

CS/IS F214 Logic in Computer Science

MODULE: TEMPORAL LOGICS

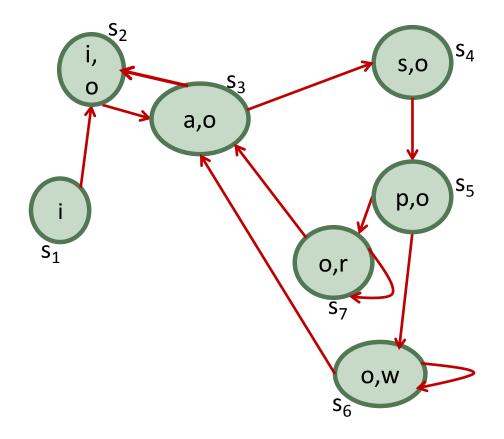
**LTL: Semantics and Examples** 

## **Semantics of LTL formulas**

- Let  $M = (S, \rightarrow, L)$  be a model and s is a state in S.
- Let  $\phi$  be an LTL formula.
- Then we say M,  $s = \phi$  if
  - for every execution path  $\pi$  of M starting at s:
  - $\pi \mid = \phi$



## **Examples**



What do the following formulas mean?

- 1) XGo
- 2)  $F(w \vee r)$
- 3) X (o U w)
- 4) XX (aUw)
- 5) **GFs**
- 6)  $GF(w \vee r)$
- 7)  $GF((w \lor r) \land (X a))$

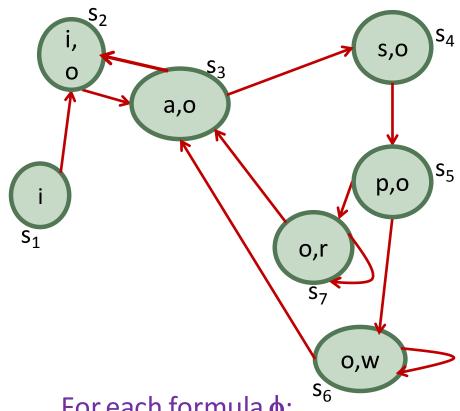
For each formula,  $\phi$  argue whether

$$M, s_1 \mid = \phi$$

holds or not.



## **Examples**



## Consider the following formulas:

- ΧGο
- $F(w \vee r)$
- 3) X (o U w)
- XX (aUw)
- GFs
- 6)  $GF(w \vee r)$
- 7)  $GF((w \lor r) \land (X a))$

For each formula **φ**:

- find whether there exists a state  $\mathbf{s}_i$  such that  $\mathbf{M}$ ,  $\mathbf{s}_i \mid = \phi$
- find whether in all states  $s_i$  M,  $s_i = \phi$

