

1. This part of paper is of 20 marks. Five questions of 4 marks each.
2. Maximum time for this part of paper is 60 minutes.
3. Use of Thermodynamics table is permitted.
4. Space provided is sufficient to solve the question. Do not write anything outside of the box.

- Q 1. Consider two cases for increasing the efficiency of a Carnot Engine: (a) increase the source temperature ( $T_H$ ) by  $\Delta T$  while sink temperature ( $T_L$ ) is constant, (b) Decrease the sink temperature ( $T_L$ ) by  $\Delta T$  while source temperature ( $T_H$ ) is constant. Explain with proof which of these two cases is more effective.

Solution:

The Carnot engine efficiency is given by:  $\eta = 1 - \frac{T_L}{T_H}$

Case (a) the Carnot efficiency can be written as:  $\eta_I = 1 - \frac{T_L}{T_H + \Delta T}$  (1)

Case (b) The Carnot efficiency can be written as:  $\eta_{II} = 1 - \frac{T_L - \Delta T}{T_H}$  (2)

Subtract equation (2) from equation (1)

$$\eta_I - \eta_{II} = \left(1 - \frac{T_L}{T_H + \Delta T}\right) - \left(1 - \frac{T_L - \Delta T}{T_H}\right) = +\frac{T_L - \Delta T}{T_H} - \frac{T_L}{T_H + \Delta T}$$

$$= \frac{(T_L - \Delta T)(T_H + \Delta T) - T_H T_L}{T_H(T_H + \Delta T)} = \frac{T_H T_L + (\Delta T)(T_L - T_H) - T_H T_L}{T_H(T_H + \Delta T)} = \frac{\Delta T(T_L - T_H)}{T_H(T_H + \Delta T)}$$

The denominator is always positive, since  $\Delta T > 0$ , and  $T_L - T_H < 0$

Therefore,  $\eta_I - \eta_{II} < 0$  or  $\eta_{II} > \eta_I$ , we can conclude that case (b) is always better than case (a)

- Q 2. A balloon filled with helium at 20 °C, 100 kPa and a volume of 0.5 m<sup>3</sup> is moving with a velocity of 15 m/s at an elevation of 0.5 km relative to an exergy reference environment for which  $T_0 = 20$  °C,  $p_0 = 100$  kPa. Using the ideal gas model, determine the specific exergy of the helium, in kJ/kg. Take acceleration due to gravity ( $g$ ) equal to 9.8 m/s<sup>2</sup>.

**Conceptual Q1-solution [5 marks from Simanchal]**

$$e = u - u_0 + P_0(v - v_0) - T_0(s - s_0) + V^2/2 + gZ$$

$$e = C_v(T - T_0) + P_0(RT/P - RT_0/P_0) - T_0[C_p \ln(T/T_0) - R \ln(P/P_0)] + V^2/2 + gZ - 2 \text{ Marks}$$

$$e = 15 \cdot 15/2 + 9.8 \cdot 500$$

$$e = 5.0125 \text{ kJ} - 2 \text{ Marks (Ans.)}$$

- Q 3. Air is flowing steadily in an insulated duct the pressure and temperature measurement of air at two stations A and B are given below. Establish the direction of the flow of air in the duct. Assuming constant specific heat of the air

Properties	A	B
Pressure (kPa)	130	100
Temperature (°C)	50	13

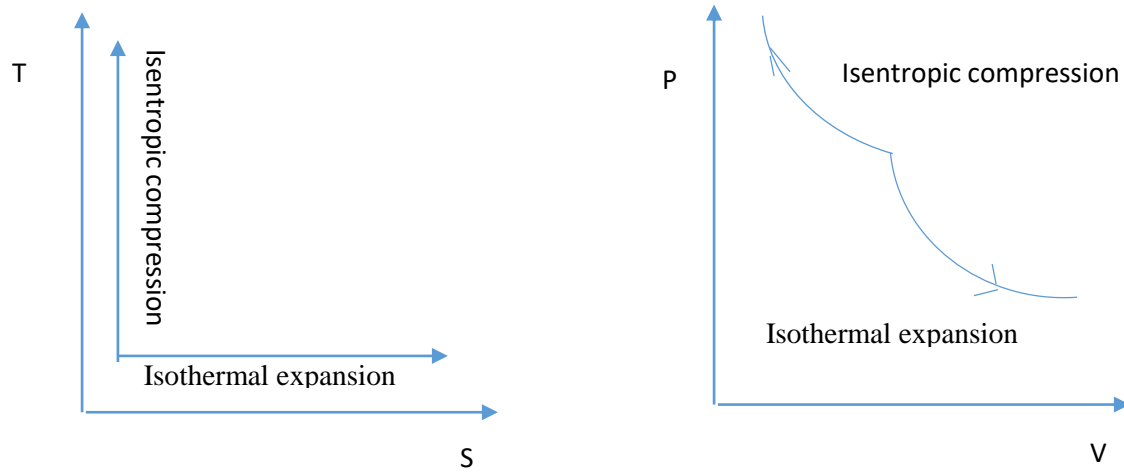
$$s_B - s_A = 1.005 \ln(T_B/T_A) - 0.287 \ln(p_B/p_A) =$$

$$= 1.005 \ln(286/323) - 0.287 \ln(100/300) = -0.1223 + 0.0753 = -0.047$$

$$\Delta S_{univ} = -0.047 \text{ kJ/kg}$$

**Hence the flow will be from B to A**

- Q 4. Sketch the T-S and P-V diagrams for an ideal gas undergoing the following transformations, all starting from the same state ( $V_1, P_1, T_1, S_1$ ). **Draw and name** two curves on T-S and two curves on P-V diagram.
- Isothermal expansion to double the initial volume
  - Adiabatic and reversible compression to half the initial volume



- Q 5. (a) Heat is lost through a plane wall steadily at a rate of 800 W. If the inner and outer surface temperatures of the wall are 20°C and 5°C, respectively, and the environment temperature is 0°C. What is the rate of exergy destruction within the wall?
- (b) A block of ice melts when left in a sunny location. Does its exergy increase or decrease? Explain in one sentence.

a)

$$\frac{800}{278} - \frac{800}{293} = S_{gen} = 0.147322 \text{ W/K}$$

$$\text{Exergy destruction} = T_0 S_{gen} = 40.22 \text{ W}$$

- b) Exergy of the system decreases as the system comes in thermodynamics equilibrium with the surrounding. Hence the exergy of the ice decreases as it melts.