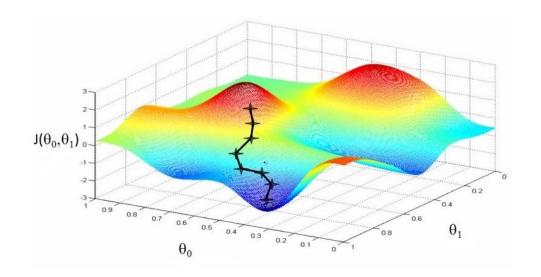


M2 – Optimisation in Computer Vision Part 2 – Poisson Editing

Karim Lekadir karim.lekadir@ub.edu

Optimisation



- The act of making something as good as possible (dictionary)
- Making the best out of situation
- Finding maximum or minimum of a function (mathematics)
- Finding the best possible solution, given some criteria

Optimisation

Well-posed problem:

- 1. A solution exists
- 2. The solution is unique
- 3. The solution's behaviour changes continuously with the initial conditions

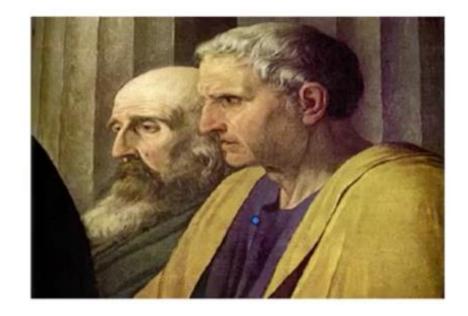
- In computer vision, we often deal with complex ill-posed problems.
- Analytical solutions are often not available.
- Optimisation can help find an acceptable solution to an ill-posed problem

Optimisation in Computer Vision

- 1. Define a set of **criteria** to solve the computer vision problem
- 2. Define each criterion semantically
- 3. Then, define each criterion mathematically
- 4. Find a solution that is an "optimal" compromise of the different criteria
- 5. For example, find a method to minimise or maximise an energy function that is the sum of multiple terms corresponding to the different criteria

 Inpainting is the process of producing a complete image from an image with damaged, deteriorating, or missing parts



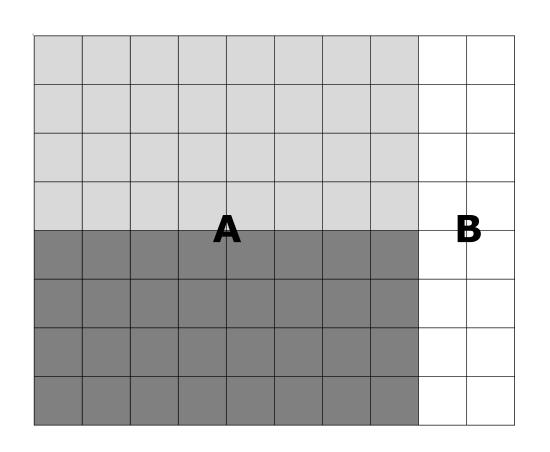


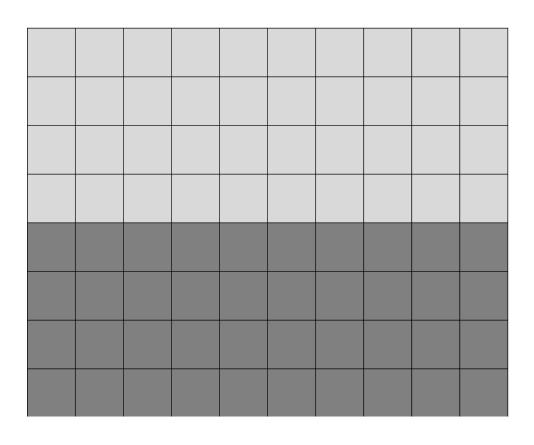
 Inpainting is the process of producing a complete image from an image with damaged, deteriorating, or missing parts



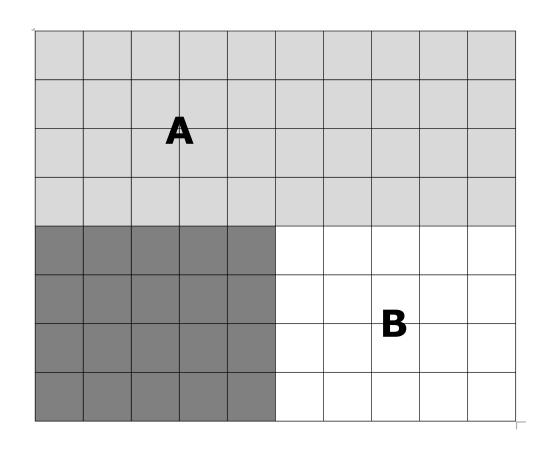


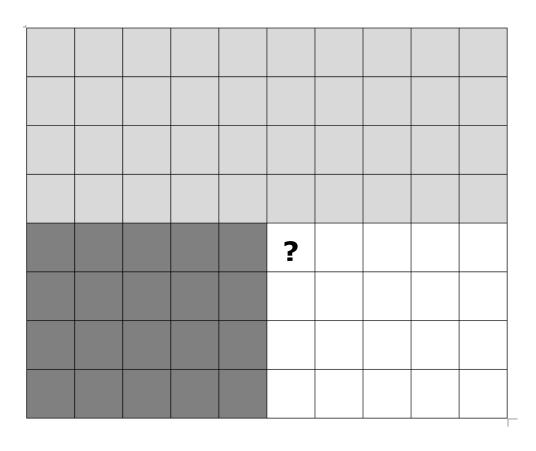
Well-posed problem





Ill-posed problem





- We have an image U = (A, B), we produce a new image V
- Criteria:
 - 1. In A, the inpainted image should be the same in V as in U
 - 2. In B, the inpainted image should be smooth

$$V(x,y) = U(x,y)$$
 at each (x,y) in A

$$4V(x,y) - (V(x-1,y) + V(x-1,y) + V(x,y-1) + V(x,y+1)) = 0$$
 at each (x,y) in B

- We must solve this for m by n pixels (e.g. 128 * 128 = 16384)
- We will have m by n equations and unknowns (system of linear equations)
- But we will work with (m+2) by (n+2) images (ghost boundaries)

Code

```
A=sparse(idx Ai, idx Aj, a ij, ???, ???); %??? and ???? is the size of matrix A
x=mldivide(A,b); u ext=reshape(x, ni+2, nj+2);
%Inner points
for j=2:nj+1
    for i=2:ni+1
        %from image matrix (i,j) coordinates to vectorial (p) coordinate
        p = (j-1) * (ni+2) + i;
        if (dom2Inp ext(i,j)==1) %If we have to inpaint this pixel
            %Fill Idx Ai, idx Aj and a ij with the corresponding values and
            %vector b
            %TO COMPLETE
```



Image A

Image B





Image H (Incorrect)



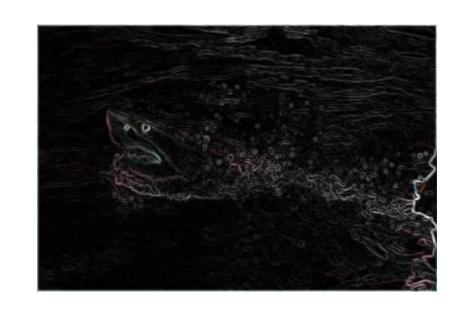
Image H (Correct)

Image H (new)

Image B



√B (gradient)



 Criterion 1: We want the transition between A and B to be smooth

$$H(x,y) = A(x,y)$$
 at each (x,y) of the boundary of B

 Criterion 2: We want to keep the details of image B, i.e. the gradients at each point

$$\nabla H(x,y) = \nabla B(x,y)$$
 at each (x,y) inside B

 Criterion 1: We want the transition between A and B to be smooth

$$H(x,y) = A(x,y)$$
 at each (x,y) of the boundary of B

 Criterion 2: We want to keep the details of image B, i.e. the gradients at each point

$$4H(x,y) - \sum H(x + dx, y + dy) = 4B(x,y) - \sum B(x + dx, y + dy)$$