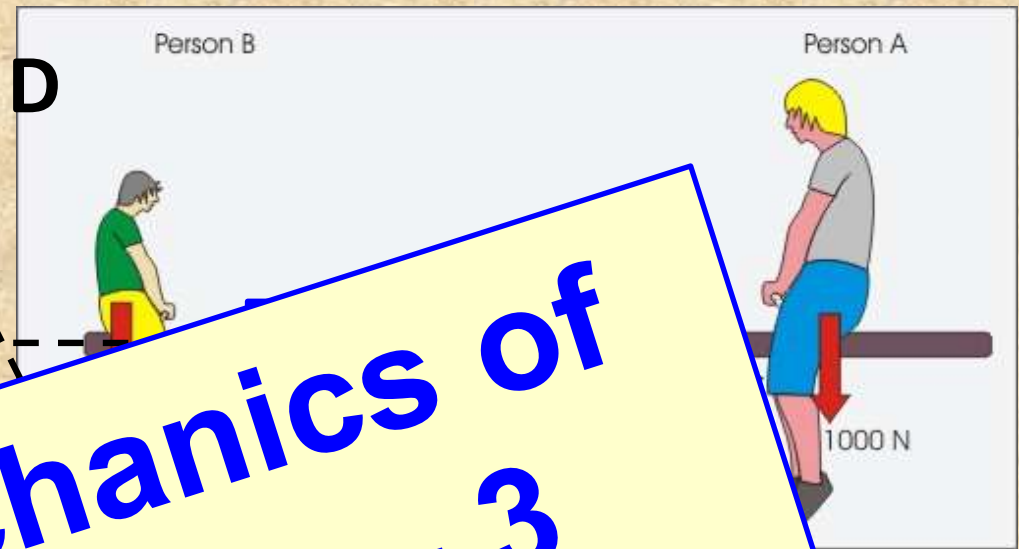




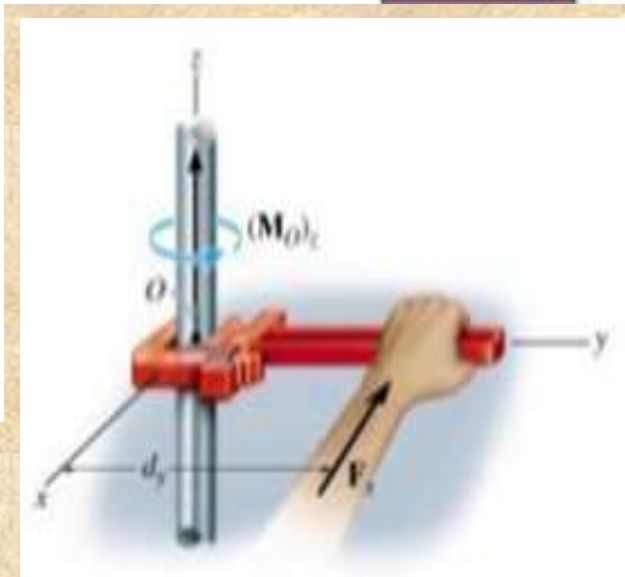
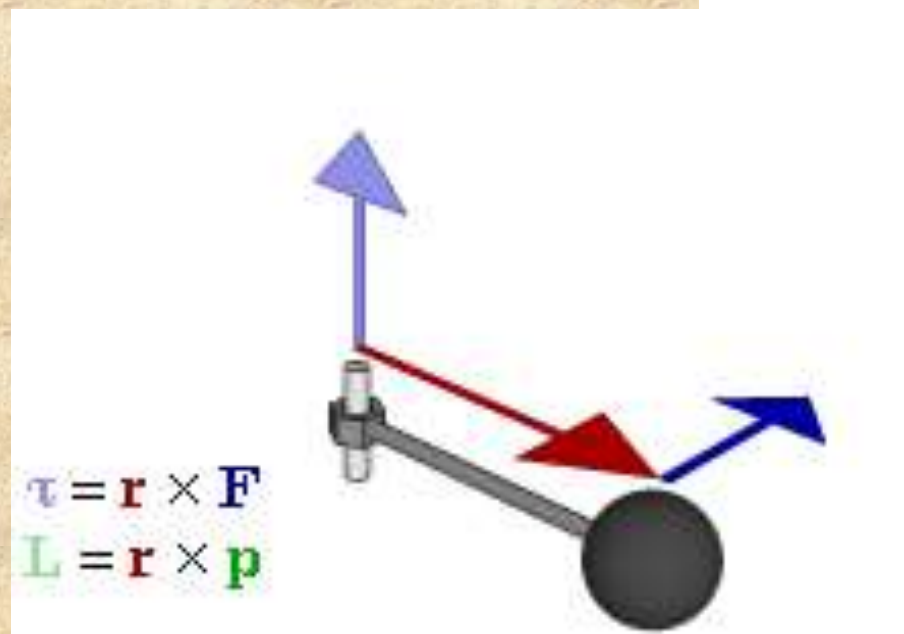
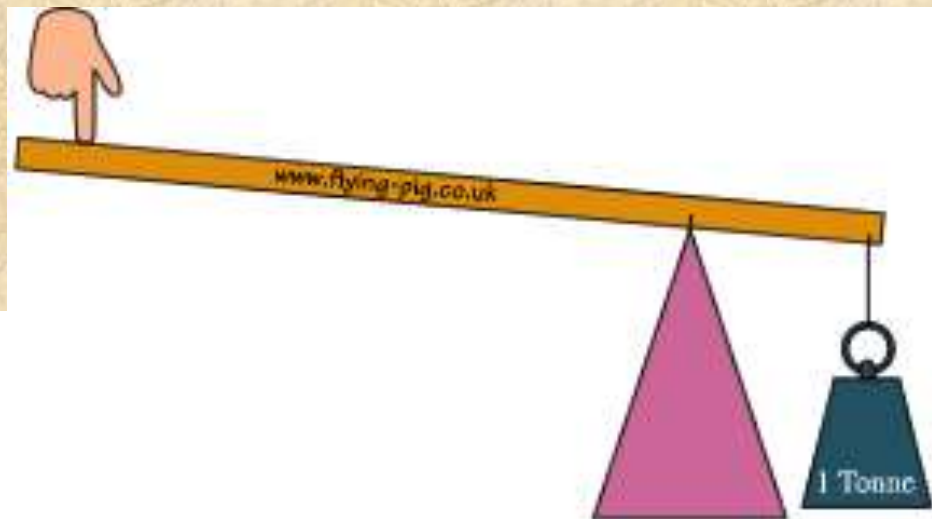
Area			
Rectangle			
Square		$\frac{a^4}{12}$	$\frac{a^4}{6}$
Triangle		$\frac{h^3}{36}$	$\frac{bh}{36}(b^2 - ba + a^2)$

# Mechanics of Robots - 3

## FY - DESH - VIT



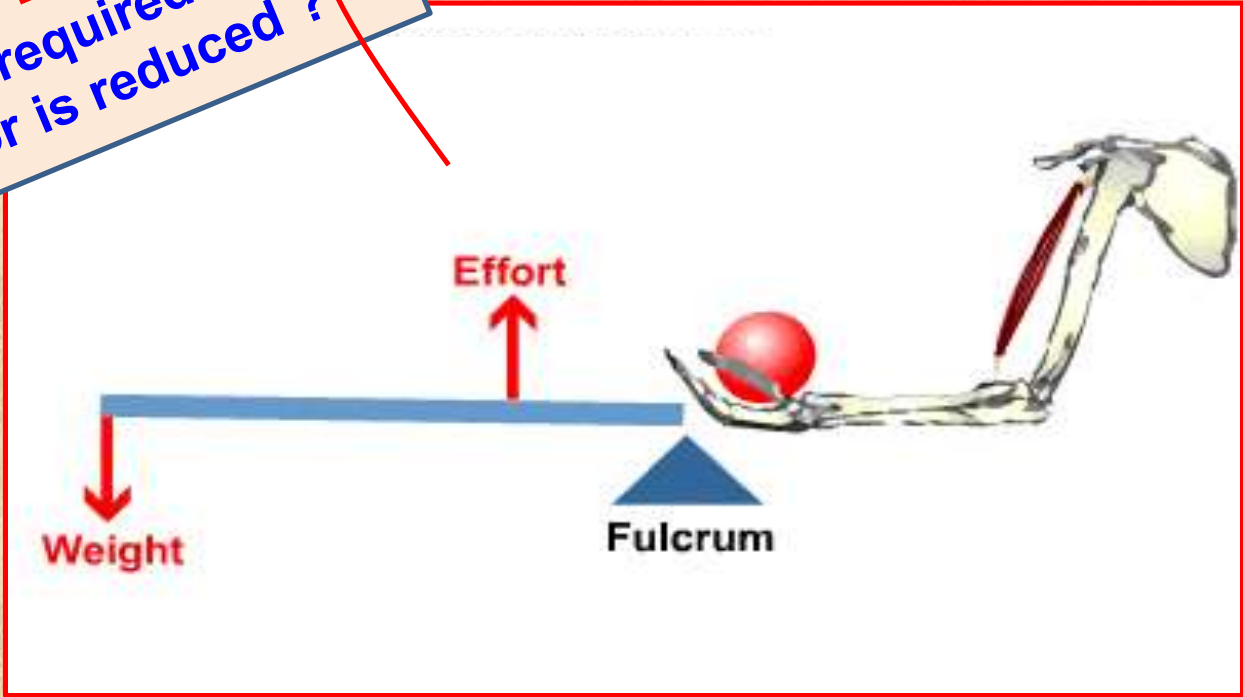
Observe these actions carefully -



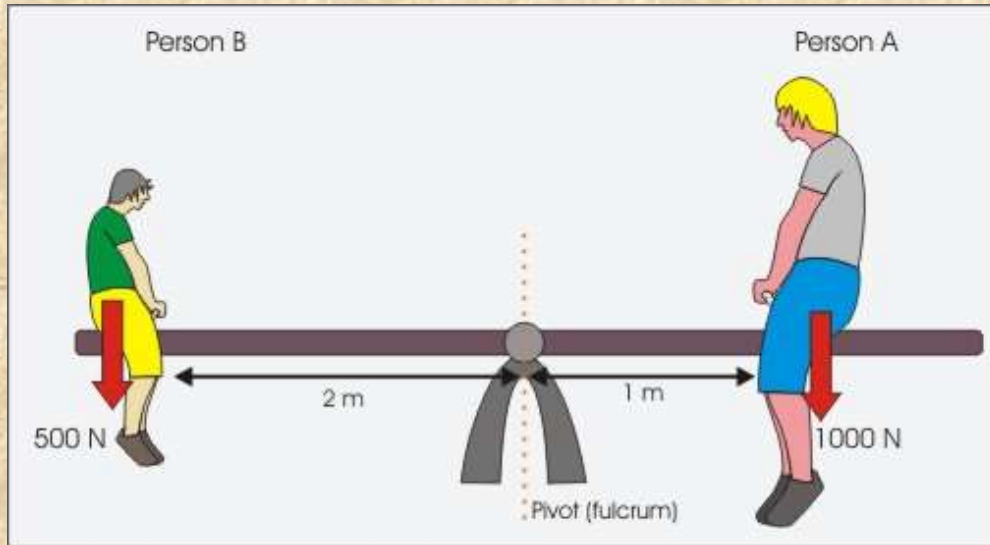
Observe these actions carefully -

In Robotics, this Effort is provided by an **actuator** for e.g. an electric motor or pneumatic actuator. The (load), the different distances should regulate the power of the actuator.

Can you suggest a better location for **Effort** so that the Power required by the Actuator is reduced ?



Observe these actions carefully -





## Moment of a Force is .....

.... the **Turning effect** produced by the force on the body.

.... a **measure of its tendency to cause a body to rotate** about a specific point or axis. (also known as Torque)

A moment is due to a force not having an equal and opposite force directly along it's line of action. Thus ....

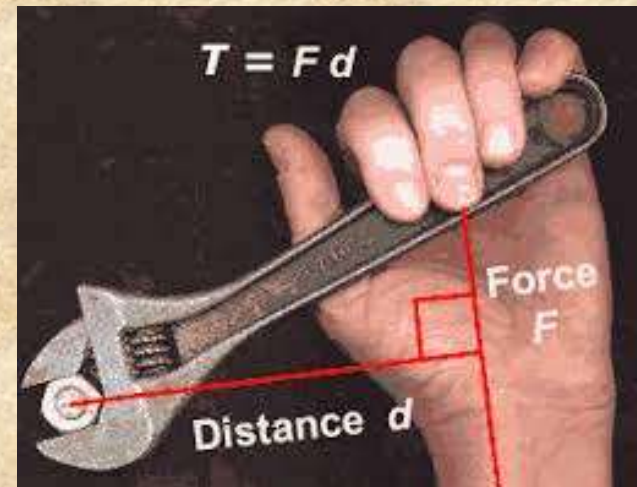
$$\text{Torque} = \text{Force} \times \text{Distance} (\perp)$$

The moment of the force is **zero** when either .....

1) the force is **zero**

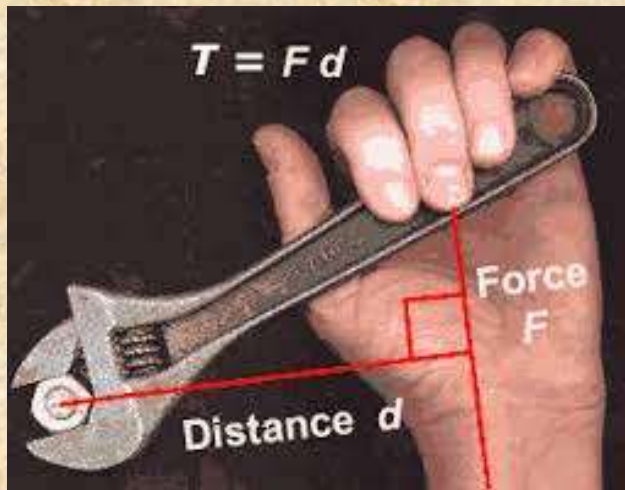
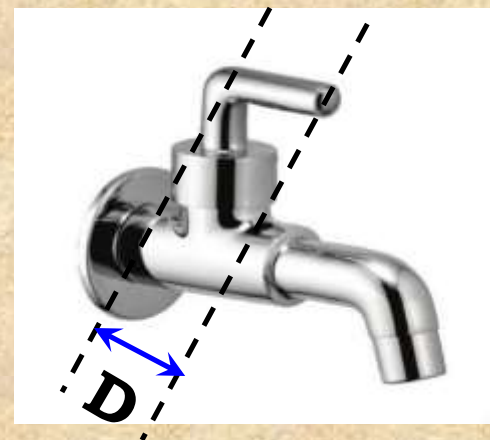
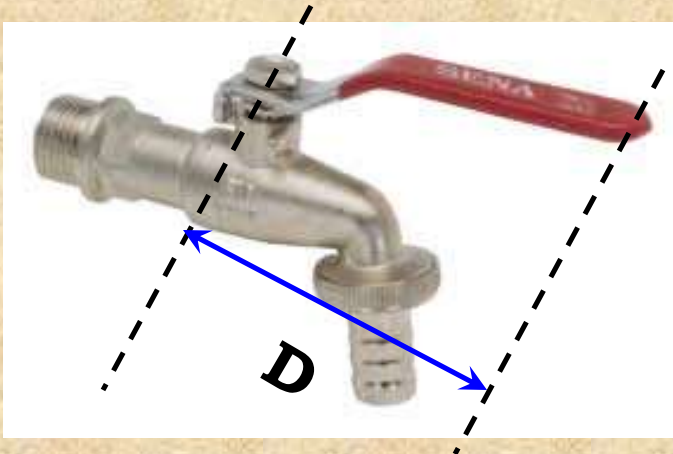
OR

2) when the perpendicular distance is **zero**



# Moment of a Force .....

Which tap is **EASY** to operate ?



# Moment of a Force .....

Comment on these two photos ....





## Couple -



Comment on the two **steering positions** in the above images.



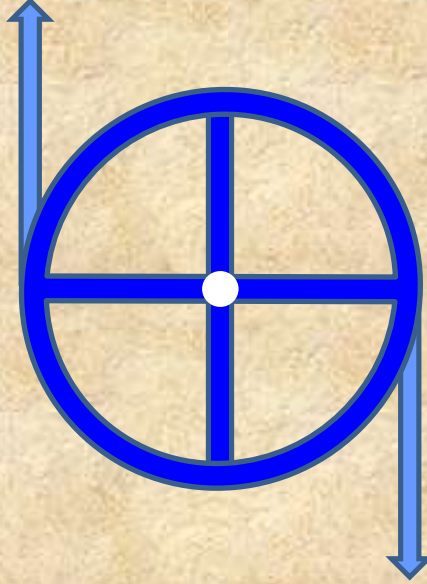


## Couple -

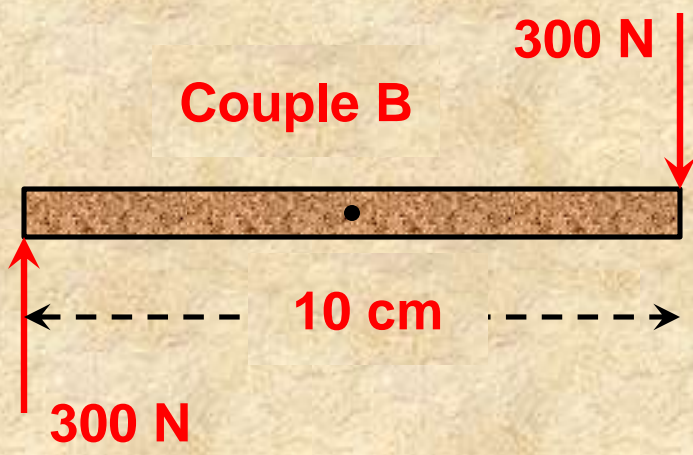
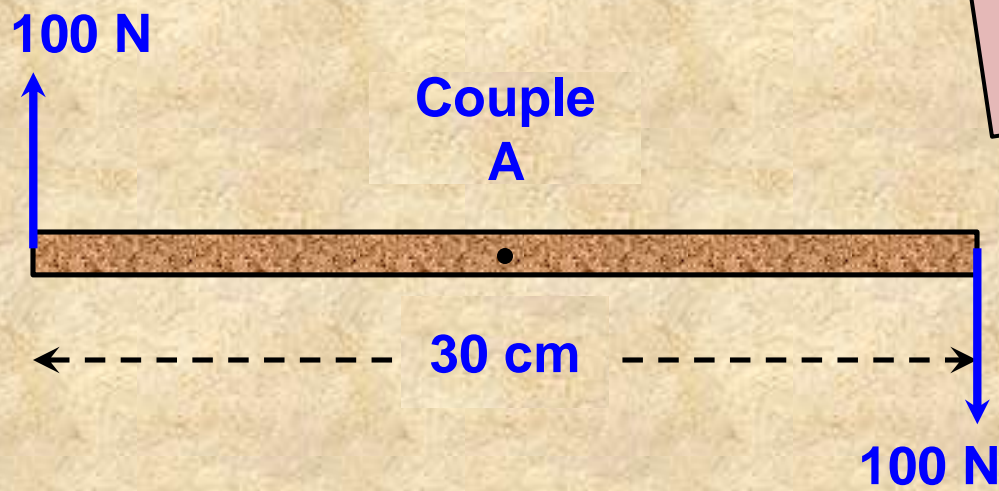
A couple is formed by two forces that are .....

- a) equal in magnitude ,
  - b) opposite in direction and
  - c) parallel in action
- The effect of a couple on the body is to produce **rotation**.
  - **Moment of Arm of Couple** - The perpendicular distance between the two lines of action of forces forming the couple is called the “ **Moment Arm**” of the couple.
  - The **magnitude** of couple is defined as the **product** of the **magnitude** of the force and the moment arm.
  - The sense of the couple could be CW (**-ve**) or CCW (**+ve**). Couple is measured in “**N-m**”.

## Couple -



# Couple -



**Are both the couples Equivalent ...?**

For equivalence ....

couples should have

- 1) Same magnitude
- 2) Same sense

**Which one is easy to operate manually ?  
Why ?**

**Do both have the same sense ?**



# Moment of Inertia of a body

M.I. is a quantity which expresses a **tendency to resist angular rotation.**

It is just like .....

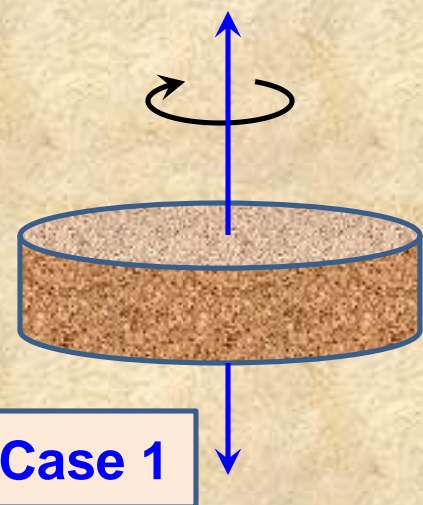
How much **force** is required to **linearly accelerate** a mass ?

How much **torque** is required to **angularly accelerate** a mass ?

The amount of torque needed to cause any given **angular acceleration** (the rate of change in angular velocity) is proportional to the moment of inertia of the body.

Moment of Inertia is also called as **Second Moment of Area**  
OR **Area Moment of Inertia.**

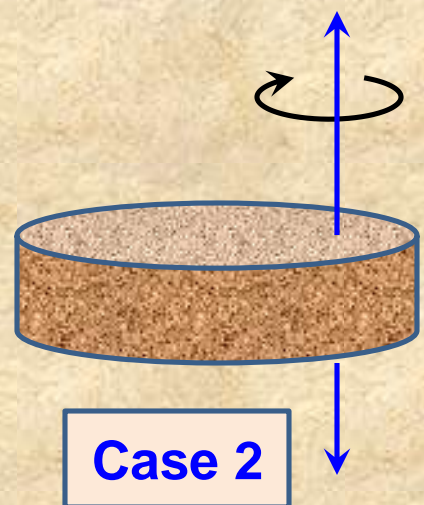
# Moment of Inertia of a body -



The body rotates about a certain axis. If the axis changes, the moment of inertia of the body will definitely change.

*Will the M.I. change? Justify!*

*Which case will have higher M.I.? Justify!*



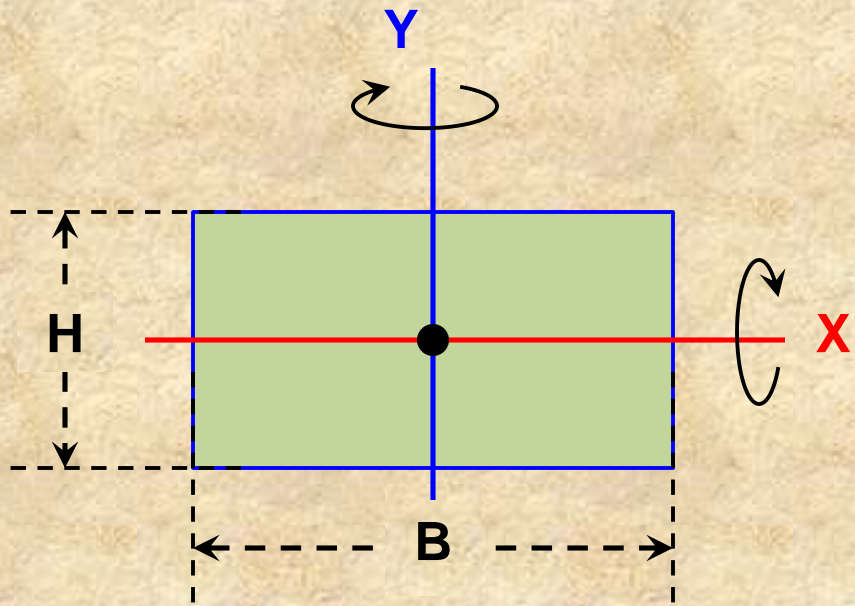
**Moment of inertia is defined as the product of *mass* of section (*m*) and the square of the distance ( $r^2$ ) between the reference axis and the Centroid of the section.**

$$I_P = \sum_{i=1}^N m_i r_i^2$$

*$m_1, m_2, m_3$  ..... are the masses of all particles.*

*$r_1, r_2, r_3$  ..... are the respective distances (squared) from the axis of rotation.*

# Moment of Inertia of a body – list of formulae



About	Formula
X	$\frac{B H^3}{12}$
Y	$\frac{B^3 H}{12}$



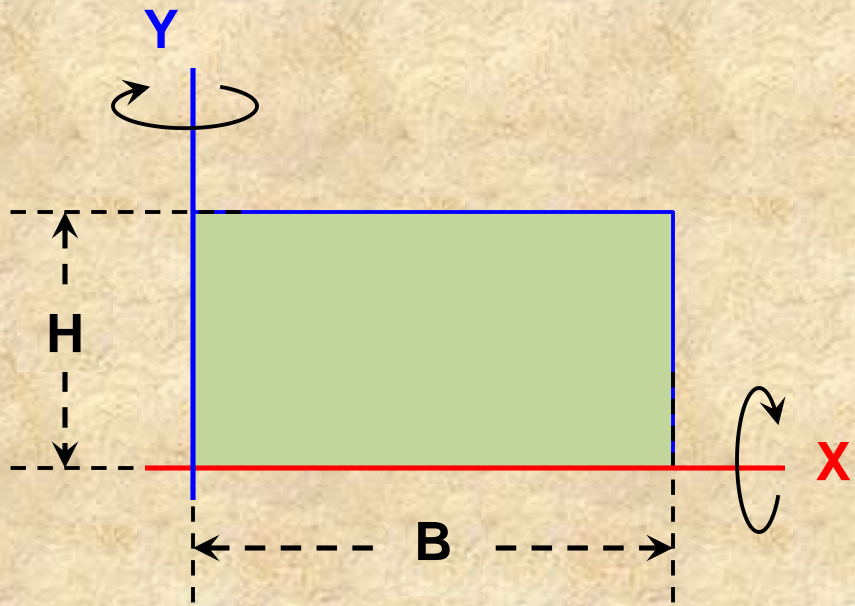
Point of confusion :- Which term to be **cubed** ? B or H ?

That length which is at right angles to the axis of rotation .....

**Point to remember : axes are passing through the centre ....**



# Moment of Inertia of a body – list of formulae

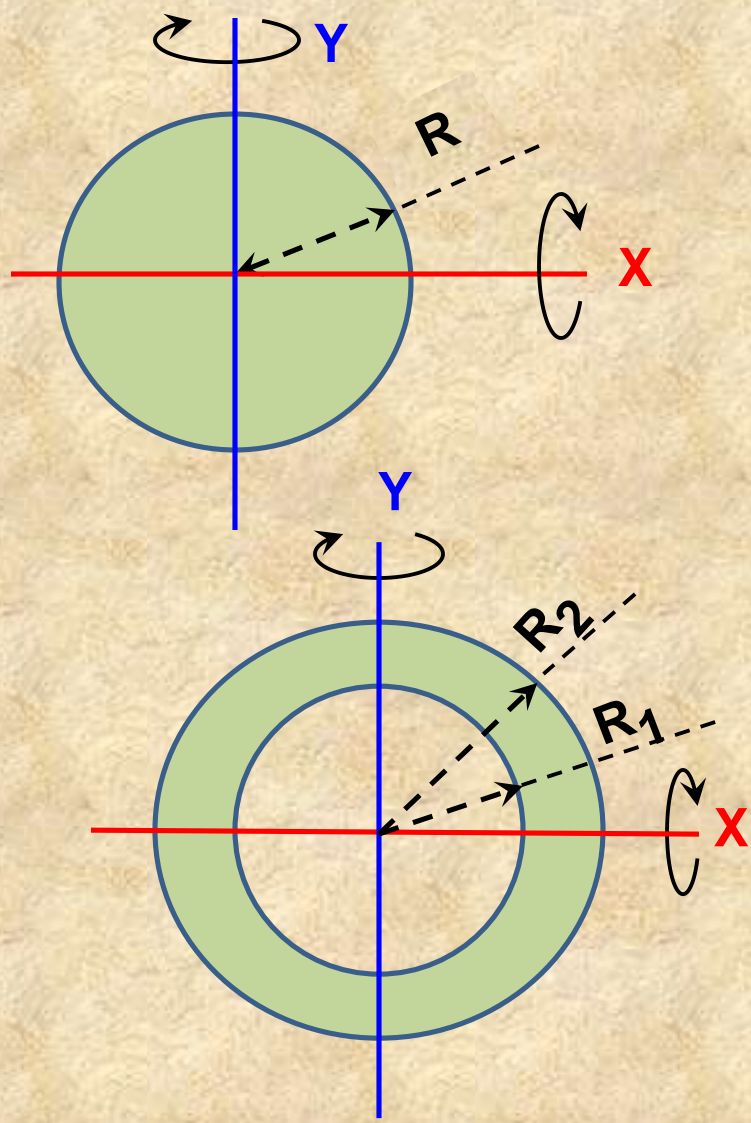


About	Formula
X	$\frac{B H^3}{3}$
Y	$\frac{B^3 H}{3}$

**Why the M.I. is higher in this case ?  
 (axes are on the edges )**



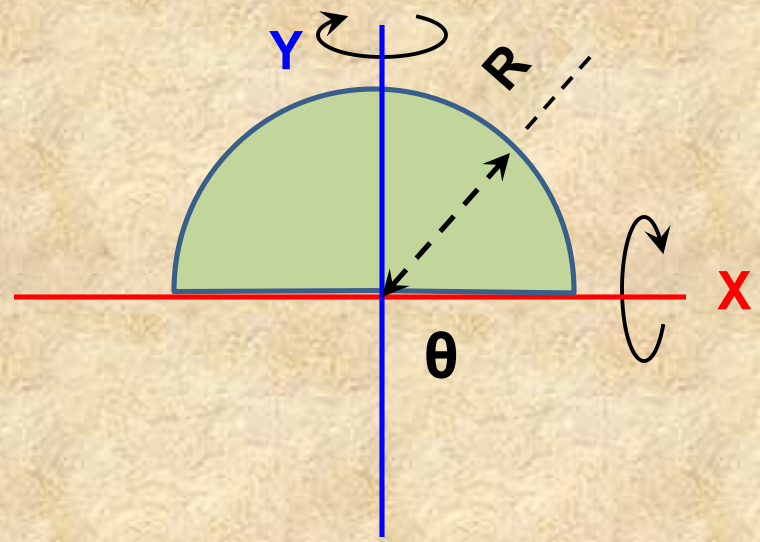
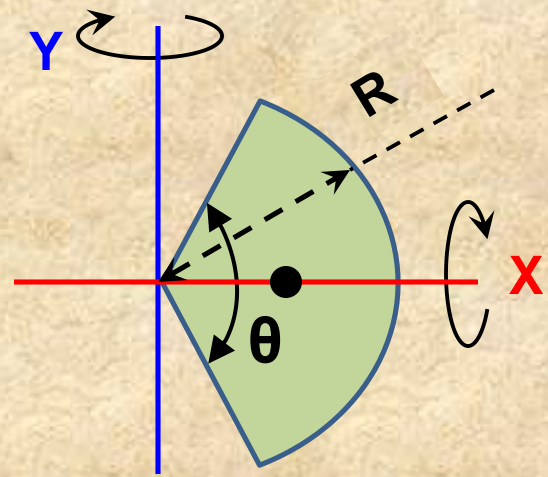
# Moment of Inertia of a body – list of formulae



About	Formula
X	$\frac{\pi R^4}{4}$
Y	$\frac{\pi R^4}{4}$

X	$\frac{\pi (R_2^4 - R_1^4)}{4}$
Y	$\frac{\pi (R_2^4 - R_1^4)}{4}$

# Moment of Inertia of a body – list of formulae

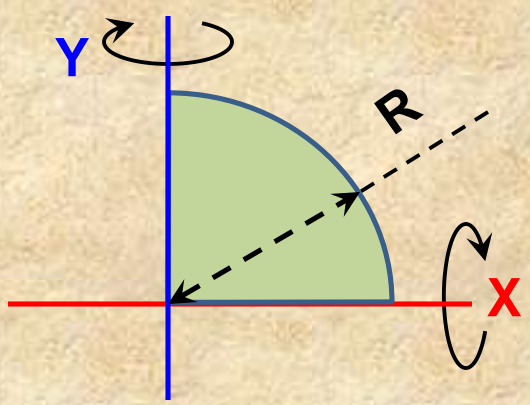
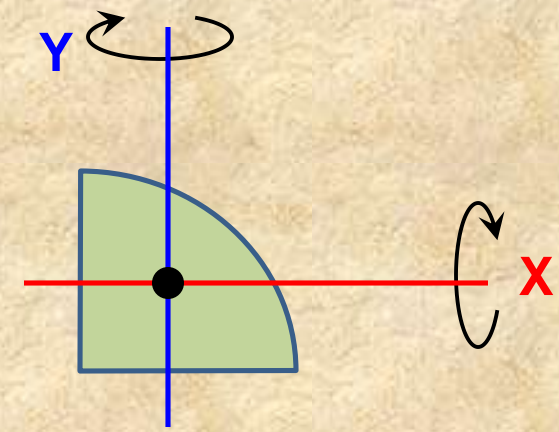


About	Formula
X	$\frac{(\theta - \sin \theta) R^4}{8}$
Y	$\frac{\pi R^4}{4}$

X	$\frac{\pi R^4}{8}$
Y	$\frac{\pi R^4}{8}$

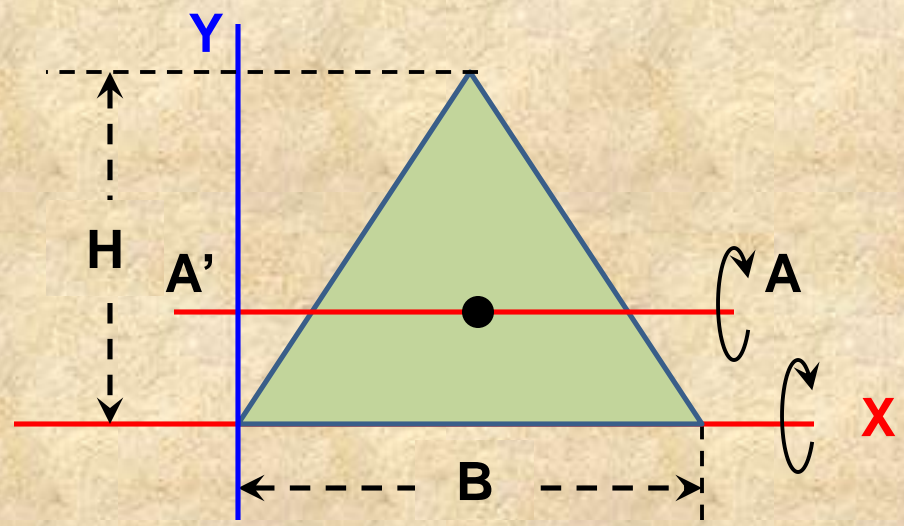


# Moment of Inertia of a body – list of formulae

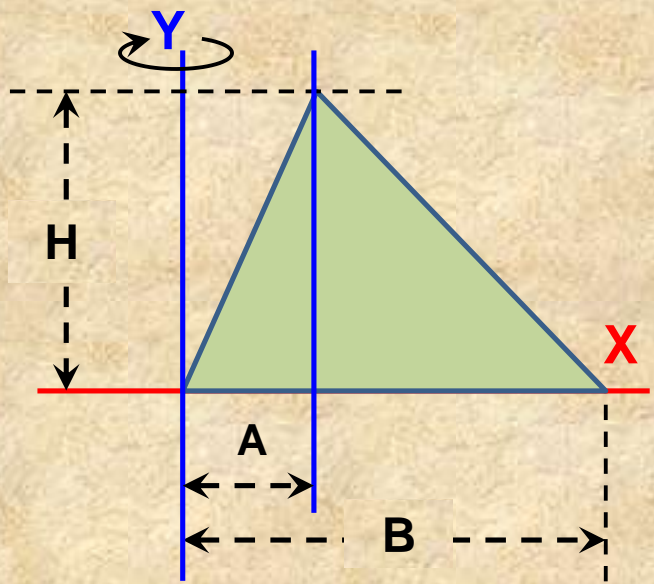


About	Formula
X Through Centroid	$0.0549 R^4$
Y Through Centroid	$0.0549 R^4$
X	$\frac{\pi R^4}{16}$
Y	$\frac{\pi R^4}{16}$

# Moment of Inertia of a body – list of formulae



About	Formula
A-A' through centroid	$\frac{B H^3}{36}$
X	$\frac{B H^3}{12}$



About	Formula
Y	$\frac{H B^3 + H A B^2 + H A^2 B}{36}$

## Parallel Axis Theorem -

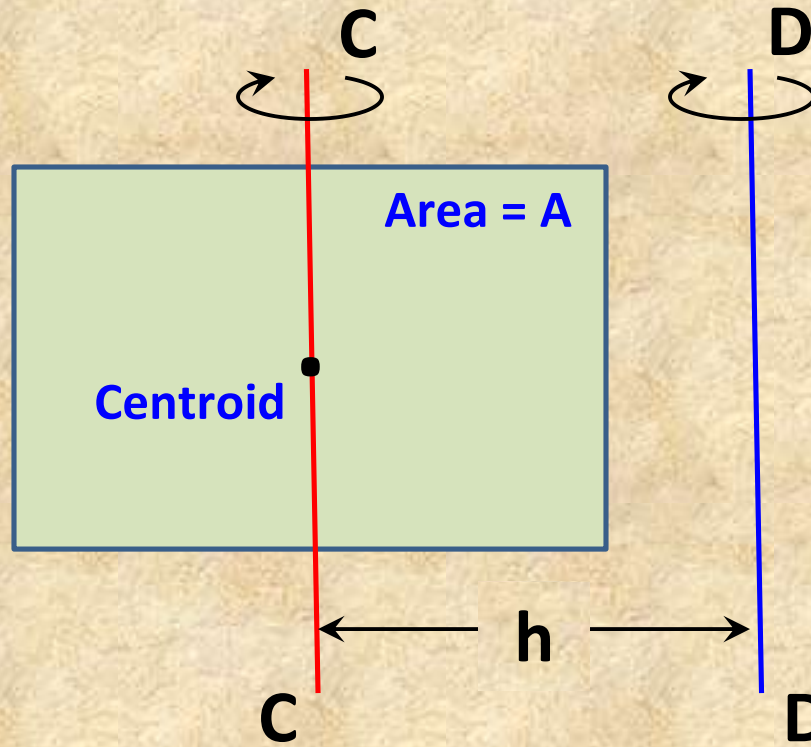
**Statement :-** The moment of inertia of a plane area with respect to any reference axis in its plane is equal to the sum of moment of Inertia with respect to a parallel centroidal axis and product of total area and the square of the distance between the two axes.

$$I_{AB} = IG + Ah^2$$

Parallel axis theorem is used to find M. I. about an axis which is not passing through C.G. of the section.



# Parallel Axis Theorem -



CC is centroidal axis.

CC is parallel to DD with distance = h

$$\text{M.I. about DD} = \text{M.I. about CC} + A \cdot h^2$$

$$I_{DD} = I_{CC} + A \cdot h^2$$

## Perpendicular Axis Theorem -

**Statement :-** The moment of inertia of an area with respect to an axis perpendicular to the x-y plane (z-axis) and passing through origin will be equal to the sum of moments of inertia of the same area about x-x and y-y axis.

$$I_{zz} = I_{xx} + I_{yy}$$

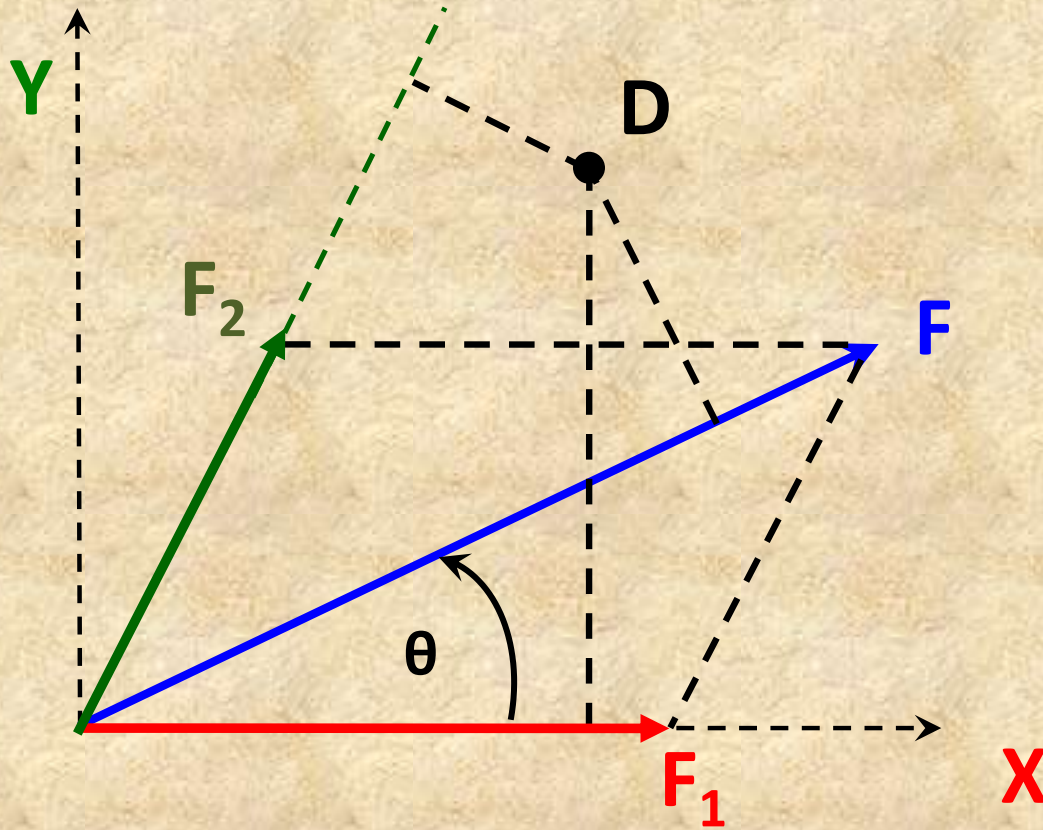
This theorem is kept for **SELF STUDY !**

You are supposed to study this topic of your own in all directions including numericals on it.

All the best wishes ...!

- **Verignon's Theorem** – The algebraic sum of the moments of all forces about any point in their plane is equal to the moment of their resultant about the same point.
- **Verignon's Theorem** – Moment of Force about any point is equal to the sum of the moments of its components about the same point.
- **Verignon's Theorem** – It is used to determine the position of Resultant of Parallel force system.

# Varignon's Theorem -



$F_1$  and  $F_2$  are  
the two  
components  
of  $F$

Moments of  $F$  about  $D$  = Moments of  $F_1$  about  $D$   
+ Moments of  $F_2$  about  $D$





Area			
Rectangle			
Square		$\frac{a^4}{6}$	
Triangle		$\frac{h^3}{36}$	$\frac{bh}{36}(b^2 - ba + a^2)$

**Mechanics of Robots - 3**

**Thanks!**

**FY - DESH - VIT**

