$$\eth_s Y_{lm}(\hat{n}) = \sqrt{(\ell - s)(\ell + s + 1)}_{s+1} Y_{lm}(\hat{n})$$

$$\bar{\eth}_s Y_{lm}(\hat{n}) = -\sqrt{(\ell + s)(\ell - s + 1)}_{s-1} Y_{lm}(\hat{n})$$