



BITS Pilani
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PREDICATE LOGIC

Horn Clauses and Prolog Programming

Prolog Programming and Horn Clauses

- Prolog uses Horn Clauses as the basis for programming:
 - A Horn Clause is an implication with zero or more antecedents and one implicand:
 - All antecedents and the implicand are predicates.
 - i.e. a Horn Clause is of the form:
 - $p_1(T_{11}, \dots, T_{1K_1}) \wedge p_2(T_{21}, \dots, T_{2K_2}) \wedge \dots \wedge p_m(T_{m1}, \dots, T_{mK_m}) \rightarrow q(T_{q1}, \dots, T_{qK_q})$
 - where each p_i is a predicate name and each T_{ij} is a term: i.e.
 - a constant
 - a variable or
 - a function term
- A single predicate $p(T_1, \dots, T_K)$ is a degenerate implication:
 - $\text{TRUE} \rightarrow p(T_1, \dots, T_K)$

Prolog Programming and Horn Clauses

- In Prolog, a typical Horn Clause of the form
 - $p_1(T_{11}, \dots, T_{1K1}) \wedge p_2(T_{21}, \dots, T_{2K2}) \wedge \dots \wedge p_m(T_{m1}, \dots, T_{mKm}) \rightarrow q(T_{q1}, \dots, T_{qKq})$
- is represented as:
 - $q(T_{q1}, \dots, T_{qKq}) \text{ :- } p_1(T_{11}, \dots, T_{1K1}), p_2(T_{21}, \dots, T_{2K2}), \dots, p_m(T_{m1}, \dots, T_{mKm}).$
i.e.
 - the implicand is on the left most end,
 - the antecedents occur on the right of :- (read this as <--),
 - the commas separating the antecedents indicate conjunction, and
 - there is a period ending the clause.

Prolog Programming and Horn Clauses

- A Prolog program is a conjunction of Horn Clauses and the conjunction is implicit:
 - i.e. syntactically, a Prolog program is a list of Horn Clauses.
- A degenerate clause (with a single predicate) is referred to as a ***fact*** in Prolog: e.g.
 - `nat(0).`
- A typical Horn Clause is referred to as a ***rule*** in Prolog: e.g.
 - `nat(s(X)) :- nat(X).`
 - Note: A fact is a special form of a rule. End of Note.
- Argue that these two rules form a specification of natural numbers in Prolog.
- Exercise:
 - Specify the addition operation in Prolog.



Prolog Syntax

- Write a grammar for Prolog (i.e. Horn Clause formulas) syntax:
 - A Prolog program is a conjunction of Horn Clauses.
 - The conjunction is implicit: i.e.
 - a program is just a list of Horn Clauses.
 - Each Horn Clause is terminated by a period i.e. ‘.’
 - Horn-Clause syntax:
 - The *implicand* appears at the beginning of the clause,
 - followed by the implication symbol “:-”,
 - which is followed by a comma-separated list of *antecedents*
 - *e.g.* $p(X) :- q(X,Y), r(Y,Z).$

