

MAE598

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### Homework 3.

#### Design Optimization.

#### 1. (i) Least squares problem.

The training data is provided:

$$X = \{x_1, x_2\}$$

$$y = p.$$

There are 11 data points for  $x$  &  $y$ .

The problem is to fit  $(x, y)$  in the function

$$p = x_1 \exp\left(A_{12} \left(\frac{A_{21} x_2}{A_{12} x_1 + A_{21} x_2}\right)^2\right) p_{1sat} + x_2 \exp\left(A_{21} \left(\frac{A_{12} x_1}{A_{12} x_1 + A_{21} x_2}\right)^2\right) p_{2sat}$$

Here,  $p_{1sat}$  &  $p_{2sat}$  are evaluated from the given data of  $a_1, a_2$  &  $a_3$  and the Antoine equation

$$\log(p_{sat}) = a_1 - \frac{a_2}{T + a_3}$$

$$T = 20^\circ\text{C}.$$

The function can be generalized as

$$y = XB + \epsilon$$

$$\epsilon \rightarrow \text{error} \quad \& \quad B = \{A_{12}, A_{21}\}.$$



The problem at hand is to estimate  $\beta$  such that the  $L_2$  norm of  $\epsilon$  is minimized.

i.e. find  $\beta$  such that  $\min \|y - X\beta\|^2$ , the given function being a non-linear model.