Practice Problems AE321A

Q1. For a Fixed Wing Aircraft

- a). Derive the expression of total lift curve slope of aircraft?
- b). Derive the expression of total lift coefficient of aircraft at zero-degree angle of attack?

Q.2. For a Fixed Wing Aircraft

- a). Derive the expression of total pitch stability derivative of aircraft?
- b). Derive the expression of total pitching moment coefficient of aircraft at zero-degree angle of attack?
- c). Prove that the neutral point of aircraft is an equivalent to aerodynamic centre of wing alone

Data for question 3 to 12:

For a Fixed Wing Aircraft, the following data is applicable:

$$\begin{split} \text{Weight of aircraft} &= 300 \text{ kg,} V_{cruise} = 35\text{m/s,} \rho_{sea} = 1.2256 \frac{\text{kg}}{\text{m}^3}, C_{L_{\alpha w}} = 4.5279/\text{rad.} \;\;, \\ C_{L_{\alpha t}} &= 4/\text{rad,} \;\; \alpha_{L=0} = -3^\circ, \qquad \left(C_{m_{ac}}\right)_w = -0.08, \;\; \bar{c} = 1\text{m,} \;\; S_w = 7m^2 \;\;, \;\; S_{HT} = 1.5m^2 \;\; b = 7\text{m,} \\ \eta_t &= 0.9 \;\;, (X_{ac})_{wing} = 0.25\text{m} \qquad , (X_{ac})_{Tail} = 3.0\text{m} \;\; \tau = 0.4, \\ \frac{\text{d}\epsilon}{\text{d}\alpha} = 0.4118, \qquad \epsilon_0 = 1.2375^\circ, \\ i_t &= -1.0 \textit{deg,} \;\; i_w = 0.0 \textit{deg,} \;\; \text{static margin (SM)=10\%} \end{split}$$

Useful formula:

$$\begin{split} C_L &= C_{L0} + C_{L_{\alpha}}\alpha + C_{L_{\delta_e}}\delta_e \\ C_m &= C_{m0} + C_{m_{\alpha}}\alpha + C_{m_{\delta_e}}\delta_e \\ C_{L_{\delta_e}} &= \tau.\,\eta_t.\frac{S_{HT}}{S_w}C_{L_{\alpha t}} \\ C_{m_{\delta_e}} &= -\tau.\,\eta_t.\frac{S_{HT}}{S_w}.\frac{\left((X_{ac})_{Tail} - \left(X_{cg}\right)\right)}{\overline{c}}.\,C_{L_{\alpha t}} \end{split}$$

The nomenclature has their usual aerodynamic meaning

Note 1:(neglect the effect of fuselage on stability)

Note 2:(Location of aerodynamic centre of wing and tail has been measured from the wing leading edge)

