Operating Systems Autumn 2024

race conditions, mutual exclusion

What is a thread?

- An abstraction for a single running process
- A multi-threaded program has more than one point of execution
 - Multiple program counters, one for each thread
 - They share code, heap, and global variables
 - Each thread has its own stack
 - Each thread has its own private set of registers

Data race

- A program has a data race if it is possible for a thread to modify an addressable location at the same time that another thread is accessing the same location
- The result/correctness depends on the sequence/timing of events;
 i.e., how things end up being scheduled.

Shared counter

Two threads updating a single shared variable cnt

• What happens when two threads execute concurrently?

Order of execution of threads

Possible implementation of cnt++:

- OS might decide to context switch from one thread to another at any time
- Thus the atomic actions of concurrent threads may be interleaved in any possible order

Possible interleaving

eax_i denotes the value of register in thread i

```
eax_1 := cnt
eax_1 := eax_1 + 1
<switch>
eax_2 := cnt
eax_2 := eax_2 + 1
cnt := eax_2
<switch>
cnt := eax_1
```

• Result: cnt one less than correct! (lost update)

• Consider 2 threads sharing a global variable count, initially 10:

```
// Thread A
count++;

//Thread B
count--;
```

• What are the possible values for count after both threads finish executing?

```
int count = 0;
// Thread 1
for (i=0; i < 10; i++) {
    count++;
}</pre>
// Thread 2
for (i=0; i < 10; i++) {
    count++;
}
```

- What is the final value of count?
 - A value between 2 and 20

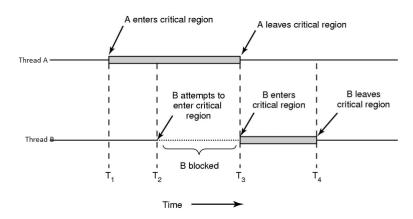
count = 2

- t1 and t2 read count
- t1 increments 9 times. so count becomes 9
- t2 increments once. so count becomes 1
- t1 reads count (value is 1)
- t2 increments 9 times. so count becomes 10
- t1 increments once. so count becomes 2

Critical section

- Critical section: code that access shared resource (e.g., variable or data structure)
- Race condition: arises when multiple threads simultaneously enter critical section leading to a non-deterministic outcome

Critical section



What basic mechanism can stop thread B from entering critical region when thread A in?

Requirements for a good solution

- Mutual exclusion (safety property)
 - At most one thread can be in CS at a time

Requirements for a good solution

- Mutual exclusion (safety property)
 - At most one thread can be in CS at a time
- Progress (liveness property)
 - If no thread is currently in CS and threads are trying to access, one should eventually be able to enter the CS

Requirements for a good solution

- Mutual exclusion (safety property)
 - At most one thread can be in CS at a time
- Progress (liveness property)
 - If no thread is currently in CS and threads are trying to access, one should eventually be able to enter the CS
- Bounded waiting (liveness property)
 - Once a thread T starts trying to enter the CS, there is a bound on the number of times other threads get in

Progress vs. Bounded waiting

• Liveness requirements are needed for a solution to be useful

Progress vs. Bounded waiting

- Liveness requirements are needed for a solution to be useful
- Progress
 - If no thread can enter CS, we don't have progress

Progress vs. Bounded waiting

- Liveness requirements are needed for a solution to be useful
- Progress
 - If no thread can enter CS, we don't have progress
- Bounded waiting
 - If thread A is waiting to enter CS while B repeatedly leaves and re-enters CS ad infinitum, we don't have bounded waiting

Mutual exclusion: legacy solutions

 Mutual exclusion algorithm solely based on read and write operations to a shared memory

Mutual exclusion: legacy solutions

- Mutual exclusion algorithm solely based on read and write operations to a shared memory
- First correct solution for two threads by Dekker in 1966
- Peterson proposed a simpler solution in 1981

Mutual exclusion: legacy solutions

Solution for 2 threads T_0 and T_1

```
Algorithm 1 Peterson's algorithm for thread T_i
Global Variables:
 1: bool wants[2] = {false, false};
 2: int not_turn; /* can be 0 or 1 */
 3: enter_CS()
   wants[i] = true;
 5: not\_turn = i;
    while wants[1-i] == true and not_turn == i do
    /* do nothing */
     end while
 8:
 9: leave_CS()
10: wants[i] = false;
```

Peterson's algorithm: a few comments

- wants: To declare that the thread wants to enter
- not_turn: To arbitrate if the 2 threads want to enter
- Line 6: "The other thread wants to access and not our turn, so loop"

Correctness (1)

Algorithm 1 Peterson's algorithm for thread T_i

```
Global Variables:
```

```
1: bool wants[2] = {false, false};
2: int not_turn; /* can be 0 or 1 */

3: enter_CS()
4: wants[i] = true;
5: not_turn = i;
6: while wants[1-i] == true and not_turn == i do
7: /* do nothing */
8: end while

9: leave_CS()
10: wants[i] = false;
```

- Mutual exclusion
 - \bullet Assume both threads want to enter CS, then wants[0] = wants[1] = 1
 - not_turn can only be 0 or 1
 - the condition of the while loop can only resolve to false for one of the threads

Correctness (2)

Algorithm 1 Peterson's algorithm for thread T_i

```
Global Variables:
 1: bool wants[2] = {false, false};
 2: int not_turn; /* can be 0 or 1 */
 3: enter_CS()
     wants[i] = true;
   not\_turn = i:
     while wants[1-i] == true and not_turn == i do
     /* do nothing */
     end while
 8:
 9: leave_CS()
     wants[i] = false;
10:
```

- Progress
 - If T_0 doesn't want CS, wants[0] == false, so T_1 won't loop
 - If both threads try to enter, one thread will succeed

Correctness (3)

Algorithm 1 Peterson's algorithm for thread T_i

```
Global Variables:
 1: bool wants[2] = {false, false};
 2: int not_turn; /* can be 0 or 1 */
 3: enter_CS()
     wants[i] = true;
     not\_turn = i:
      while wants[1-i] == true and not_turn == i do
      /* do nothing */
      end while
 8:
 9: leave_CS()
      wants[i] = false;
10:
```

Bounded waiting

• If T_1 was blocked from CS and T_0 tries to re-enter, T_0 will set not_turn = 0, allowing T_1 in

- Consider a modified algorithm where lines 4 and 5 are swapped
- Does this solution work?

```
Global Variables:
1: bool wants[2] = {false, false};
2: int not turn; /* can be 0 or 1 */
3: enter CS()
4: not turn = i;
5: wants[i] = true;
6: while wants[1-i] == true and not turn == i do
       /* do nothing */
8: end while
9: leave CS()
10: wants[i] = false;
```

- Mutual exclusion violation
- Bad trace
 - T1 does not_turn = 1
 - T0 does not_turn = 0
 - T0 does wants[0] = true
 - T0 does while (wants[1] == true and not_turn == 0); // (false and true) \rightarrow false

- Mutual exclusion violation
- Bad trace
 - T1 does not_turn = 1
 - T0 does not_turn = 0
 - T0 does wants[0] = true
 - T0 does while (wants[1] == true and not_turn == 0); // (false and true) \rightarrow false
 - T0 enters the CS

- Mutual exclusion violation
- Bad trace
 - T1 does not_turn = 1
 - T0 does not_turn = 0
 - T0 does wants[0] = true
 - T0 does while (wants[1] == true and not_turn == 0); // (false and true) \rightarrow false
 - T0 enters the CS
 - T1 does wants[1] = true
 - \bullet T1 does while (wants[0] == true and not_turn == 1); // (true and false) \to false

- Mutual exclusion violation
- Bad trace
 - T1 does not_turn = 1
 - T0 does not_turn = 0
 - T0 does wants[0] = true
 - T0 does while (wants[1] == true and not_turn == 0); // (false and true) \rightarrow false
 - T0 enters the CS
 - T1 does wants[1] = true
 - T1 does while (wants[0] == true and not_turn == 1); // (true and false) \rightarrow false
 - T1 enters the CS

Q2 - take home

- Assume the while statement in line 6 is changed to
 - while (wants[1-i] == true and not_turn != i)
- Show a trace in which there is a mutual exclusion violation
- Show a trace in which there is NO mutual exclusion violation

Peterson's algorithm: a few more comments

- Given solution works for 2 threads
- Can be generalized to *n* threads but *n* must be known in advance
- To implement a general lock, processors provide hardware primitives