

# Birla Institute of Technology & Science, Pilani (Rajasthan)

First Semester 2018-2019

## Quiz – 1 (Set A)

<b>Course Number:</b>	CS F222
<b>Date and Time:</b>	Sep 13, 2018 (9.00 To 9.45 AM)

<b>Course Title:</b>	Discrete Structures for Computer Science
<b>Max. Marks, Nature, &amp; Set :</b>	30 (15 % Weightage) [Closed Book]

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<b>Marks Obtained:</b> → _____  <b>Examiner's Signature:</b> → _____
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**Note:** Each question from Q1 to Q20 carry 1 mark, whereas each question from Q21 to Q25 carry 2 marks. There is NO NEGATIVE MARKING. You need to mark to most appropriate option. Q21-25 are to be answered in the space provided along with the question.

Q.→	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20
<b>Ans. →</b>	<b>D</b>	<b>D</b>	<b>X</b>	<b>X</b>	<b>C</b>	<b>X</b>	<b>A</b>	<b>D</b>	<b>C</b>	<b>A/C</b>	<b>D</b>	<b>D</b>	<b>X</b>	<b>C</b>	<b>B</b>	<b>B</b>	<b>B</b>	<b>A</b>	<b>C</b>	<b>C</b>

**Q.1** The number of relations on a set of  $n$  elements that are both antisymmetric and symmetric:

- (A)  $2^{n^2}$  (B)  $2^{n(n-1)}$  (C)  $2^{n(n+1)/2}$  (D)  $2^n$

**Q.2** The number of ways to go down a 7-step staircase if you go down 1, 2, or 3 steps at a time, would be:

- (A) 12 (B) 28 (C) 34 (D) 44

**Q.3** which is the correct solution for the recurrence relation  $T(n) = 4T\left(\frac{n}{2}\right) + n^2$ , with the base case  $T(1) = 1$ . Assume  $n = 2^k$ , for some integer  $k \geq 1$ .

- (A)  $n^2$  (B)  $n \log_2 n$   
(C)  $n (\log_2 n)^2$  (D)  $n^2 \log_2 n$

**Q.4** Let  $R$  be the relation on  $Z$  (set of integers) given by  $xRy$  iff  $x^2 - y^2 \leq 2$ .

- (A) Reflexive and symmetric, but not transitive.  
(B) Reflexive, not symmetric, and transitive.  
(C) Reflexive not symmetric and not transitive.  
(D) Not Reflexive, Not symmetric, and transitive.

**Q.5** Which of the following statement is true for all sets  $A$ ?

- (I) If  $R$  is an equivalence relation on  $A$ , then  $R \circ R$  is an equivalence relation on  $A$ .  
(II) If  $R$  is a partial order relation on  $A$ , then  $R \circ R$  is a partial order relation on  $A$ .  
(III) If  $R$  is a relation on  $A$  but  $R$  is not an equivalence relation, then  $R \circ R$  is not an equivalence relation on  $A$ .

- (A) II (B) III (C) I, II (D) I, II, III

**Q.6** Exactly which of the following relations  $R_1, R_2, R_3$  on  $Z^+$  (set of positive integers) are antisymmetric?

$$R_1 = \{(a, b) \mid \text{if } a^2 - b^2 = 3(a - b)\}$$

$$R_2 = \{(a, b) \mid \text{if } a \leq 2b\}$$

$$R_3 = \{(a, b) \mid \text{if } |a - b| < 4\}.$$

- (A)  $R_1, R_3$  (B)  $R_2, R_3$  (C)  $R_1, R_2$  (D)  $R_1$

**Q.7** Let  $R$  be the relation  $R = \{(a, b) \mid a < b\}$  on the set of integers. Which of the following statement is correct?

- (A)  $R^{-1} = \{(a, b) \mid a > b\}$  and  $\overline{R} = \{(a, b) \mid a \geq b\}$   
(B)  $R^{-1} = \{(a, b) \mid a \geq b\}$  and  $\overline{R} = \{(a, b) \mid a > b\}$   
(C)  $R^{-1} = \{(a, b) \mid a > b\}$  and  $\overline{R} = \{(a, b) \mid a > b\}$   
(D)  $R^{-1} = \{(a, b) \mid a \geq b\}$  and  $\overline{R} = \{(a, b) \mid a \geq b\}$   
 $\overline{R}$  = complement of  $R$ .

**Q.8** Let  $R$  be the relation  $\{(1, 2), (1, 3), (2, 3), (2, 4), (3, 1)\}$ , and let  $S$  be the relation  $\{(2, 1), (3, 1), (3, 2), (4, 2)\}$ . Which one of the following is the correct value of the reflexive closure of  $S \circ R$ ?

- (A)  $\{(2, 2), (2, 3), (3, 2), (3, 3), (3, 4), (4, 3), (4, 4)\}$   
(B)  $\{(1, 1), (2, 2), (2, 3), (3, 2), (3, 3), (3, 4), (4, 3), (4, 4)\}$   
(C)  $\{(1, 1), (1, 2), (2, 1), (2, 2)\}$   
(D) None of the above

**Q.9** If  $R = \{(x, y) \mid x \text{ and } y \text{ are bit strings containing the same number of 0s}\}$ . Which one of the following is true with respect to the equivalence class of various binary strings?

- (A)  $[1] =$  all strings which represent odd number  
(B)  $[00] =$  all strings that contain two consecutive 0's  
(C)  $[101] =$  all string which contain exactly one 0  
(D)  $[1010] \text{ not } = [00]$

**Q.10** Let  $R$  is the relation on set  $A = \{1, 2, 3, 4, 5, 6\}$  such that  $aRb$  if  $|a - b| \leq 3$ . Which of the following is true?

- (A)  $R$  is not a partial order relation  
(B)  $R^2$  is the transitive closure of relation  $R$   
(C)  $R^3$  is  $A \times A$   
(D)  $R^2$  is an equivalence relation

**Q.11** Which of the relation(s) on the given sets is(are) antisymmetric?

$S_1: A = \{1, 2, 3, 4, 5\}, R = \{(1, 3), (1, 1), (2, 4), (3, 2), (5, 4), (4, 2)\}$

$S_2: \text{set of real numbers } xRy \text{ iff } x^2 = y^2.$

- (A) Only  $S_1$  (B) Only  $S_2$  (C) Both  $S_1$  and  $S_2$  (D) Neither  $S_1$  nor  $S_2$

**Q.12** Let  $A = \{2,3,5,7,8\}$ . Which of the following relation is an equivalence relation?

- (A)  $R = \{(a,b) \mid a < 2b\}$   
 (B)  $R = \{(a,b) \mid a \bmod 3 = b \bmod 2\}$   
 (C)  $R = \{(a,b) \mid b \bmod a = 0\}$   
 (D)  $R = \{(a,b) \mid a + b \text{ is even}\}$

**Q.13** Which one of the following is the transitive closure of the relation given by the matrix?

$$\begin{bmatrix} 1 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 \end{bmatrix}$$

(A)  $\begin{bmatrix} 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$

(B)  $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$

(C)  $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$

(D)  $\begin{bmatrix} 1 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 1 \end{bmatrix}$

**Q.14** Which of the following statement is FALSE

- (A) It is not possible to obtain two consecutive even terms in the Fibonacci sequence  
 (B) not possible to obtain three consecutive odd terms in the Fibonacci sequence  
 (C) Fibonacci sequence is a bounded sequence.  
 (D) The characteristic roots of Fibonacci recurrence relation are irrationals.

**Q.15** Let  $r(R)$ ,  $s(R)$  and  $t(R)$  be the reflexive, symmetric and transitive closures of a relation  $R$  respectively. Which of the following statement is NOT correct?

- (A)  $r(s(R)) = s(r(R))$  (B)  $s(t(R)) = t(s(R))$

- (C)  $r(t(R)) = t(r(R))$  (D)  $t(s(r(R))) = r(t(s(R)))$

**Q.16** The number of bit operations required to compute the transitive closure of a relation defined on a set with 4 elements, using connectivity relation  $R^*$  and using Warshall's Algorithm are respectively:

- (A) 256, 64 (B) 384, 128 (C) 640, 128 (D) 384, 64

**Q.17** If  $R$  is the equivalence relation defined on the set  $B = \{1,2,3,4\}$  by  $R = \{(1,1), (1,2), (2,1), (2,2), (3,3), (3,4), (4,3), (4,4)\}$  then the number of equivalence classes is:

- (A) 1 (B) 2 (C) 3 (D) 4

**Q.18** A relation  $R$  is defined on ordered pairs of integers as follows :  $(x, y) R (u, v)$  if  $x < u$  and  $y > v$ . Then  $R$  is

- (A) Neither a Partial Order nor an Equivalence Relation  
 (B) A Partial Order but not a Total Order  
 (C) A Total Order  
 (D) An Equivalence Relation

**Q.19** The Hasse diagram for the partial order  $R = \{(a, b), (a, c), (a, d), (a, e), (b, e), (b, d), (c, d), (a, a), (b, b), (c, c), (d, d), (e, e)\}$  has levels.

- (A) 1 (B) 2 (C) 3 (D) 4

**Q.20** If  $C$  is a condition that elements of the  $n$ -ary relations  $R$  and  $S$  may satisfy, then

- (I)  $s_C(R \cup S) = s_C(R) \cup s_C(S)$ .  
 (II)  $s_C(R \cap S) = s_C(R) \cap s_C(S)$ .

- (A) Only I (B) Only II  
 (C) Both I and II (D) Neither I nor II

**Q.21.** A vending machine dispensing books of stamps accepts only 1 Rupee coins, 1 Rupee currency notes, and 2 Rupee currency notes. Let  $a_n$  denote the number of ways of depositing  $n$  Rupees in the vending machine, where the order in which the coins and currency notes are deposited matters.

The recurrence relation for  $a_n = 2a_{n-1} + a_{n-2}$  with initial condition  $a_0 = 1, a_1 = \underline{\quad 2 \quad}$

**Q.22.** The recursive definition of the function  $a_n = n^2 + n$  can be given as  $a_n = a_{n-1} + 2n$  with the initial condition  $a_1 = 2$

**Q.23** Consider the following C code of a recursive function named "fun". Write (in one sentence) the output printed by this function, when called as **fun(arr, 0, n-1)** where "arr" is an array of integers of size  $n$ .

**Sum of all subsets of the array**

**Q.24** Draw the hasse diagram for the POSET  $(\{1,2,4,5,10,12,20,25\}, \mid)$

**Q.25** The diagram at the right is the matrix representation of a relation  $R$ .

Which of the following properties are applicable to the relation  $R$ .

Reflexive, Symmetric, Antisymmetric, Transitive

**Reflexive only**

```
void fun(int arr[], int l, int n, int sum=0)
{
    if (l > n)
    {
        printf("%d ", sum);
        return;
    }
    fun(arr, l+1, n, sum+arr[l]);
    fun(arr, l+1, n, sum);
}
```

$$M_R = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 \end{pmatrix}$$