

# MATHEMATICS ASSIGNMENT - 04

## VECTOR SPACES AND SUBSPACES

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Solve all the questions

August 25, 2018

### Question 01

Find the rank of the following matrices

$$A = \begin{bmatrix} 5 & -2 & 5 \\ 11 & 4 & -8 \\ 5 & 9 & 8 \\ 1 & 11 & 23 \end{bmatrix} \quad B = \begin{bmatrix} 2 & 5 & 4 & 6 \\ 8 & 5 & 6 & 9 \\ 4 & 5 & 6 & 8 \end{bmatrix} \quad (1)$$

### Question 02

Use Rank-Nullity theorem to compute the rank of following matrix

$$A = \begin{bmatrix} 1 & 1 & 2 & 3 \\ 3 & 4 & -1 & 2 \\ -1 & -2 & 5 & 4 \end{bmatrix} \quad (2)$$

### Question 03

Find the basis for Row Space as well as Column Space for:

$$A = \begin{bmatrix} 5 & 6 & 5/4 \\ 7 & 7 & 7/3 \\ 1 & 3 & 8 \end{bmatrix} \quad (3)$$

### Question 04

Find the basis of Null Space of A as well as  $A^T$  for

$$A = \begin{bmatrix} 8 & 7 & 4 & 2 \\ 3 & 8 & 2 & 2 \\ 8 & 7 & 8 & 2 \end{bmatrix} \quad (4)$$

### Question 05

Determine the existence and uniqueness of solutions of the system:

$$\begin{aligned} 3x_2 - 6x_3 + 6x_4 + 4x_5 &= -5 \\ 3x_1 - 7x_2 + 8x_3 - 5x_4 + 8x_5 &= 9 \\ 3x_1 - 9x_2 + 12x_3 - 9x_4 + 6x_5 &= 15 \end{aligned}$$

### Question 06

Find the basis of the row space for

$$A = \begin{bmatrix} 4 & 5 & 6 \\ 2 & -5 & 6 \\ 8 & 10 & 12 \end{bmatrix} \quad (5)$$

**Question 07**

Suppose a  $3 \times 5$  coefficient matrix for a system has three pivot columns. Is the system consistent? Why or why not?

**Question 08**

Let  $A = \begin{bmatrix} 2 & 0 & 6 \\ -1 & 8 & 5 \\ 1 & -2 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 10 \\ 3 \\ 3 \end{bmatrix}$  and let  $W$  be the set of all linear combinations of columns of  $A$ .

- Is  $b$  in  $W$ ?
- Show that the third column of  $A$  is in  $W$ .

**Question 09**

Find solution of  $Ax=B$  for the following non-homogeneous system :

$$A = \begin{bmatrix} 3 & 5 & -4 \\ -3 & -2 & 4 \\ 6 & 1 & -8 \end{bmatrix} \quad B = \begin{bmatrix} 7 \\ -1 \\ -4 \end{bmatrix} \quad (6)$$