

Assignment 1

Group 25

November 17, 2018

Solⁿ1 :

Two dice are rolled,
total possibilities = 36
probability of getting sum is 5,
 $P(\text{sum}=5) = 4/36$
 $P(\text{sum}=5) = 1/9$

Solⁿ2 :

Die is rolled and coin is tossed,
Total possibility = 6
 $P(\text{odd}) = 3/6 = 1/2$
 $P(\text{head}) = 1/2$
 $p(\text{odd} \cap \text{head}) = 1/4$

Solⁿ3 :

Total = 1, 2, 3, 4, 5

(a) $P(\text{Odd at first time}) = 3/5$

(b) $P(\text{odd at second time}) = P(\text{even, then odd}) + P(\text{odd, then odd})$
 $= 2/5 * 3/4 + 3/5 * 2/4$
 $= 3/10 + 3/10$
 $= 3/5$

(c) $P(\text{Odd, Both times}) = 3/5 * 2/4 = 3/10$

Solⁿ4 :

No. of teams = 16
No. of rounds = 4
Matches played = 14

$$(a) P(A \text{ wins}) = 5/6 * 5/6 * 5/6 * 5/6 = 625/1296$$

$$(b) P(A \text{ runner up}) = 5/6 * 5/6 * 5/6 * 1/6 = 125/1296$$

$$(c) P(A \text{ reach semi Final}) = 5/6 * 5/6(1/6 + 5/6 * 1/6 + 5/6 * 5/6) = 25/36$$

$$(d) P(A \text{ out in round 2}) = 5/6 * 1/6 = 5/36$$

Solⁿ5 :

3 coins tossed,

Total Possibilities = 8

(a) Exactly 2 tails,

$$P(T=2) = 3/8$$

(b) Atleast 1 tail,

$$P(T \geq 1) = 7/8$$

Solⁿ6 :

Two dice thrown,

Total possibilities = 36

Getting a multiple of 2 on one and a multiple of 3 on the other,

Total Cases = 6

$$P(S) = 6/36 = 1/6$$

Solⁿ7 :

Bolts = 50, Rusted Bolts = 25

Nuts = 150, Rusted Nuts = 75

$$P(\text{Rusted}) = 100/200 = 1/2$$

$$P(\text{Bolt}) = 50/200 = 1/4$$

$$P(\text{Rusted} \cap \text{Bolt}) = 25/200 = 1/8$$

$$P(\text{Rusted} \cup \text{Bolt}) = P(\text{Rusted}) + P(\text{Bolt}) - P(\text{Rusted} \cap \text{Bolt})$$

$$P(\text{Rusted} \cup \text{Bolt}) = 1/2 + 1/4 - 1/8 = 5/8$$

Solⁿ8 :

Total = 200 (1.....200)

Divisible by 6 or 8

P(Divisible by 6) = 33/200

P(Divisible by 8) = 25/200

P(Divisible by 6 and 8) = 8/200

$P(\text{Divisible by } 6 \cup \text{by } 8) = P(/6) + P(/8) - P(/6 \cap /8)$

$P(\text{Divisible by } 6 \cup \text{by } 8) = 33/200 + 25/200 - 8/200 = 1/4$

Solⁿ9 :

Two dice are rolled,

Neither divisible by 3 nor 4

Total Possibilities = 16

$P(\text{not } 3 \cap \text{not } 4) = 1 - P(3 \cup 4)^c$
 $= 1 - 20/36 = 16/36$

Solⁿ10 :

Die is rolled twice

Total Possibilities = 36

(a) Getting an even no in the first time or a total of 8

let, E = Even no in first time

$P(E) = 18/36 = 1/2$

F = Total of 8

$P(F) = 5/36$

$P(E \cap F) = 3/36$

$P(E \cup F) = P(E) + P(F) - P(E \cap F)$
 $= 18/36 + 5/36 - 3/36 = 5/9$

(b) Getting an even no in first time and a total of 8)

$P(E \cap F) = 3/36$

Solⁿ11 :

Rolling 6 sided Die thrice,

$$P(\text{Getting different number each time}) = 6/6 * 5/6 * 4/6 = 5/9$$

Solⁿ12 :

Total Cases = 20

Let E = No. of die in left hand is greater than sum of no of die in right hand

$$P(E) = 20/216 = 5/54$$

Solⁿ13 :

Red = 5, Blue = 6, Green = 8

Set of 3 balls is randomly selected,

(a) Getting of same color,

With replacement

$$= ({}^5C_3 * {}^6C_3 * {}^8C_3) / {}^{19}C_3$$

without replacement

$$= (5*4*3 + 6*5*4 + 8*7*6) / {}^{19}C_3$$

(b) Getting of different color,

With replacement

$$= (5*6*8) / {}^{19}C_3$$

without replacement

$$= ({}^5C_1 * {}^6C_1 * {}^8C_1) / 19$$

Solⁿ14 :

Die is rolled 6 times,

Total possibilities = 6^4

six comes up atleast once

$P(6 \geq 1) = 1 - \text{atmost once}$

$= 1 - [P(0) + P(1)]$

$= 1 - [(5/6)^4]$

Solⁿ15 :

$P(\text{female}) = 0.52$

$P(\text{CS}) = 0.05$

$P(W \cup \text{CS}) = 0.02$

(a) Female, given majoring in CS

$P(F | \text{CS}) = P(F \cap \text{CS}) / P(\text{CS}) = 0.02/0.05 = 2/5$

(b) Majoring in CS, given Female

$P(\text{CS} | F) = P(F \cap \text{CS}) / P(F) = 0.02/0.52 = 2/52$

Solⁿ16 :

A contains 4 red and 3 black, B contains 5 Red and 4 Black, C contains 4 Red and 4 black

Total Balls = 24

Probability of 3 balls(2 Red, 1 Black)

$= (4/7 * 5/9 * 4/8) + (4/7 * 4/9 * 5/8) + (3/7 * 5/9 * 4/8)$

$= (80 + 64 + 60) / 504 = 204/504 = 51/126$

Solⁿ17 :

Coin is tossed until head occurs for the first time,

Probability that No. of tosses required is odd

$$= 1 + 3 + 5 + \dots$$

$$= H + TTH + TTTTH + \dots$$

$$= 1/2 + (1/2)^3 + (1/2)^5 + \dots \text{ Infinite G.P. Series,}$$

$$= (1/2) / (1 - 1/4)$$

$$= (1/2) / (3/4) = 2/3$$

Solⁿ18 :

Let, Probability of Saurabh's success = $p(E)$

Probability of Mangesh's success = $P(F)$

$$P(E) = 1/3, P(E^c) = 2/3$$

$$P(F) = 1/5, P(F^c) = 4/5$$

1.) Only 1 of them is selected,

$$\begin{aligned} &= P(E) * P(F^c) + P(E^c) * P(F) \\ &= (1/3) * (4/5) + (2/3) * (1/5) = 2/5 \end{aligned}$$

2.) Both Selected

$$P(E \cup F) = (1/3) * (1/5) = 1/15$$

3.) Atleast One

$$\begin{aligned} P(E \cap F) &= P(E) + P(F) - P(E \cup F) \\ &= (1/3) + (1/5) - (1/15) \\ &= 7/15 \end{aligned}$$

Solⁿ19 :

$$P(A) = 1/3, P(B) = 2/7, P(C) = 3/8$$

$$P(A^c) = 2/3, P(B^c) = 5/7, P(C^c) = 5/8$$

Only one of them will solve it,

$$\begin{aligned}
&= P(A) P(B^c) P(C^c) + P(A^c) P(B) P(C^c) + P(A^c) P(B^c) P(C) \\
&= (1/3)*(5/7)*(5/8) + (2/3)*(2/7)*(5/8) + (2/3)*(5/7)*(3/8) \\
&= (25+20+30)/(3*7*8) \\
&= 25/26
\end{aligned}$$

Solⁿ20 :

$P(X) = 0.60$, $P(Y) = 0.40$
According to Baye's Theorem,

$$\begin{aligned}
&= (0.4*0.78)/(0.6*0.96 + 0.4*0.78) \\
&= 312/888 = 39/111
\end{aligned}$$

Solⁿ21 :

Total 10 people seated around a circular table,
Two particular always sit together,

For circular arrangement, Possible combination = $(n-1)!$

$$\begin{aligned}
P(E) &= (2! * (n-2)!)/(n-1)! \\
&= (2! * 8!)/9! = 2/9
\end{aligned}$$

Solⁿ23 :

Store(A, B, C) have employees(50, 75, 100) and women(.25, .45, .70)

$$\begin{aligned}
P(\text{Women and Works in C}) &= (70/100) / (25/50 + 45/75 + 70/100) \\
&= (7/10) / (5/10 + 6/10 + 7/10) \\
&= 7/18
\end{aligned}$$

Solⁿ24 :

$P(X) = 0.7$, $P(Y) = 0.5$, $P(X^c) = 0.3$, $P(Y^c) = 0.5$

$$\begin{aligned}
P(X \cup Y) &= 1 - P(X^c \cap Y^c) \\
&= 1 - 0.60 \\
&= 0.40
\end{aligned}$$

$$\begin{aligned}
P(X \cap Y) &= P(X) + P(Y) - P(X \cup Y) \\
&= 0.7 + 0.5 - 0.4
\end{aligned}$$

$$= 0.8$$

Solⁿ25 :

$$P(\text{Gun hits plane}) = P(1) + P(1^c).P(2) + P(1^c).P(2^c).P(3) + P(1^c).P(2^c).P(3^c).P(4)$$

$$= 0.4 + 0.6*0.3 + 0.6*0.7*0.2 + 0.6*0.7*0.8*0.1$$

$$= 4/10 + 18/100 + 84/1000 + 336/10000$$

$$= 6976/10000$$

$$= 0.6976$$

Solⁿ26 :

A has 5 Black and 3 White and B has 4 Black and 4 white balls.

To make composition of A equal to B, transfer 1B ball from A to B and then transfer 1W from A to B.

$$P(E) = (5/8)*(4/9)$$

$$= 5/18$$

Solⁿ27 :

REMAINS

Vowels = 3

Position for Vowels = 4

$$\text{Ways Vowels occurs at Odd places} = {}^4C_3 * 3! * 4!$$

$$= 4*6*24$$

$$= 576$$

Solⁿ28 :

RAINBOW

$$\text{All vowels together} = 3! * 5!$$

$$= 6*120 = 720$$

Solⁿ29 :

A failing = 0.07

B failing = 0.10

C failing = 0.05

$$\text{a) } P(\text{All work correctly}) = (93/100)*(90/100)*(95/100)$$

$$\begin{aligned} \text{b) } P(\text{All fail}) &= (7*10*5)/(100*100*100) \\ &= 35/10^5 \end{aligned}$$

$$\text{c) } P(\text{Only one operates correctly}) = (93*10*5)/10^6 + (7*90*5)/10^6 + (95*10*7)/10^6$$

$$\begin{aligned} \text{d) } P(\text{atleast one Opearte correctly}) &= 1 - P(\text{No one operates correctly}) \\ &= 1 - 35/10^5 \end{aligned}$$

Solⁿ30 :

E = Second card will be ace if first card is king

$$\begin{aligned} P(E) &= (4/52)*(4/51) \\ &= 4/663 \end{aligned}$$