A Coupled k-Nearest Neighbor Algorithm for Multi-label Classification

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Abstract. ML-kNN is a well-known algorithm for multi-label classification. Although effective in some cases, ML-kNN has some defect due to the fact that it is a binary relevance classifier which only considers one label every time. In this paper, we present a new method for multi-label classification, which is based on lazy learning approaches to classify an unseen instance on the basis of its k nearest neighbors. By introducing the coupled similarity between class labels, the proposed method exploits the correlations between class labels, which overcomes the shortcoming of ML-kNN. Experiments on benchmark data sets show that our proposed Coupled Multi-Label k Nearest Neighbor algorithm (CML-kNN) achieves superior performance than some existing multi-label classification algorithms.

Keywords: Multi-label · Coupled · Classification · Nearest neighbor

1 Introduction

Although traditional single-label classification approaches have been proved to be successful in handling some real world problems, for the problems which the objects not fit the single-label rule, they may not work well, for example, in image classification, an image may contain several concepts simultaneously, such as beach, sunset and kangaroo. Such tasks are usually denoted as multi-label classification problems. In fact, a conventional single-label classification problem can simply be taken as a special case of the multi-label classification problem where there has only one label in the class label space. Multi-label classification problems exist in many domains, for example, in automatic text categorization, a document can associate with several topics, such as arts, history and Archeology; and in gene functional analysis of bio-informatics, a gene can belong to both metabolism and transcription classes; and in music categorization, a song may labeled as Mozart and sad.

In the last decades, there have been a variety of methods developed for multilabel classifications. These methods are generally grouped into two categories: One is the problem transformation methods and another is the algorithm adaptation methods. Problem transformation methods first transform the multi-label learning tasks into multiple single-label learning tasks, which are then handled

T. Cao et al. (Eds.): PAKDD 2015, Part I, LNAI 9077, pp. 176-187, 2015.

DOI: 10.1007/978-3-319-18038-0_14

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by the standard single-label learning algorithms. Another approach is called algorithm adaptation method, which modifies existing single-label learning algorithms in order to extend its ability to handle multi-label data, such as ML-kNN [17], IBLR [7], BSVM [2], and BP-MLL [16].

Researchers have tried to extend the $k{\rm NN}$ concept to handle the multi-label classification problem, such as ML- $k{\rm NN}$. ML- $k{\rm NN}$ applies maximum a posteriori principle for classification and ranking, and the likelihood is estimated by using the k nearest neighbors of an instance. Although simple and powerful, there are some shortcomings in its processing strategy. ML- $k{\rm NN}$ uses the popular binary relevance (BR) strategy [13], which may transfer the problem into many classimbalance tasks, and then tend to degrade the performance of the classifiers. Another problem of it is the estimation of the posteriori may be affected by the facts that the instances with and without a particular label are typically highly imbalanced. Furthermore, its ignorance of the inter relationship between labels is another issue which limits its usage. Such relationship is described as a Coupled behavior in some previous research [4,6]. In [8,14], Can and Liu etc. analysis the coupling relationship on categorical data. These works all proved the effectiveness of considering the dependency between different attributes.

In this paper, we propose a novel kNN-based multi-label learning approach (CML-kNN for short) based on non-iidness [5]. The major contribution of this paper is summarized as follows:

- We propose a novel multi-label learning algorithm that based on lazy learning and the inner relationship between labels.
- We introduce a new coupled label similarity for multi-label kNN algorithm.
 Rather than only select the neighbors with a specific label, the coupled label similarity will include more similar neighbors in the process to overcome the problem of lacking neighbors with certain label.
- We extended the concept of the nearest neighbor in multi-label classification
 with coupled label similarity. Based on this extended nearest neighbors, we
 introduce a new frequency array strategy.

The structure of this paper is organized as follows. Section 2 briefly reviews the ML-kNN algorithm. Preliminary definitions are specified in Section 3.1. And section 3 gives a detailed description of the new algorithm we proposed. The experimental results are discussed in Section 4. Finally, the conclusion is discussed in Section 5.

$2 \quad \text{ML-}k\text{NN}$

A number of multi-label learning methods are adapted from kNN [3,11,15,17]. ML-kNN, the first multi-label lazy learning approach, is based on the traditional kNN algorithm and the maximum a posteriori (MAP) principle [17].

The main idea of the ML-kNN approach is that an instance's labels depend on the number of neighbors that possess identical labels. Given an instance xwith an unknown label set $L(x) \subseteq L$, ML-kNN first identifies the k nearest neighbors in the training data and counts the number of neighbors belonging to each class (i.e. a variable z from 0 to k). Then the maximum a posteriori principle is used to determine the label set for the test instance. The posterior probability of $l_i \in L$ is given by

$$P(l_i \in L(x)|z) = \frac{P(z|l_i \in L(x)) \cdot P(l_i \in L(x))}{P(z)} \tag{1}$$

where z is the number of neighbors belonging to each class $(0 \le z \le k)$. Then, for each label $l_i \in L$, the algorithm builds a classifier h_i using the rule

$$h_i(x) = \begin{cases} 1 \ P(l_i \in L(x)|z) > P(l_i \notin L(x)|z) \\ 0 \quad \text{otherwise} \end{cases}$$
 (2)

where $0 \le z \le k$. If $h_i(x) = 1$, it means label l_i is in x's real label set, while 0 means it does not. The prior and likelihood probabilities in Eq. 1 are estimated from the training data set in advance.

ML-kNN has two inheriting merits from both lazy learning and MAP principle: One is the decision boundary can be adaptively adjusted due to the varying neighbors identified for each new instance, and another one is the class-imbalance issue can be largely mitigated due to the prior probabilities estimated for each class label. However, ML-kNN is actually a binary relevance classifier, because it learns a single classifier h_i for each label independently. In other words, it does not consider the correlations between different labels. The algorithm is often criticized because of this drawback.

3 Methodology

3.1 Problem Statement

We formally define the multi-label classification problem as this: Let X denotes the space of instances and $Y = \{l_1, \ldots, l_n\}$ denotes the whole label set where |Y| = n. $T = \{(x_1, L(x_1)), \ldots, (x_m, L(x_m))\}$ (|T| = m) is the multi-label training data set, whose instances are drawn identically and independently from an unknown distribution D. Each instance $x \in X$ is associated with a label set $L(x) \in Y$. The goal of our multi-label classification is to get a classifier $h: X \to Y$ that maps a feature vector to a set of labels, while optimizing some specific evaluation metrics.

3.2 Coupled Label Similarity

It is much easier for numerical data to calculate the distance or similarity, since the existing metrics such as Manhattan distance and Euclidean distance are mainly built for numeric variables, but the labels are categorical data. How to denote the similarity between them is a big issue. As we all know, matching and frequency [1] are the most common ways to measure the similarity of categorical data. Accordingly, two popular similarity measures are defined: For two categorical value v_i and v_j , the Overlap Similarity is defined as

Sim_Overlap
$$(v_i, v_j) = \begin{cases} 1, & \text{if } v_i = v_j \\ 0, & \text{if } v_i \neq v_j, \end{cases}$$
 (3)

and the Frequency Based Cosine Similarity between two vectors V_i and V_j is defined as

$$Sim_Cosine(V_i, V_j) = \frac{V_i \cdot V_j}{||V_i|| ||V_i||}.$$
(4)

The overlap similarity between two categorical values is to assign 1 if they are identical otherwise 0 if different. Further, for two multivariate categorical data points, the similarity between them will be proportional to the number of features in which they match. While for frequency based measures, they assume the different categorical values but with the same occurrence times as the same.

Hence, the Overlap measure and Frequency Based measure are too simplistic by just giving the equal importance to matches and mismatches. The co-occurrence information in categorical data reflects the interaction between features and can be used to define what makes two categorical values more or less similar. However, such co-occurrence information hasn't been incorporated into the existing similarity metrics.

To capture the inner relationship between categorical labels, we introduce an *Intra-Coupling Label Similarity (IaCLS)* and an *Inter-Coupling Label Similarity (IeCLS)* below to capture the interaction of two label values from two different labels.

Definition 1. Given a training multi-label data set D and two different labels l_i and l_j $(i \neq j)$, the label value is v_i^x, v_j^y respectively. The **Intra-Coupling Label Similarity** (IaCLS) between label values v_i^x and v_j^y of label l_i and l_j is formalized as:

$$\delta^{Intra}(v_i^x, v_j^y) = \frac{RF(v_i^x) \cdot RF(v_j^y)}{RF(v_i^x) + RF(v_j^y) + RF(v_i^x) \cdot RF(v_j^y)},$$
 (5)

where $RF(v_i^x)$ and $RF(v_j^y)$ are the occurrence frequency of label value v_i^x and v_j^y in label l_i and l_j , respectively.

The Intra-coupling Label Similarity reflects the interaction of two different label values in the label space. The higher these similarities are, the closer such two values are. Thus, Equation (5) is designed to capture the label value similarity in terms of occurrence times by taking into account the frequencies of categories. Besides, since $1 \leq RF(v_i^x), RF(v_j^y) \leq m$, then $\delta^{Intra} \in [1/3, m/(m+2)]$.

In contrast to the Intra-Coupling, we also define an *Inter-Coupling Label Similarity* below to capture the interaction of two different label values according to the co-occurrence of some value (or discretized value group) from feature spaces.

Definition 2. Given a training multi-label data set D and two different labels l_i and l_j ($i \neq j$), the label value is v_i^x, v_j^y respectively. v_i^x and v_j^y are defined to be Inter-Coupling related if there exists at least one pair value (v_p^{zx}) or (v_p^{zy}) that occurs in feature a_z and labels of instance U_p . The Inter-Coupling Label Similarity (IeCLS) between label values v_i^x and v_i^y according to feature value v_p^z of feature a_z is formalized as:

$$\delta^{Inter}(v_i^x, v_j^y | v_p^z) = \frac{\min(F(v_p^{zx}), F(v_p^{zy}))}{\max(RF(v_i^x), RF(v_j^y))},$$
(6)

where $F(v_p^{zx})$ and $F(v_p^{zy})$ are the co-occurrence frequency count function for value pair v_p^{zx} or v_p^{zy} , and $RF(v_i^x)$ and $RF(v_j^y)$ is the occurrence frequency of related class label. v_p^z is the value in categorical feature a_z or the discretized value group in numerical feature a_z .

Accordingly, we have $\delta^{Ie} \in [0,1]$. The Inter-Coupling Label Similarity reflects the interaction or relationship of two label values from label space but based on the connection to some other features.

Definition 3. By taking into account both the Intra-Coupling and the Inter-Coupling, the **Coupled Label Similarity** (CLS) between two label values v_i^x and v_i^y is formalized as:

$$CLS(v_i^x, v_j^y) = \delta^{Intra}(v_i^x, v_j^y) \cdot \sum_{k=1}^n \delta^{Inter}(v_i^x, v_j^y | v_k), \tag{7}$$

where v_i^x and v_j^y are the label values of label l_i and l_j , respectively. δ^{Intra} and δ^{Inter} are the intra-coupling label similarity (Eq. 5) and inter-coupling label similarity (Eq. 6), respectively. The n is the number of attributes and v_k denotes the values in the kth feature a_k .

		_		
Instances	Label1	Label2	Label3	Label4
u_1	l_1			l_4
u_2			l_3	l_4
u_3	l_1		l_3	
u_4		l_2	l_3	
u_5		l_2	l_3	l_4

Table 1. An Example of Multi-label Data

The Coupled Label Similarity defined in Eq. 7 reflects the interaction or similarity of two different labels. The higher the CLS, the more similar two labels be. In Table 1, for example, $CLS(l_1, l_4) = 0.33$, $CLS(l_1, l_3) = 0.25$, so in the data set, an instance with label l_4 is more similar or close to instances with label l_1 than those instances with label l_3 do. That is to say, label pair (l_1, l_4) is closer to each other than the label pair (l_1, l_3) . For Table 1, we got the coupled label similarity array which showed in Table 2.

	Label1	Label2	Label3	Label4
Label1	1.0	0	0.25	0.33
Label2	0	1.0	0.50	0.33
Label3	0.25	0.50	1.0	0.50
Label4	0.33	0.33	0.50	1.0

Table 2. CLS Array

3.3 Extended Nearest Neighbors

Based on the Coupled Label Similarity, we introduce our extended nearest neighbors. Based on the similarity between labels, we can transfer a label set into a set with only a certain label, it also means a multi-label instance can be extended to a set of single-label. If we specify a basic label l_b , then any instance can be transformed into a set with only one label l_b . For example, in Table 1, instance u_5 has a label set of $\{l_2, l_3, l_4\}$, then according to the label similarity array Table 2, it can be transformed into $\{1 \cdot l_2, 0.5 \cdot l_2, 0.33 \cdot l_2\}$ if we choose label l_2 as the basic label. We can then call the original multi-label instance u_5 equals a single-label instance with a label of $\{1.83 \cdot l_2|l_2\}$.

instance	Extended Neighbors	To Label
u_5	$0 \cdot l_1 + 0.25 \cdot l_1 + 0.33 \cdot l_1$	l_1
u_5	$1 \cdot l_2 + 0.5 \cdot l_2 + 0.33 \cdot l_2$	l_2
u_5	$0.5 \cdot l_3 + 1 \cdot l_3 + 0.5 \cdot l_3$	l_3
u_5	$0.33 \cdot l_4 + 0.5 \cdot l_4 + 1 \cdot l_4$	l_{A}

Table 3. Extended Nearest Neighbors

If u_5 is the neighbor of some instance, when we consider the label l_2 , the instance u_5 can be presented as an instance which contains 1+0.5+0.33=1.83 label l_2 , and vice versa, instance u_5 also presents there are (1-1)+(1-0.5)+(1-0.33)=1.17 instances which not contain the label l_2 , and there will have $(1.83+1.17=3=|L(u_5)|)$. This is the basic idea when we finding our extended nearest neighbors.

3.4 Coupled ML-kNN

For the unseen instance x, lets N(x) represents the set of its k nearest neighbors identified in data set D. For the j-th class label, CML-kNN chooses to calculate the following statistics:

$$C_j = Round(\sum_{i=1}^k \delta_{L_i^*|j})$$
(8)

Where L_i is the label set of the *i*-th neighbor and $L_i \in N(x)$, and $\delta_{L_i^*|j}$ denotes the sum of the CLS values of the *i*-th neighbor's label set to the *j*-th label l_j , and Round() is the rounding function.

Namely, C_j is a rounding number which records all the CLS value of all x's neighbors to label l_j .

Let H_j be the event that x has label l_j , and $P(H_j|C_j)$ represents the posterior probability that H_j holds under the condition that x has exactly C_j neighbors with label l_j . Correspondingly, $P(\neg H_j|C_j)$ represents the posterior probability that H_j doesn't hold under the same condition. According to the MAP rule, the predicted label set is determined by deciding whether $P(H_j|C_j)$ is greater than $P(\neg H_j|C_j)$ or not:

$$Y = \{l_j | \frac{P(H_j | C_j)}{P(\neg H_j | C_j)} > 1, 1 \le j \le q\}$$
(9)

According to the Bayes Theory, we have:

$$\frac{P(H_j|C_j)}{P(\neg H_i|C_i)} = \frac{P(H_j) \cdot P(C_j|H_j)}{P(\neg H_i) \cdot P(C_i|\neg H_i)} \tag{10}$$

Here, $P(H_j)$ and $P(\neg H_j)$ represents the prior probability that H_j holds and doesn't hold. Furthermore, $P(C_j|H_j)$ represents the likelihood that x has exactly C_j neighbors with label l_j when H_j holds, and $(P(C_j|\neg H_j))$ represents the likelihood that x has exactly C_j neighbors with label l_j when H_j doesn't hold.

When we count the prior probabilities, we integrated our coupled label similarity into the process:

$$P(H_j) = \frac{s + \sum_{i=1}^{m} \delta_{L_i^*|j}}{s \times 2 + m \times n};$$

$$P(\neg H_j) = 1 - P(H_j);$$
(11)

where $(1 \leq j \leq n)$ and m is the records number in training set, and s is a smoothing parameter controlling the effect of uniform prior on the estimation which generally takes the value of 1 (resulting in Laplace smoothing).

Same as ML-kNN, for the j-th class label l_j , our CML-kNN maintains two frequency arrays α_j and β_j . As our method considers the other labels which have a similarity to a specific label, the frequency arrays will contain $k \times n + 1$ elements:

$$\alpha_{j}[r] = \sum_{i=1}^{m} \delta_{L_{i}^{*}|j} | C_{j}(x_{i}) = r \qquad (\delta_{L_{i}^{*}|j} \ge 0.5)$$

$$\beta_{j}[r] = \sum_{i=1}^{m} (n - \delta_{L_{i}^{*}|j}) | C_{j}(x_{i}) = r \quad (\delta_{L_{i}^{*}|j} < 0.5)$$
(12)

Where $(0 \le r \le k \times n)$. We take an instance with $\delta_{L_i^*|j} \ge 0.5$ as an instance which does have label j and we take an instance with $\delta_{L_i^*|j} < 0.5$ as an instance which doesn't have label j. Therefore, $\alpha_j[r]$ counts the sum of CLS values to label j of training examples which have label l_j and have exactly r neighbors

with label l_j , while $\beta_j[r]$ counts the CLS to label j of training examples which don't have label l_j and have exactly r neighbors with label l_j . Afterwards, the likelihood can be estimated based on elements in α_j and β_j :

$$P(C_j|H_j) = \frac{s + \alpha_j[C_j]}{s \times (k \times n + 1) + \sum_{r=0}^{k \times n} \alpha_j[r]}$$

$$P(C_j|\neg H_j) = \frac{s + \beta_j[C_j]}{s \times (k \times n + 1) + \sum_{r=0}^{k \times n} \beta_j[r]}$$

$$(1 \le j \le n, 0 \le C_j \le k \times n)$$

$$(13)$$

Thereafter, by combing the prior probabilities (Eq.11) and the likelihoods (Eq.13) into Eq.(10), we will get the predicted label set in Eq.(9).

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Algorithm 1. Coupled ML-kNN Algorithm
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Input: An unlabeled instance x_t and a labeled dataset
    T\{(x_1, L(x_1)), \dots, (x_m, L(x_m))\}\, where |T| = m and |L| = n
Output: The label set L(x_t) of instance x_t
 1: Calculate the CLS array A(L) according to Eq. (7);
2: for i = 1 to m do;
3:
        Identify the k nearest neighbors N(x_i) for x_i
4: end for
5: for j = 1 to n do
       Calculate P(H_j) and P(\neg H_j) according to Eq.(11)
7:
       Maintain the label-coupled frequency arrays \alpha_i, \beta_i using Eq.(12)
8: end for
9: Identify the k nearest neighbors N(x_t) for x_t
10: for j = 1 to n do
        Calculate the statistic C_j according to Eq.(8)
12: end for
13: Return the label set L(x_t) of instance x_t according to Eq.(9)
```

3.5 Algorithm

Given an unknown test instance x_t , the algorithm determines the final label set of the instance. Algorithm 1 illustrates the main idea of our process. Our proposed CML-kNN contains of six main parts. a)Maintain the label similarity array; b)Finding the nearest neighbors for every instance in training set; c)Getting the prior probabilities and frequency arrays; d)Finding the nearest neighbors for the target instance; e)Calculate the statistics value; f)Calculate the result.

Firstly, we calculate the label similarity according to their inter-relationships and maintain the Coupled Label Similarity Array A(L) from the training data set. Secondly, for every training instance, we identify its traditional k nearest neighbors. After that, for every different label, we calculate its prior probability which combined with CLS. Simultaneously, we expand the neighbors set for every instance to a new label-coupled neighbors set using the CLS, and calculate

the frequency array for every label. After these works done, we identify the k neighbors of the test instance x_t . After applying CLS on this neighbor set and calculate the label statistics, we can finally get the predicted label set.

It is worth noting that our key idea is the label similarity, which tries to learn the label distance and then transfer any label into a specific label.

4 Experiments and Evaluation

4.1 Experiment Data

A total of eight commonly used multi-label data sets are tested for experiments in this study, and the statistics of the data sets are shown in Table 4. Given a multi-label data set $M = \{(x_i, L_i) | 1 \le i \le q\}$, we use |M|, f(M), La(M), F(M) to represent the number of instances, number of features, number of total labels, and feature type respectively. In addition, several multi-label statistics [9] are also shown in the Table. The Label cardinality (LC(M)) measures the average number of labels per example; the Label density (LD(M)) normalizes LC(M) by the number of possible labels; the Distinct label sets (DL(M)) counts the number of distinct label combinations appeared in the data set; the Proportion of distinct label sets (PDL(M)) which normalizes DL(M) by the number of instances. As shown in Table 4, eight data sets are included and are ordered by Label density LD(M).

4.2 Experiment Setup

In our experiments, we compare the performance of our proposed CML-kNN with that some state-of-the-art multi-label classification algorithms: ML-kNN, IBLR and BSVM. All nearest neighbor based algorithms are parameterized by the size of the neighborhood k. We repeat the experiments with k=5,7,9 respectively (odd number for voting), and use the Euclidean metric as the distance function when computing the nearest neighbors. For BSVM, models are learned via the cross-training strategy[2]. We also choose the BR-kNN as the basic algorithm to compare with. We perform 10-fold cross-validation three times on all the above data sets.

Data Set	M	f(M)	La(M)	LC(M)	LD(M)	DL(M)	PDL(M)	F(M)
emotions	593	72	6	1.869	0.311	27	0.046	n
yeast	2417	103	14	4.237	0.303	198	0.082	n
image	2000	294	5	1.236	0.247	20	0.010	n
scene	2407	294	6	1.074	0.179	15	0.006	n
enron	1702	1001	53	3.378	0.064	753	0.442	c
genbase	662	1185	27	1.252	0.046	32	0.048	c
medical	978	1449	45	1.245	0.028	94	0.096	c
bibtex	7395	1836	159	2.402	0.015	2856	0.386	\mathbf{c}

Table 4. Experiment Data Sets

4.3 Evaluation Criteria

Multi-label classification requires different metrics than those used in traditional single-label classification. A lot of criteria have been proposed for evaluating the performance of multi-label classification algorithms [12]. In this paper, we use three popular evaluation criteria for multi-label classification: the **Hamming Loss**, the **One Error** and the **Average Precision**. The definitions of them can be found in [10].

4.4 Experiment Results

The experiment results are shown in Table 5 - Table 7. For each evaluation criterion, "\perp " indicates "the smaller the better", while "\perp " indicates "the bigger the better". And the numbers in parentheses denote the rank of the algorithms among the five compared algorithms.

The result tables indicate that CML-kNN and BSVM outperforms other algorithms significantly, which implies that exploiting the frequency of neighbors' label is effective, and especially for our CML-kNN, the improvement is significant compared to BR-kNN, that means incorporating the label relationship will greatly improve the BR strategy. Meanwhile, ML-kNN, IBLR and BR-kNN do not perform as well compared to the other algorithms. This implies that only exploiting the exact neighbor information is not sufficient, and the similar neighbor (correlations between labels) should also be considered.

	CML-kNN	\mathbf{BR} - $k\mathbf{NN}$	ML-kNN	IBLR	BSVM
emotions	0.189(1)	0.219(5)	0.194(2)	0.201(4)	0.199(3)
yeast	0.194(1)	0.205(5)	0.195(2)	0.198(3)	0.199(4)
image	0.157(1)	0.189(5)	0.172(2)	0.182(4)	0.176(3)
scene	0.078(1)	0.152(5)	0.084(2)	0.089(3)	0.104(4)
enron	0.061(4)	0.052(2)	0.052(2)	0.064(5)	0.047(1)
genbase	0.003(2)	0.004(3)	0.005(4)	0.005(4)	0.001(1)
medical	0.013(1)	0.019(4)	0.016(3)	0.026(5)	0.013(1)
bibtex	0.013(1)	0.016(4)	0.014(2)	0.016(4)	0.015(3)
AvgRank	(1.50)	4.13	2.38	4.00	2.50

Table 5. Experiment Result1 - Hamming Loss \

Table 6. Experiment Result2 - One Error↓

	CML-kNN	\mathbf{BR} - $k\mathbf{NN}$	ML-kNN	IBLR	BSVM
emotions	0.244(1)	0.318(5)	0.263(3)	0.279(4)	0.253(2)
yeast	0.222(1)	0.235(4)	0.228(2)	0.237(5)	0.232(3)
image	0.267(1)	0.601(5)	0.319(3)	0.432(4)	0.314(2)
scene	0.197(1)	0.821(5)	0.219(2)	0.235(3)	0.251(4)
enron	0.308(3)	0.237(1)	0.313(4)	0.469(5)	0.245(2)
genbase	0.008(2)	0.012(5)	0.009(3)	0.011(4)	0.002(1)
medical	0.158(2)	0.327(4)	0.252(3)	0.414(5)	0.151(1)
bibtex	0.376(1)	0.631(5)	0.589(3)	0.576(2)	0.599(4)
AvgRank	(1.50)	4.25	2.88	4.00	2.38

	CML-kNN	\mathbf{BR} - $k\mathbf{NN}$			BSVM
emotions	0.819(1)	0.595(5)	0.799(3)	0.798(4)	
yeast	0.769(1)	0.596(5)	0.765(2)	0.759(3)	0.749(4)
image	0.824(1)	0.601(5)	0.792(3)	0.761(4)	
scene	0.885(1)	0.651(5)	0.869(2)	0.862(3)	0.849(4)
enron	0.591(3)	0.435(5)	0.626(2)	0.564(4)	\ /
genbase	0.994(3)	0.992(4)	0.989(5)	0.994(2)	\ /
medical	0.876(1)	0.782(4)		0.686(5)	
bibtex	0.567(1)	0.329(5)	0.351(4)	0.476(3)	0.531(2)
AvgRank	(1.50)	4.75	3.00	3.50	2.25

Table 7. Experiment Result3 - Average Precision↑

Overall, our proposed CML-kNN outperforms all the compared methods on all three measures. The average ranking of our method on these data sets using three different metrics is the first one, with (1.50, 1.50, 1.50) respectively, while the second best algorithm, BSVM, only achieves (2.50, 2.38, 2.25). The BR-kNN performs the worst, which only achieves (4.13,4.25,4.75).

It is worth noting that although our proposed method runs the best on average, it does not mean that it is suitable for all kinds of data. For example, when used on data set "enron" and "genbase", the result is not as good as on other data sets. Sometimes it even got a worse result than BR-kNN. For example, when used on "enron" and evaluated by the Hamming Loss, our supposed CML-kNN only achieved a 4th rank(0.061), while BR-kNN can get a second well result(0.052). The reason is because of the weak or loose connection between different labels in those data sets, and our extended neighbors may introduce more noisy information than useful information. But in terms of average performance, our method performs the best (the first rank).

5 Conclusions and Future Work

ML-kNN learns a single classifier h_i for each label l_i independently, so it is actually a binary relevance classifier. In other words, it does not consider the correlations between different labels. The algorithm is often criticized for this drawback. In this paper, we introduced a coupled label similarity, which explores the inner-relationship between different labels in multi-label classification according to their natural co-occupance. This similarity reflects the distance of the different labels. Furthermore, by integrating this similarity into the multi-label kNN algorithm, we overcome the ML-kNN's shortcoming and improved the performance. Evaluated over three commonly-used multi-label data sets and in terms of Hamming Loss, One Error and Average Precision, the proposed method outperforms ML-kNN, BR-kNN, IBLR and even BSVM. This result shows that our supposed coupled label similarity is appropriate for multi-label learning problems and can work more effectively than other methods.

Our future work will focus on expanding our coupled similarity to categorical multi-label data, and even mixed type multi-label data for which current numerical distance metrics is not suitable.

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