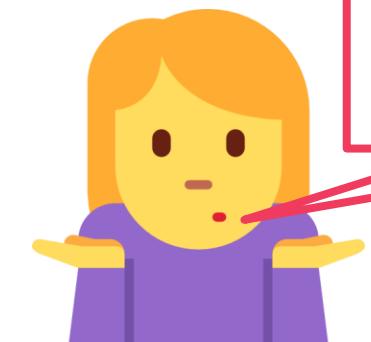
Useful for predicting expenditure

Not useful for predicting expenditure



(EXPENDITURE)

Can we perform automatic  
feature selection?



# Feature Selection??



- DIET (VEG/NON-VEG)
- ✖ EYE COLOR
- TOTAL INCOME
- EDUCATION LEVEL
- FAMILY SIZE
- ✖ HOUSE NO (ODD/EVEN)
- NO OF CHILDREN
- RENTED/SELF OWNED
- ✖ SURNAME LENGTH

Useful for predicting expenditure

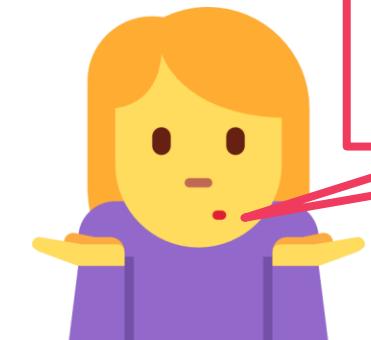
Not useful for predicting expenditure



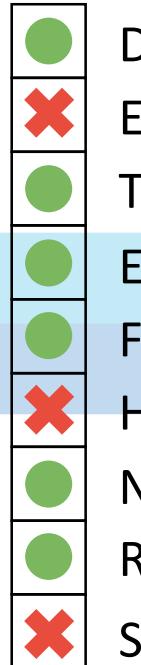
(EXPENDITURE)

Can we perform automatic feature selection?

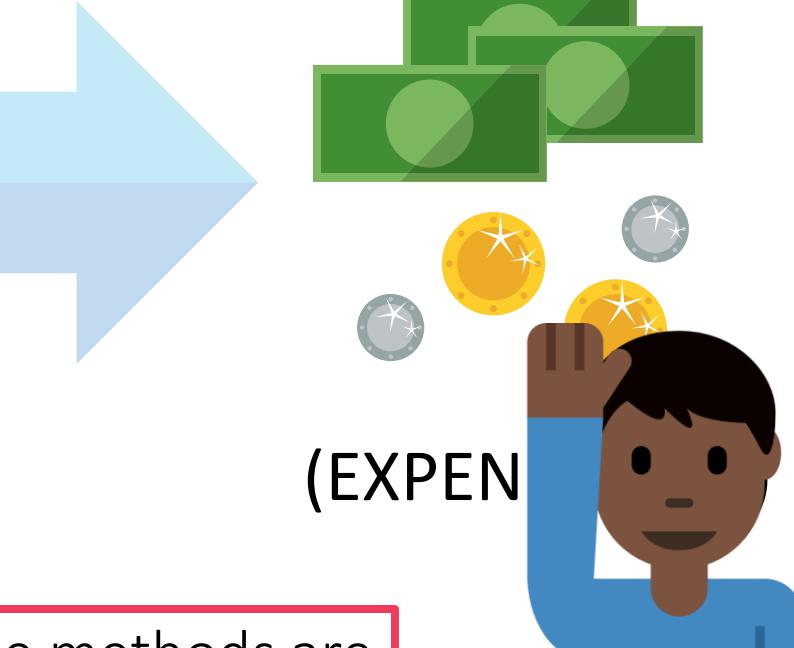
Yes indeed, but those methods are a bit advanced for now!



# Feature Selection??



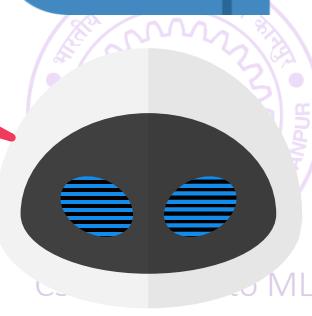
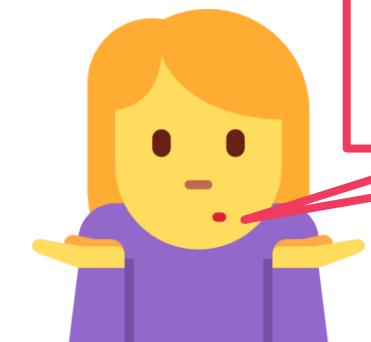
DIET (VEG/NON-VEG)  
EYE COLOR  
TOTAL INCOME  
EDUCATION LEVEL  
FAMILY SIZE  
HOUSE NO (ODD/EVEN)  
NO OF CHILDREN  
RENTED/SELF OWNED  
SURNAME LENGTH



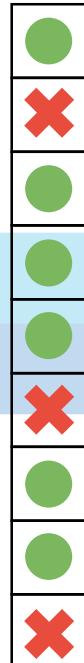
(EXPEN

Can we perform automatic feature selection?

Yes indeed, but those methods are a bit advanced for now!

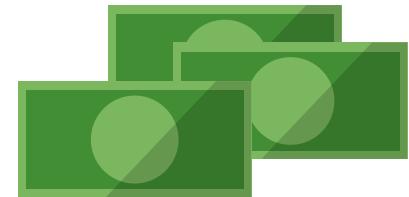
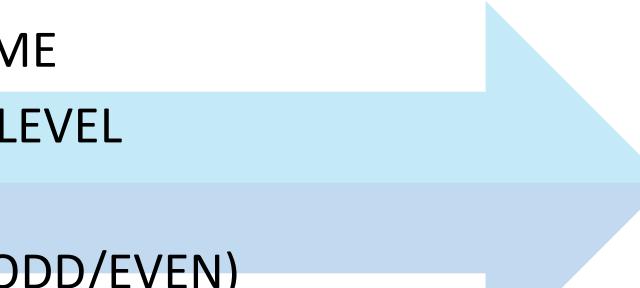


# Feature Selection??

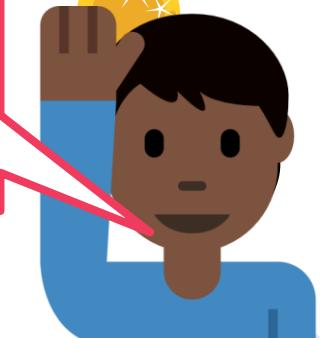


Useful for predicting expenditure

Not useful for predicting expenditure

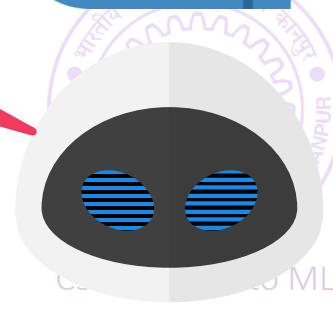
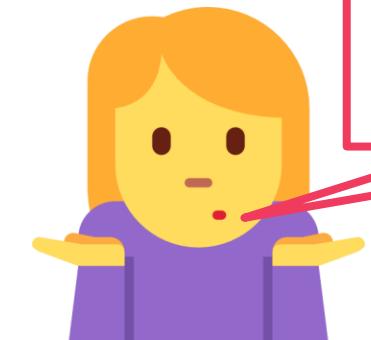


In fact, one reason for the success  
of deep learning is that it learns  
good features themselves!

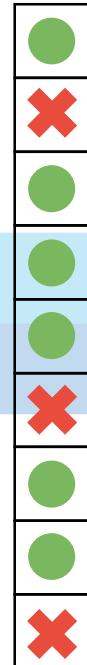


Can we perform automatic  
feature selection?

Yes indeed, but those methods are  
a bit advanced for now!

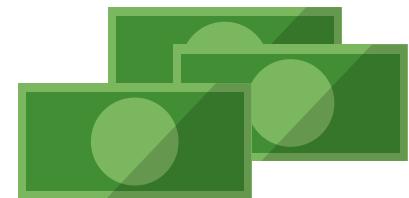


# Feature Selection??

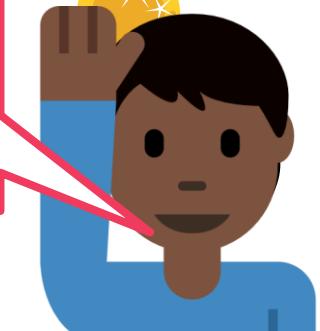


Useful for predicting expenditure

Not useful for predicting expenditure



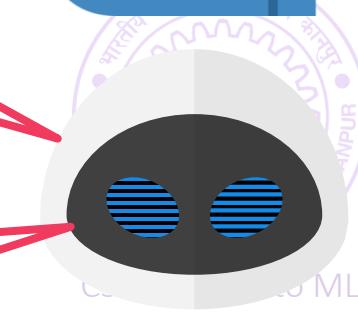
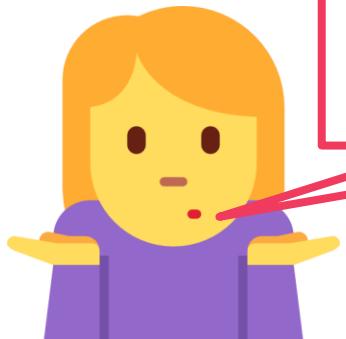
In fact, one reason for the success of deep learning is that it learns good features themselves!



Can we perform automatic feature selection?

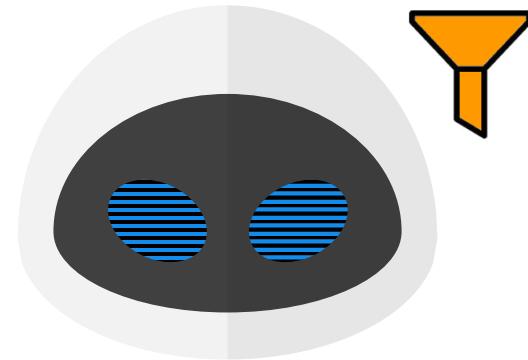
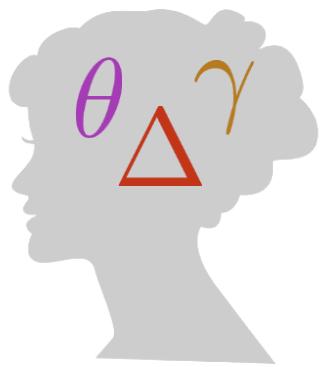
Yes indeed, but those methods are a bit advanced for now!

True, but more on deep learning later! For now, back to basics.



# A bit of caution with features

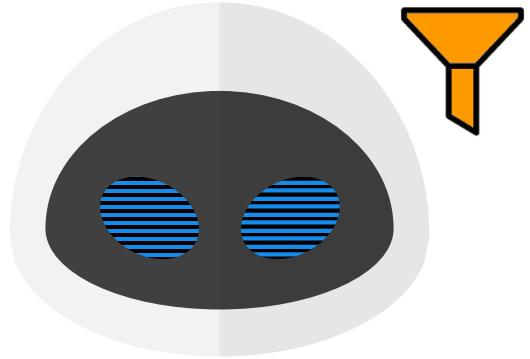
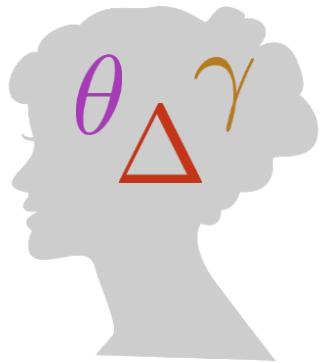
122



CS771: Intro to ML

# A bit of caution with features

122



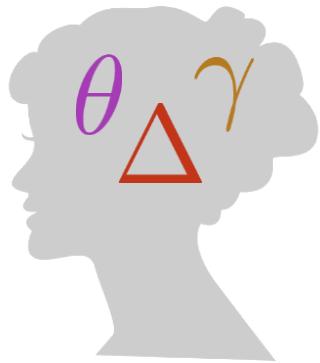
Tricks, mnemonics lessen  
cognitive load, increase speed



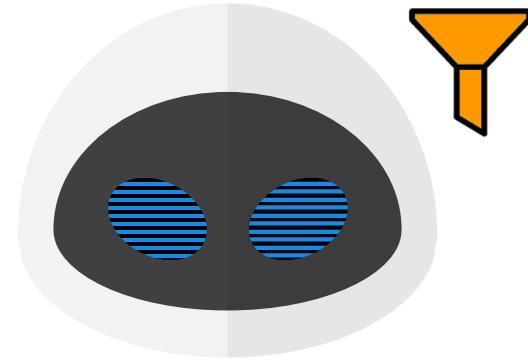
CS771: Intro to ML

# A bit of caution with features

122



Tricks, mnemonics lessen  
cognitive load, increase speed

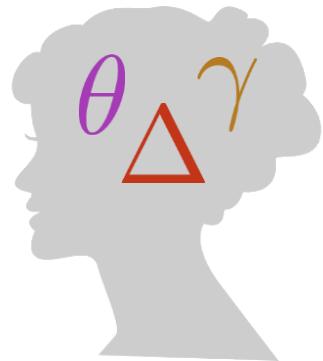


Derived features make learning  
easier, faster at test



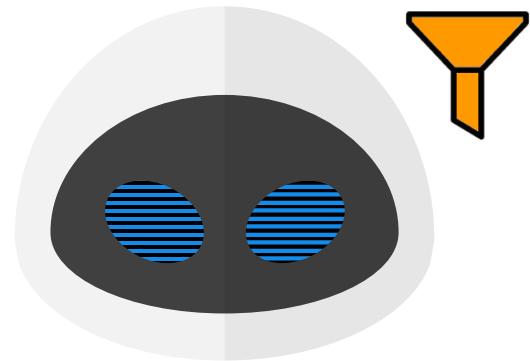
# A bit of caution with features

122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

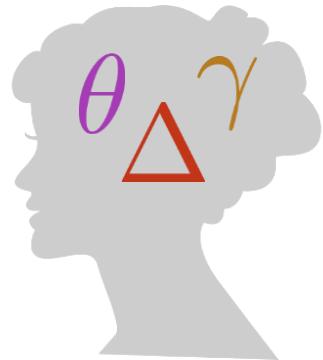


Derived features make learning easier, faster at test



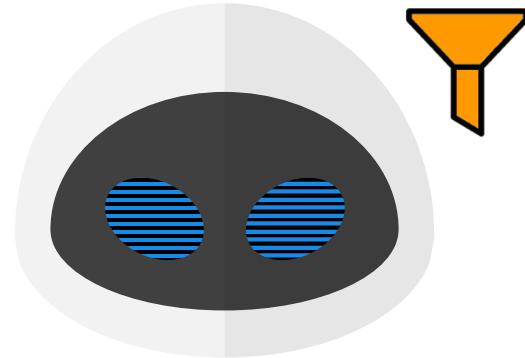
# A bit of caution with features

122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!



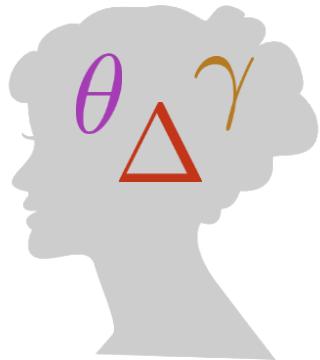
Derived features make learning easier, faster at test

What you are trying to predict is just another feature of the data!



# A bit of caution with features

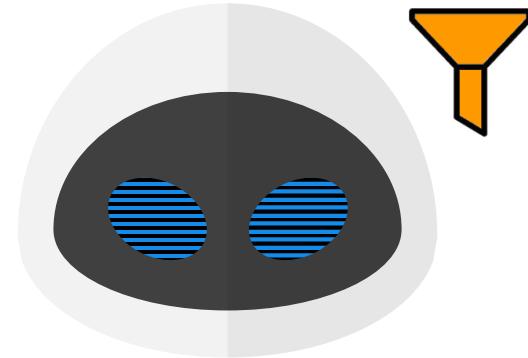
122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

Too many mnemonics can confuse you at time of exam



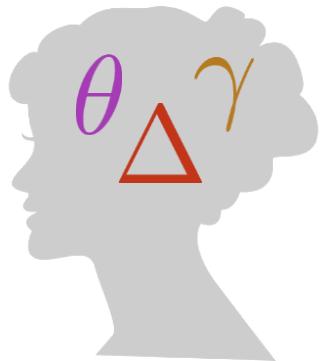
Derived features make learning easier, faster at test

What you are trying to predict is just another feature of the data!



# A bit of caution with features

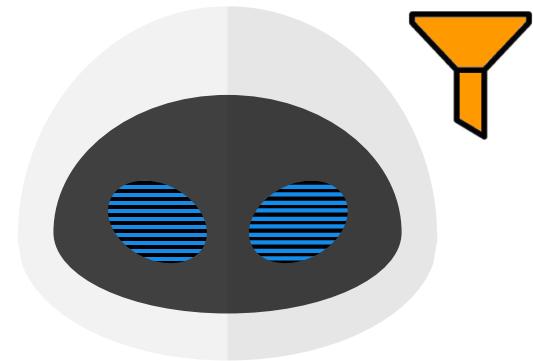
122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

Too many mnemonics can confuse you at time of exam



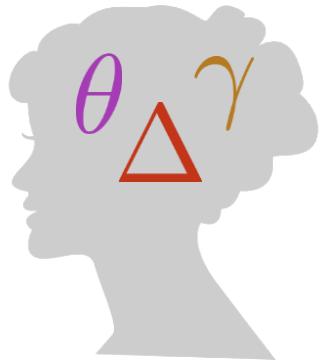
Derived features make learning easier, faster at test

What you are trying to predict is just another feature of the data!

Too many useless features can confuse classifier

# A bit of caution with features

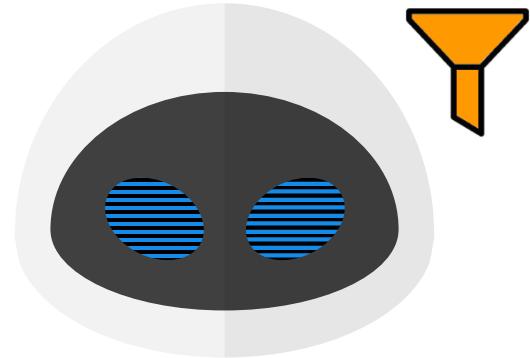
122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

Too many mnemonics can confuse you at time of exam



Derived features make learning easier, faster at test

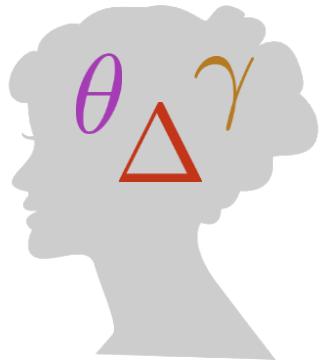
What you are trying to predict is just another feature of the data!

Too many useless features can confuse classifier



# A bit of caution with features

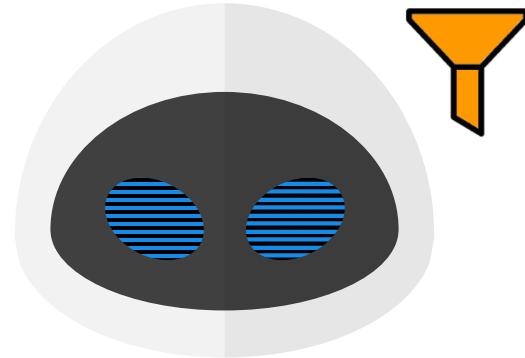
122



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

Too many mnemonics can confuse you at time of exam



Derived features make learning easier, faster at test

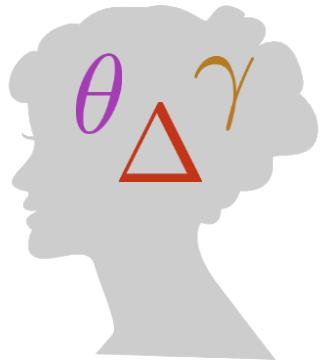
What you are trying to predict is just another feature of the data!

Too many useless features can confuse classifier

In fact, one of the main challenges in deep learning is that it learns way too many features



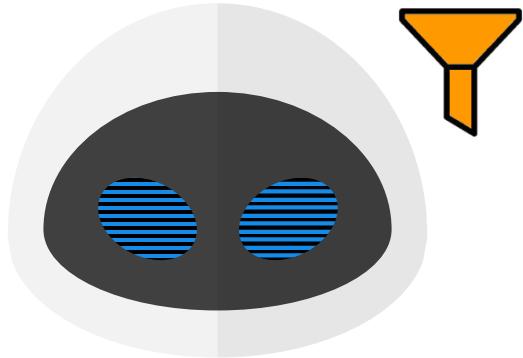
# A bit of caution with features



Tricks, mnemonics lessen cognitive load, increase speed

Easy questions can be solved in one step with a mnemonic!

Too many mnemonics can confuse you at time of ex

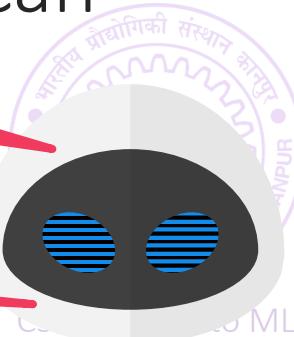


Derived features make learning easier, faster at test

What you are trying to predict is just another feature of the data!

However, not to worry. For most of this course, we will give you pre-made feature vectors ☺ can

In fact, one of the main challenges in deep learning is that it learns way too many features



# What are Vectors

Consider a  $d$ -dimensional real vector  $\mathbf{x} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_d], \mathbf{x}_i \in \mathbb{R}$

For a physicist, a vector is a way to encode a magnitude and direction

For a mathematician, a vector is an object in a vector space

For an ML person, a vector is simply a list of numbers, each number representing a useful piece of information about an object

**Example:** spam filter, a vector stored which words occurred in email

**Example:** image recognition, a vector stored the pixel RGB values

# What are Vectors

Consider a  $d$ -dimensional real vector  $\mathbf{x} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_d], \mathbf{x}_i \in \mathbb{R}$

For a physicist, a vector is a way to encode a magnitude and direction

For a mathematician, a vector is an object in a vector space

For an ML person, a vector is simply a list of numbers, each number representing a useful piece of information about an object

**Example:** spam filter, a vector stored which words occurred in email

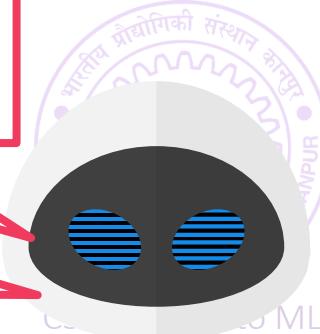
**Example:** image recognition, a vector stored the pixel RGB values



Does this mean I will have  
to learn math to do ML?

A bit of math will be required  
but 1) it will be simple and 2)  
it will be totally worth it!

True, for me, vectors are just like arrays of numbers.  
However, sometimes I do indeed do math with them



# Operations on Vectors

134

Given two  $d$ -dimensional vectors  $\mathbf{x}, \mathbf{y} \in \mathbb{R}^d$ , we can do the following

**Sum** of two vectors (is also a vector of same dimension)

$$a = \mathbf{x} + \mathbf{y} \in \mathbb{R}^d$$

**Difference** of two vectors (is also a vector of same dimension)

$$b = \mathbf{x} - \mathbf{y} \in \mathbb{R}^d$$

**Dot product** of two vectors (is a real number, possibly negative)

$$p = \langle \mathbf{x}, \mathbf{y} \rangle = \mathbf{x}^\top \mathbf{y} = \sum_{j=1}^d \mathbf{x}_j \mathbf{y}_j$$

**Euclidean length** of a vector (is a positive real number, possibly zero)

$$q = \|\mathbf{x}\|_2 = \sqrt{\sum_{j=1}^d \mathbf{x}_j^2} = \sqrt{\mathbf{x}^\top \mathbf{x}}$$



# Operations on Vectors

135

Given two  $d$ -dimensional vectors  $\mathbf{x}, \mathbf{y} \in \mathbb{R}^d$ , we can do the following

**Sum** of two vectors (is also a vector of same dimension)

$$a = \mathbf{x} + \mathbf{y} \in \mathbb{R}^d$$

**Difference** of two vectors (is also a vector of same dimension)

$$b = \mathbf{x} - \mathbf{y} \in \mathbb{R}^d$$

**Dot product** of two vectors (is a real number, possibly negative)

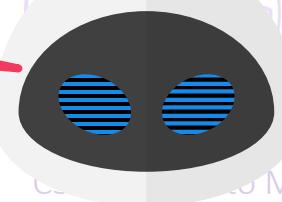
$$p = \langle \mathbf{x}, \mathbf{y} \rangle = \mathbf{x}^\top \mathbf{y} = \sum_{i=1}^d \mathbf{x}_i \mathbf{y}_i$$

**Euclidean length** of

Good point – just wait a second for some intuition.

However, to be honest, sometimes it is good in ML not to hunt too much for intuition and just let the math be!

So I can take two feature vectors and add them.  
But what sense does it make to add two emails?



# ML Operations on Feature Vectors

136

Given  $n$  feature vectors  $\mathbf{x}^1, \mathbf{x}^2, \dots, \mathbf{x}^n \in \mathbb{R}^d$

Average feature vector

$$\boldsymbol{\mu} = \frac{1}{n} \sum_{i=1}^n \mathbf{x}^i$$

Euclidean distance between two feature vectors

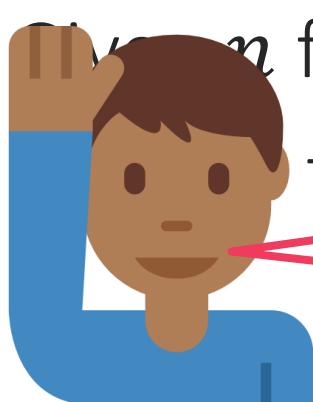
$$d_2(\mathbf{x}^1, \mathbf{x}^2) = \|\mathbf{x}^1 - \mathbf{x}^2\|_2 = \sqrt{\sum_{j=1}^d (\mathbf{x}_j^1 - \mathbf{x}_j^2)^2}$$

Distance of a feature vector from the average vector

$$d_2(\mathbf{x}^1, \boldsymbol{\mu}) = \|\mathbf{x}^1 - \boldsymbol{\mu}\|_2$$



# ML Operations on Feature Vectors



I can use this to find out if two emails are similar or very different from each other

$$\mu = \frac{1}{n} \sum_{i=1}^n \mathbf{x}^i$$

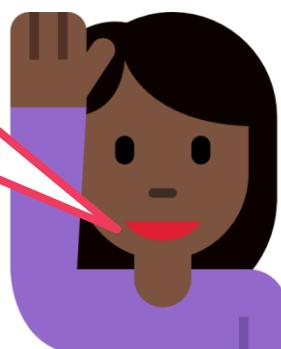
Euclidean distance between two feature vectors

$$d_2(\mathbf{x}^1, \mathbf{x}^2) = \|\mathbf{x}^1 - \mathbf{x}^2\|_2 = \sqrt{\sum_{j=1}^n (\mathbf{x}_j^1 - \mathbf{x}_j^2)^2}$$

Distance of a feature vector from the average vector

$$d_2(\mathbf{x}^1, \mu) = \|\mathbf{x}^1 - \mu\|$$

Excellent! We are now ready for our first ML algorithm!!



# Learning with Prototypes

- The basic mantra here is

“ If a new email looks similar to an average spam email, it maybe spam. On the other hand, if a new email looks similar to an average normal email, it should be normal ”

- In ML, the word *prototype* is used to refer to something that is representative or captures the qualities of a class of objects?
- How can we do ML using prototypes?



# Bird or not!

139

# Bird or not!

139



# Bird or not!

139



# Bird or not!

139



# Bird or not!

139

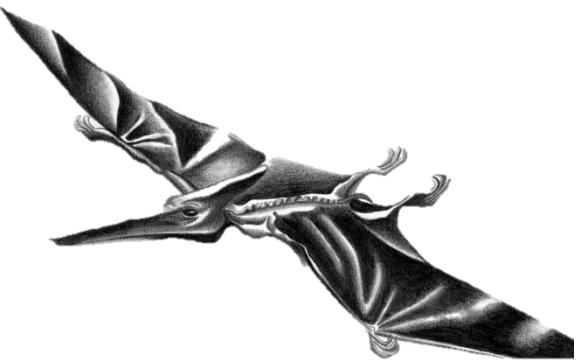


# Bird or not!



# Bird or not!

139



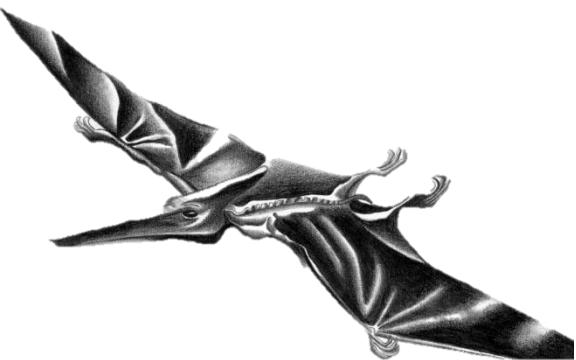
# Bird or not!

139



# Bird or not!

139



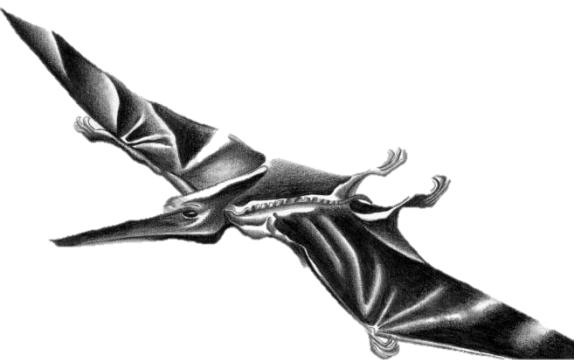
# Bird or not!

139



# Bird or not!

139



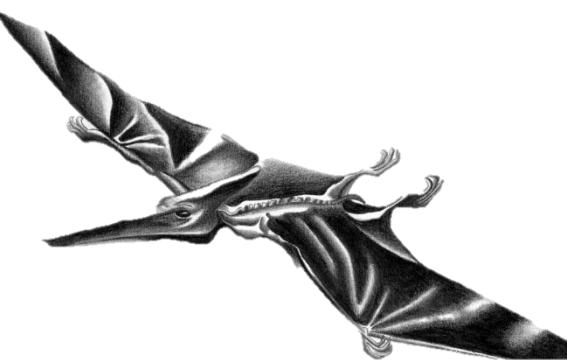
# Bird or not!

139



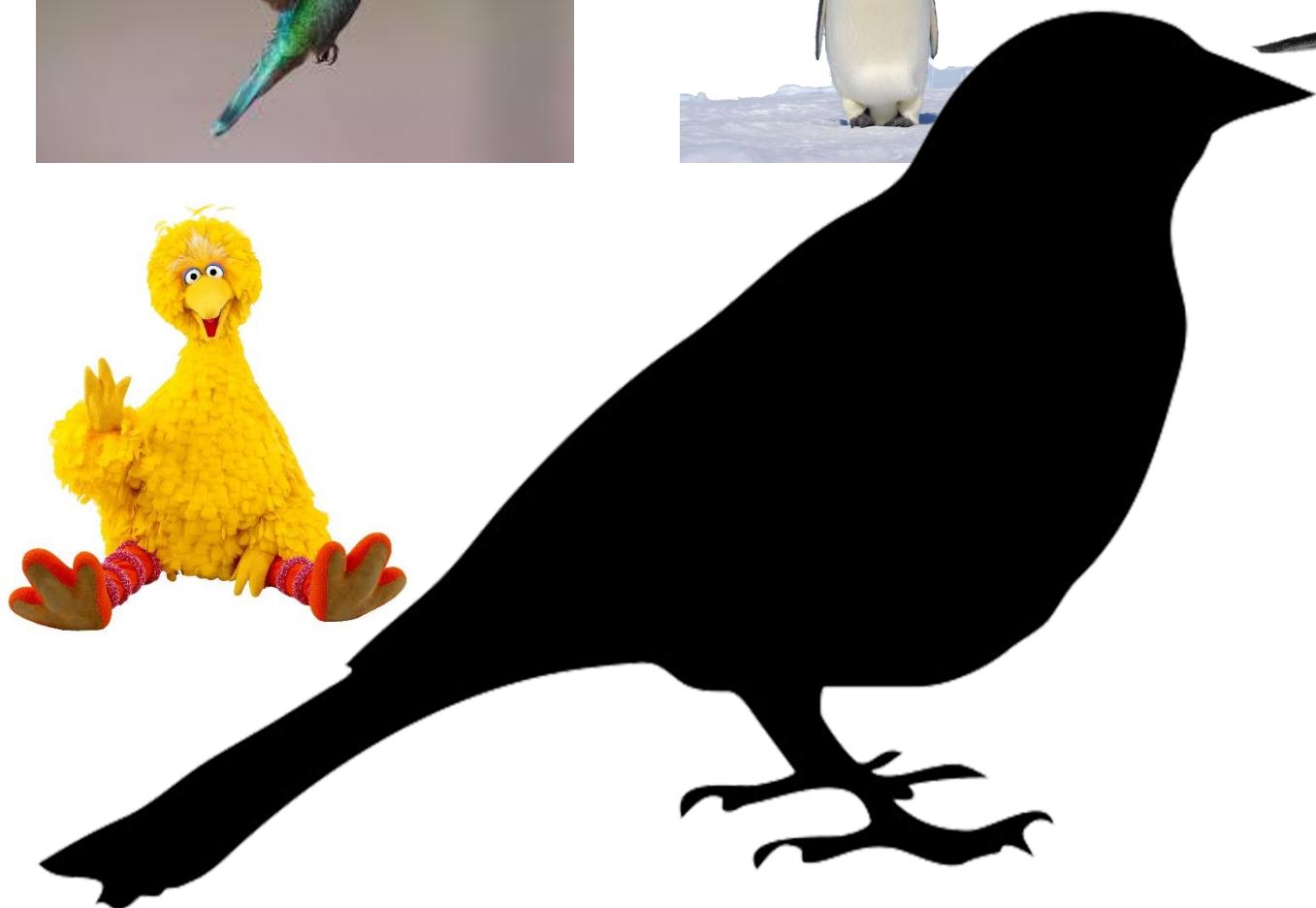
# Bird or not!

139



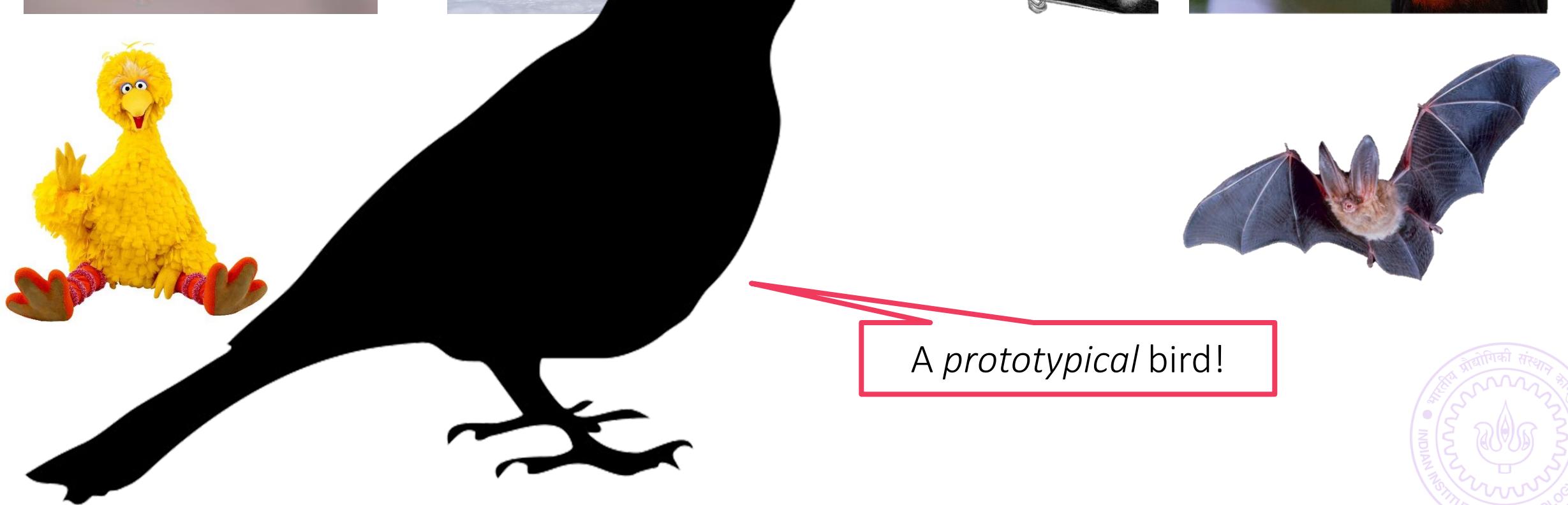
# Bird or not!

139



# Bird or not!

139



# Bird or not!

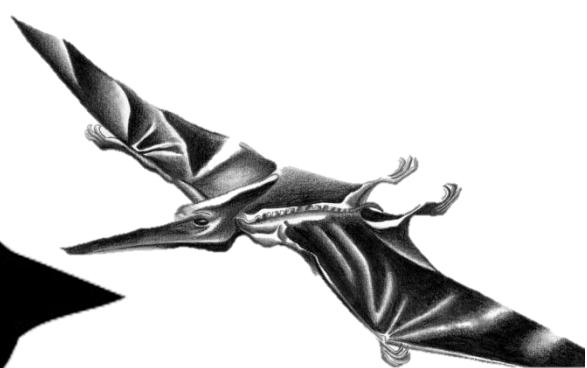
139



*A prototypical bird!*

# Bird or not!

139

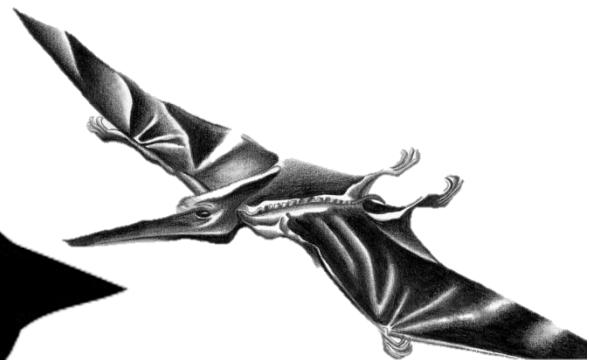


A prototypical bird!

What abstract qualities do we associate with “birdness”

# Bird or not!

139



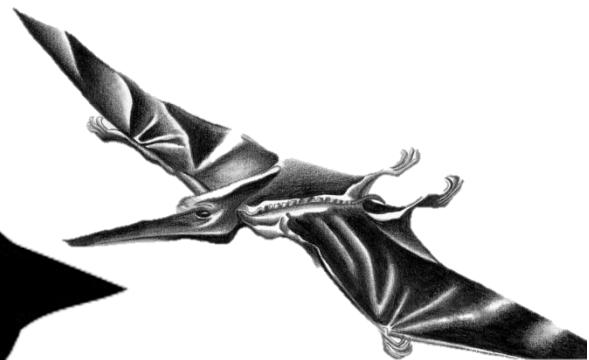
PIXABAY.COM, INDEPENDENT.CO.UK, YOUTUBE.COM, NEWDINOSAURS.COM, WIKIPEDIA.COM, CLIPARTQUEEN.COM

What abstract qualities do we associate with “birdness”



# Bird or not!

139



- Has wings
- Can fly
- Can sing
- Has a beak

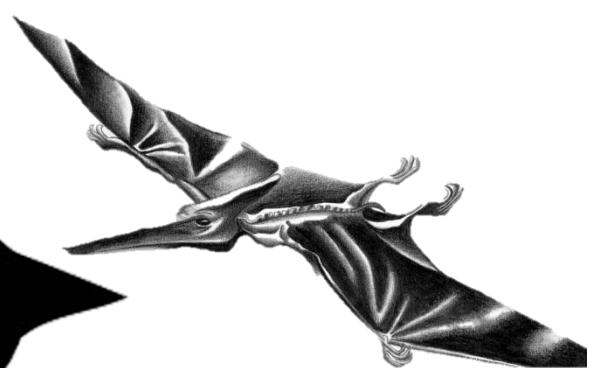


What abstract qualities do we associate with “birdness”



# Bird or not!

139



Has wings

Can fly

Can sing

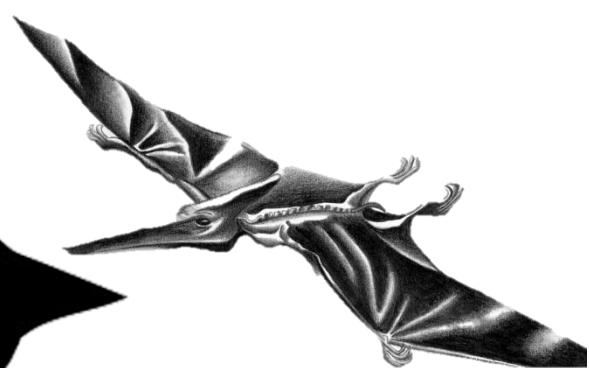


Has a beak

What abstract qualities do we associate with “birdness”

# Bird or not!

139



Has wings  
Can fly

Can sing

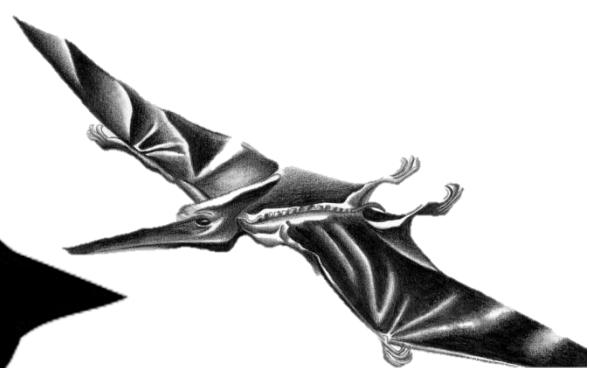


Has a beak

What abstract qualities do we associate with “birdness”

# Bird or not!

139



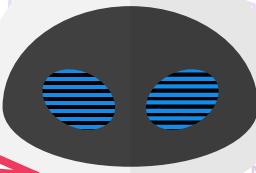
Has wings  
Can fly

Can sing



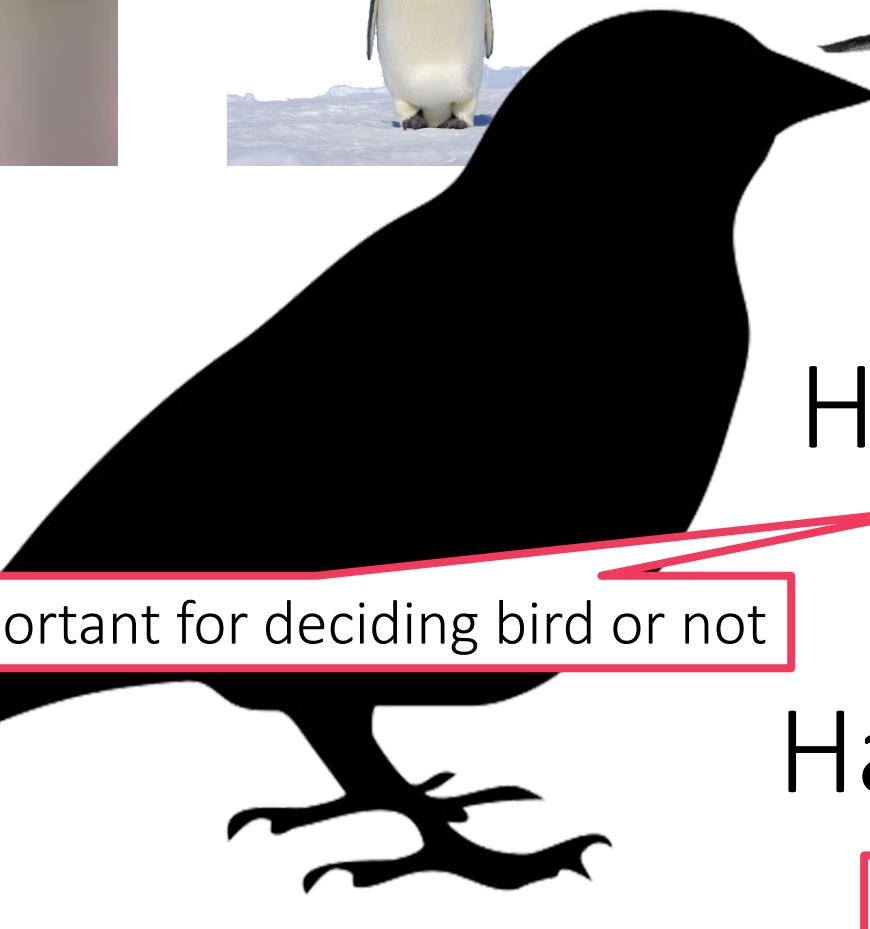
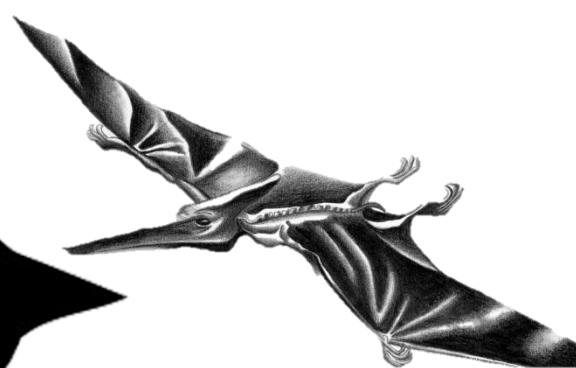
Has a beak

What abstract qualities do we associate with “birdness”



# Bird or not!

139



Not that important for deciding bird or not

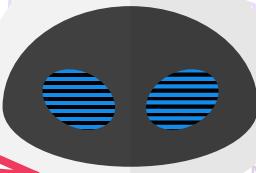
Has wings  
Can fly

Can sing



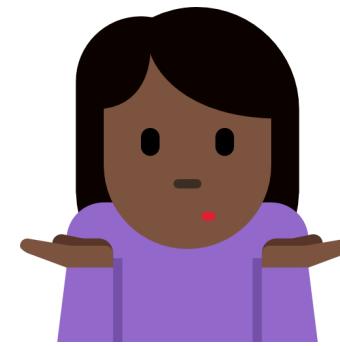
Has a beak

What abstract qualities do we associate with “birdness”



# Bird or not!

139



Not that important for deciding bird or not

**Has wings**

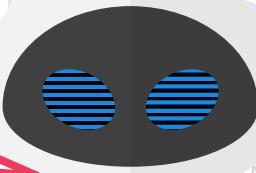
Can fly



Can sing

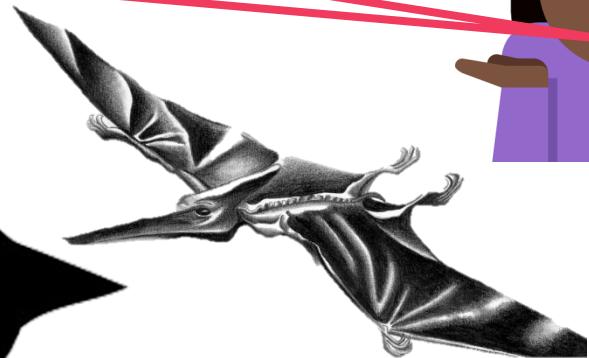
**Has a beak**

What abstract qualities do we associate with “birdness”



# Bird or not?

But the Pterosaur will still get classified as a bird – it has wings and a beak



Not that important for deciding bird or not

**Has wings**

Can fly

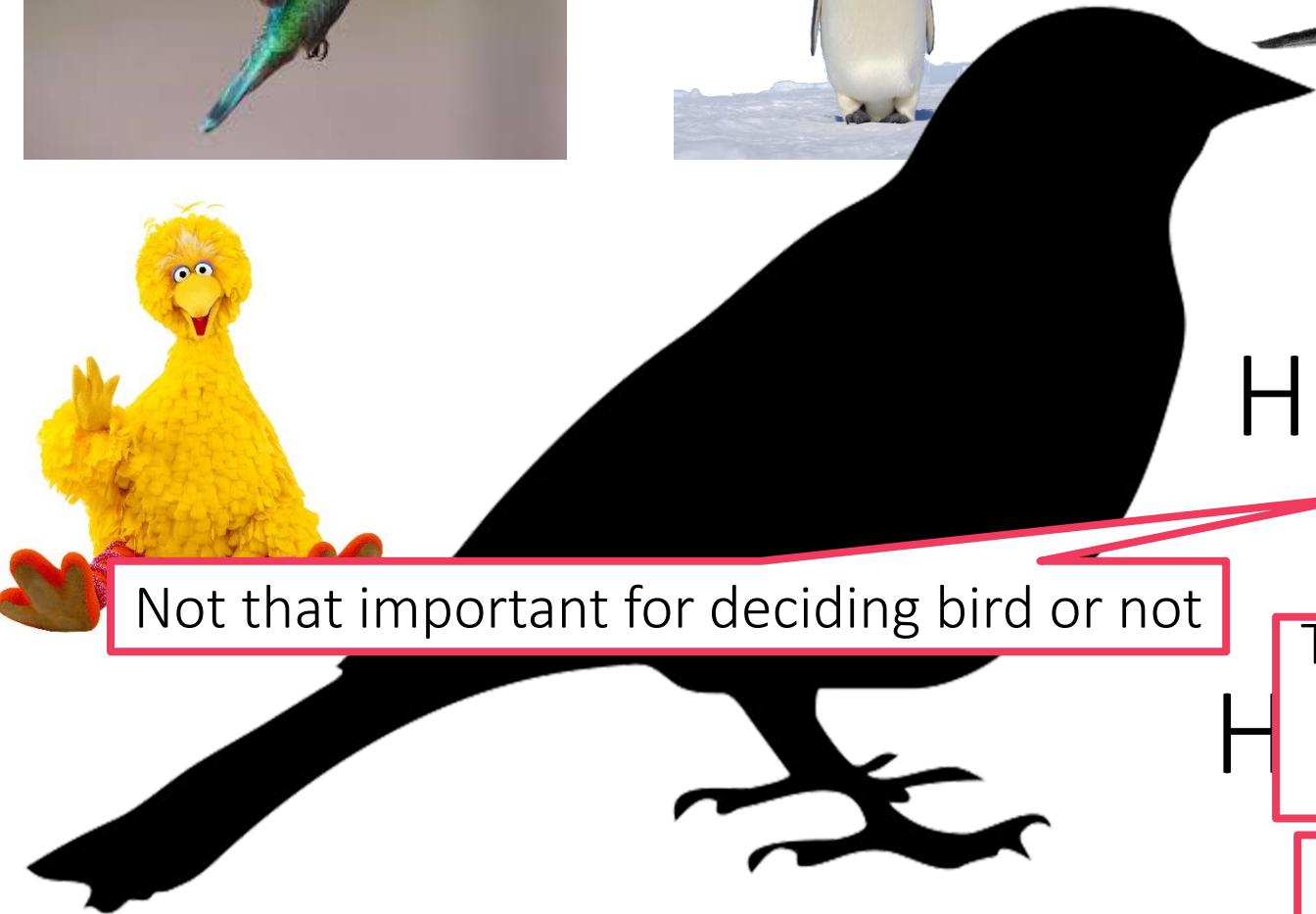
**Has a beak**

What abstract qualities do we associate with “birdness”



# Bird or not?

But the Pterosaur will still get classified as a bird – it has wings and a beak



Not that important for deciding bird or not

**Has wings**

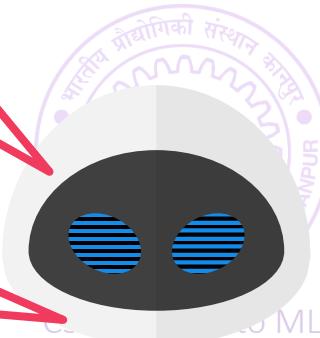
Can fly



Can sing

This means that our prototype is not good enough and we may need better features

What abstract qualities do we associate with “birdness”



# Learning with Prototypes

165



CS771: Intro to ML

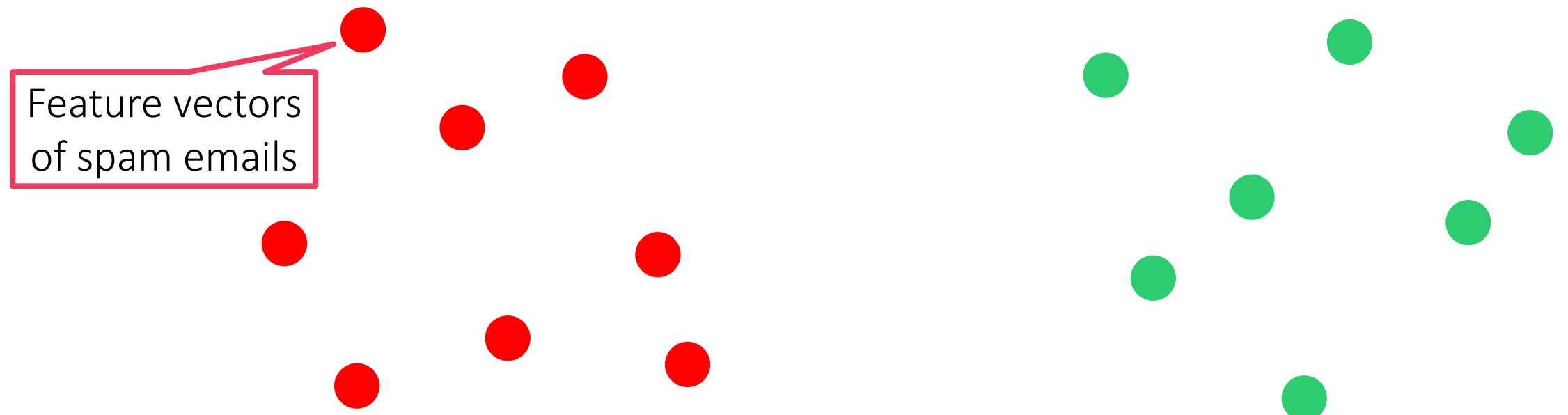
# Learning with Prototypes

165

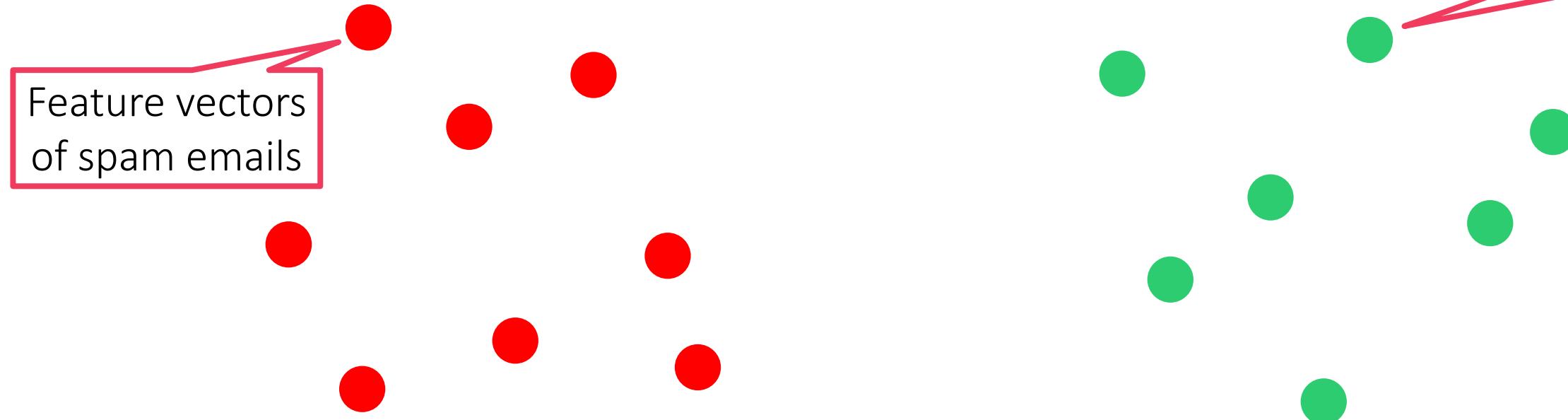


# Learning with Prototypes

165



# Learning with Prototypes

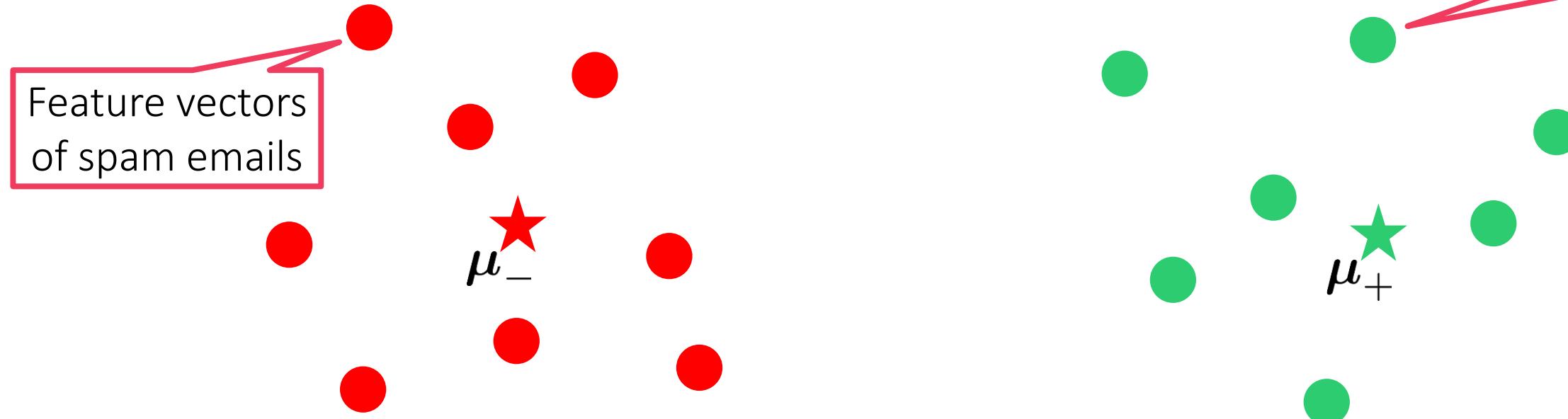


Feature vectors  
of normal emails

Feature vectors  
of spam emails



# Learning with Prototypes



Feature vectors  
of normal emails

Feature vectors  
of spam emails



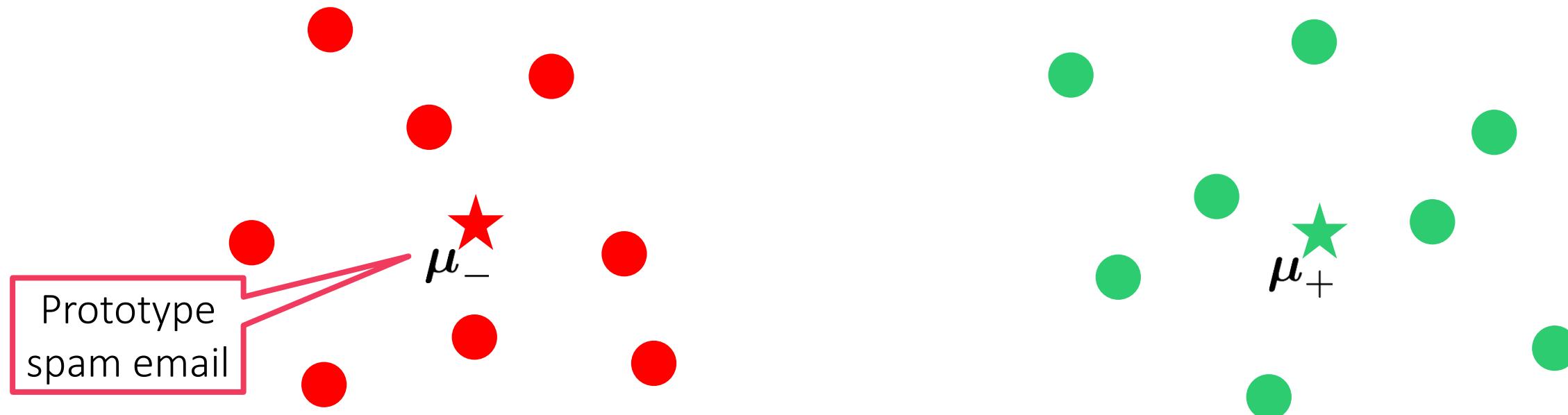
# Learning with Prototypes

165



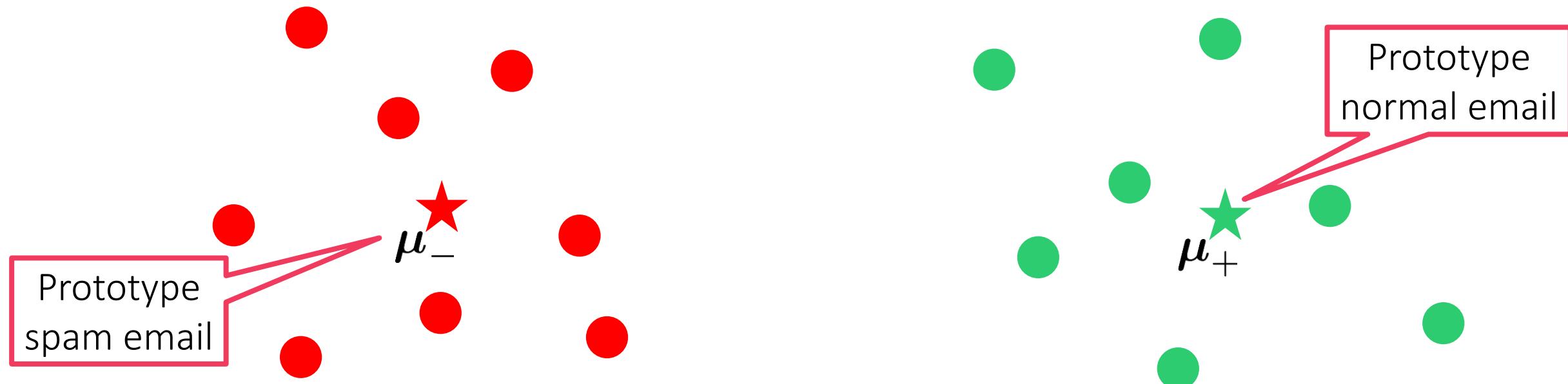
# Learning with Prototypes

165



# Learning with Prototypes

165



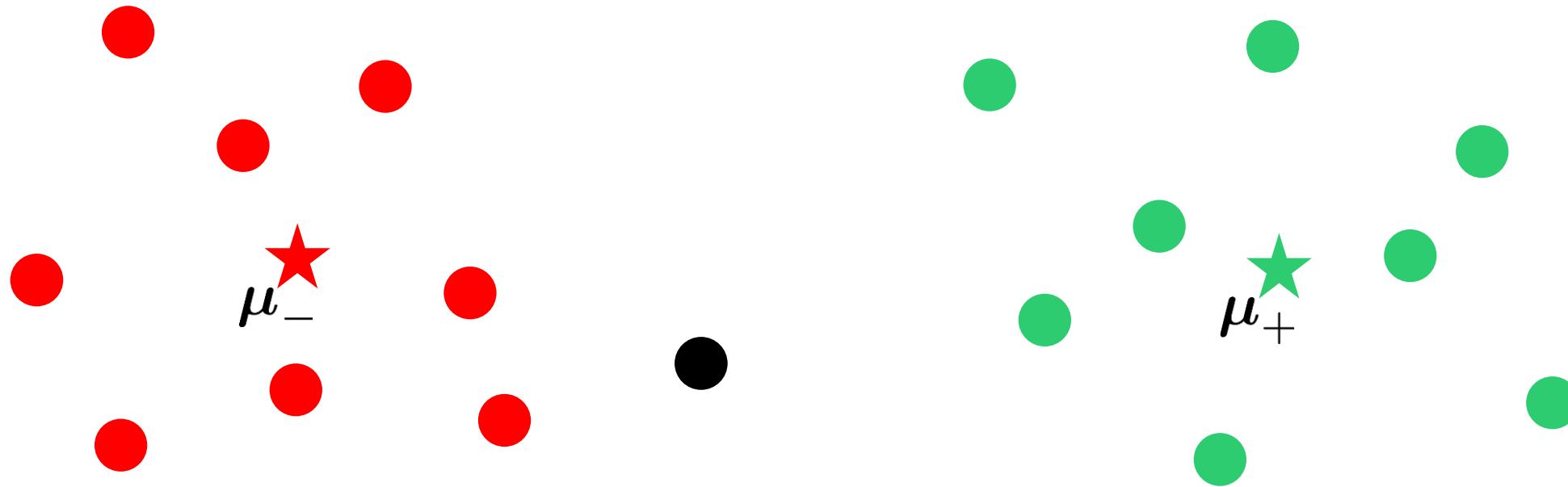
# Learning with Prototypes

165



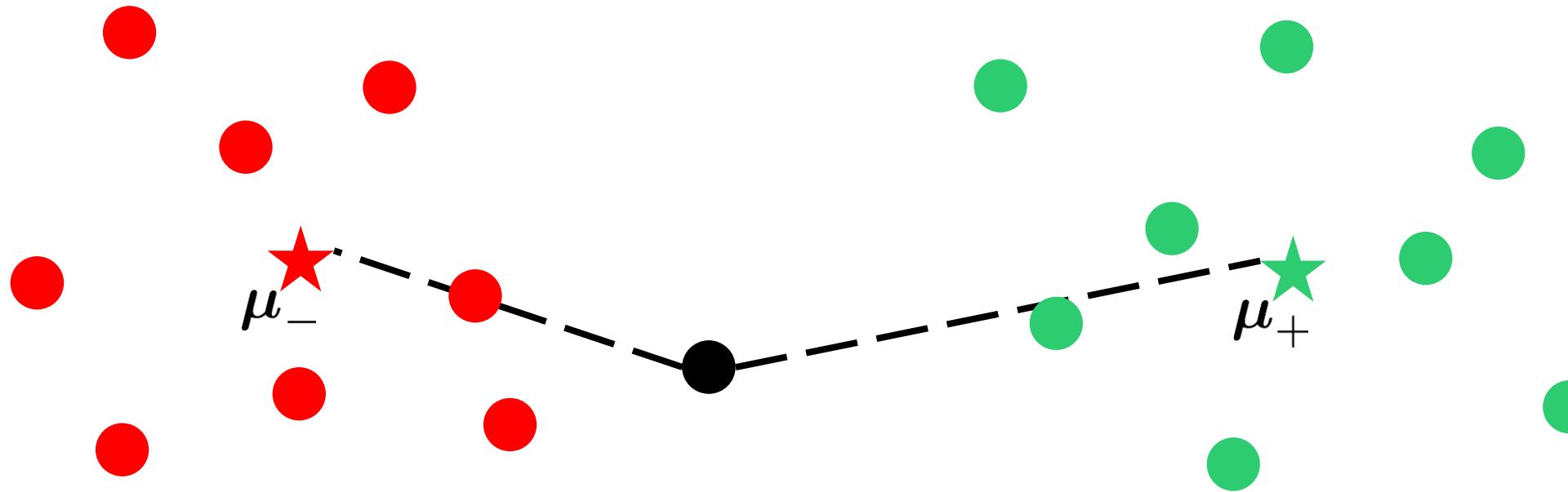
# Learning with Prototypes

165



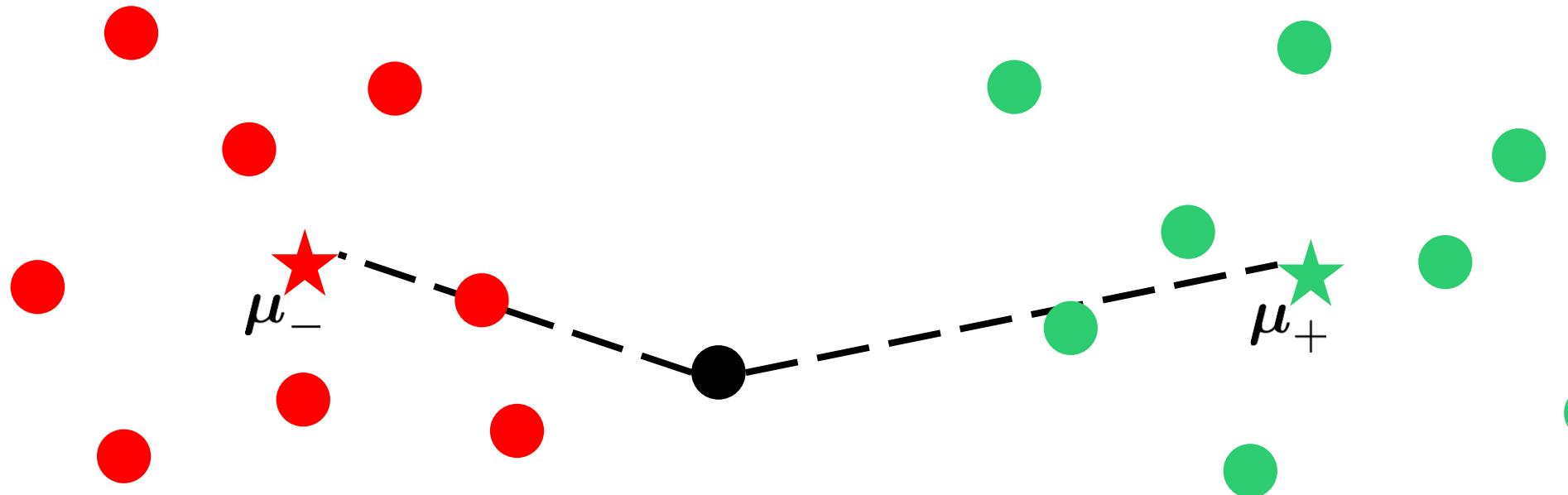
# Learning with Prototypes

165



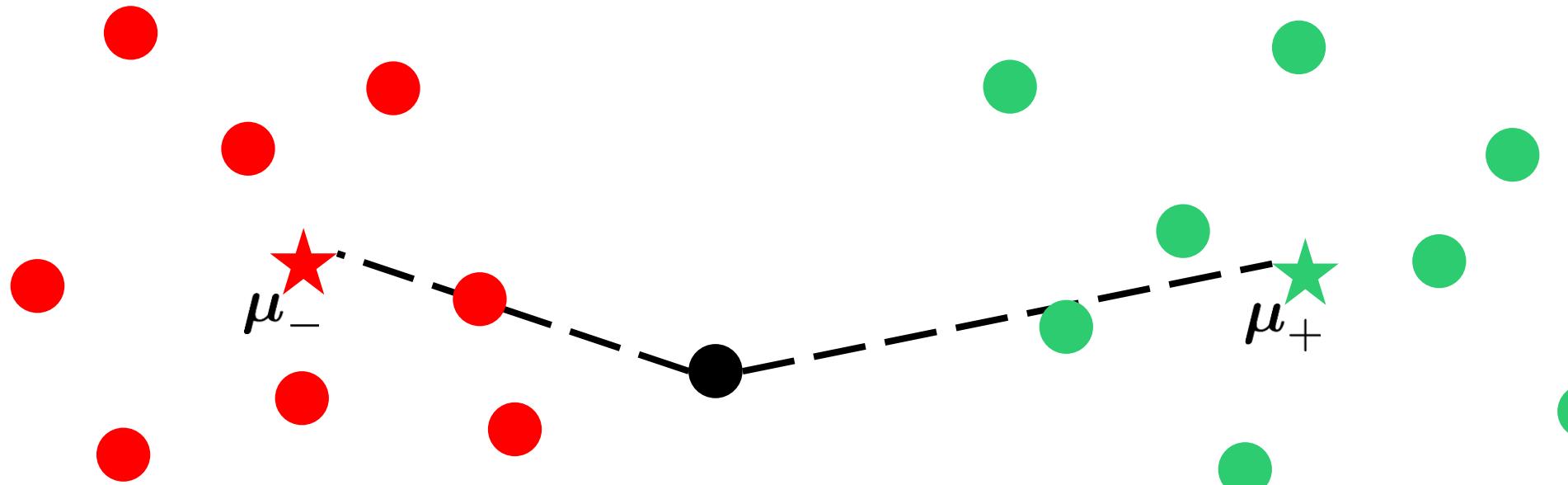
# Learning with Prototypes

165

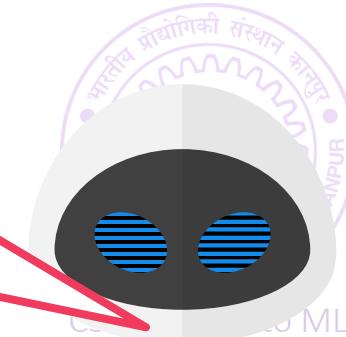


# Learning with Prototypes

165

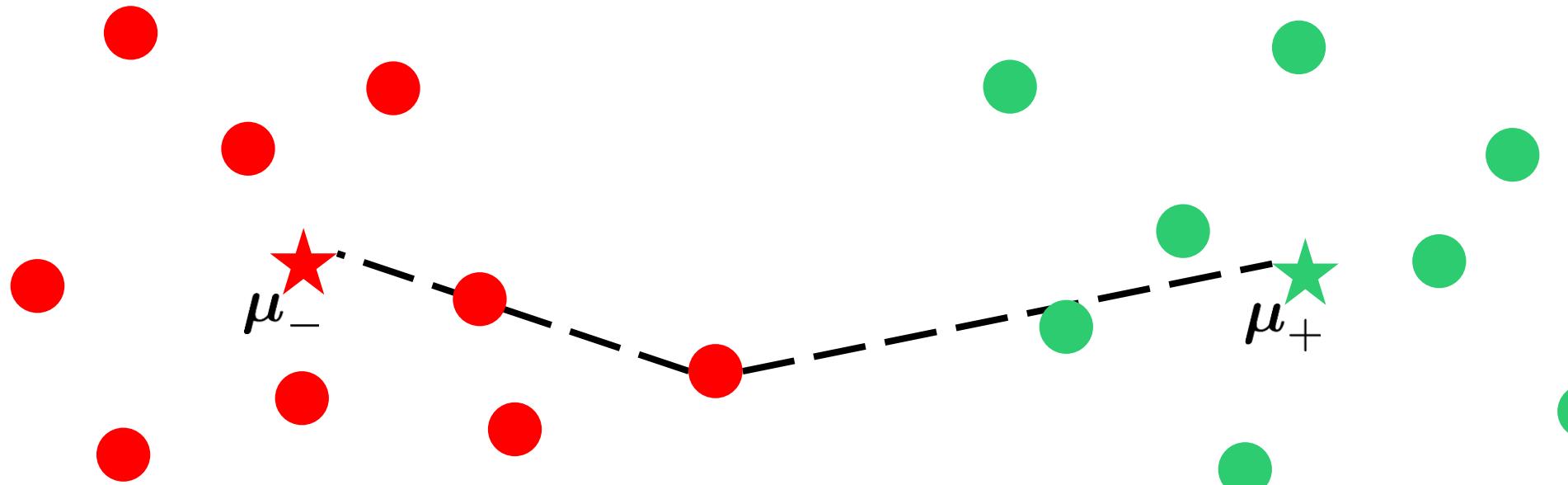


This email is closer to the prototype spam email than the prototype normal email so I will classify this new email as spam!

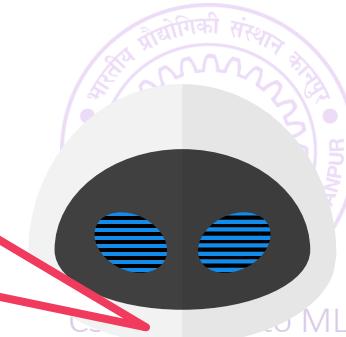


# Learning with Prototypes

165



This email is closer to the prototype spam email than the prototype normal email so I will classify this new email as spam!



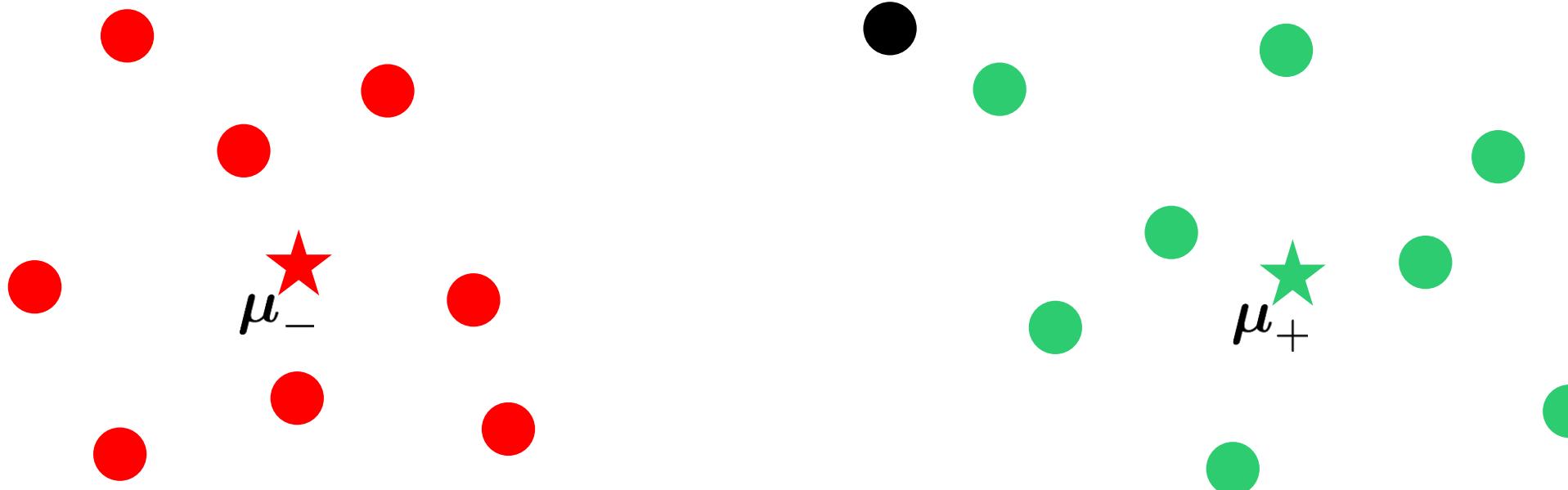
# Learning with Prototypes

165



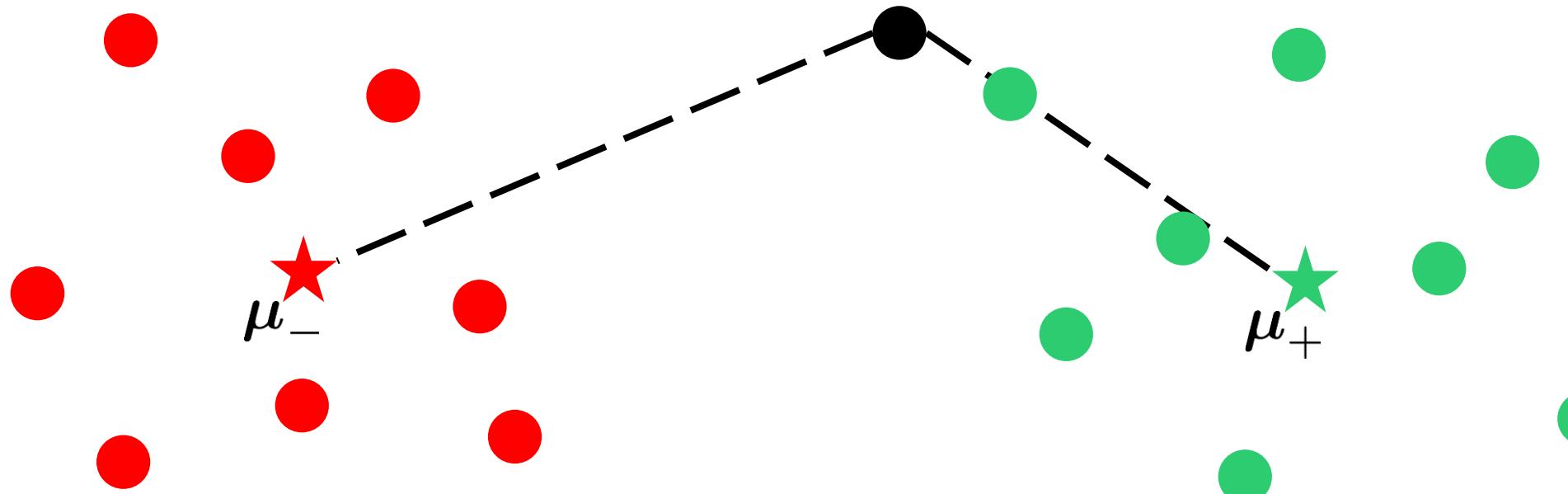
# Learning with Prototypes

165



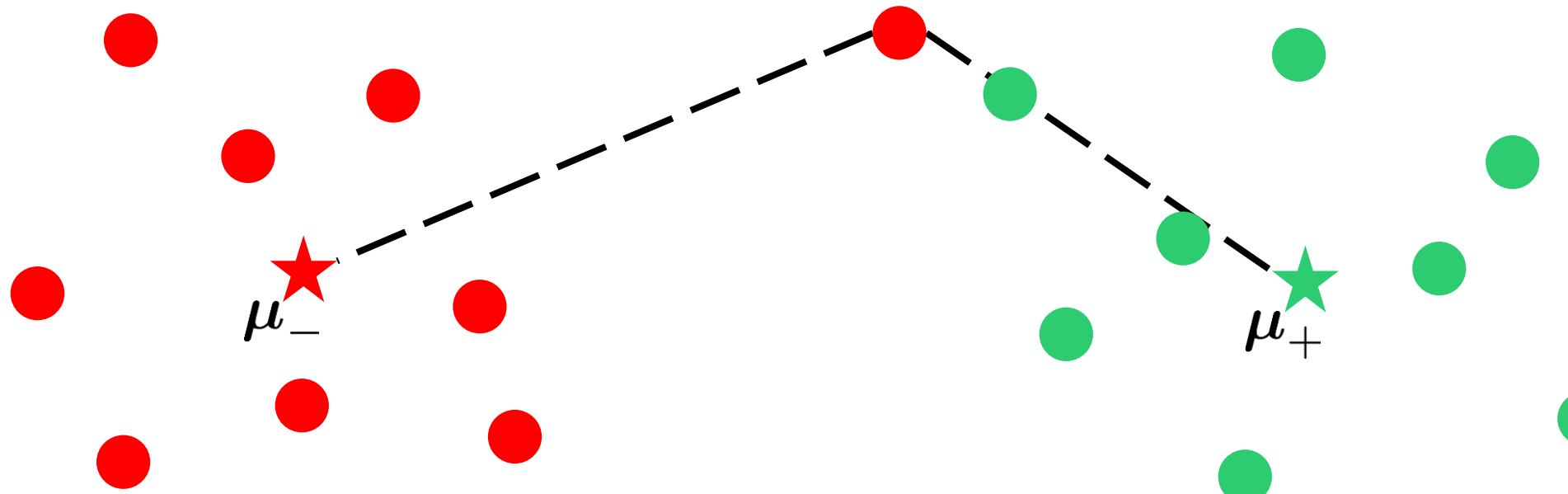
# Learning with Prototypes

165



# Learning with Prototypes

165



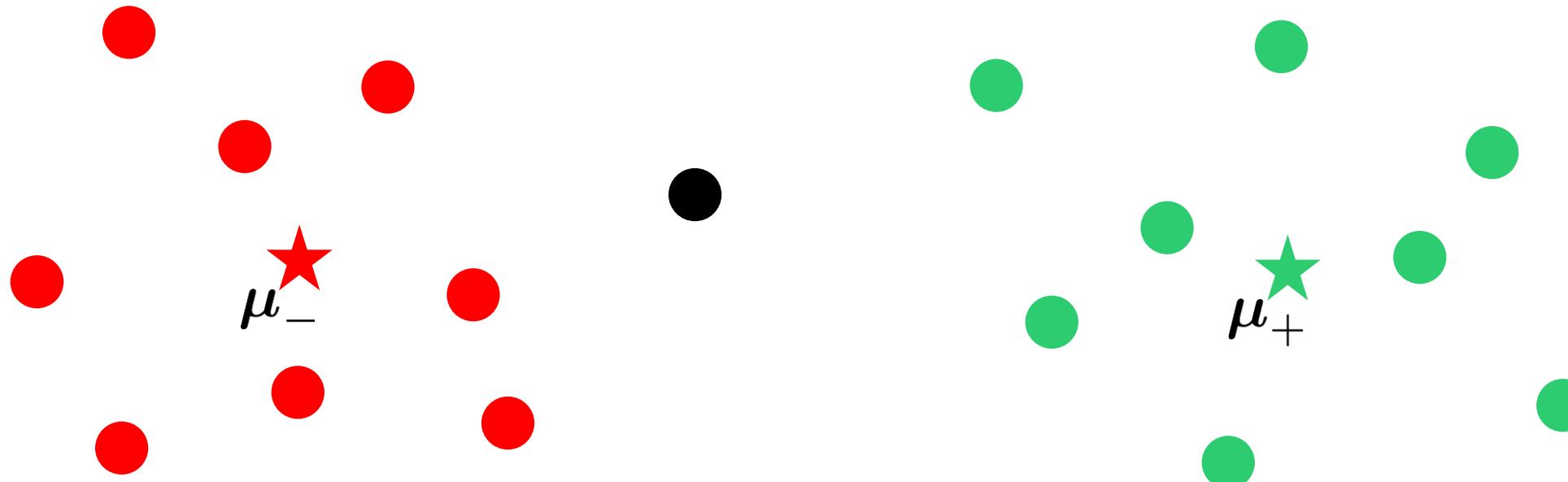
# Learning with Prototypes

165



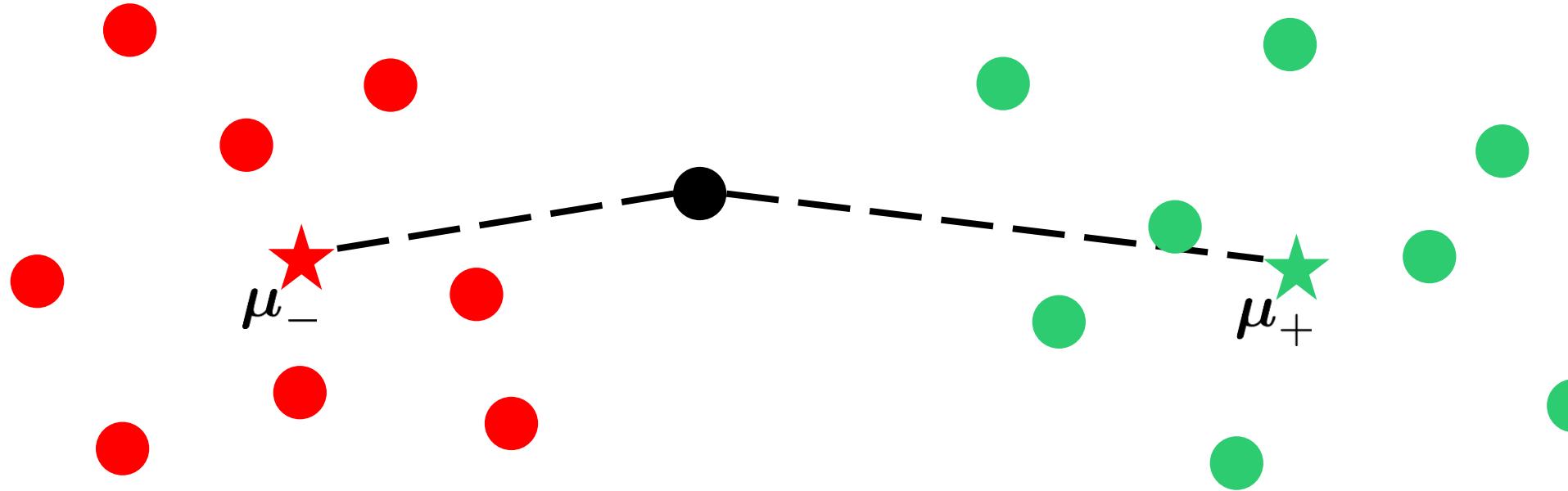
# Learning with Prototypes

165



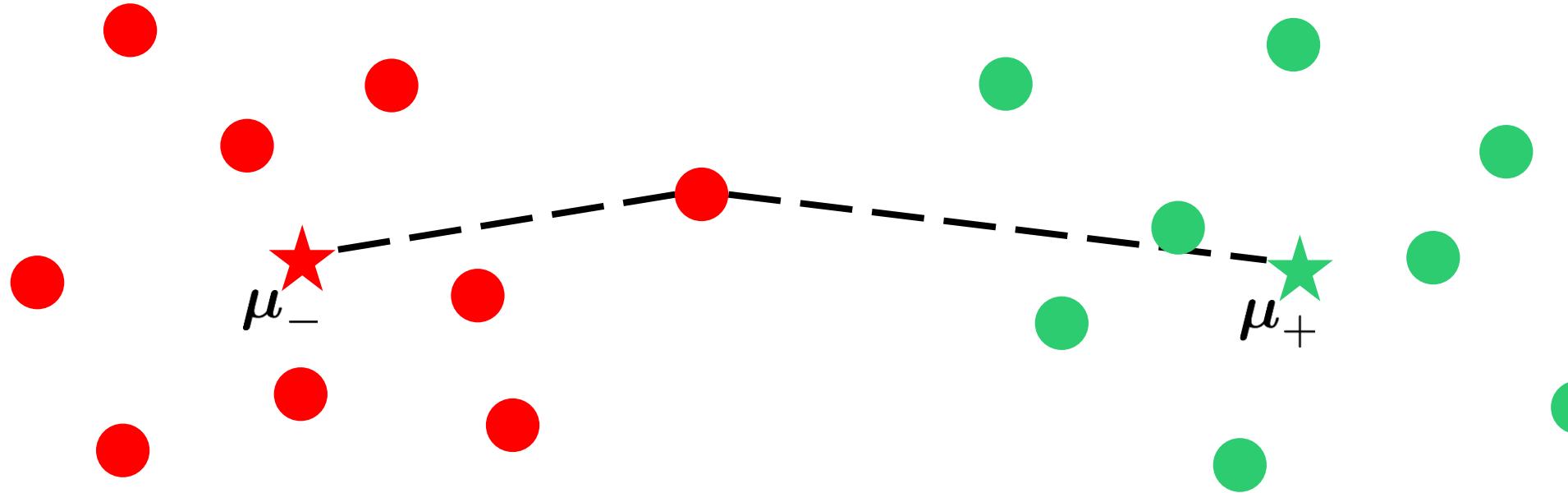
# Learning with Prototypes

165



# Learning with Prototypes

165



# Learning with Prototypes

165



# Learning with Prototypes

165

$$\mu_-^*$$

$$\mu_+^*$$



# Learning with Prototypes

165

$$\mu_-^*$$

$$\mu_+^*$$



$$\Upsilon = (\mu_-^*, \mu_+^*)$$

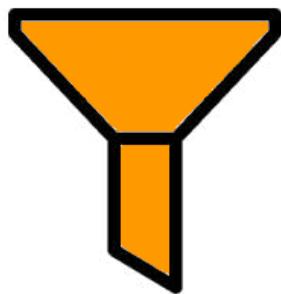


# Learning with Prototypes

165

$$\mu_-^*$$

$$\mu_+^*$$



$$Y = (\mu_-^*, \mu_+^*)$$

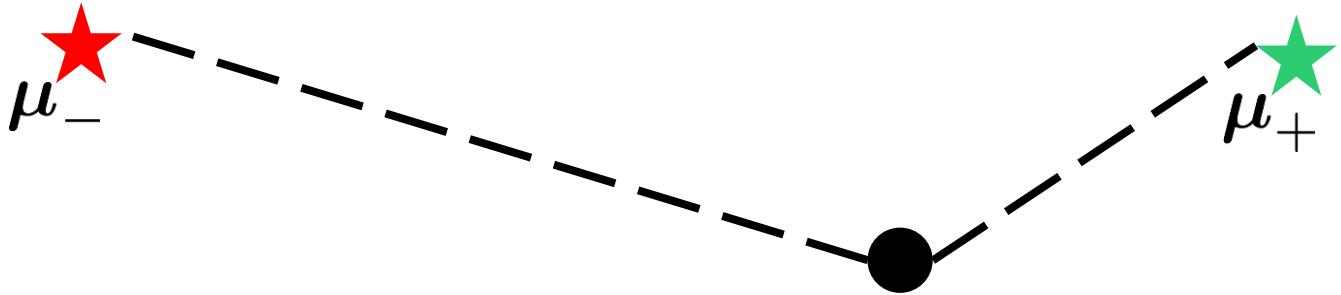


In order to classify a new email as spam/non-spam I only need the two prototypes, not the training emails



# Learning with Prototypes

165



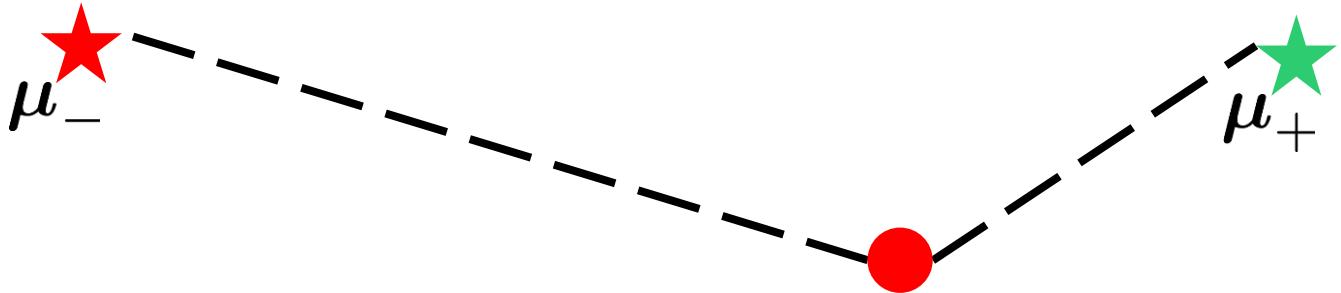
$$\mathcal{Y} = (\mu_-, \mu_+)$$

In order to classify a new email as spam/non-spam I only need the two prototypes, not the training emails



# Learning with Prototypes

165



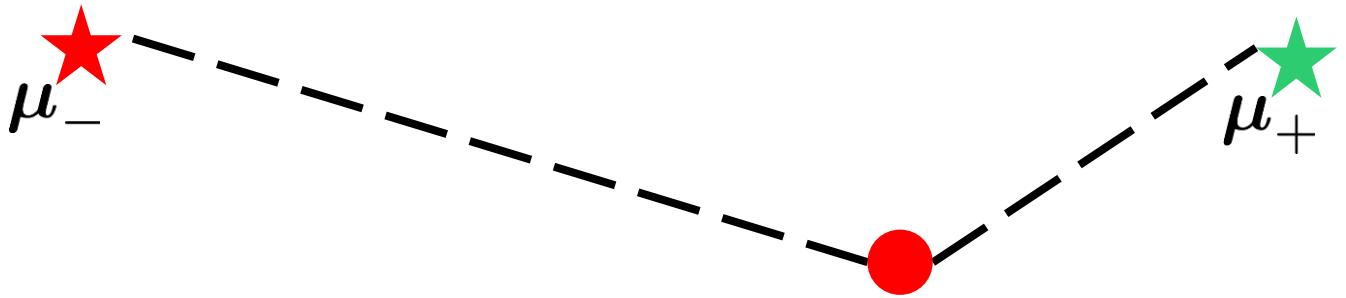
$$\mathcal{Y} = (\mu_-, \mu_+)$$

In order to classify a new email as spam/non-spam I only need the two prototypes, not the training emails



# Learning with Prototypes

165

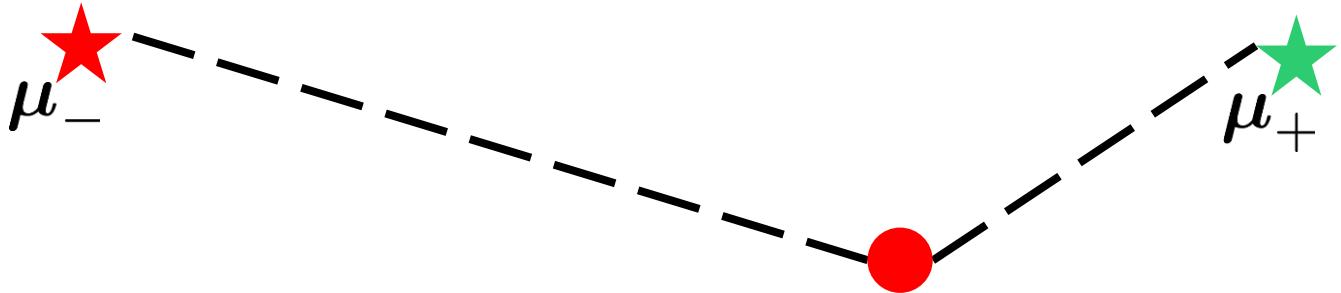


$$\Upsilon = (\mu_-, \mu_+)$$



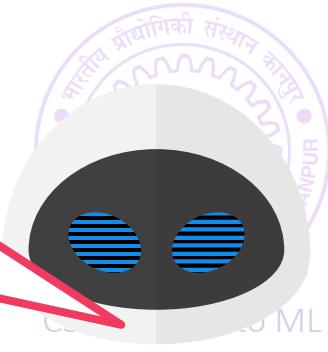
# Learning with Prototypes

165



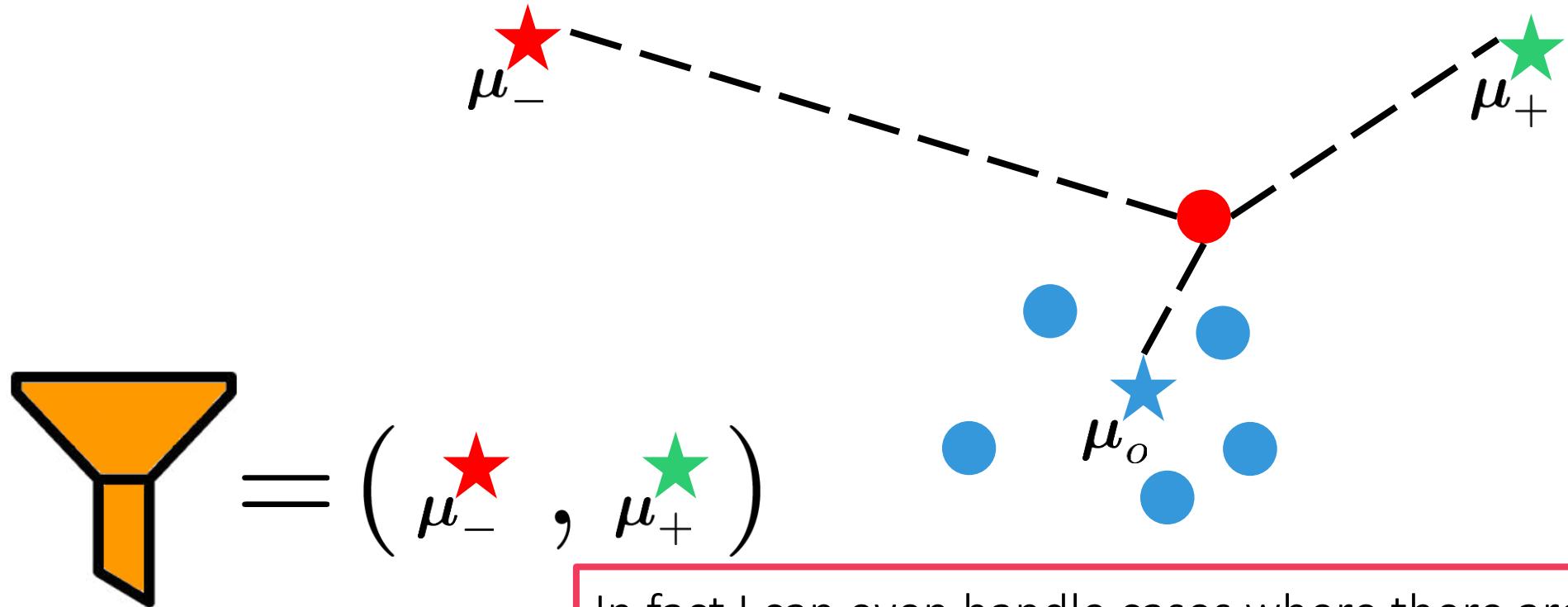
$$\Upsilon = (\mu_-, \mu_+)$$

In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...

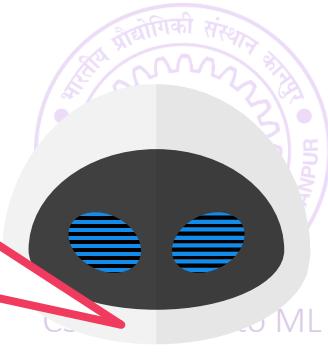


# Learning with Prototypes

165

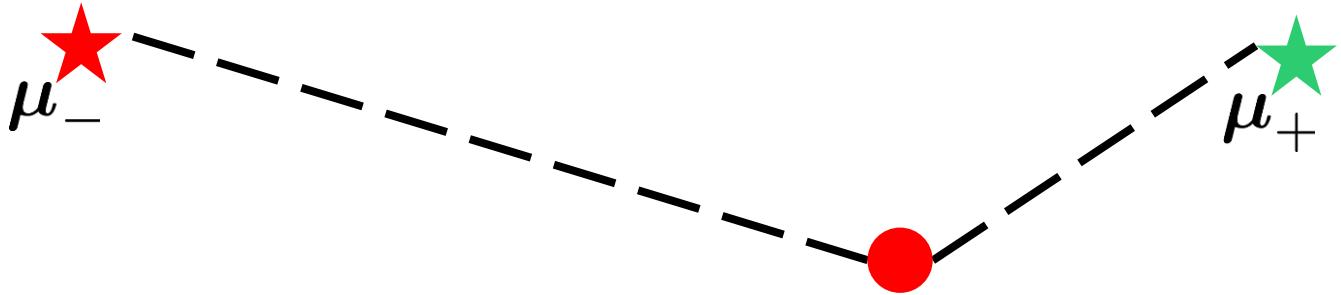


In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...



# Learning with Prototypes

165



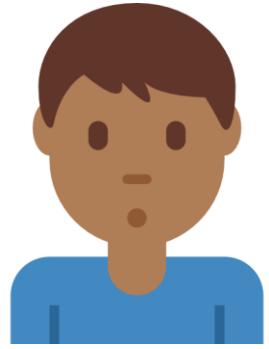
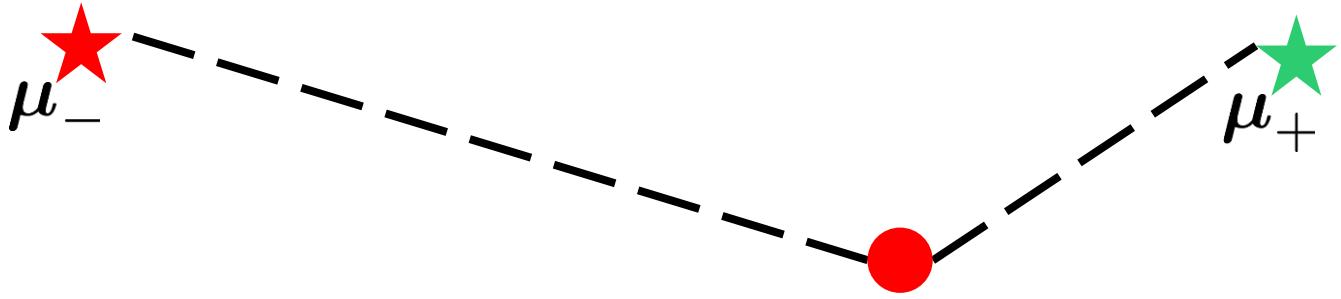
$$\Upsilon = (\mu_-, \mu_+)$$

In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...



# Learning with Prototypes

165



$$\Upsilon = (\mu_-, \mu_+)$$

In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...

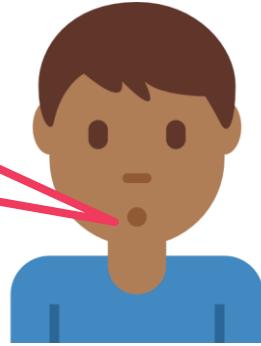


# Learning with Prototypes

165

$\mu_-$

Wow! So so this is your model – just two vectors. You were able to distil all the information in the training emails into just two prototype vectors!!



$$\mathcal{Y} = (\mu_-, \mu_+)$$

In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...

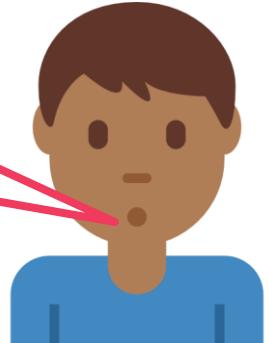


# Learning with Prototypes

165

$\mu_-$

Wow! So so this is your model – just two vectors. You were able to distil all the information in the training emails into just two prototype vectors!!



$$\mathcal{Y} = (\mu_-, \mu_+)$$

In fact I can even handle cases where there are more than two classes e.g. instead of spam/non-spam, suppose the classes were Primary, Social, Updates ...



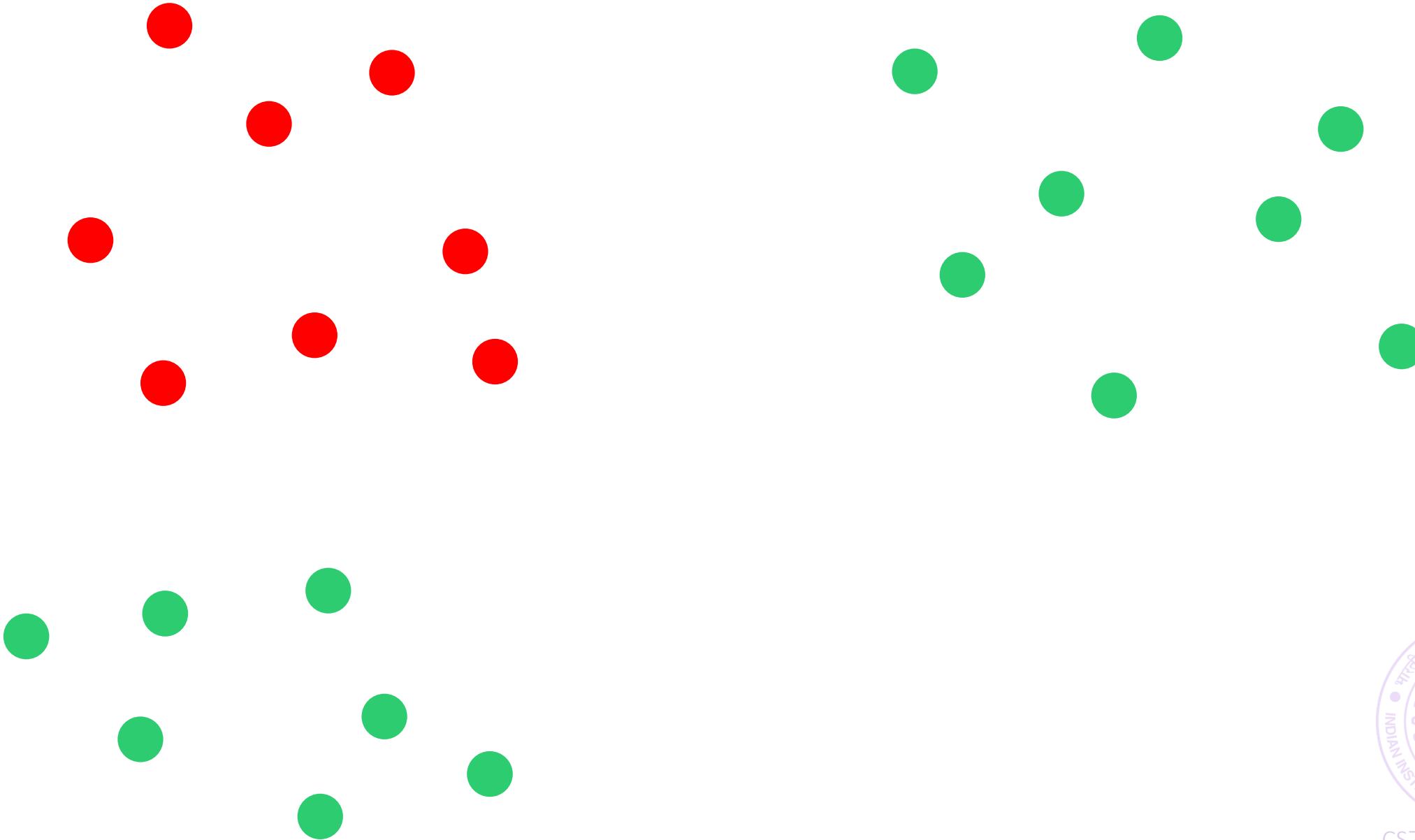
# Learning with Prototypes - Issues

200

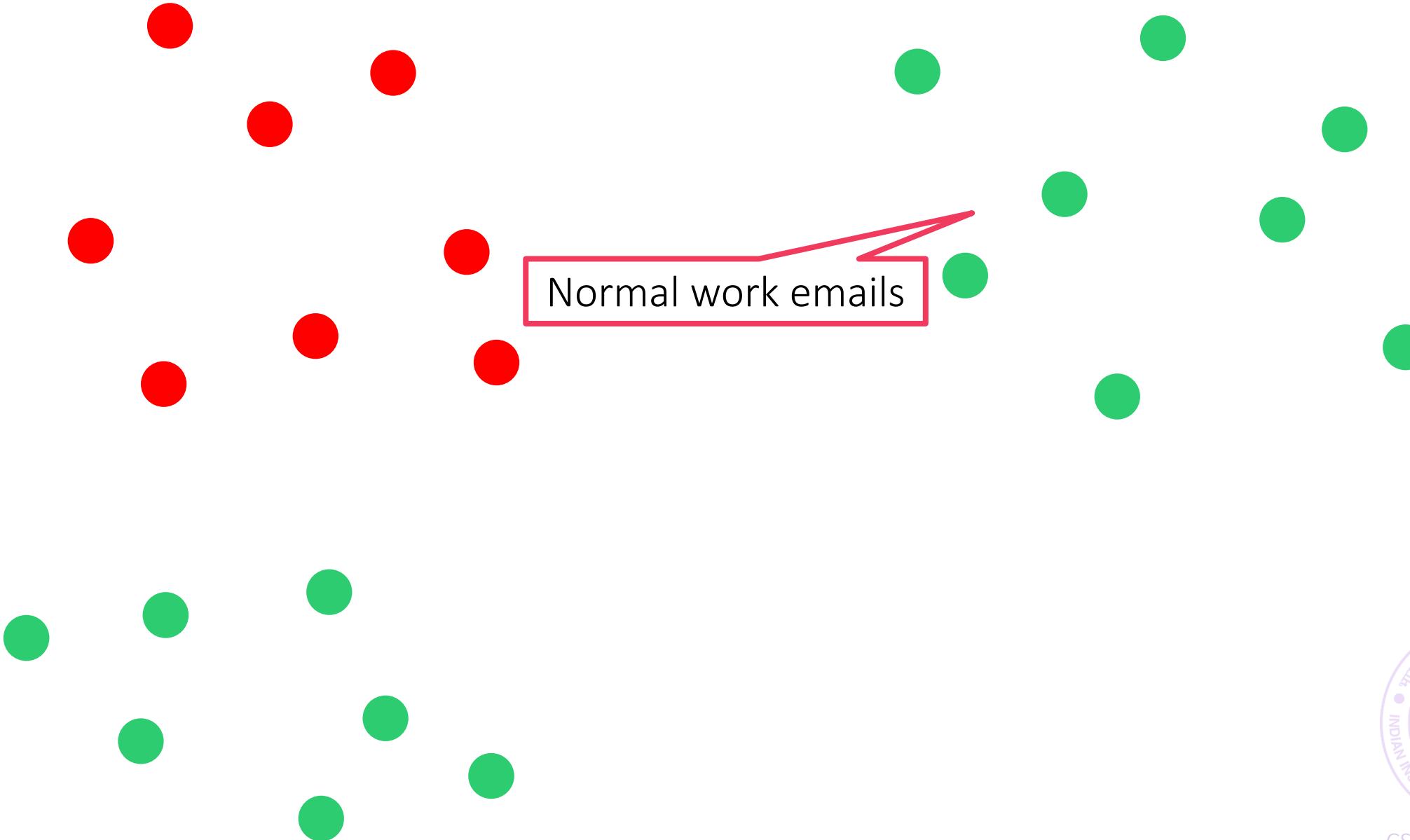


# Learning with Prototypes - Issues

200

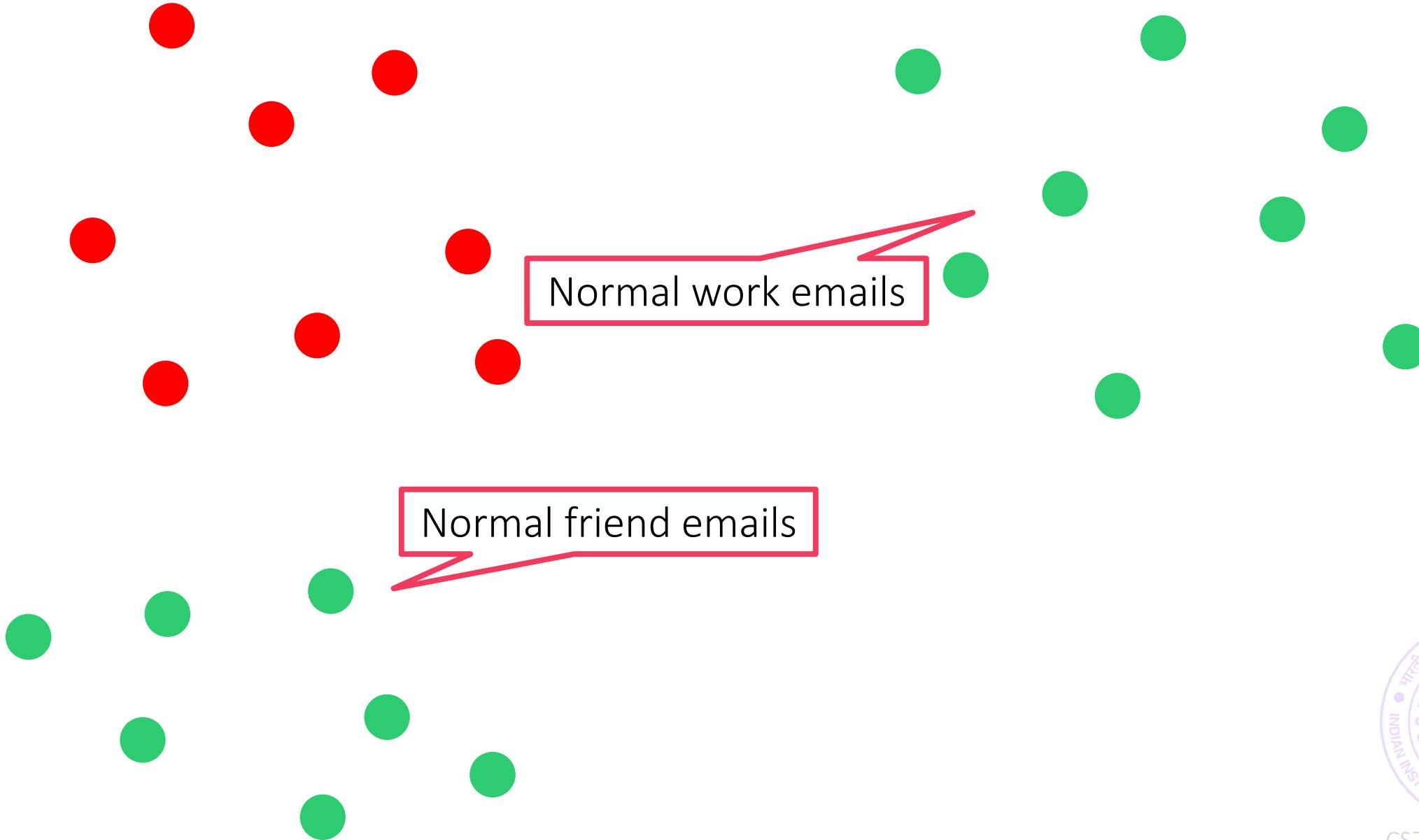


# Learning with Prototypes - Issues



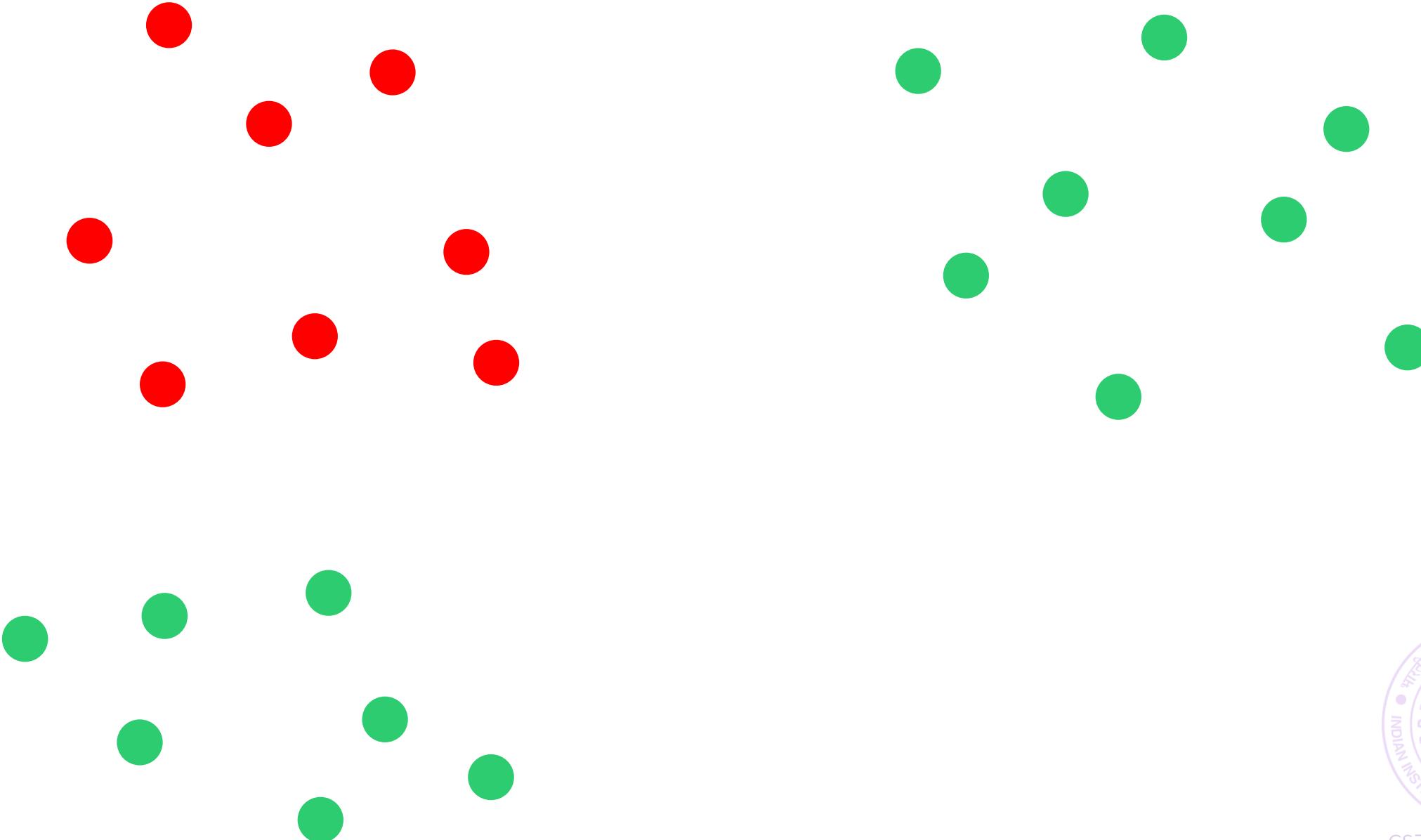
# Learning with Prototypes - Issues

200



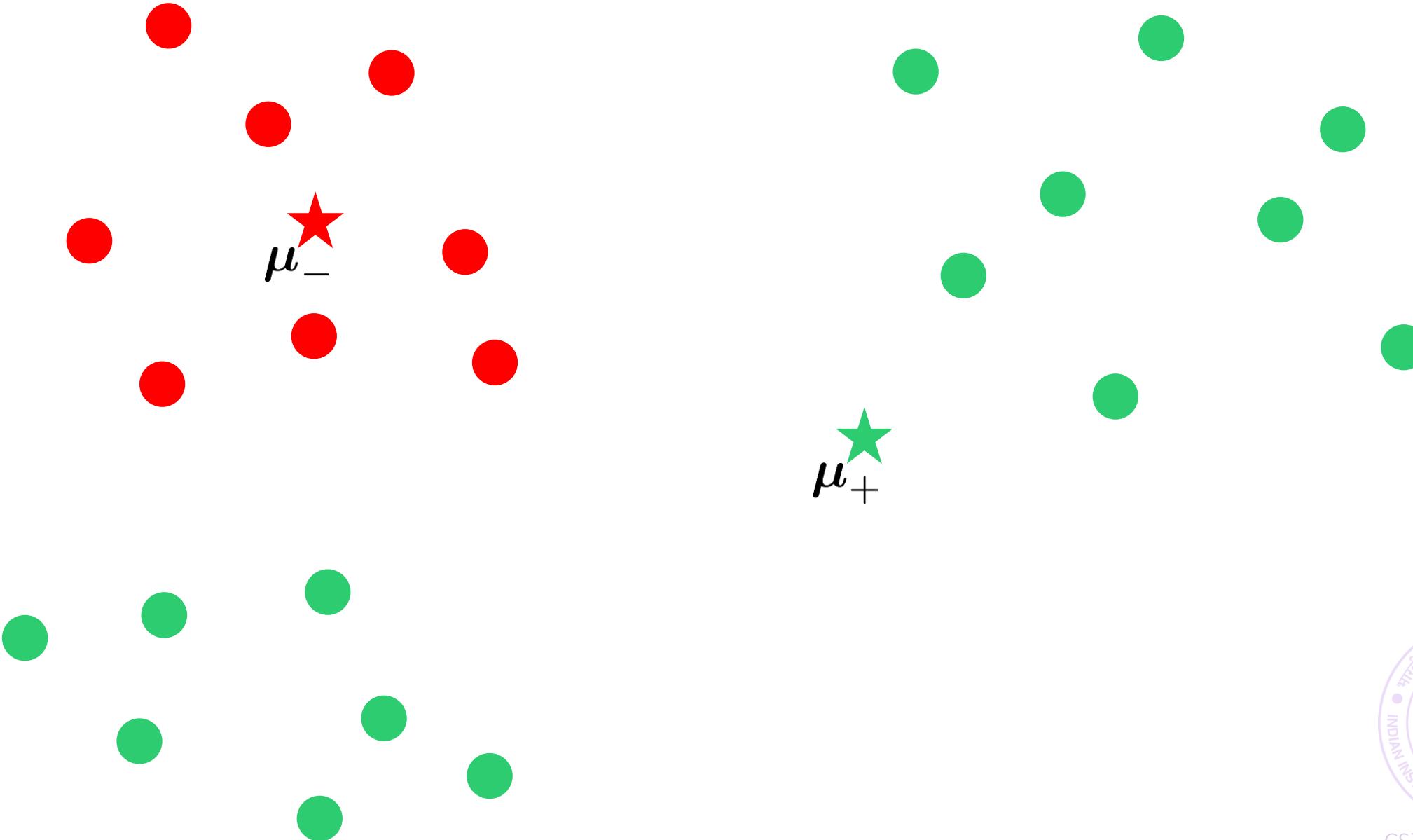
# Learning with Prototypes - Issues

200



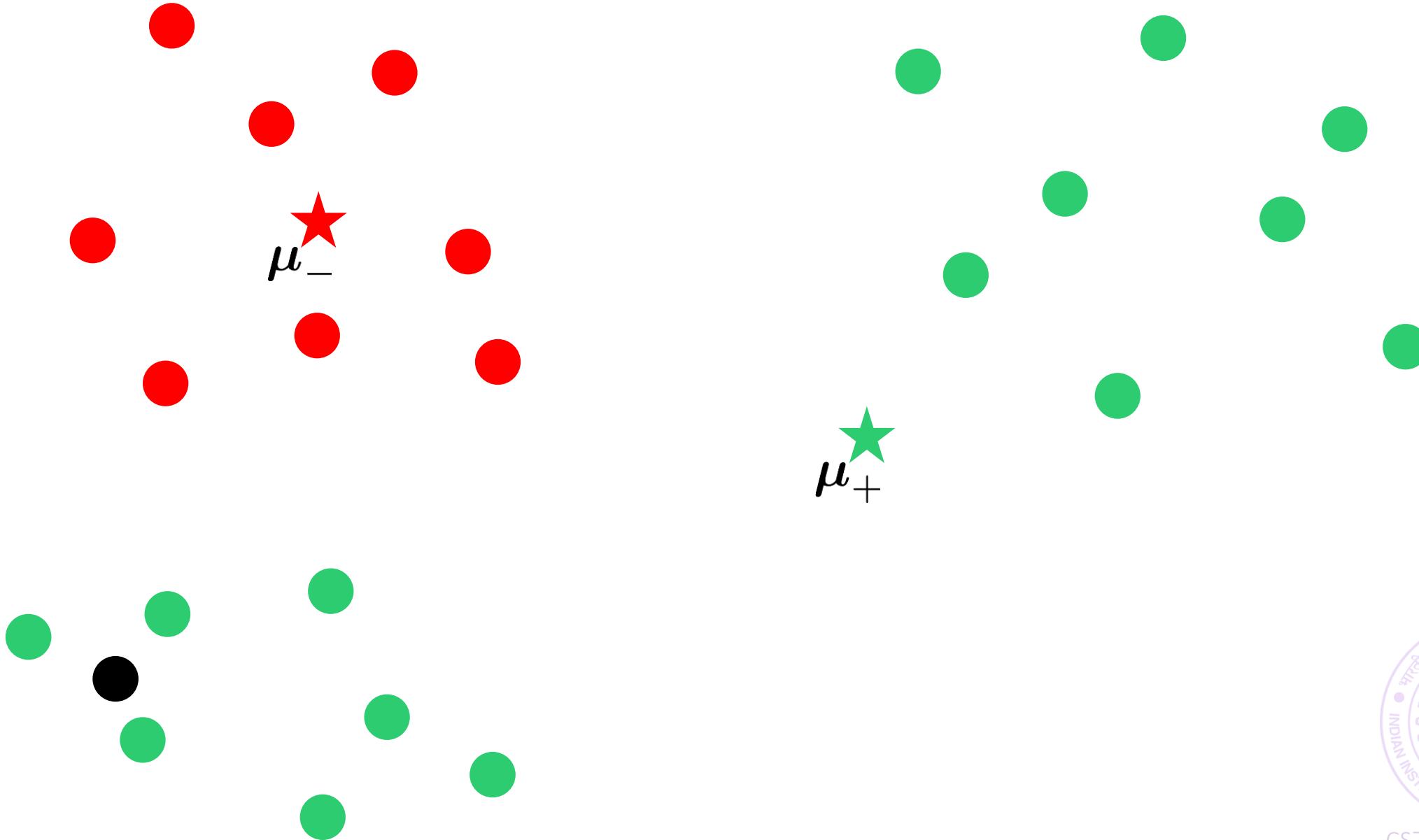
# Learning with Prototypes - Issues

200



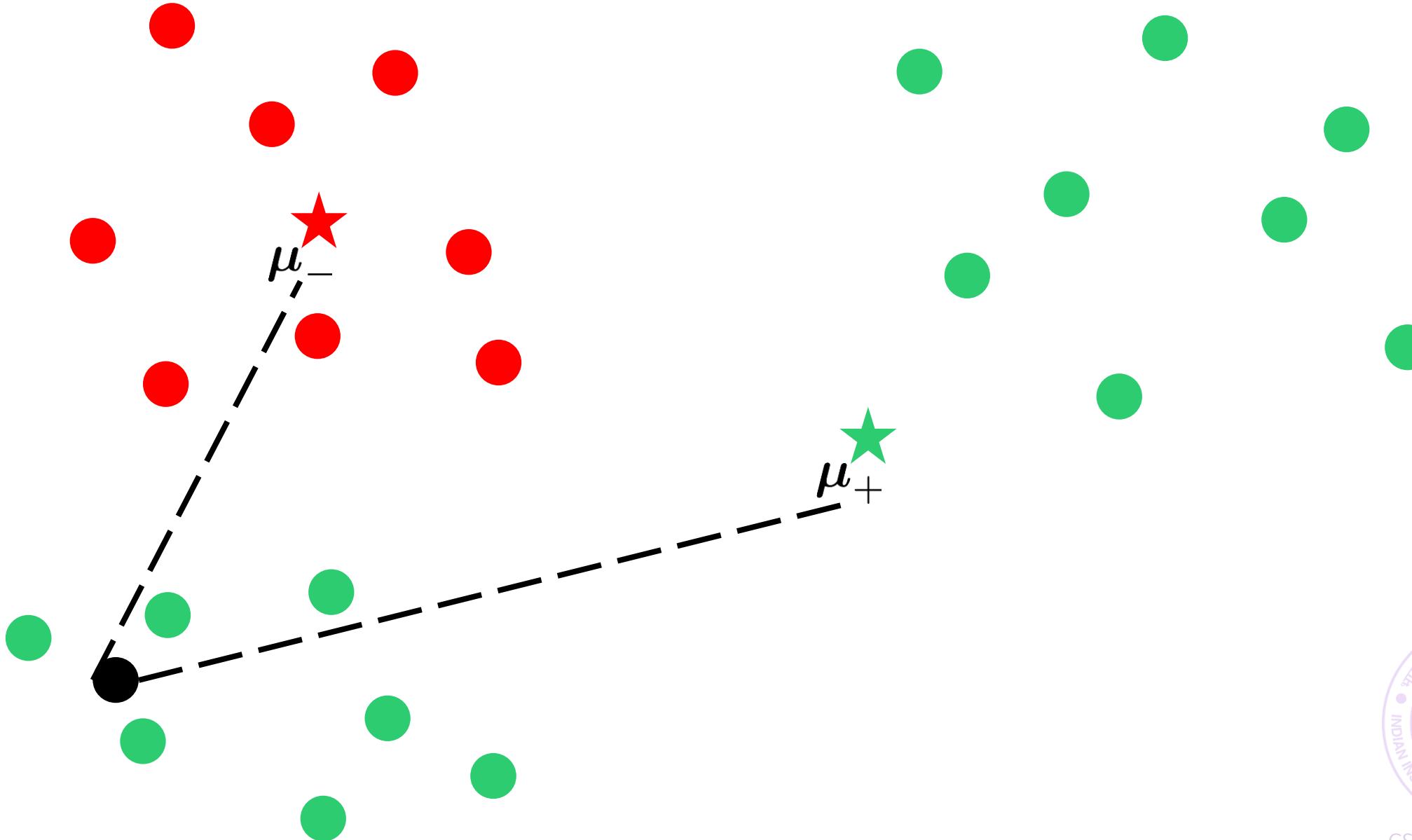
# Learning with Prototypes - Issues

200



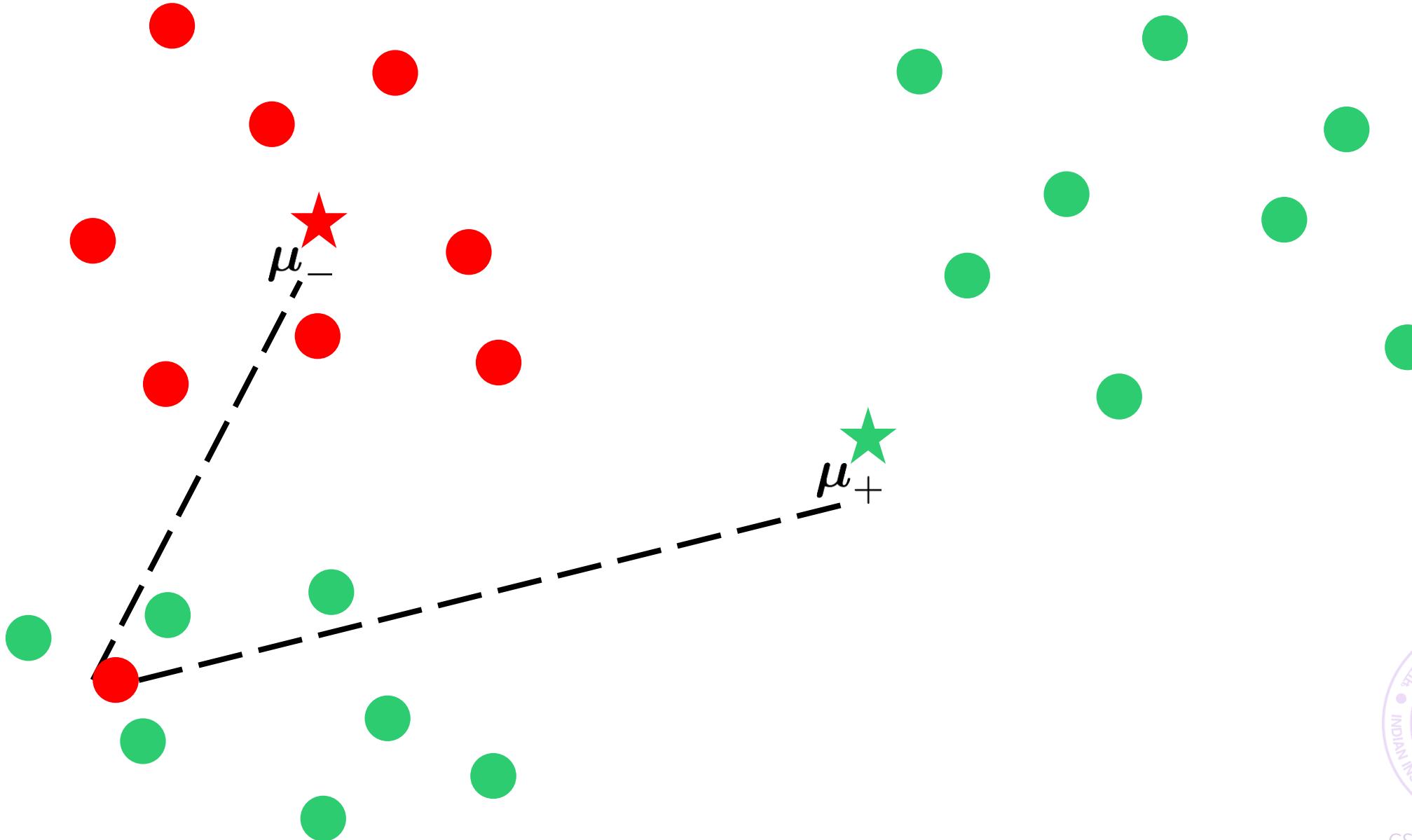
# Learning with Prototypes - Issues

200



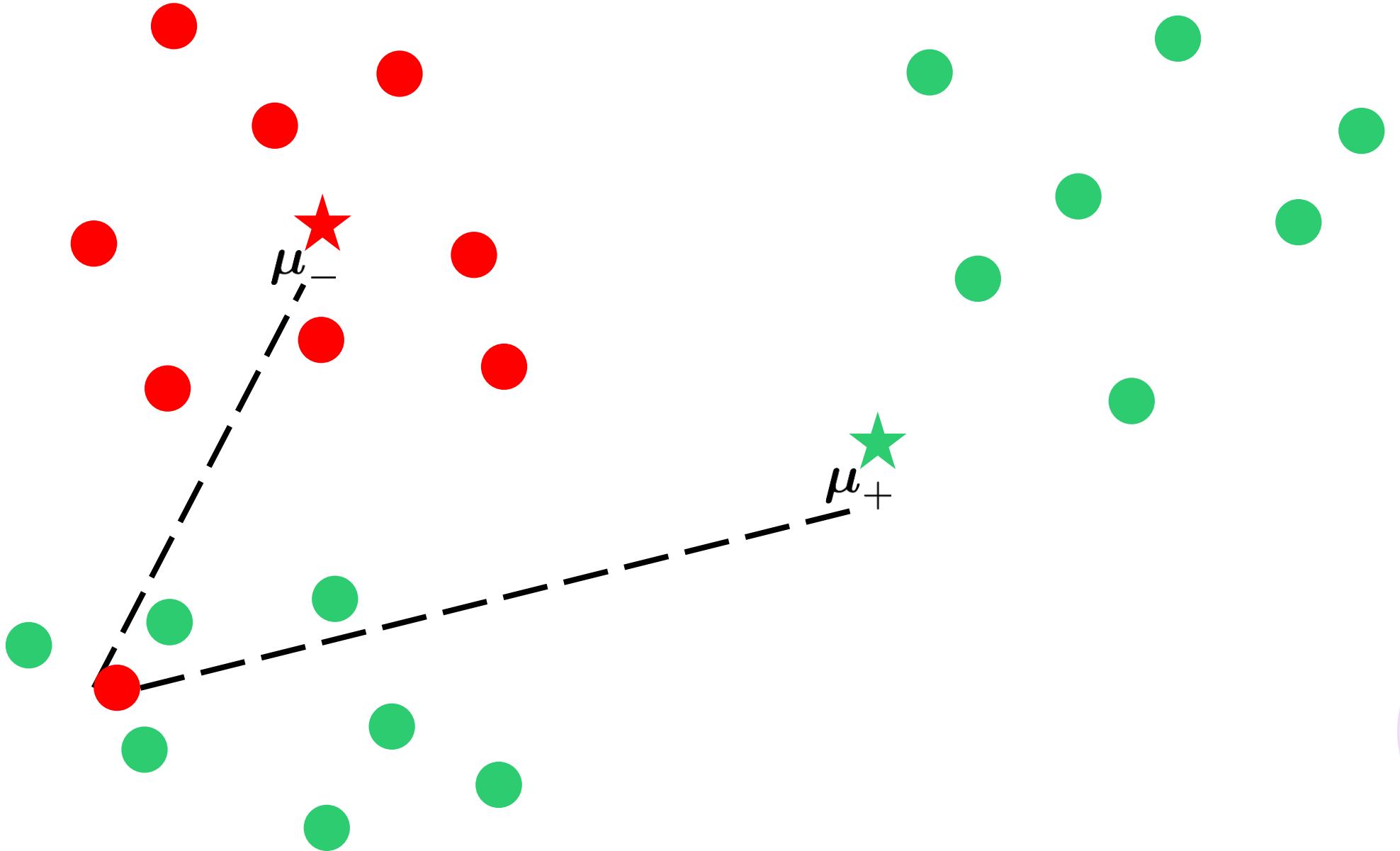
# Learning with Prototypes - Issues

200



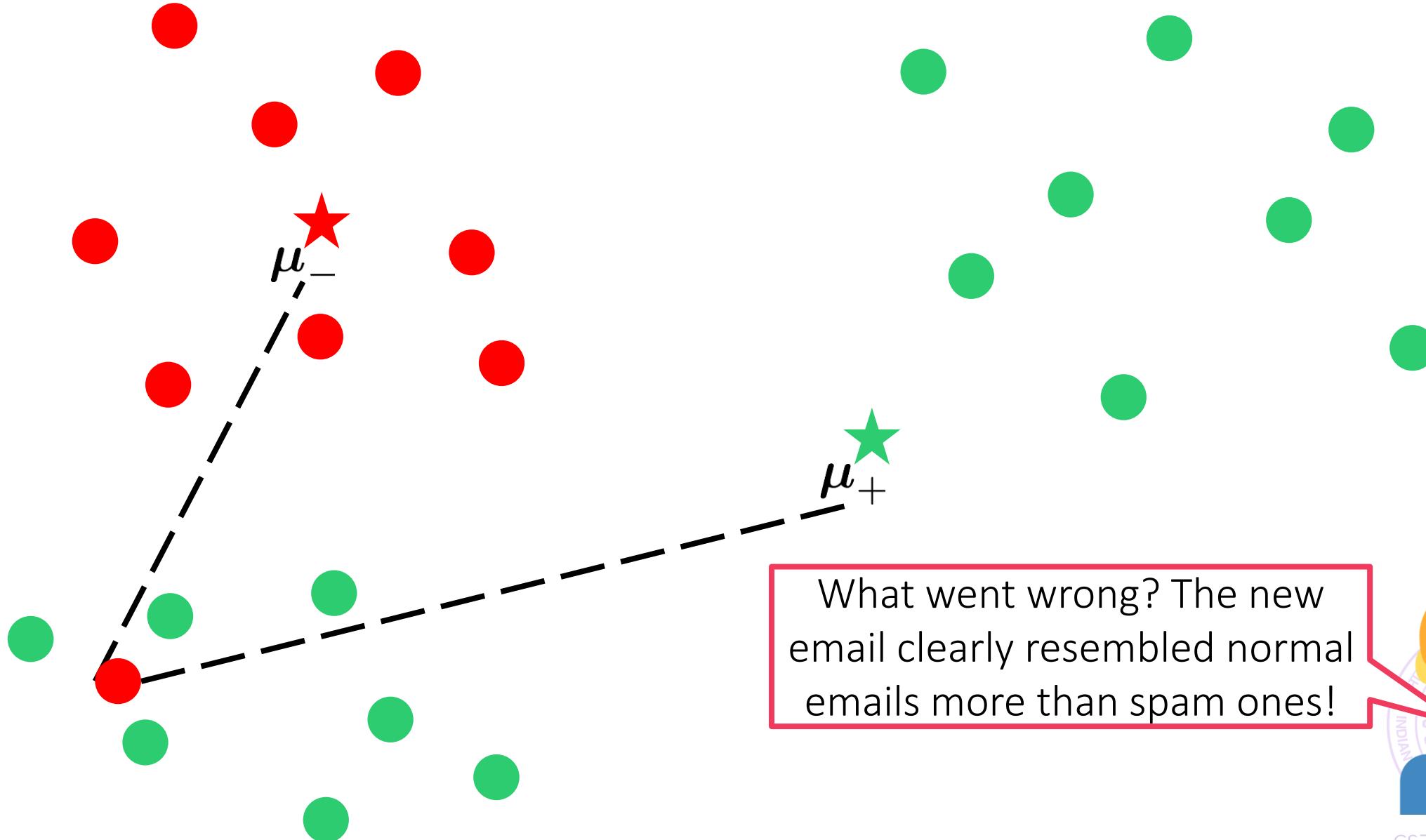
# Learning with Prototypes - Issues

200

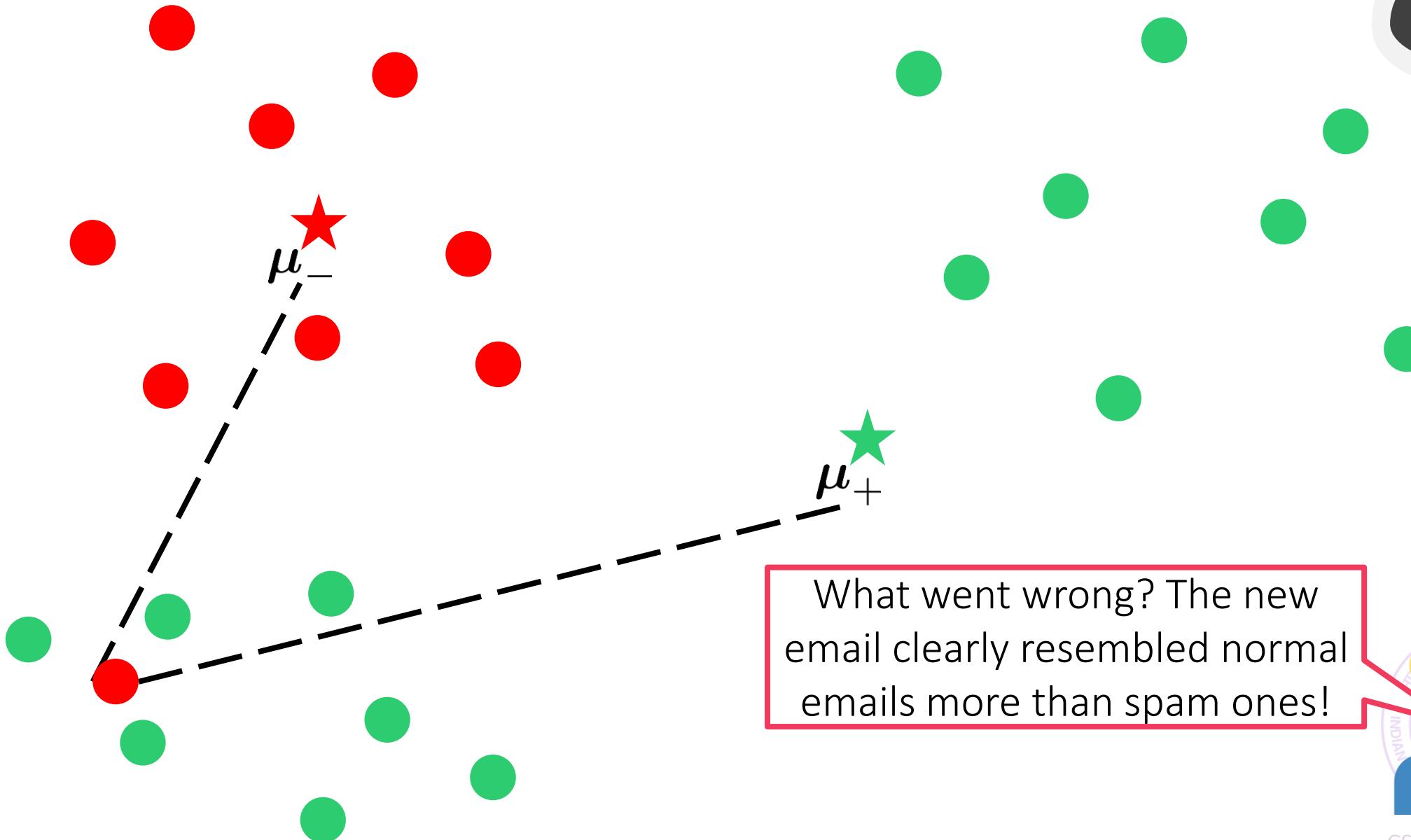


# Learning with Prototypes - Issues

200

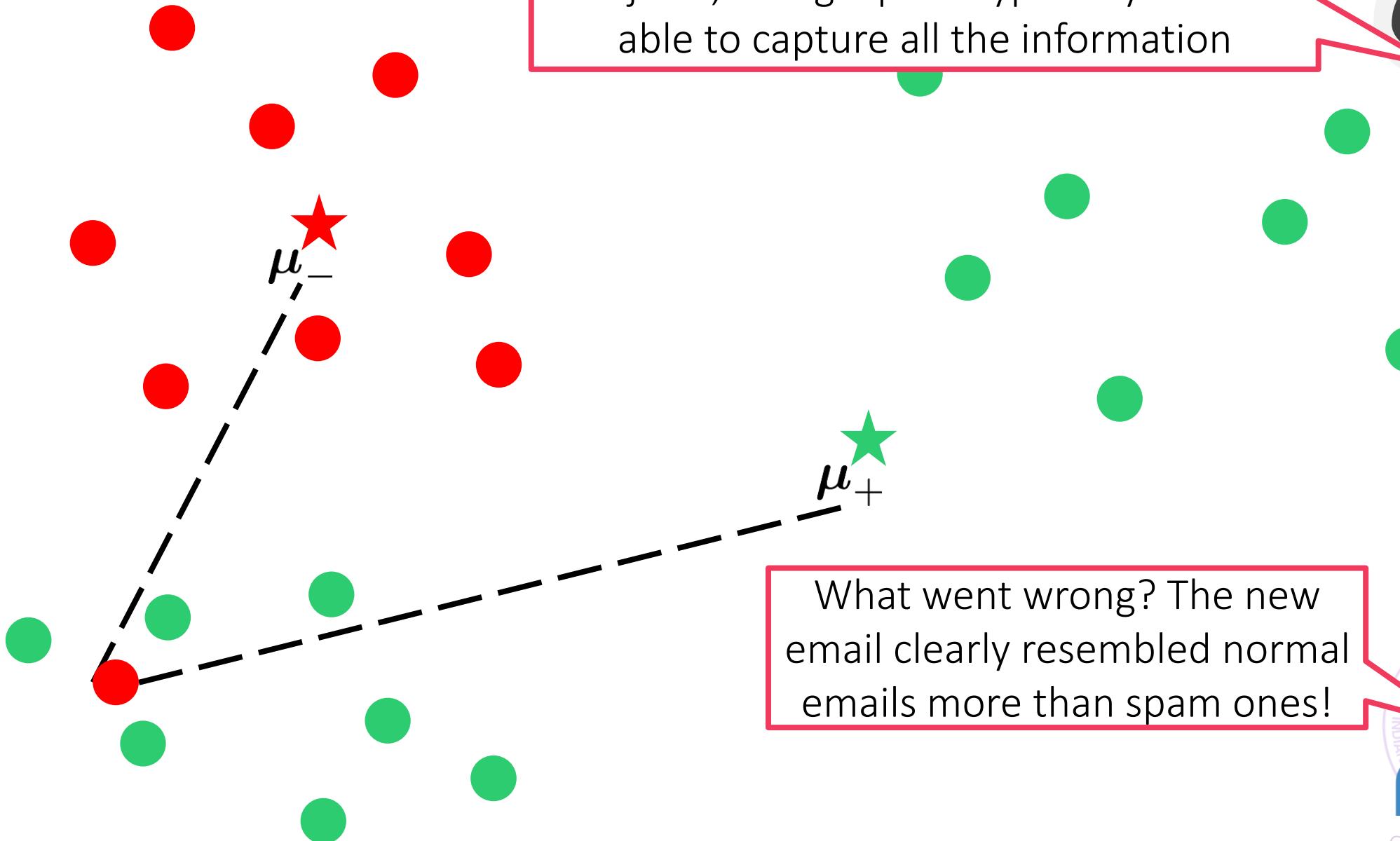
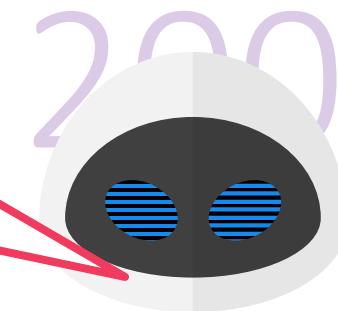


# Learning with Prototypes - Issues

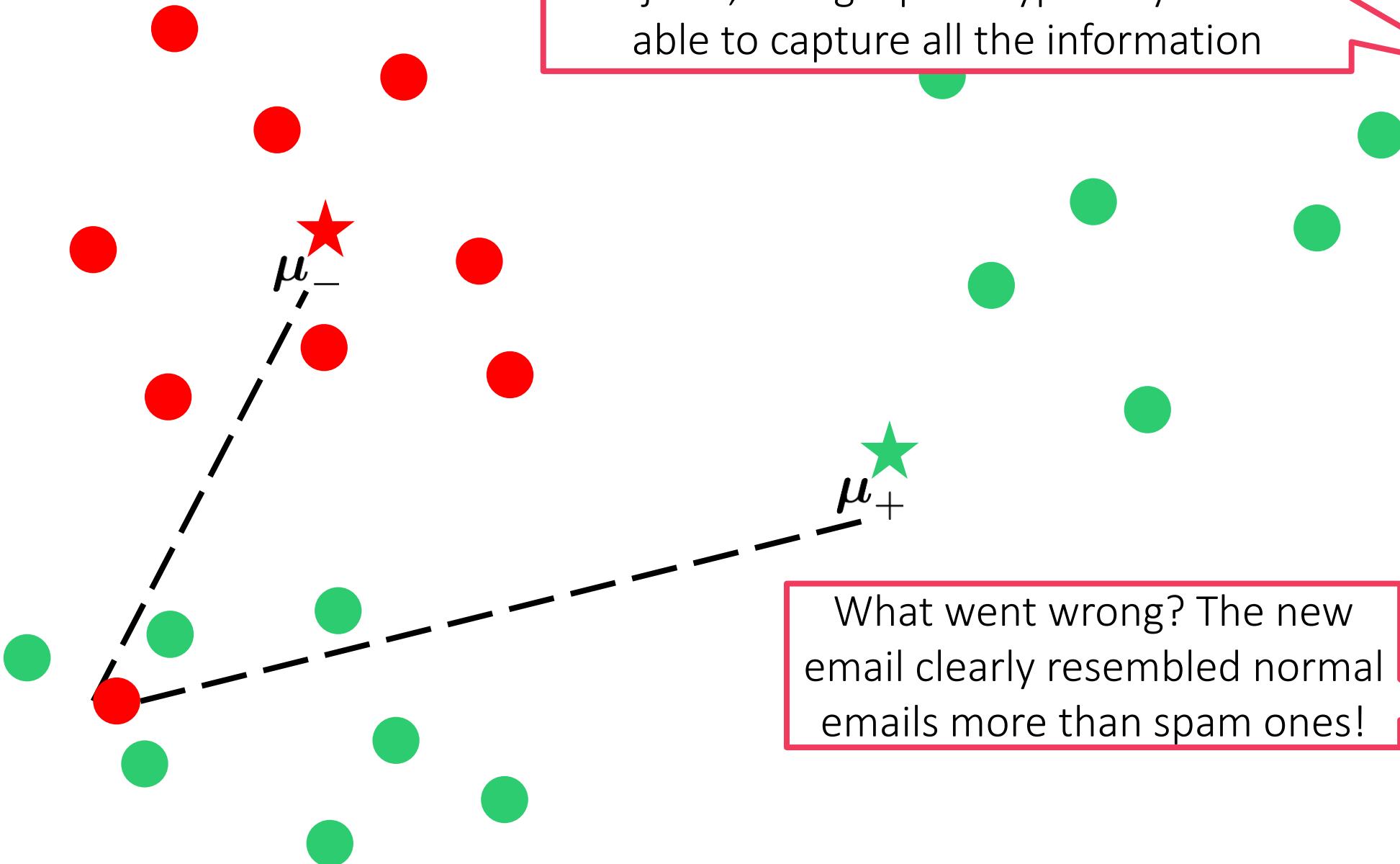


# Learning with Prototypes

If there is too much diversity in a class of objects, a single prototype may not be able to capture all the information

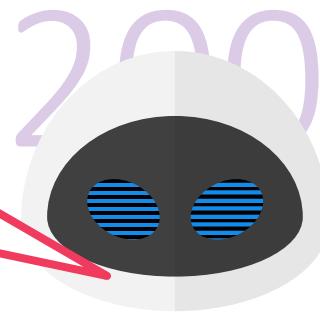
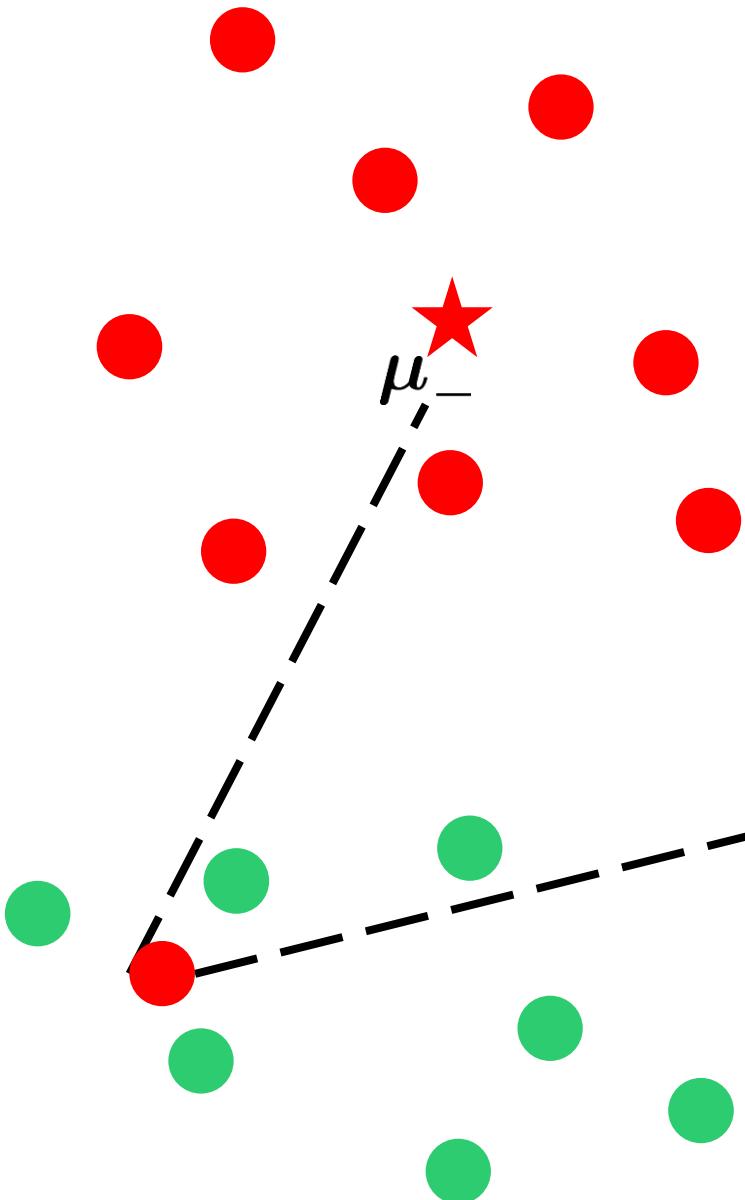


# Learning with Prototypes

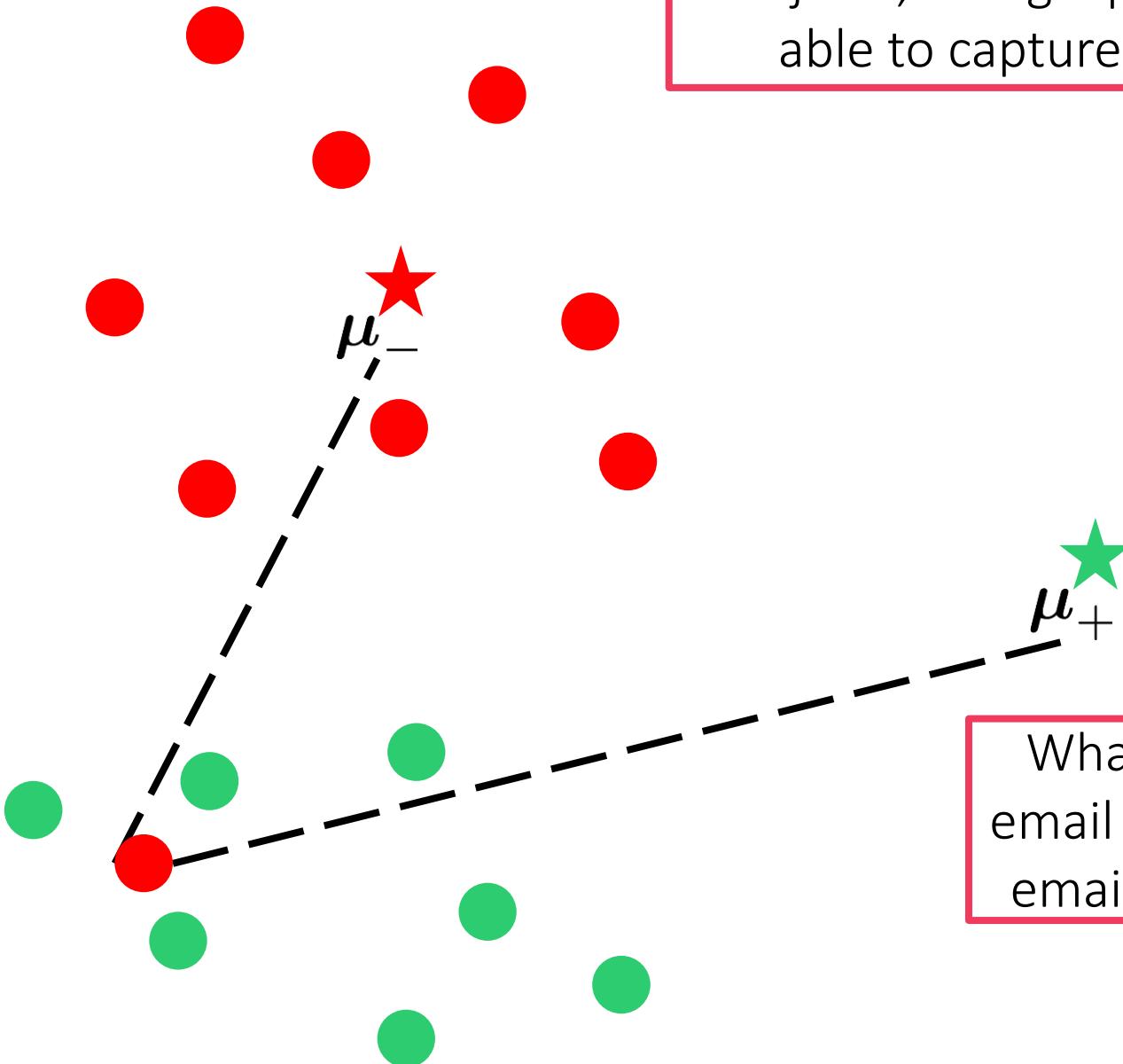


# Learning with Prototypes

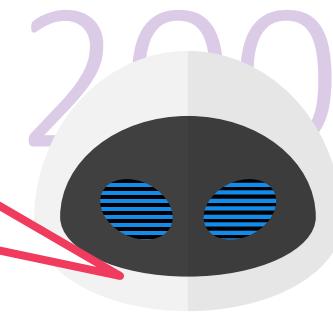
If there is too much diversity in a class of objects, a single prototype may not be able to capture all the information



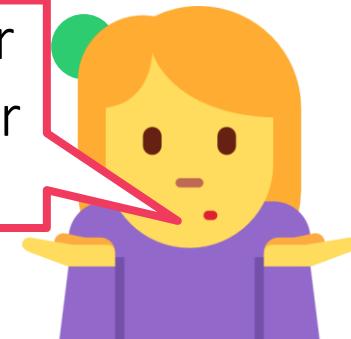
# Learning with Prototypes



If there is too much diversity in a class of objects, a single prototype may not be able to capture all the information



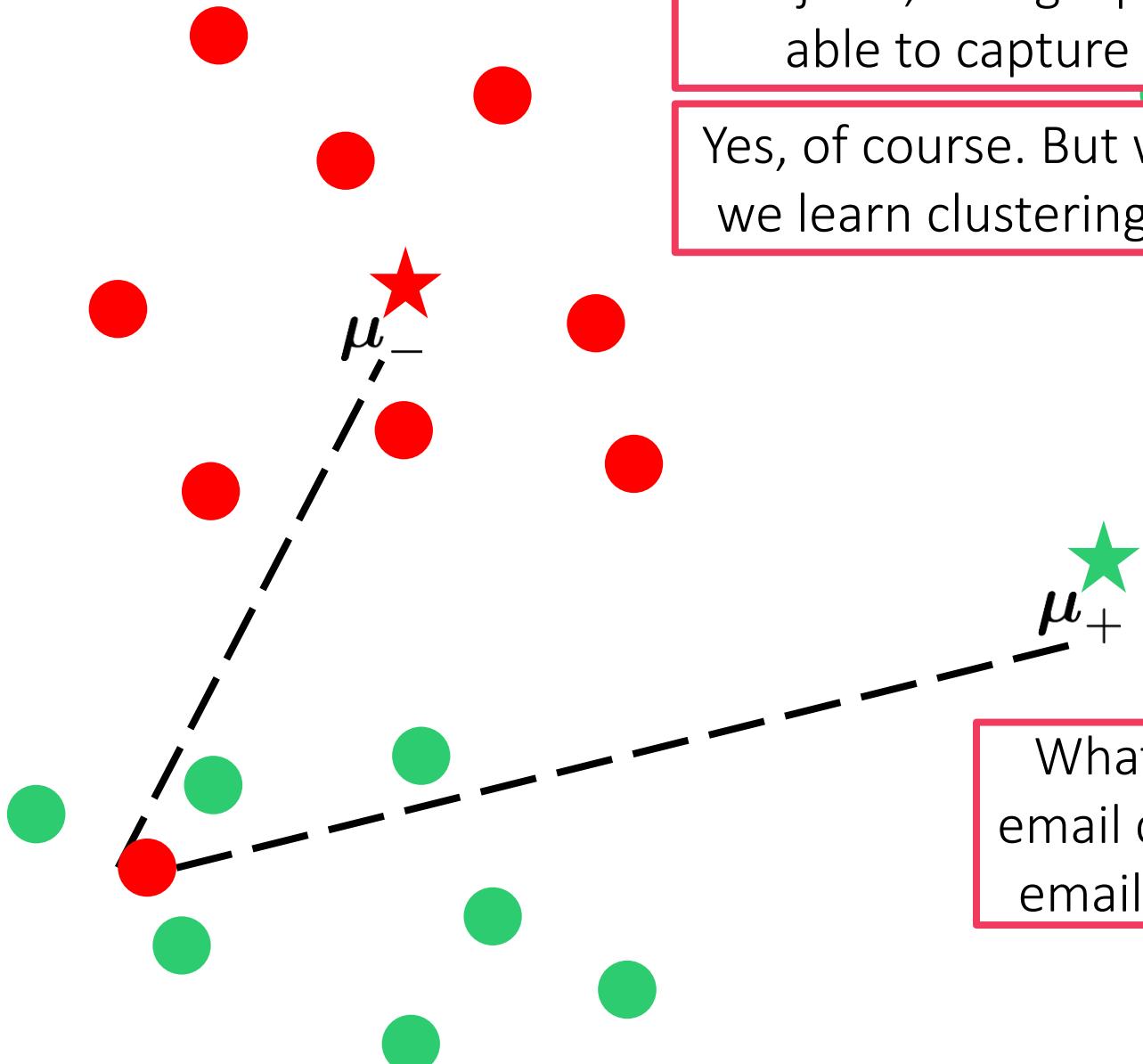
Can we have two or more prototypes for the normal class?



What went wrong? The new email clearly resembled normal emails more than spam ones!



# Learning with Prototypes

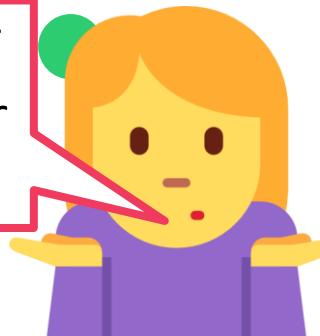
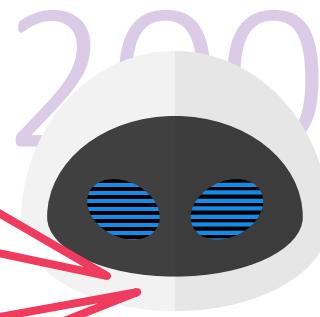


If there is too much diversity in a class of objects, a single prototype may not be able to capture all the information

Yes, of course. But we will have to wait till we learn clustering before we can do so.

Can we have two or more prototypes for the normal class?

What went wrong? The new email clearly resembled normal emails more than spam ones!



# Learning with Prototypes - Issues

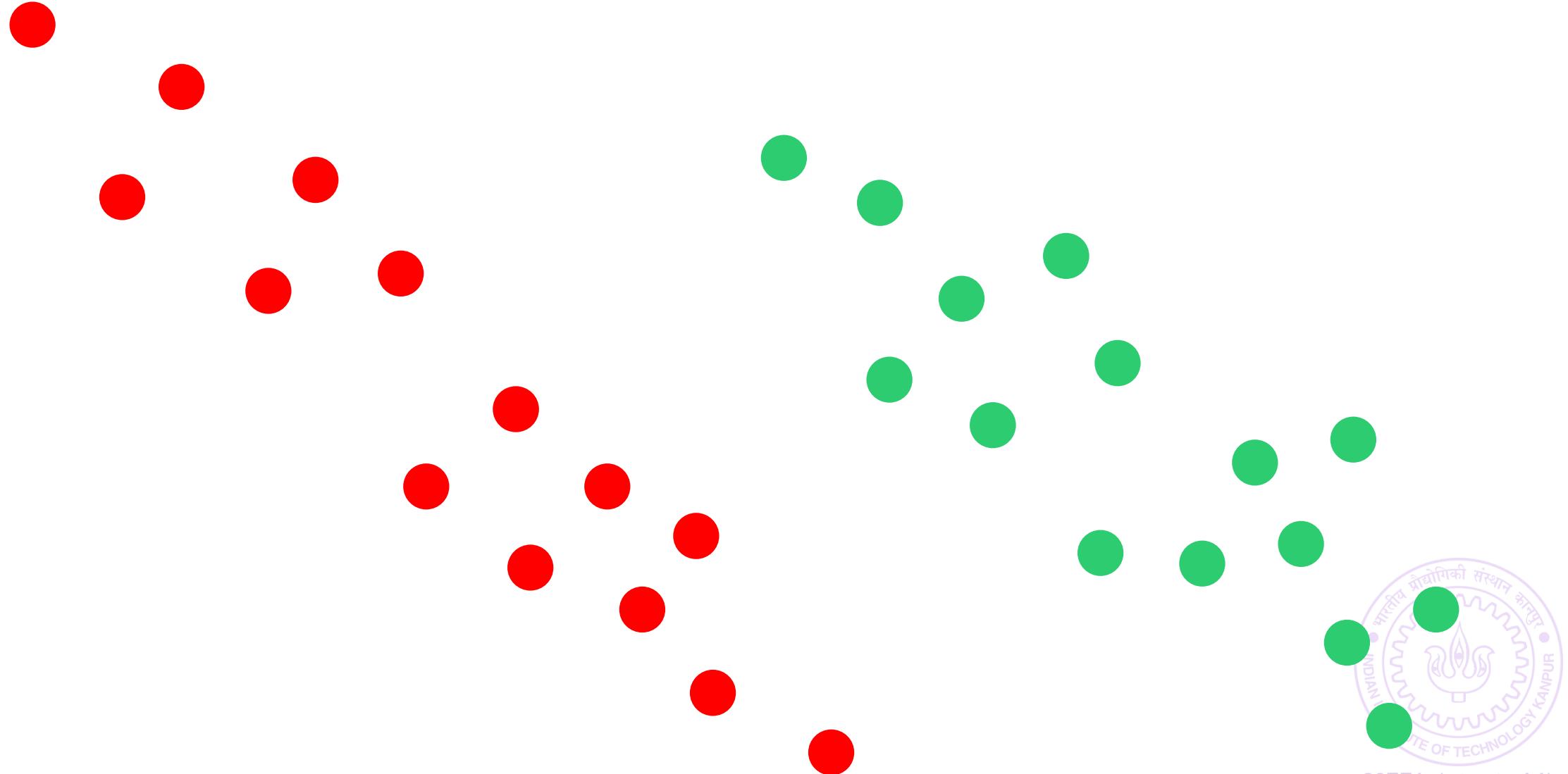
217



CS771: Intro to ML

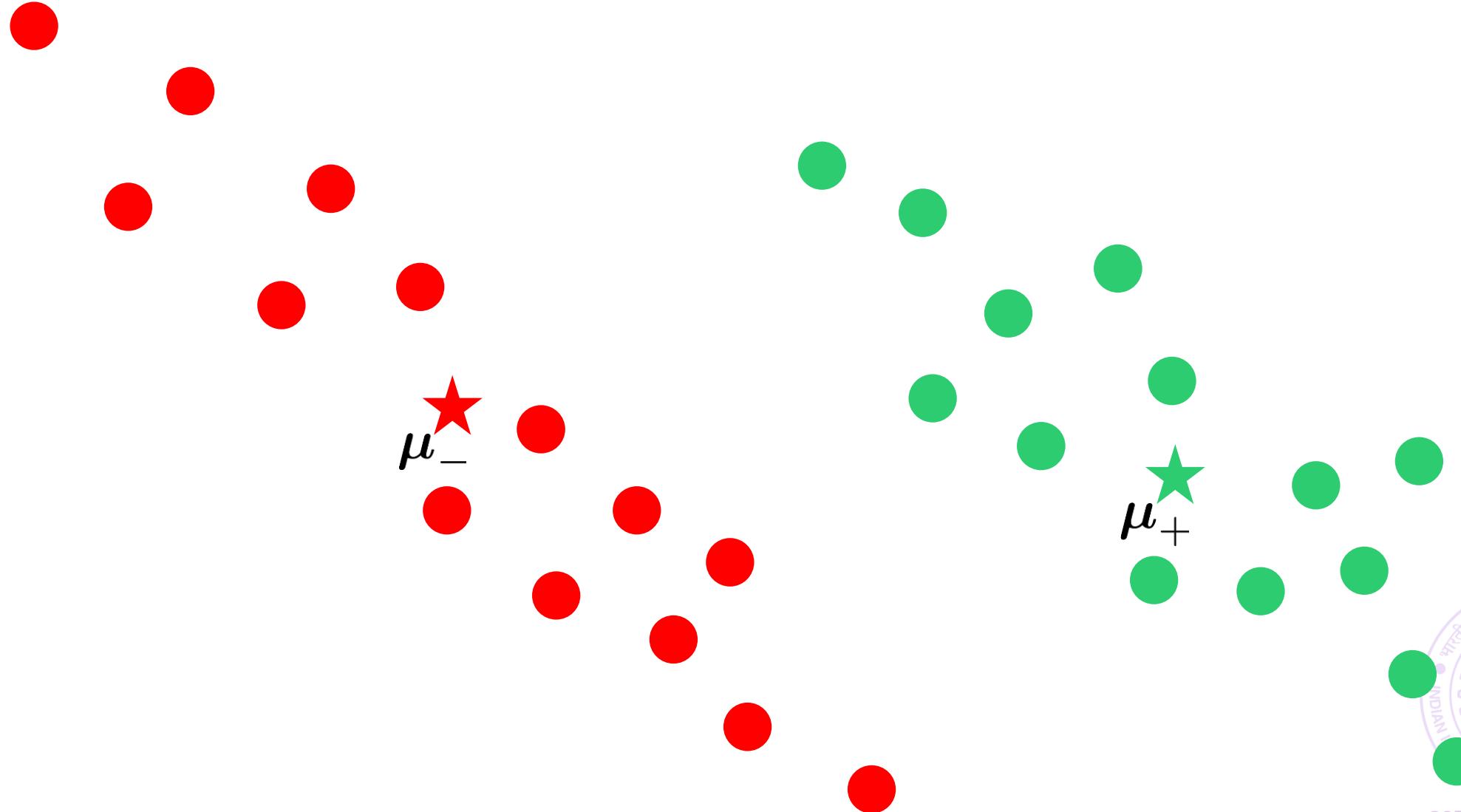
# Learning with Prototypes - Issues

217



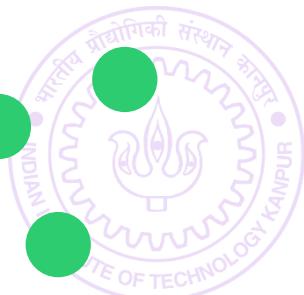
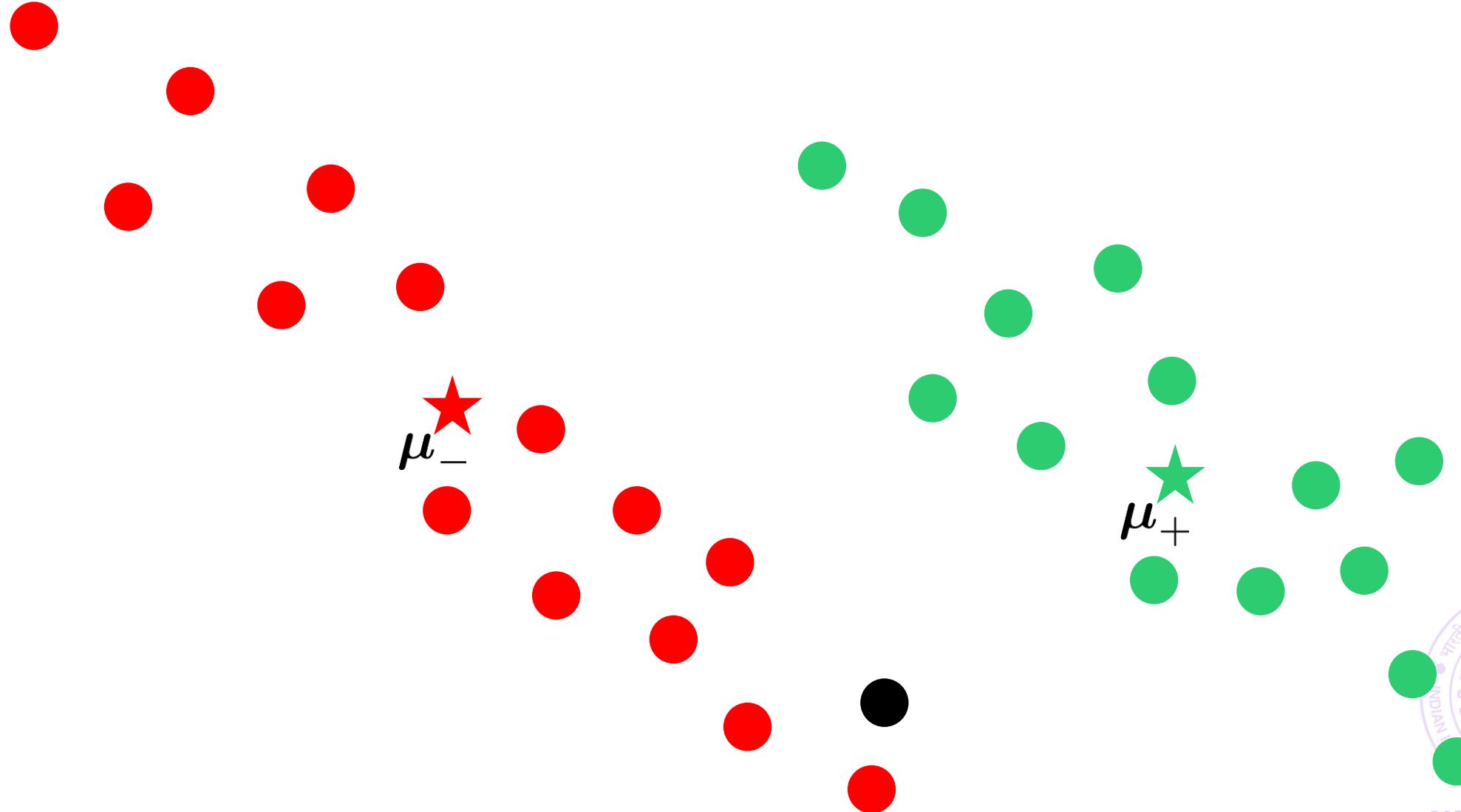
# Learning with Prototypes - Issues

217



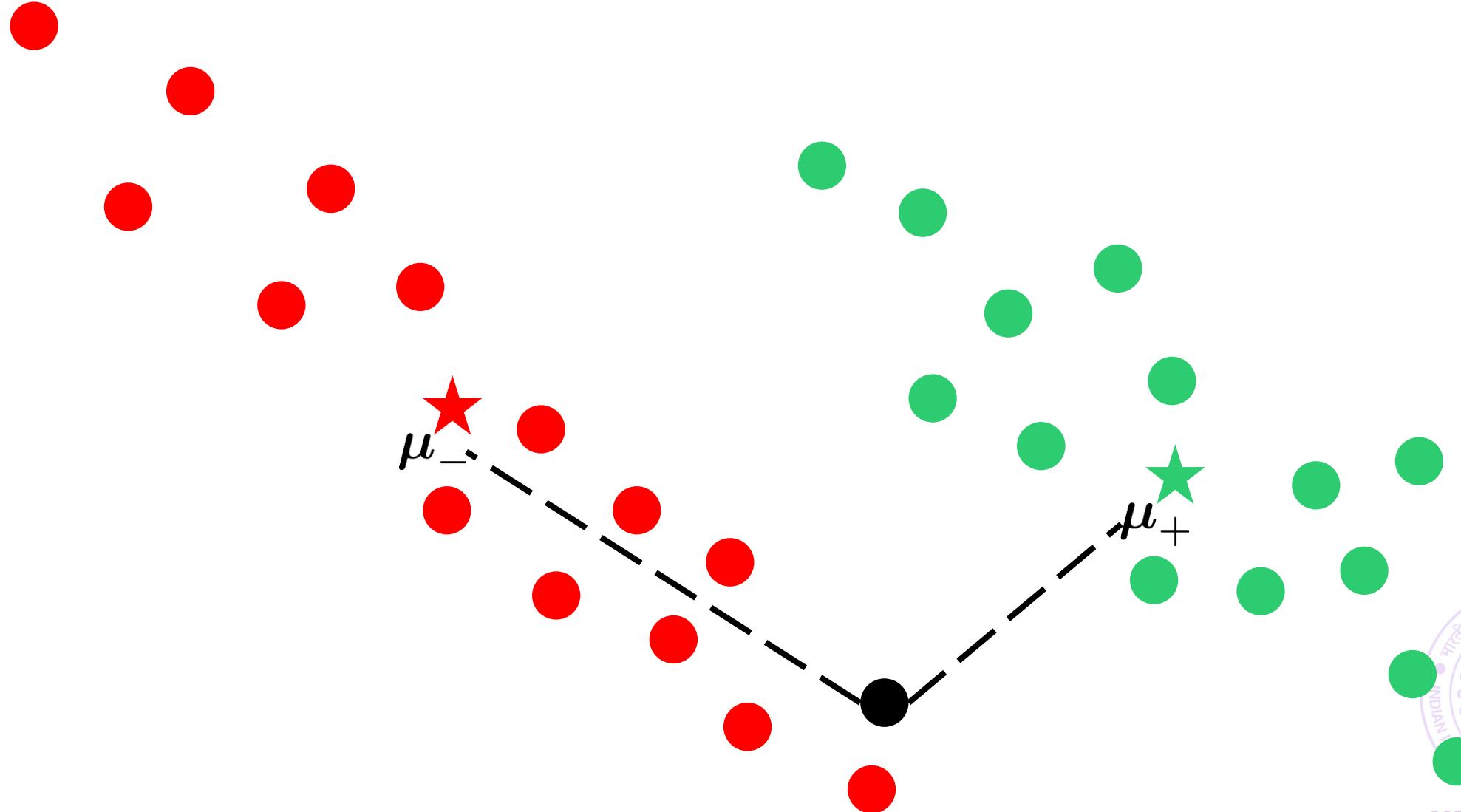
# Learning with Prototypes - Issues

217



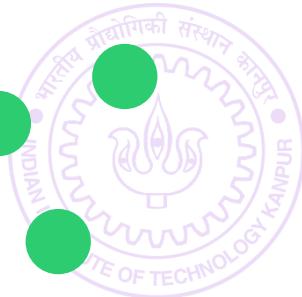
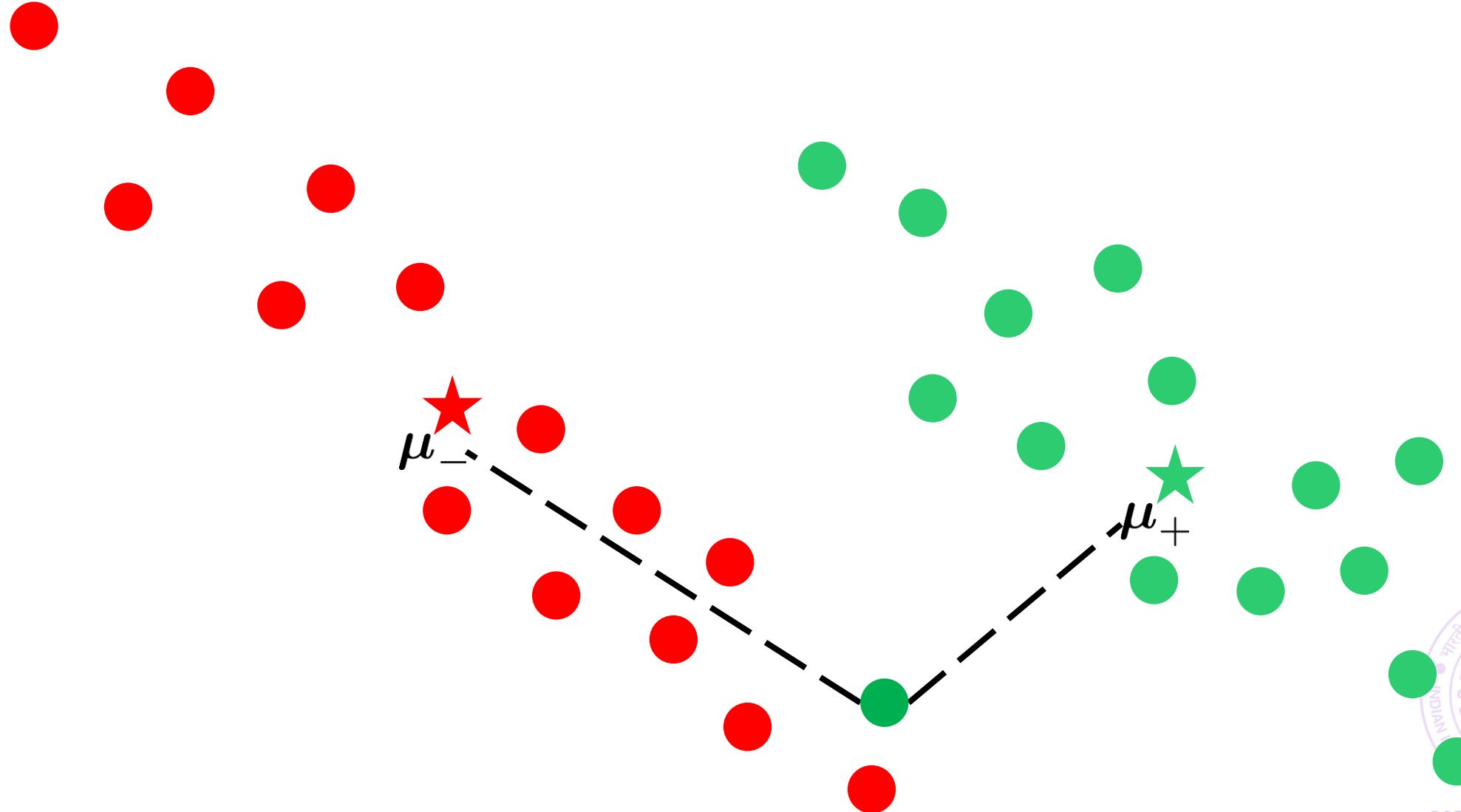
# Learning with Prototypes - Issues

217



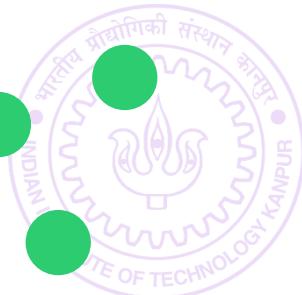
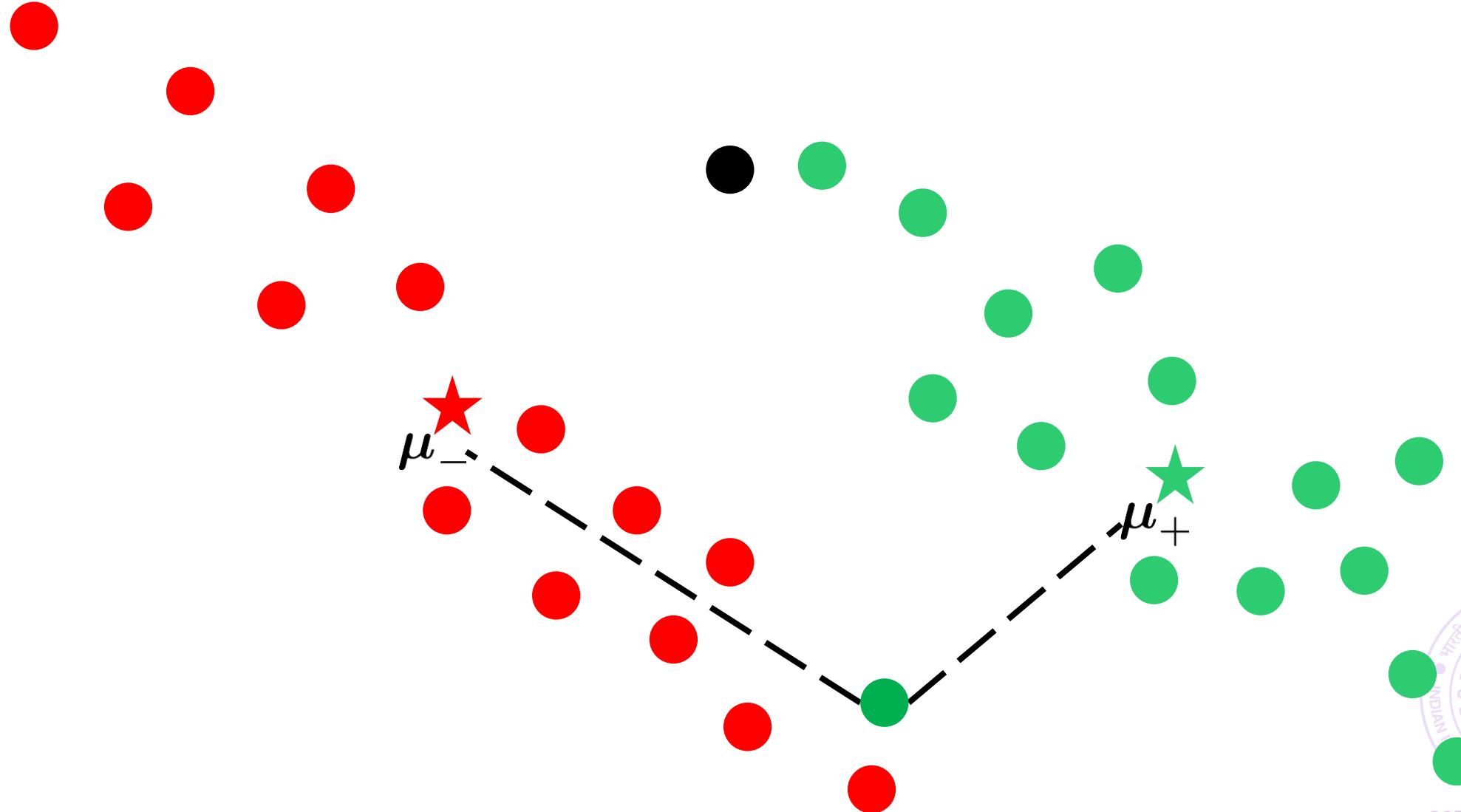
# Learning with Prototypes - Issues

217



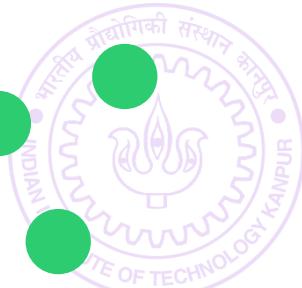
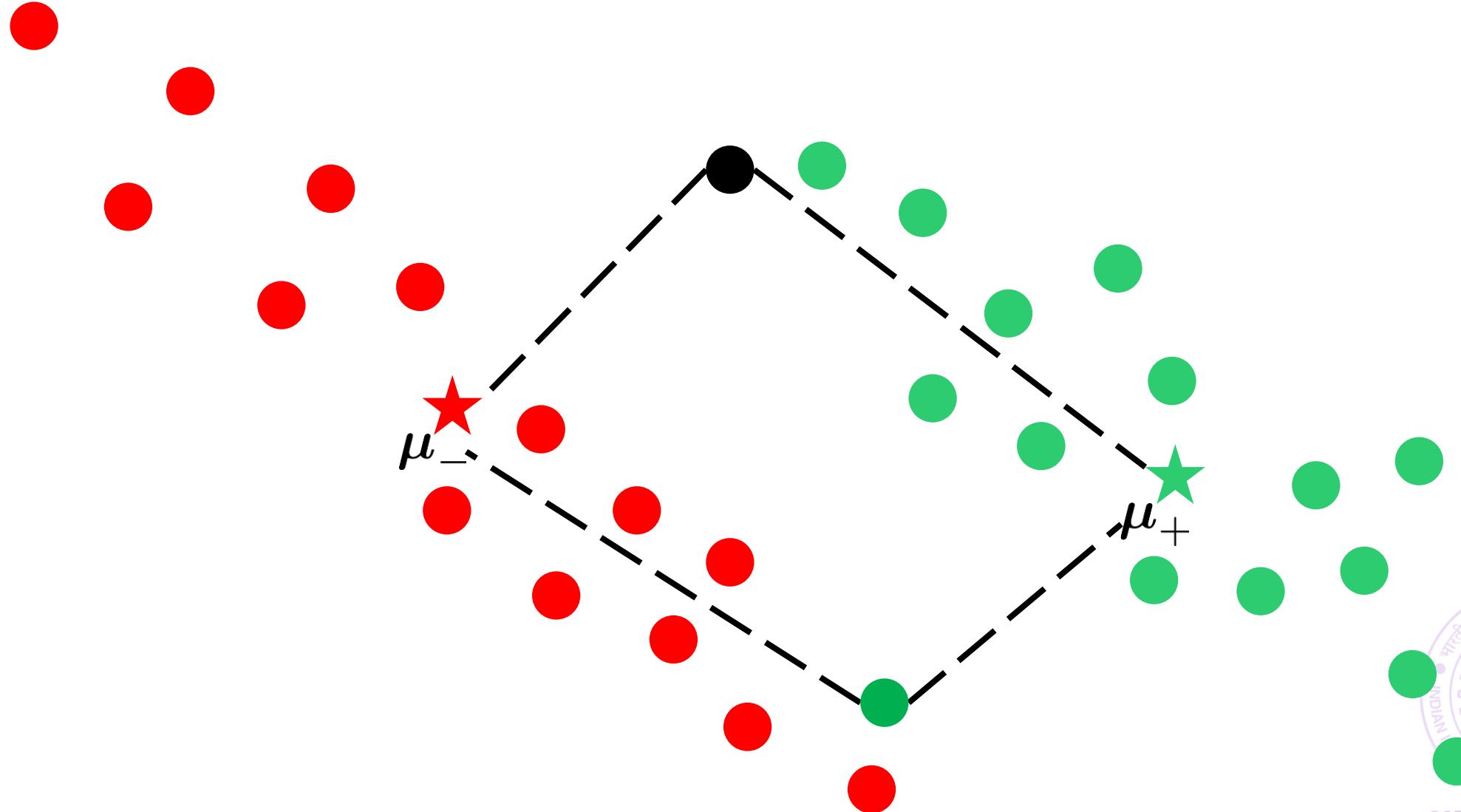
# Learning with Prototypes - Issues

217



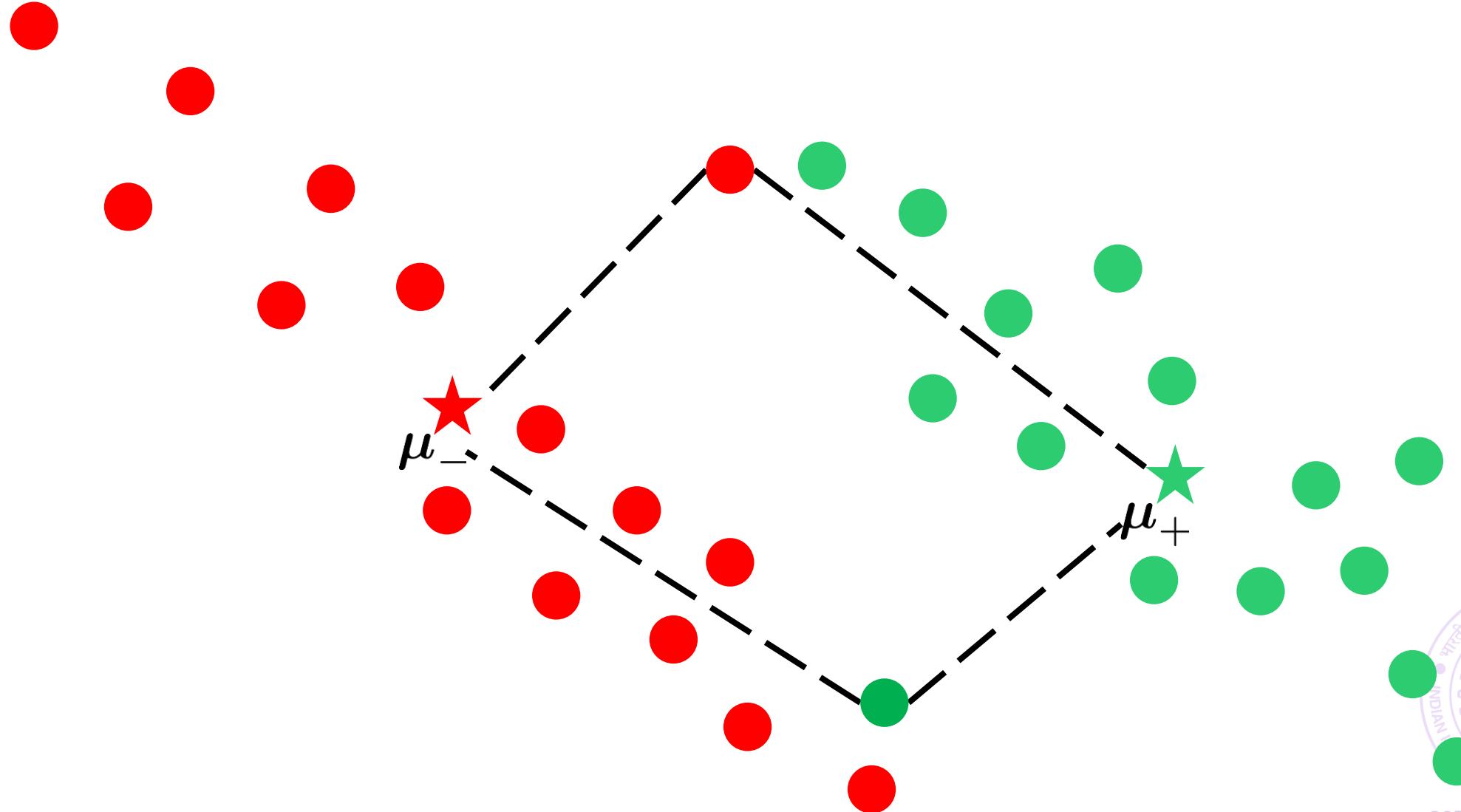
# Learning with Prototypes - Issues

217



# Learning with Prototypes - Issues

217

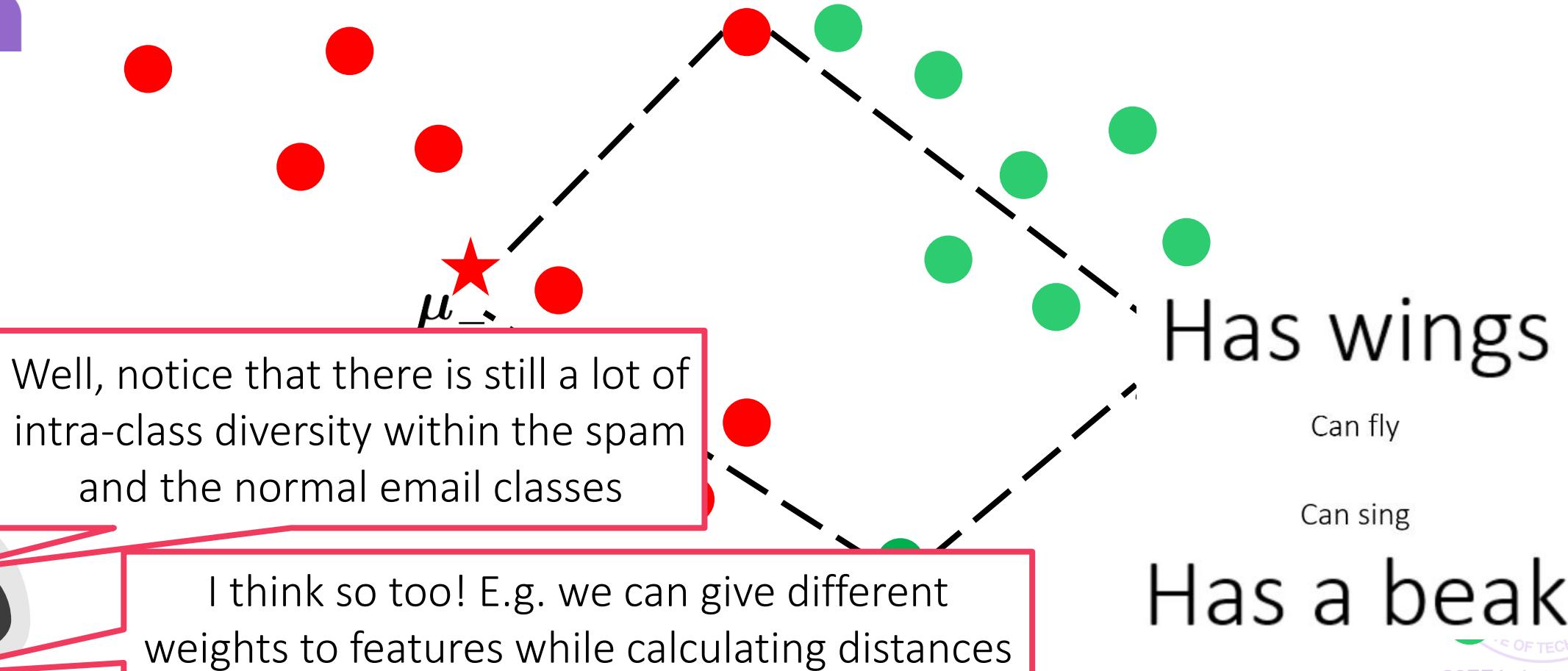


# Learning with Issues - Issues



I think this time another issue is how we calculated distances. Can we use non-Euclidean distances?

What went wrong this time?



# Learning with Issues - Issues



I think this time another issue is how we calculated distances. Can we use non-Euclidean distances?

What went wrong this time?



$$d(\mathbf{x}^1, \mathbf{x}^2) = \sqrt{\sum_{j=1}^d w_j \cdot (\mathbf{x}_j^1 - \mathbf{x}_j^2)^2}$$

$\mu_{\_}$

Well, notice that there is still a lot of intra-class diversity within the spam and the normal email classes

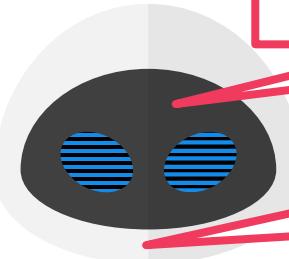
I think so too! E.g. we can give different weights to features while calculating distances

Has wings

Can fly

Can sing

Has a beak



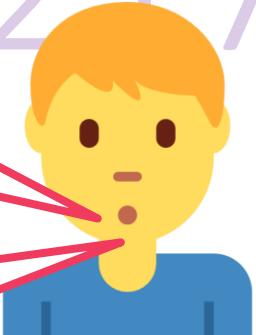
# Learning with Issues - Issues



I think this time another issue is how we calculated distances. Can we use non-Euclidean distances?

Yes, but let us revisit this issue later

What went wrong this time?



Can we learn these weights too?

$$d(\mathbf{x}^1, \mathbf{x}^2) = \sqrt{\sum_{j=1}^d w_j \cdot (\mathbf{x}_j^1 - \mathbf{x}_j^2)^2}$$

$\mu_-$

Well, notice that there is still a lot of intra-class diversity within the spam and the normal email classes

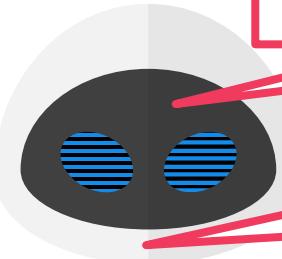
I think so too! E.g. we can give different weights to features while calculating distances

Has wings

Can fly

Can sing

Has a beak



# Learning with Prototypes - Lessons

229

An extremely simple technique to classify data

Can do binary classification (2-classes) as well as multi-classification

Very compact, light-weight model (one prototype per class)

Actually used in industrial applications like extreme classification

Actually state of the art if we have very few data points for a class

For example, if we have very few spam emails in training data

Works well when class data points are packed closely – less diversity

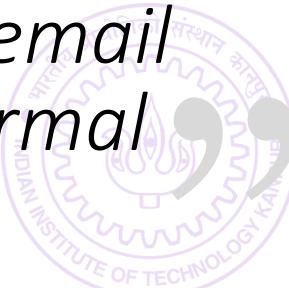
Improvements possible using multiple prototypes, metric learning  
(using a non-Euclidean distance function)



# Nearest Neighbour Classifier

- A really extreme form of learning with prototypes
- Recall that we commented that having multiple (say 2-3) prototypes may help when there is lots of diversity in a class
- With NN, every single training point becomes a prototype ☺
- The basic mantra here seems to be

‘ If the training email that most resembles a new email was spam, maybe the new email is spam too. Else, if a normal training email most resembles the new email, the new email should be normal ’



# Learning with the 1-NN Classifier

231



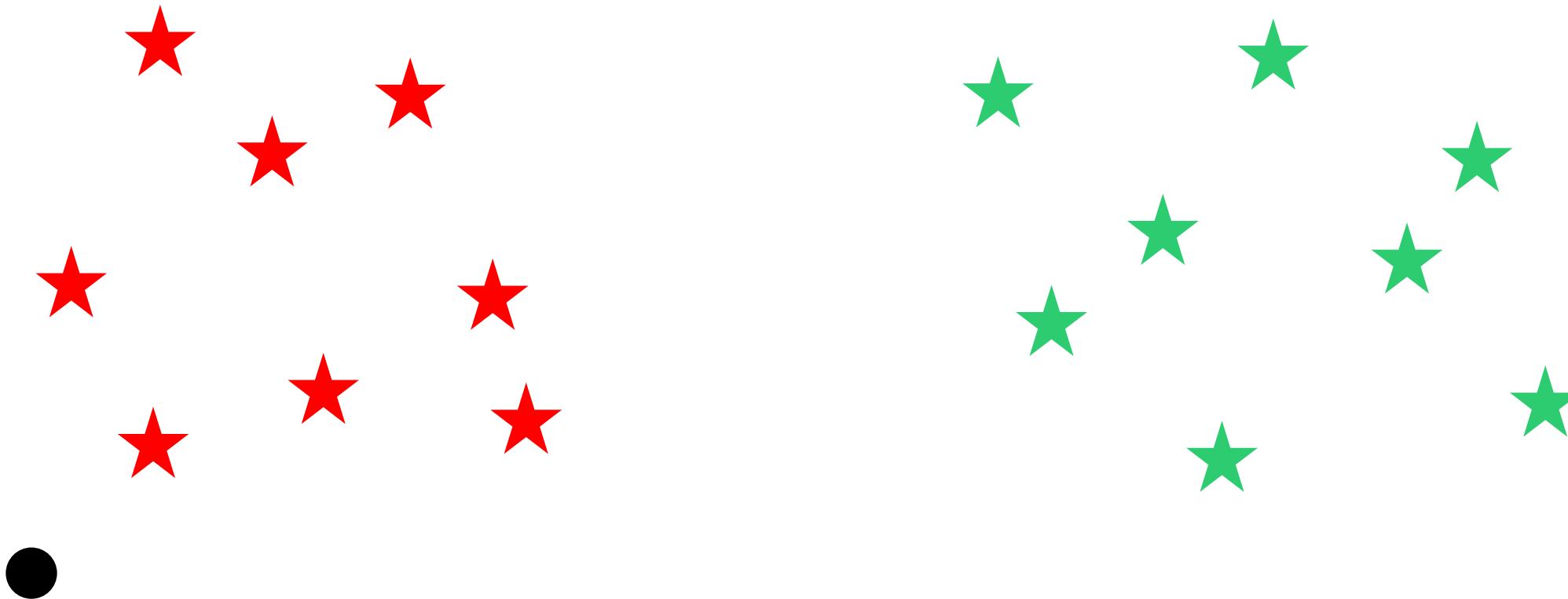
# Learning with the 1-NN Classifier

231



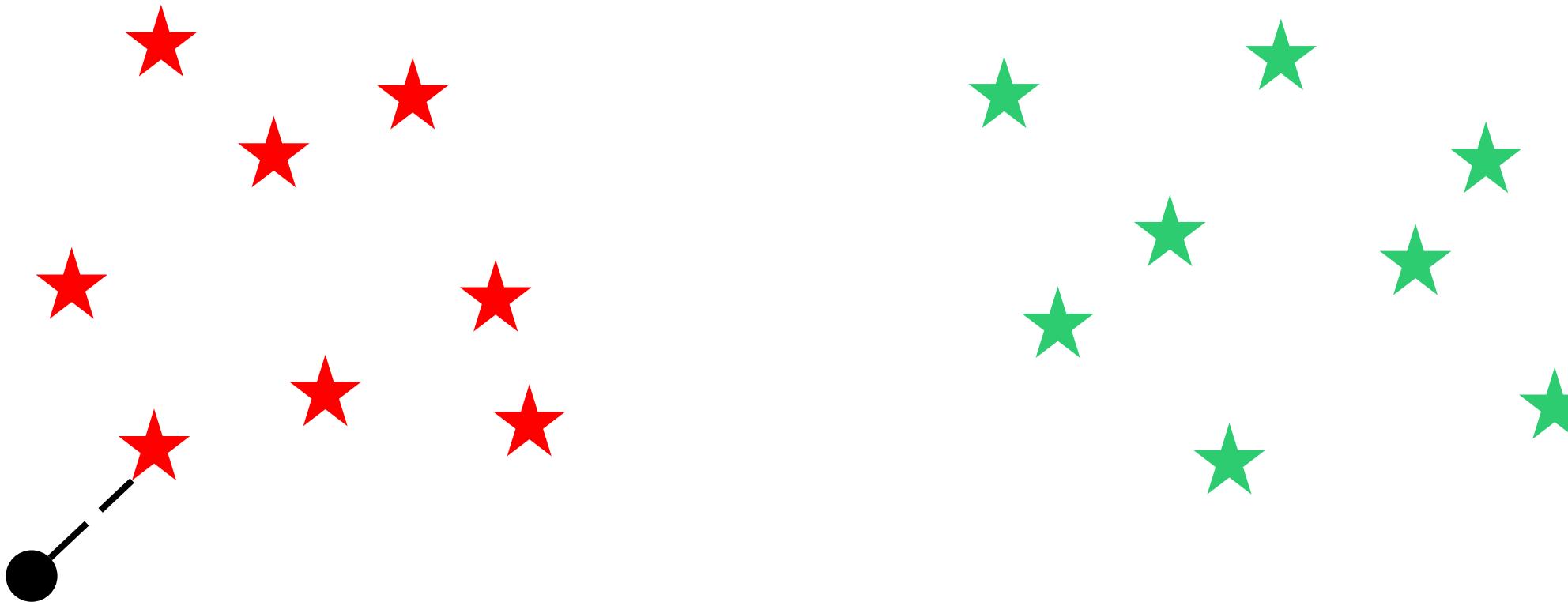
# Learning with the 1-NN Classifier

231



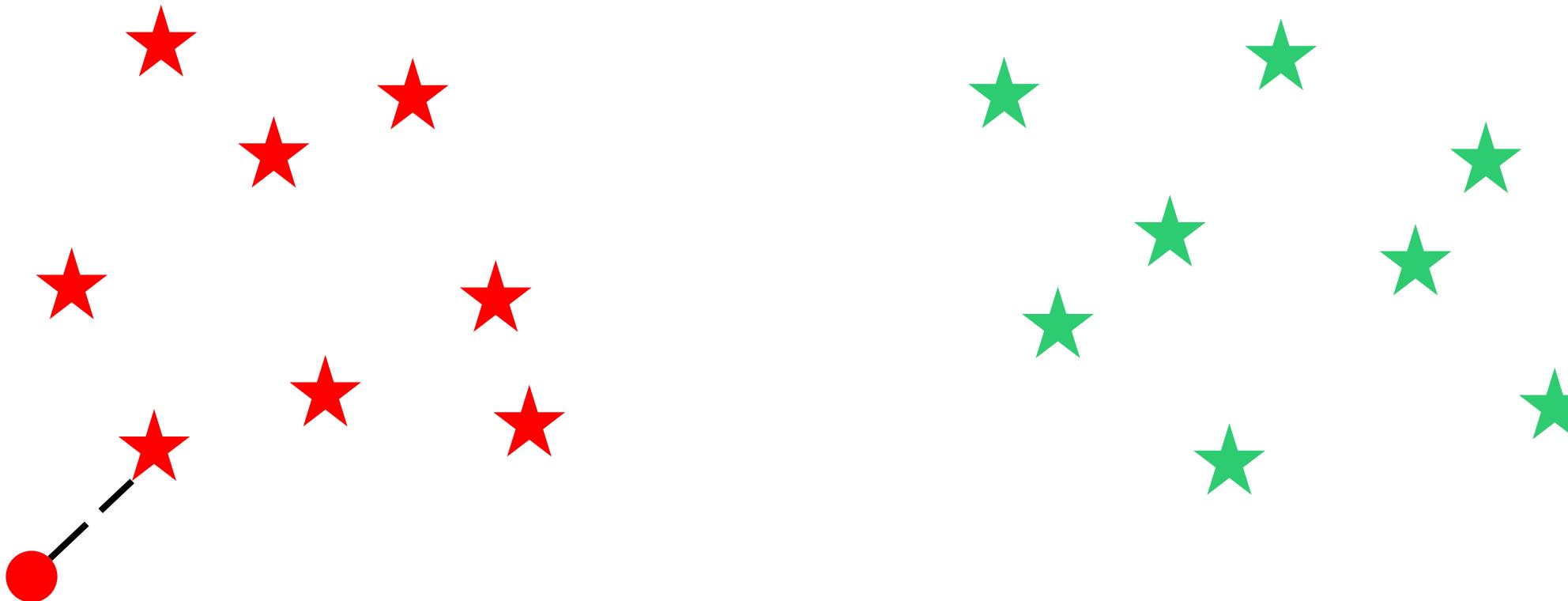
# Learning with the 1-NN Classifier

231



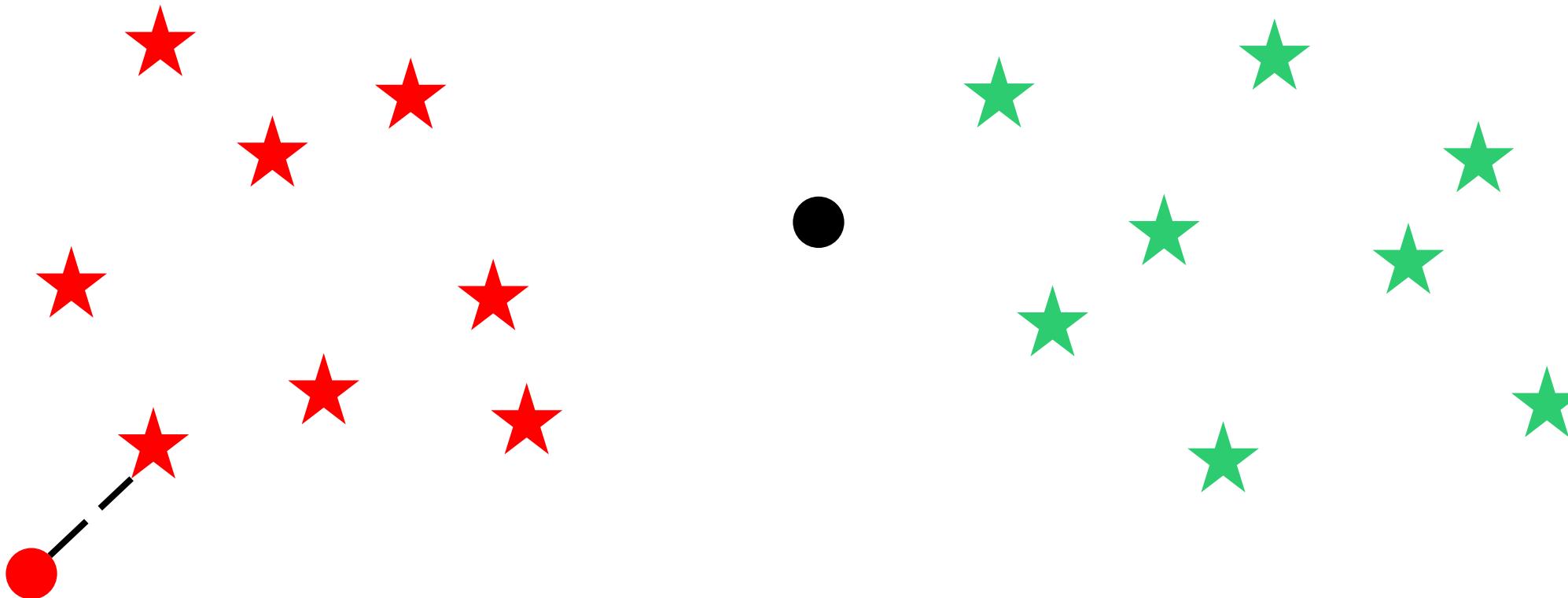
# Learning with the 1-NN Classifier

231



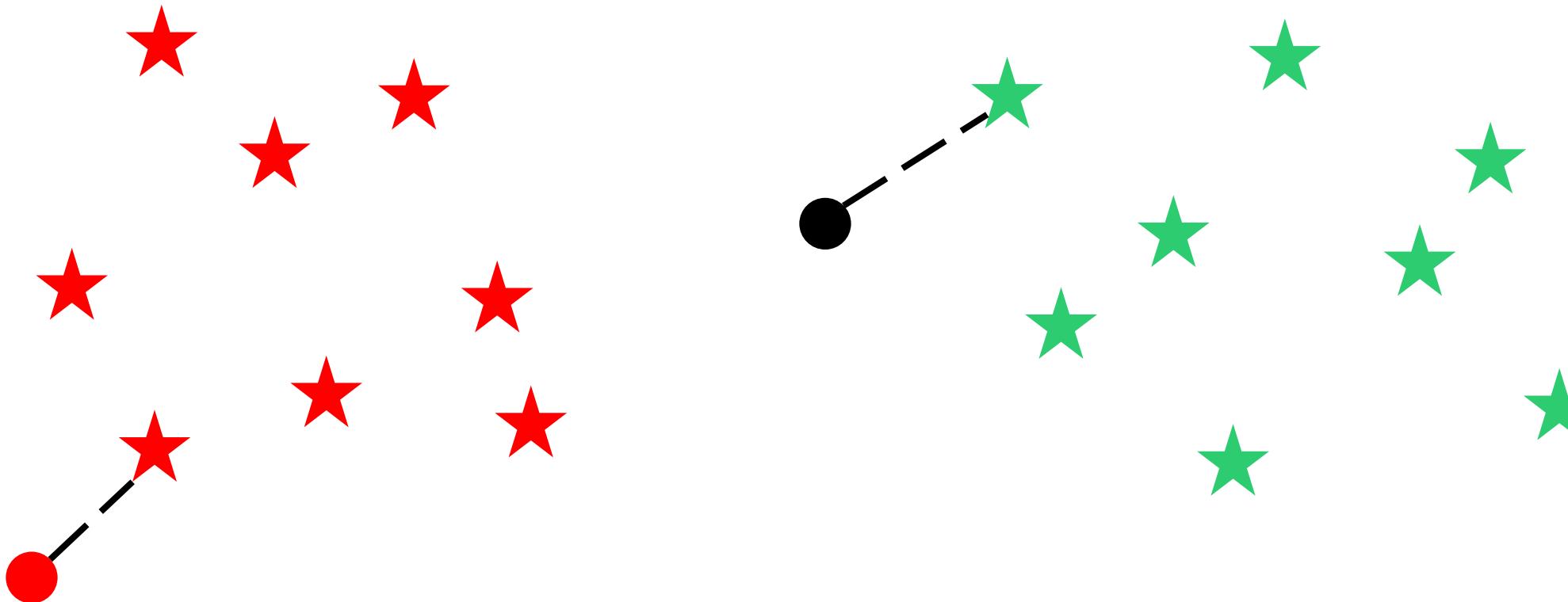
# Learning with the 1-NN Classifier

231



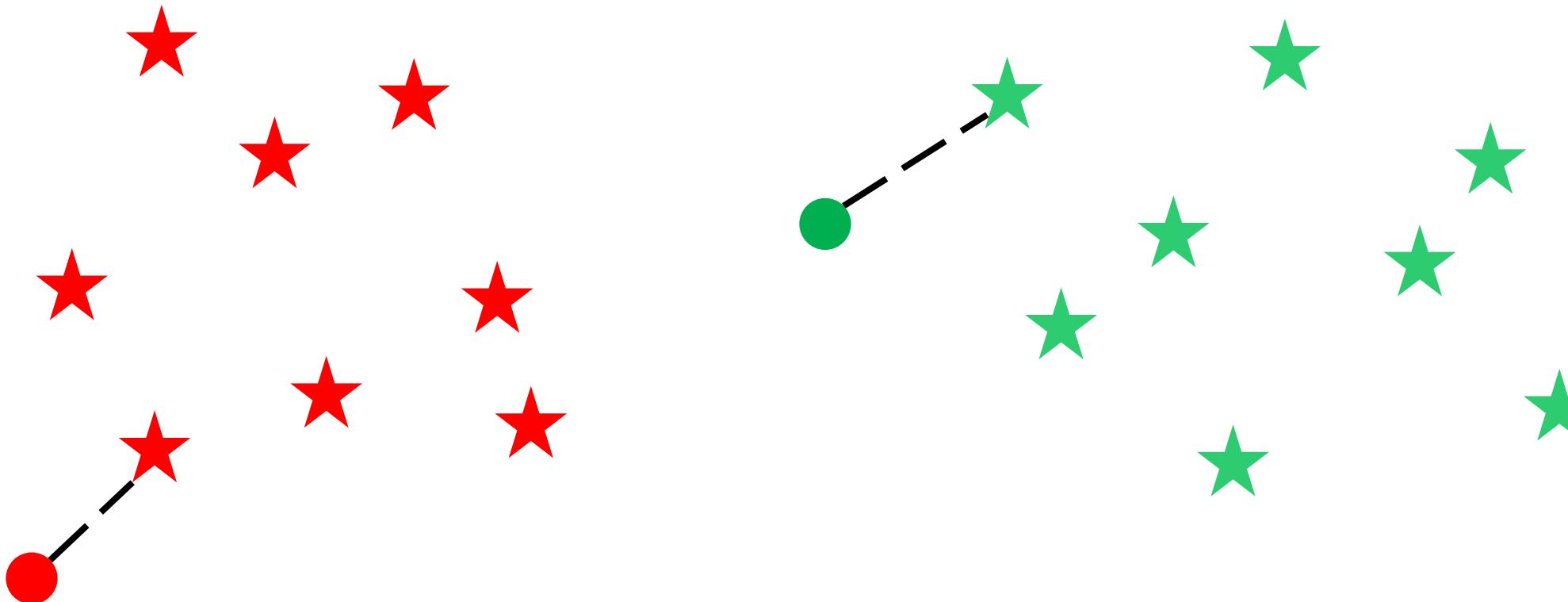
# Learning with the 1-NN Classifier

231



# Learning with the 1-NN Classifier

231



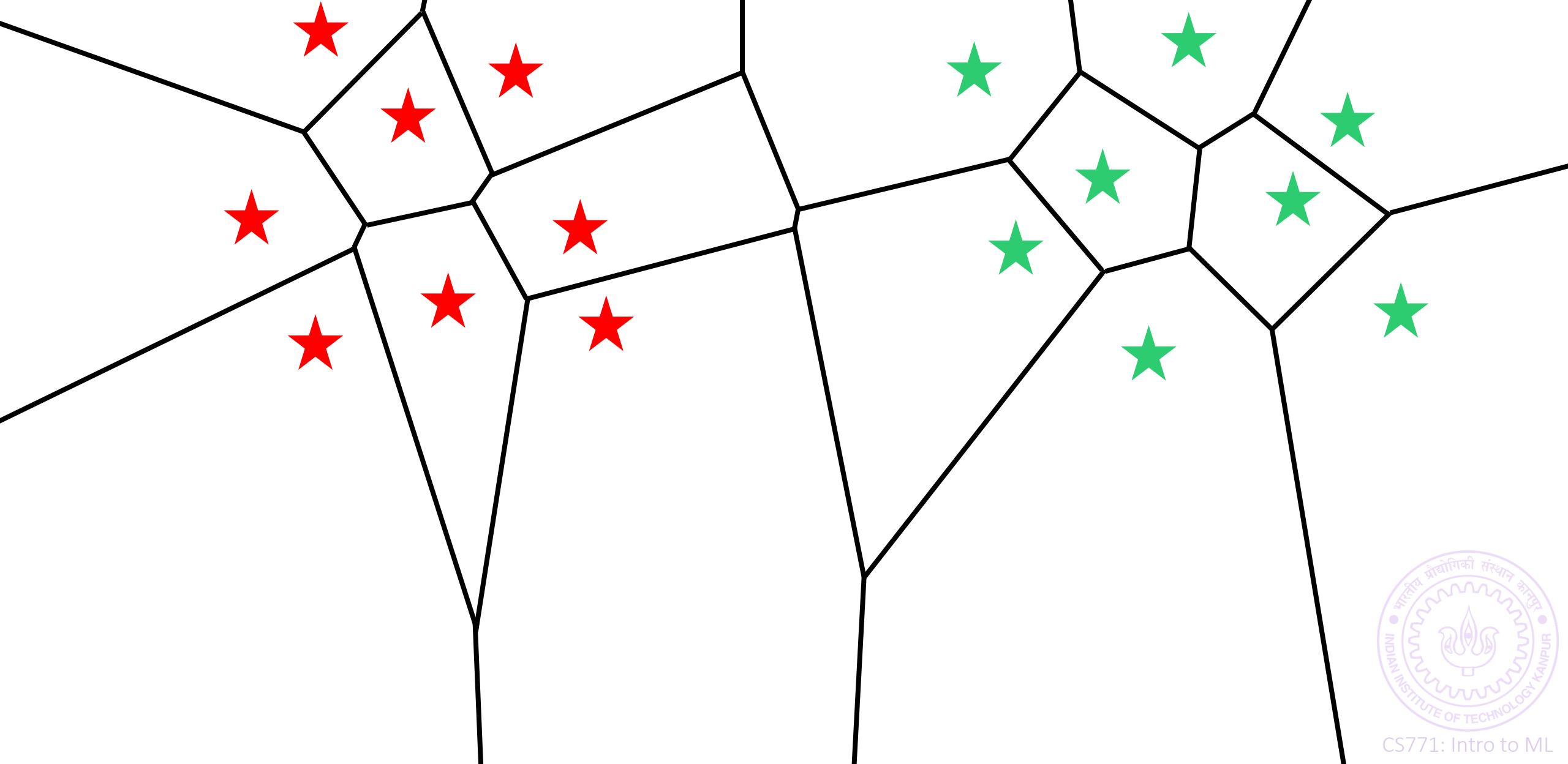
# Learning with the 1-NN Classifier

231



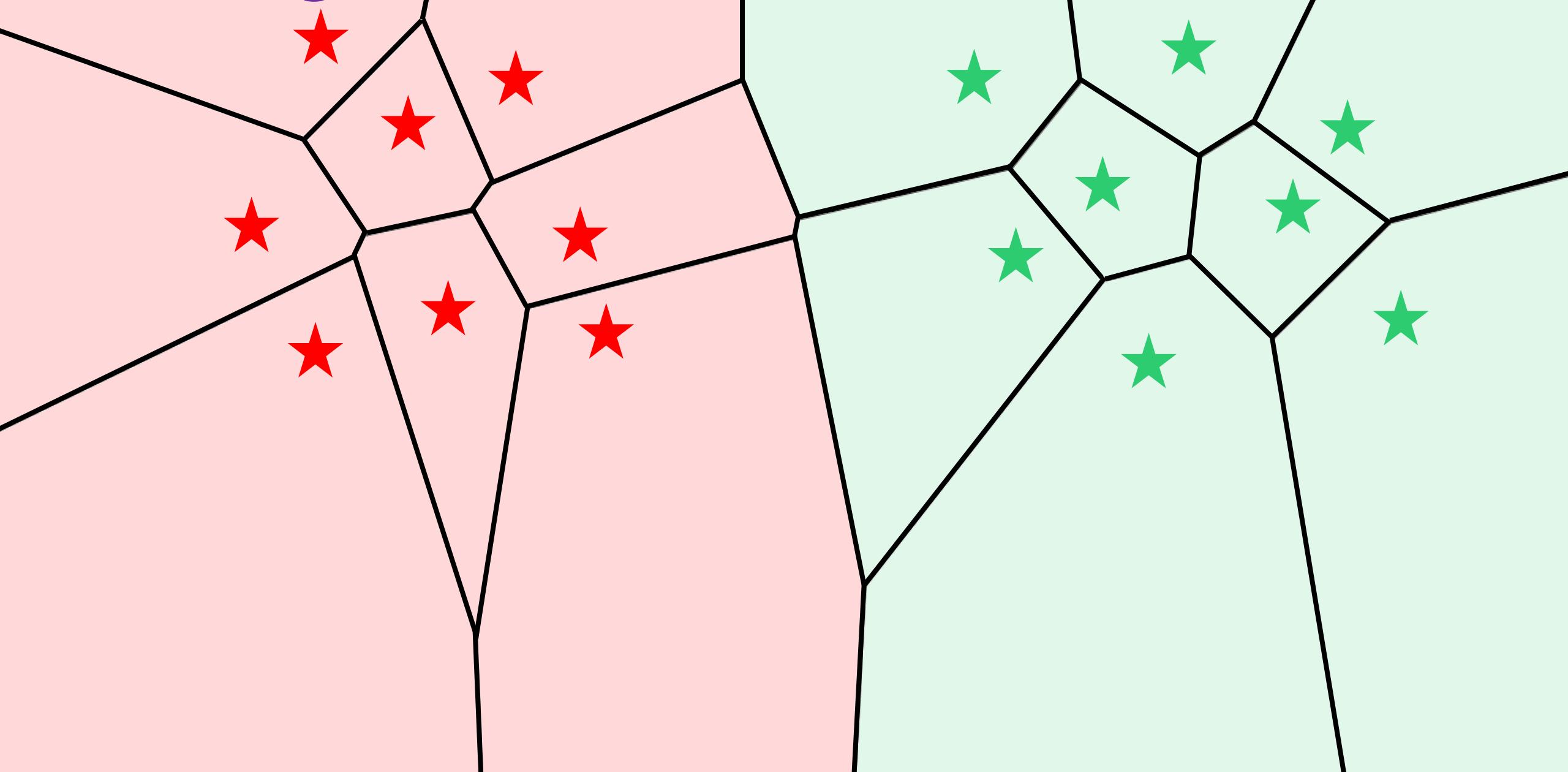
# Learning with the 1-NN Classifier

231



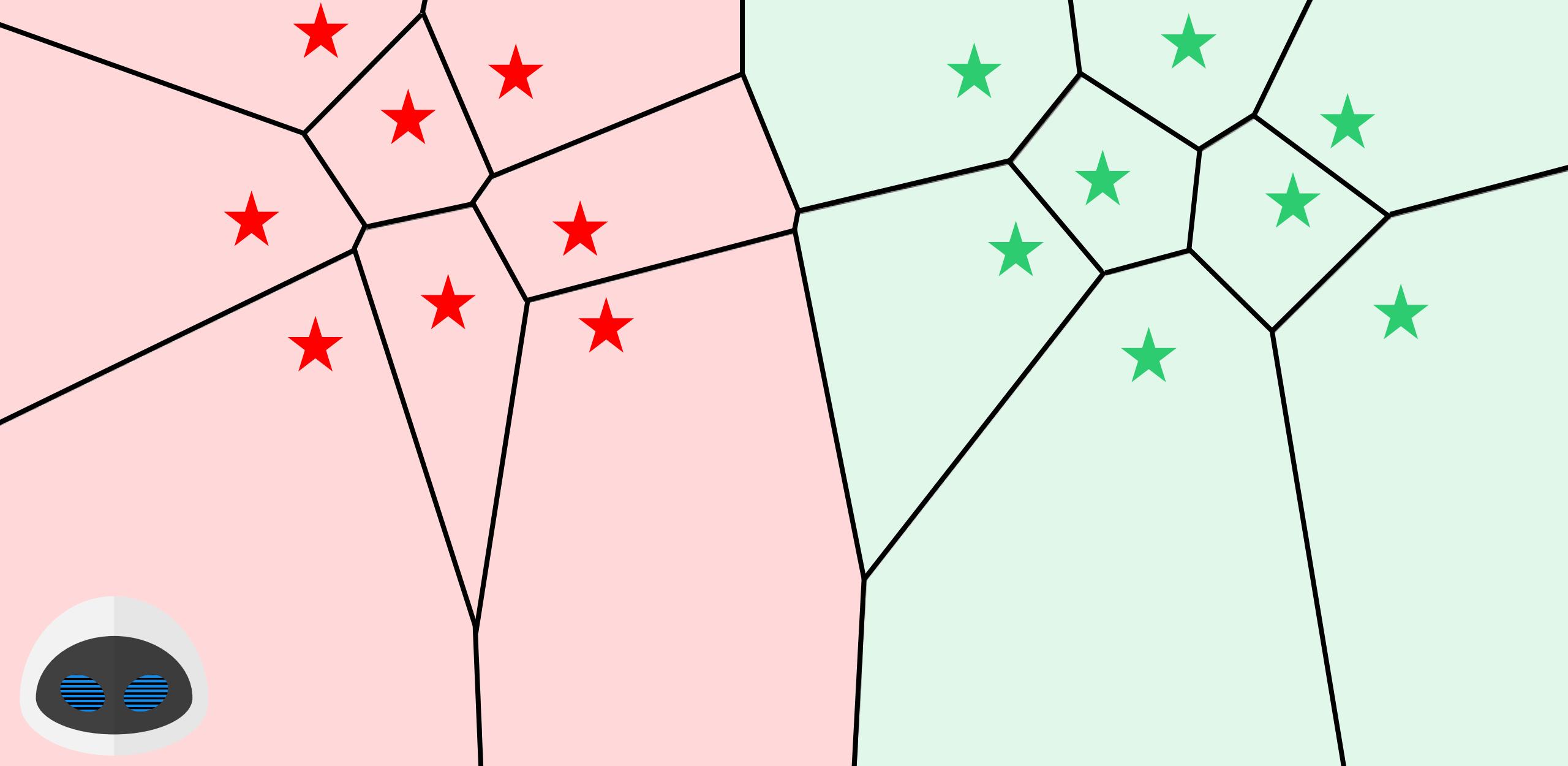
# Learning with the 1-NN Classifier

231



# Learning with the 1-NN Classifier

231



# Learning with the 1-NN Classifier

231

