

## Homework 2 – Introductory concepts

## 1. Please provide:

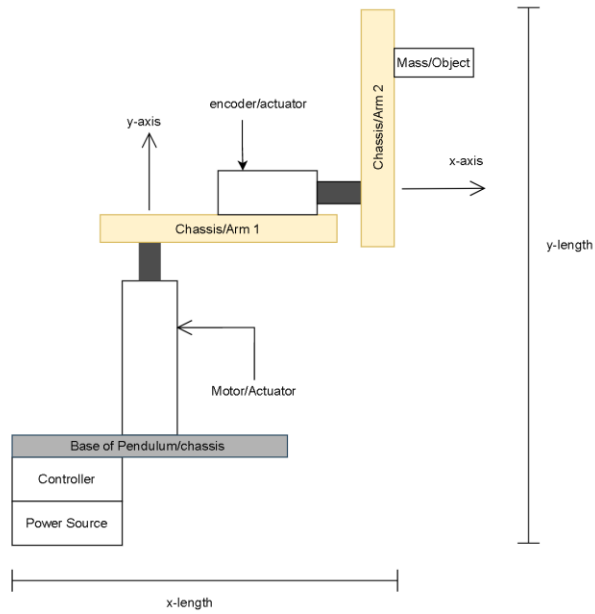
## a. Capabilities Database (project requirements)

Table 1. Capabilities Database (project requirements)

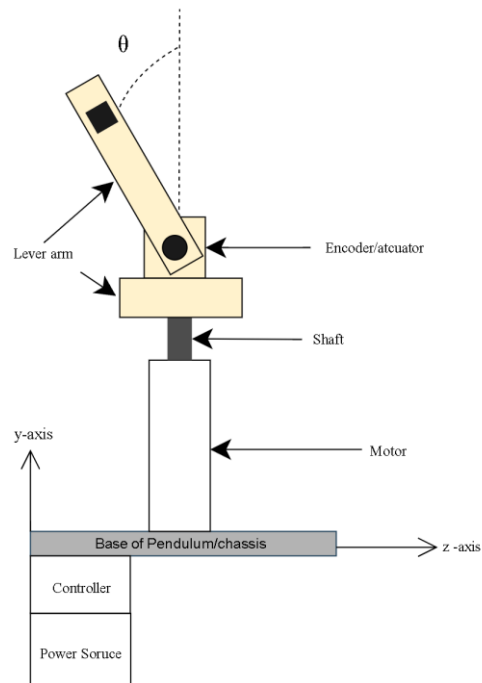
<b>1.</b>	<b>REQUIREMENTS</b>
<b>1.1</b>	<b>Introduction/Objective:</b> To design an inverted pendulum that balances vertically (up-right) by rotating on the horizontal plane.
<b>1.2</b>	<b>Stakeholder needs:</b> <ul style="list-style-type: none"> <li>• Pendulum should be able to react and respond to sudden forces or disturbances in a reasonable manner</li> <li>• Pendulum should return to its normal “state” after responding to a disturbance</li> <li>• Have the pendulum balance with some kind of actuator so the pendulum can stay upright.</li> <li>• Stay within given time frame and budget</li> <li>• Be of a proper size for application</li> </ul>
<b>1.3</b>	<b>System Requirements:</b> <ul style="list-style-type: none"> <li>• Motion control about x-axis</li> <li>• Motion control about y-axis</li> <li>• Closed loop system to respond to perturbation and disturbances</li> <li>• Keep pendulum vertical through closed loop feedback and control system design</li> </ul>
<b>1.4</b>	<b>Hardware Requirements:</b> <ul style="list-style-type: none"> <li>• Motors, actuators to respond to perturbation and disturbances</li> <li>• Rails/Chassis to build pendulum and support and house:</li> <li>• Motors, actuators</li> <li>• Encoder</li> <li>• Power source</li> <li>• Electrical wiring, sensors</li> <li>• Controller</li> </ul>
<b>1.5</b>	Implement and operational viewpoint of the project requirements
<b>1.6</b>	Implement a logical/functional viewpoint of project requirements

## b. Operational Viewpoint

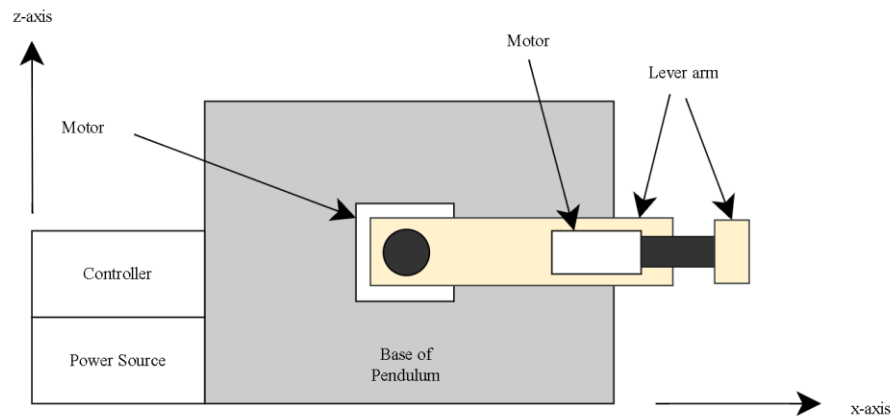
### Furuta Pendulum Operational Viewpoint/Schematic



**Figure 1. – Side View**



**Figure 2. Front View**

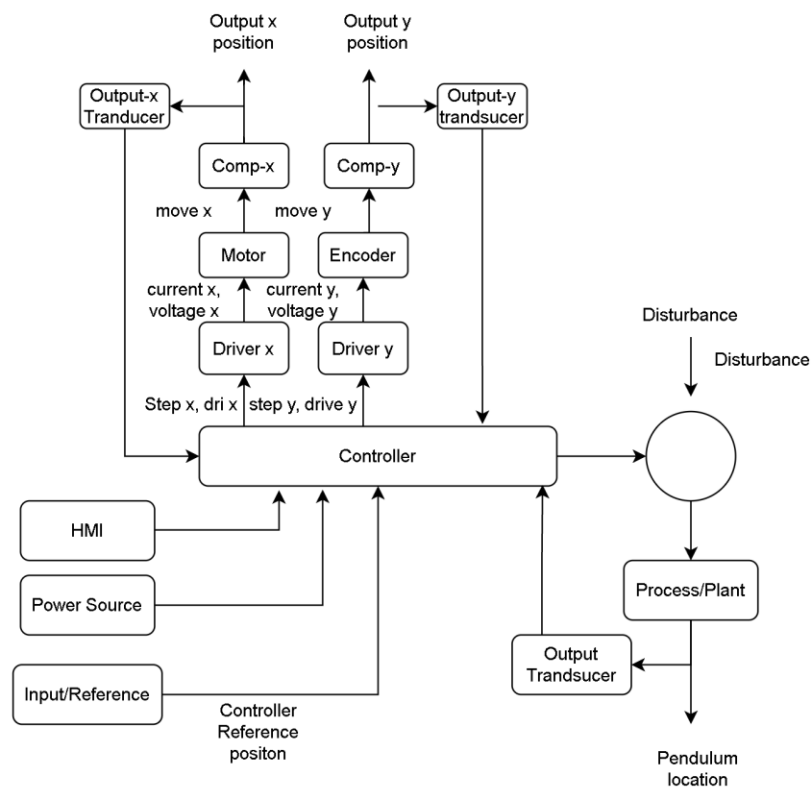


**Figure 3. Top View**

The inputs for the controller can be programmed through a computer or human machine interface (HMI) to program and test control system.

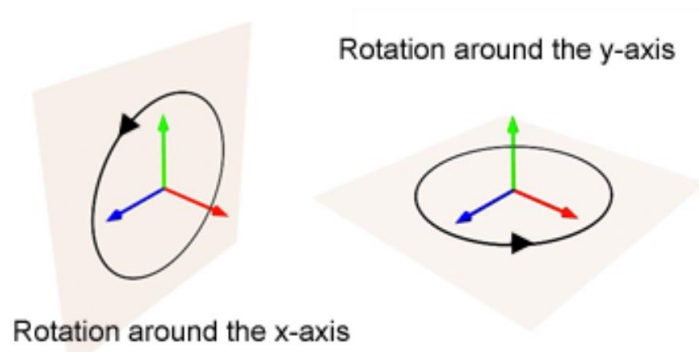
### c. Logical/functional viewpoint

#### Furuta Pendulum Logical/functional viewpoint

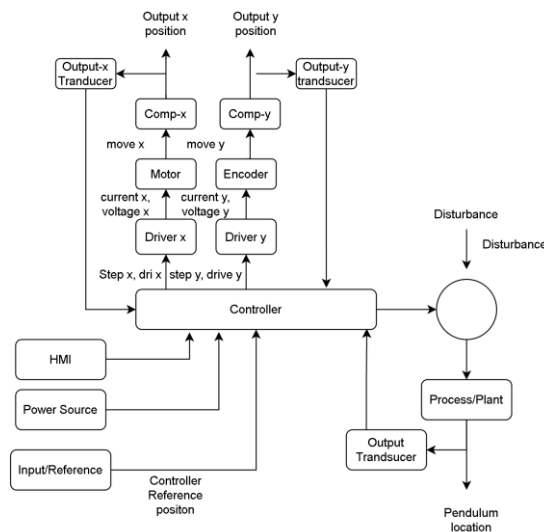


**Figure 4. Logical/functional Viewpoint**

The logical/functional viewpoint was based off of the motor/actuator moving about the y-axis and the encoder moving about the x-axis. Since the shafts are moving about the y-axis or x-axis, the motors can be controlled based on where about the x-axis or y-axis they are. An input/reference will be used so the motors where the reference about the x or y axis is. If there is a disturbance, the output will change and the motors can then adjust their positions to get back the input/reference position. The output of the x position and output of the y position are related to the output of the pendulum position as seen in the logical diagram.



**2. Part of the logical/function diagram that corresponds to the control system that I am designing.**



**Figure 4.** Logical/functional Viewpoint

Based off of figure 4, the logical/functional viewpoint for the Furuta pendulum, the part that corresponds to the area of focus is the control around the x and y axis of the encoder and motor. From the operational viewpoint of the diagram, it appears that the motors can be controlled based upon where about the x-axis or y-axis.

### 3. Task plan by dates/responsibilities of the team members which facilitates the deliverables by the deadline.

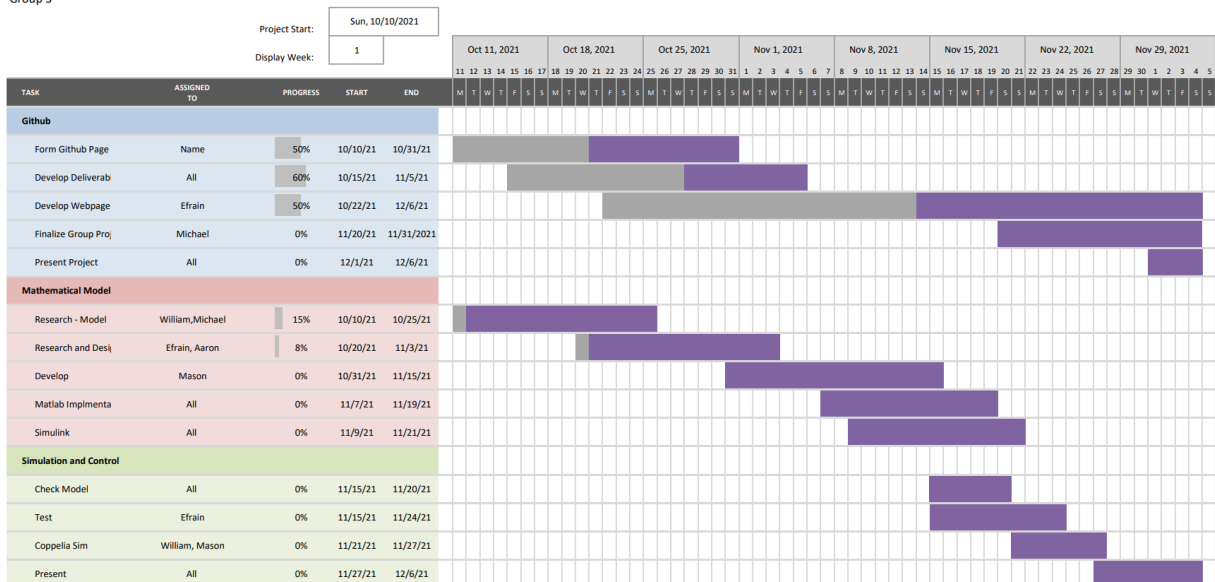
Deliverables:

- The team is expected to present their project (~ 5mins) and build a web page which contains all deliverables in GitHub.
- The mathematical model of the system must be delivered -preferably in Python or MATLAB. - The control system should be provided preferable in Simulink, State-flow, or with a high-level programming language (e.g., C, C++, or Python). However, the team must show that the control algorithm will give the design requirements for the target system. In other words, one cannot build the system solely hands-on approach similar to the videos below:
  - Pan and Tilt Mechanism
- The system will have a simulation with the control system and mathematical model by connecting Coppelia Sim to MATLAB, Simulink, or whatever the programming landscape is used.
- If the system contains hardware, the design of hardware should consist the necessary architectural explanations such as hardware and software relationships.

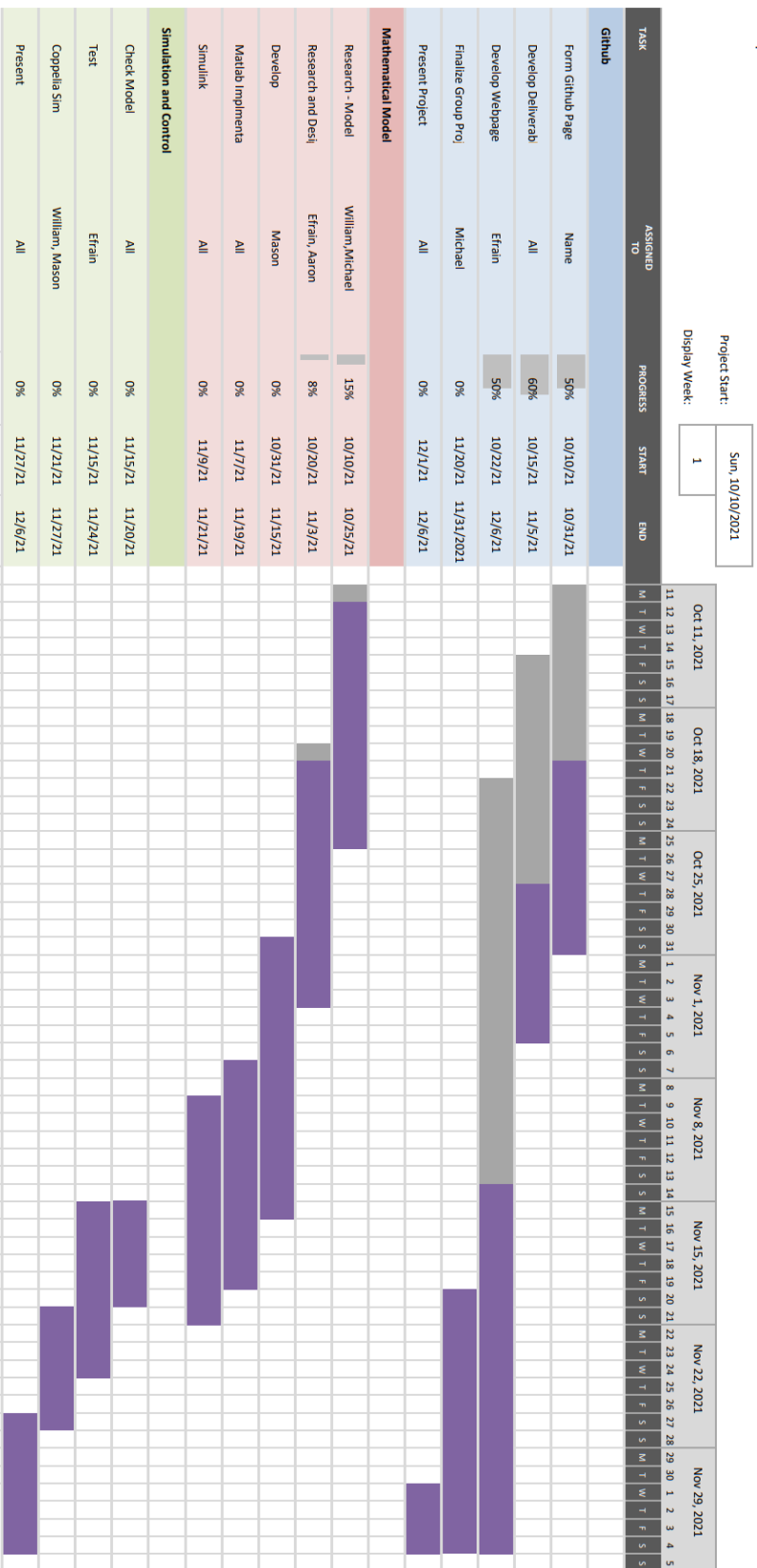
#### Furuta Pendulum

Group 3

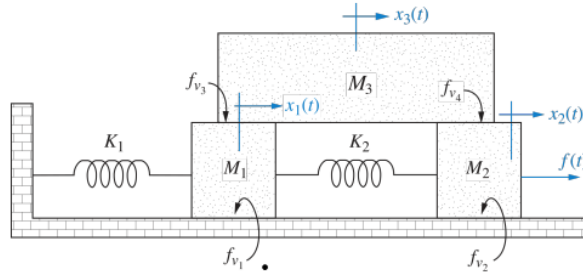
SIMPLE GANTT CHART by Vertex42.com  
<https://www.vertex42.com/ExcelTemplates/simple-gantt-chart.html>



### Group 3



4. Please find the transfer functions for the following system based on its provided equations in s-domain:



$$[M_1 s^2 + (f_{v1} + f_{v3})s + (K_1 + K_2)]X_1(s) - K_2 X_2(s) - f_{v3} s X_3(s) = 0$$

$$-K_2 X_1(s) + [M_2 s^2 + (f_{v2} + f_{v4})s + K_2]X_2(s) - f_{v4} s X_3(s) = F(s)$$

$$-f_{v3} s X_1(s) - f_{v4} s X_2(s) + [M_3 s^2 + (f_{v3} + f_{v4})s]X_3(s) = 0$$

**a. How many different transfer functions would you consider?**

Based off of the given equation and the number of degrees of freedom, it is possible to consider 3 transfer functions based off the given information. The equation for a transfer function is as follows:

$$G(s) = \frac{\text{Output}}{\text{Input}}$$

With our external force, or input being  $F(t)$  the three possible outputs can be as followed:

$x_1(t)$ ,  $x_2(t)$ ,  $x_3(t)$ . With 3 different outputs it is possible to have 3 different transfer functions based on the outputs.

Going from time domain to frequency domain:

$$x(t) \rightarrow x(s)$$

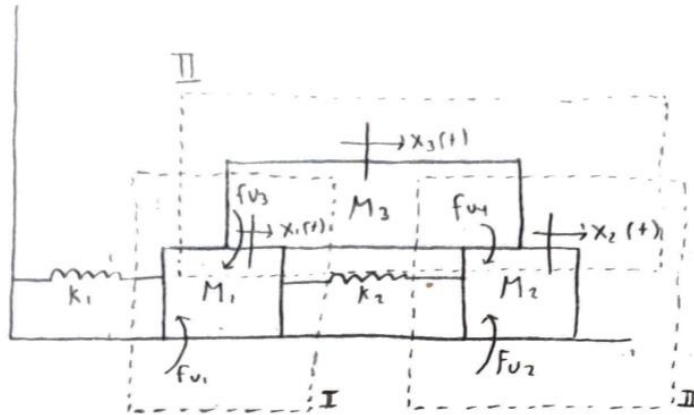
$$G_1(s) = \frac{x_1(s)}{F(s)}$$

$$G_2(s) = \frac{x_2(s)}{F(s)}$$

$$G_3(s) = \frac{x_3(s)}{F(s)}$$

b. By using Cramer's rule (by hand) without any computation tool.

Homework 2



$$M_1 // x_1 \quad [M_1 s^2 + (f_{v1} + f_{v3})s + (k_1 + k_2)] x_1(s) - k_2 x_2(s) - f_{v3} x_3(s) = 0$$

$$M_2 // x_2 \quad -k_2 x_1(s) + [M_2 s^2 + (f_{v2} + f_{v4})s + k_2] x_2(s) - f_{v4} x_3(s) = F(s)$$

$$M_3 // x_3 \quad -f_{v3} x_1(s) - f_{v4} x_2(s) + [M_3 s + f_{v3} + f_{v4}] x_3(s) = 0$$

a) Transfer functions

$$G_1(s) = \frac{x_1(s)}{F(s)} ; \quad G_2(s) = \frac{x_2(s)}{F(s)} ; \quad G_3(s) = \frac{x_3(s)}{F(s)}$$

→ Solve using Cramer's Rule

$$\begin{bmatrix} M_1 s^2 + (f_{v1} + f_{v3})s + (k_1 + k_2) & -k_2 & -f_{v3}(s) \\ -k_2 & M_2 s^2 + (f_{v2} + f_{v4})s + k_2 & -f_{v4}(s) \\ -f_{v3}(s) & -f_{v4}(s) & [M_3 s + (f_{v3} + f_{v4})]s \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ F(s) \\ 0 \end{bmatrix}$$



# Homework 2

$$G_1 = \frac{X_1(s)}{F(s)} = \frac{\begin{bmatrix} 0 & -k_2 & -fV_3(s) \\ F_1 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & -fV_4(s) \\ 0 & -fV_4(s) & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow X_1(s)}{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & -fV_3(s) \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & -fV_4(s) \\ -fV_3(s) & -fV_4(s) & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow F(s)}$$

$$G_2 = \frac{X_2(s)}{F(s)} = \frac{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & 0 & -fV_3(s) \\ -k_2 & F(s) & -fV_4(s) \\ -fV_3(s) & 0 & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow X_2(s)}{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & -fV_3(s) \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & -fV_4(s) \\ -fV_3(s) & -fV_4(s) & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow F(s)}$$

$$G_3 = \frac{X_3(s)}{F(s)} = \frac{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & 0 \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & F(s) \\ -fV_3(s) & -fV_4(s) & 0 \end{bmatrix} \leftarrow X_3(s)}{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & -fV_3(s) \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & -fV_4(s) \\ -fV_3(s) & -fV_4(s) & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow F(s)}$$

$$G_3 = \frac{X_3(s)}{F(s)} = \frac{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & 0 \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & F(s) \\ -fV_3(s) & -fV_4(s) & 0 \end{bmatrix} \leftarrow X_3(s)}{\begin{bmatrix} M_1 s^2 + (fV_1 + fV_3)s + (k_1 + k_2) & -k_2 & -fV_3(s) \\ -k_2 & M_2 s^2 + (fV_2 + fV_4)s + k_2 & -fV_4(s) \\ -fV_3(s) & -fV_4(s) & [M_3 + (fV_3 + fV_4)]s \end{bmatrix} \leftarrow F(s)}$$

### c. By using MATLAB matrix inverse

First, open a command window and type in the given transfer functions found using crammers rule

```
syms M1 M2 M3 fv1 fv2 fv3 fv4 K1 K2 s
%equations
F(s) = [M1*s^2+(fv1+fv3)*s+(K1+K2) -K2 -fv3*s;-K2 M2*s^2+(fv2+fv4)*s+K2 -fv4;-fv3*s -fv4*s M3+(fv3+fv4)*s];
X1(s)= [0 -K2 -fv3;1 M2*s^2+(fv2+fv4)*s+K2 -fv4;0 -fv4*s M3+(fv3+fv4)*s];
X2(s)= [M1*s^2+(fv1+fv3)*s+(K1+K2) 0 -fv3*s;-K2 1 -fv4;-fv3*s 0 M3+(fv3+fv4)*s];
X3(s) = [M1*s^2+(fv1+fv3)*s+(K1+K2) -K2 0;-K2 M2*s^2+(fv2+fv4)*s+K2 1;-fv3*s -fv4*s 0];

%%solving the functions using the matrix inverse

G1(s) = X1(s)/F(s)

G2(s) = X2(s)/F(s)

G3(s) = X3(s)/F(s)
```

The following transfer functions are as followed:  $G_1, G_2, G_3$

$G_1(s) =$

$$\frac{-(K_2^2 M_3 + M_2 f_{v3}^2 s^3 + f_{v2} f_{v3}^2 s^2 + f_{v3}^2 f_{v4} s^2 + K_2 f_{v3}^2 s + K_2^2 f_{v3} s + K_2^2 f_{v4} s + 2 K_2 f_{v3} f_{v4} s) / (K_1 K_2 M_3 + K_1 f_{v4}^2 s^2 + K_2 f_{v4}^2 s^2 - M_1 f_{v4}^2 s^3 + M_1 f_{v4}^2 s^4 - f_{v1} f_{v4}^2 s^2 + f_{v1} f_{v4}^2 s^3 - f_{v3} f_{v4}^2 s^2 + f_{v3} f_{v4}^2 s^3 - K_1 f_{v4}^2 s - K_2 f_{v4}^2 s + K_1 M_2 M_3 s^2 + K_2 M_1 M_3 s^2 + K_2 M_2 M_3 s^2 + M_1 M_2 M_3 s^4 + K_1 M_2 f_{v3} s^3 + K_2 M_1 f_{v3} s^3 + K_1 M_2 f_{v4} s^3 + K_2 M_1 f_{v4} s^3 + K_2 M_2 f_{v3} s^3 + K_2 M_2 f_{v4} s^3 + M_1 M_3 f_{v2} s^3 + M_2 M_3 f_{v1} s^3 + M_1 M_2 f_{v3} s^5 + M_1 M_3 f_{v4} s^3 + M_2 M_3 f_{v3} s^3 + M_1 M_2 f_{v4} s^5 + K_1 f_{v2} f_{v3} s^2 + K_2 f_{v1} f_{v3} s^2 + K_1 f_{v2} f_{v4} s^2 + K_2 f_{v1} f_{v4} s^2 + K_2 f_{v2} f_{v3} s^2 + K_1 f_{v3} f_{v4} s^2 + K_2 f_{v2} f_{v4} s^2 + K_2 f_{v3} f_{v4} s^2 + M_3 f_{v1} f_{v2} s^2 + M_1 f_{v2} f_{v3} s^4 + M_2 f_{v1} f_{v3} s^4 + M_3 f_{v1} f_{v4} s^2 + M_3 f_{v2} f_{v3} s^2 + M_1 f_{v2} f_{v4} s^4 + M_2 f_{v1} f_{v4} s^4 + M_1 f_{v3} f_{v4} s^4 + M_3 f_{v3} f_{v4} s^2 + M_2 f_{v3} f_{v4} s^4 + f_{v1} f_{v2} f_{v3} s^3 + f_{v1} f_{v2} f_{v4} s^3 + f_{v1} f_{v3} f_{v4} s^3 + f_{v2} f_{v3} f_{v4} s^3 + K_1 K_2 f_{v3} s + K_1 K_2 f_{v4} s + K_1 M_3 f_{v2} s + K_2 M_3 f_{v1} s + K_2 M_3 f_{v2} s + K_1 M_3 f_{v4} s + K_2 M_3 f_{v3} s + K_2 M_3 f_{v4} s - K_2 f_{v3} f_{v4} s),$$

$$\frac{-(K_2^2 M_3 + K_1 K_2 M_3 + f_{v3}^2 f_{v4} s^2 + K_2 f_{v3}^2 s + K_2^2 f_{v3} s + K_2^2 f_{v4} s + K_2 M_1 M_3 s^2 + K_2 M_1 f_{v3} s^3 + K_2 M_1 f_{v4} s^3 + K_2 f_{v1} f_{v3} s^2 + K_2 f_{v1} f_{v4} s^2 + K_2 f_{v3} f_{v4} s^2 + M_1 f_{v3} f_{v4} s^3 + f_{v1} f_{v3} f_{v4} s^2 + K_1 K_2 f_{v3} s + K_1 K_2 f_{v4} s + K_2 M_3 f_{v1} s + K_2 M_3 f_{v3} s + K_1 f_{v3} f_{v4} s + K_2 f_{v3} f_{v4} s) / (K_1 K_2 M_3 + K_1 f_{v4}^2 s^2 + K_2 f_{v4}^2 s^2 - M_1 f_{v4}^2 s^3 + M_1 f_{v4}^2 s^4 - f_{v1} f_{v4}^2 s^2 + f_{v1} f_{v4}^2 s^3 - f_{v3} f_{v4}^2 s^2 + f_{v3} f_{v4}^2 s^3 - K_1 f_{v4}^2 s - K_2 f_{v4}^2 s + K_1 M_2 M_3 s^2 + K_2 M_1 M_3 s^2 + K_2 M_2 M_3 s^2 + M_1 M_2 M_3 s^4 + K_1 M_2 f_{v3} s^3 + K_2 M_1 f_{v3} s^3 + K_1 M_2 f_{v4} s^3 + K_2 M_1 f_{v4} s^3 + K_2 M_2 f_{v3} s^3 + K_2 M_2 f_{v4} s^3 + M_1 M_3 f_{v2} s^3 + M_2 M_3 f_{v1} s^3 +$$

$$\begin{aligned}
& M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + \\
& fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + \\
& K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + \\
& K2*M3*fv4*s - K2*fv3*fv4*s), \\
& - (K2^2*fv4 + M2*fv3^2*s^3 + K1*K2*fv3 + K1*K2*fv4 + fv2*fv3^2*s^2 + \\
& fv3^2*fv4*s^2 + K2*fv3^2*s + K2^2*fv3*s + K1*M2*fv3*s^2 + \\
& K2*M1*fv3*s^2 + K2*M1*fv4*s^2 + K2*M2*fv3*s^2 + M1*M2*fv3*s^4 + \\
& M1*fv2*fv3*s^3 + M2*fv1*fv3*s^3 + M1*fv3*fv4*s^3 + fv1*fv2*fv3*s^2 + \\
& fv1*fv3*fv4*s^2 + K1*fv2*fv3*s + K2*fv1*fv3*s + K2*fv1*fv4*s + \\
& K2*fv2*fv3*s + K1*fv3*fv4*s + 2*K2*fv3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 \\
& + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + \\
& fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - K1*fv4^2*s - \\
& K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 \\
& + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + \\
& K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + \\
& M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + \\
& fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + \\
& K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + \\
& K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& [ (K2^2*M3 - fv4^2*s + K2*M3 + fv4^2*s^2 + K2*fv4^2*s^2 + K2*fv3*s + \\
& K2*fv4*s + M3*fv2*s + M3*fv4*s + M2*M3*s^2 + K2^2*fv3*s - K2*fv4^2*s + \\
& K2^2*fv4*s + M2*fv3*s^3 + M2*fv4*s^3 + fv2*fv3*s^2 + fv2*fv4*s^2 + \\
& fv3*fv4*s^2 + K2*M2*M3*s^2 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& K2*fv2*fv3*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + K2*M3*fv2*s + \\
& K2*M3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s
\end{aligned}$$

$$\begin{aligned}
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), (K2^2*M3 + \\
& K2*M3 + K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 + K2*fv3*s + K2*fv4*s - K1*fv4^2*s + K2^2*fv3*s - \\
& K2*fv4^2*s + K2^2*fv4*s + fv3*fv4*s^2 + K1*M2*M3*s^2 + K2*M1*M3*s^2 + \\
& K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + 2*K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) / (K1*K2*M3 + \\
& K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\
& fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\
& K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\
& M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (K2*fv4 + K2^2*fv4 + K2*fv3*s + K2^2*fv3*s + M2*fv3*s^3 + fv2*fv3*s^2 \\
& + fv3*fv4*s^2 + K2*M2*fv3*s^3 + K2*fv2*fv3*s^2 + \\
& K2*fv3*fv4*s^2) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 \\
& + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& [ \\
& (K2*fv3^2*s^2 + M2*fv3^2*s^4 + fv2*fv3^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 + fv3^2*fv4*s^3 + M2*M3*fv3*s^3 + K2*fv3*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv2*fv3*fv4*s^3 + \\
& K2*M3*fv3*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (s*(fv4*fv3^2*s^2 + K2*fv3^2*s + K2*fv4*fv3*s + K2*M3*fv3)) / (K1*K2*M3 \\
& + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\
& fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\
& K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\
& M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), (K1*K2*M3 + K1*fv4^2*s^2 + \\
& K2*fv3^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 + \\
& M2*fv3^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 + fv2*fv3^2*s^3 - \\
& fv3*fv4^2*s^2 + fv3*fv4^2*s^3 + fv3^2*fv4*s^3 - K1*fv4^2*s - \\
& K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 \\
& + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + \\
& K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + \\
& M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + \\
& fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + \\
& K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + \\
& K2*M3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 +
\end{aligned}$$

$$\begin{aligned}
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$G2(s) =$$

$$\begin{aligned}
& [ (K2^2*M3 + K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s + K2^2*fv3*s - K2*fv4^2*s + K2^2*fv4*s + \\
& K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 + \\
& K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + \\
& K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + \\
& M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + \\
& fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + \\
& K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + \\
& K2*M3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (K2^2*M3 + K1*K2*M3 + K2^2*fv3*s + K2^2*fv4*s + K2*M1*M3*s^2 + \\
& K2*M1*fv3*s^3 + K2*M1*fv4*s^3 + K2*fv1*fv3*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + K1*K2*fv3*s + K1*K2*fv4*s + K2*M3*fv1*s +
\end{aligned}$$

$$\begin{aligned}
& K2*M3*fv3*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (K2^2*fv4 + K1*K2*fv4 + K2^2*fv3*s + K2*M1*fv4*s^2 + K2*fv1*fv4*s + \\
& K2*fv3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& [ \\
& - (K2^2*M3 - K2*M3 + K2*fv4^2*s^2 + fv3*fv4^2*s^2 - K2*fv3*s - K2*fv4*s \\
& - fv3*fv4*s + K2^2*fv3*s + K2^2*fv4*s + K2*M2*M3*s^2 + K2*M2*fv3*s^3 + \\
& K2*M2*fv4*s^3 + K2*fv2*fv3*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M2*fv3*fv4*s^3 + fv2*fv3*fv4*s^2 + K2*M3*fv2*s + K2*M3*fv4*s + \\
& K2*fv3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s
\end{aligned}$$

$$\begin{aligned}
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), (K1*M3 - \\
& K2^2*M3 + K2*M3 - M1*fv4^2*s^3 - fv1*fv4^2*s^2 - fv3*fv4^2*s^2 + \\
& K1*fv3*s + K1*fv4*s + K2*fv3*s + K2*fv4*s + M3*fv1*s + M3*fv3*s + \\
& M1*M3*s^2 - K1*fv4^2*s - K2^2*fv3*s - K2*fv4^2*s - K2^2*fv4*s + \\
& M1*fv3*s^3 + M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + fv3*fv4*s^2 - \\
& K2*fv3*fv4*s^2 - K2*fv3*fv4*s)/(K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 \\
& - M1*fv4^2*s^3 + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - \\
& fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 \\
& + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + \\
& K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + \\
& K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + \\
& M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + \\
& K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + \\
& K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + \\
& M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + \\
& M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + \\
& M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + \\
& fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + \\
& K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - \\
& K2*fv3*fv4*s), \\
& - (K2^2*fv4 - K2*fv4 - K1*fv4 + M1*fv4^2*s^3 + K1*K2*fv4 + \\
& fv1*fv4^2*s^2 + fv3*fv4^2*s^2 - K2*fv3*s - fv1*fv4*s - fv3*fv4*s + \\
& K1*fv4^2*s + K2^2*fv3*s + K2*fv4^2*s - M1*fv4*s^2 + K1*M2*fv4*s^2 + \\
& K2*M1*fv4*s^2 + K2*M2*fv3*s^3 + K2*M2*fv4*s^2 + M1*M2*fv4*s^4 + \\
& K2*fv2*fv3*s^2 + K2*fv3*fv4*s^2 + M1*fv2*fv4*s^3 + M2*fv1*fv4*s^3 + \\
& M2*fv3*fv4*s^3 + fv1*fv2*fv4*s^2 + fv2*fv3*fv4*s^2 + K1*fv2*fv4*s + \\
& K2*fv1*fv4*s + K2*fv2*fv4*s + K2*fv3*fv4*s)/(K1*K2*M3 + K1*fv4^2*s^2 + \\
& K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + \\
& fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - K1*fv4^2*s - \\
& K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 \\
& + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + \\
& K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + \\
& M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + \\
& M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + \\
& fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + \\
& K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + \\
& K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& [ \\
& (K2*fv4^2*s^2 + fv3*fv4^2*s^2 + K2*fv3*fv4*s^2 + \\
& K2*M3*fv4*s)/(K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 +
\end{aligned}$$



$$\begin{aligned}
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (s*(M1*fv4^2*s^3 + K1*M3*fv4 + K2*M3*fv4 + fv1*fv4^2*s^2 + \\
& fv3*fv4^2*s^2 + K1*fv4^2*s + K2*fv4^2*s + M1*M3*fv4*s^2 + \\
& M1*fv3*fv4*s^3 + fv1*fv3*fv4*s^2 + K1*fv3*fv4*s + K2*fv3*fv4*s + \\
& M3*fv1*fv4*s + M3*fv3*fv4*s)) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 \\
& - M1*fv4^2*s^3 + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - \\
& fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 \\
& + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + \\
& K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + \\
& K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + \\
& M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + \\
& K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + \\
& K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + \\
& M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + \\
& M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + \\
& M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + \\
& fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + \\
& K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - \\
& K2*fv3*fv4*s), (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 + M1*fv4^2*s^4 \\
& + fv1*fv4^2*s^3 + fv3*fv4^2*s^3 + K1*M2*M3*s^2 + K2*M1*M3*s^2 + \\
& K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + 2*K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) / (K1*K2*M3 + \\
& K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\
& fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\
& K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\
& M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 +
\end{aligned}$$

$$K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]$$

$$G3(s) =$$

$$\begin{aligned} & [ (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv3^2*s^2 + K2*fv4^2*s^2 - \\ & M1*fv4^2*s^3 + M1*fv4^2*s^4 + M2*fv3^2*s^4 - fv1*fv4^2*s^2 + \\ & fv1*fv4^2*s^3 + fv2*fv3^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 + \\ & fv3^2*fv4*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\ & + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\ & K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\ & M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\ & M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\ & K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\ & K2*fv2*fv4*s^2 + 2*K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\ & M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\ & M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\ & fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\ & + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\ & + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) / (K1*K2*M3 + \\ & K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\ & fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\ & K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\ & M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\ & K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\ & M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\ & M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\ & K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\ & K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\ & M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\ & M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\ & fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\ & K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\ & K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\ & (fv3*s^2*(K1*fv4 + K2*fv3 + K2*fv4 + fv1*fv4*s + fv3*fv4*s + \\ & M1*fv4*s^2)) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\ & M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\ & fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\ & + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\ & K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\ & M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\ & M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\ & K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \end{aligned}$$

$$\begin{aligned}
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), \\
& (K2*fv3^2*s^2 + M2*fv3^2*s^4 + fv2*fv3^2*s^3 + fv3^2*fv4*s^3 + \\
& K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K2*M2*fv3*s^3 + M1*M2*fv3*s^5 + \\
& K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M1*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv3*fv4*s^3 + K1*K2*fv3*s)/(K1*K2*M3 + \\
& K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\
& fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\
& K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\
& M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& [ \\
& (fv3*fv4^2*s^2 + K2*fv3*s + K2*fv4*s + K2*fv4^2*s + M2*fv3*s^3 + \\
& fv2*fv3*s^2 + fv3*fv4*s^2 + M2*fv3*fv4*s^3 + fv2*fv3*fv4*s^2 + \\
& K2*fv3*fv4*s)/(K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + \\
& M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 \\
& + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + \\
& K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + \\
& M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + \\
& M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + \\
& K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + \\
& K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + \\
& M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 \\
& + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s \\
& + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s), (K1*K2*M3 + \\
& K1*fv4^2*s^2 + K2*fv4^2*s^2 + M1*fv4^2*s^4 + fv1*fv4^2*s^3 + \\
& fv3*fv4^2*s^3 + K1*fv4*s + K2*fv3*s + K2*fv4*s + M1*fv4*s^3 + \\
& fv1*fv4*s^2 + fv3*fv4*s^2 + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 \\
& + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

$$\begin{aligned}
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s) / (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv4^2*s^2 - \\
& M1*fv4^2*s^3 + M1*fv4^2*s^4 - fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - \\
& fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 \\
& + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + \\
& K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + \\
& K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + \\
& M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + \\
& K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + \\
& K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + \\
& M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + \\
& M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + \\
& M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + \\
& fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + \\
& K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s - \\
& K2*fv3*fv4*s), (K1*K2 + M1*fv4^2*s^3 + K1*K2*fv4 + fv1*fv4^2*s^2 + \\
& fv3*fv4^2*s^2 + K1*fv2*s + K2*fv1*s + K2*fv2*s + K1*fv4*s + K2*fv3*s + \\
& K2*fv4*s + K1*M2*s^2 + K2*M1*s^2 + K2*M2*s^2 + M1*M2*s^4 + K1*fv4^2*s \\
& + K2*fv4^2*s + M1*fv2*s^3 + M2*fv1*s^3 + M1*fv4*s^3 + M2*fv3*s^3 + \\
& fv1*fv2*s^2 + fv1*fv4*s^2 + fv2*fv3*s^2 + fv3*fv4*s^2 + K1*M2*fv4*s^2 \\
& + K2*M1*fv4*s^2 + K2*M2*fv4*s^2 + M1*M2*fv4*s^4 + M1*fv2*fv4*s^3 + \\
& M2*fv1*fv4*s^3 + M2*fv3*fv4*s^3 + fv1*fv2*fv4*s^2 + fv2*fv3*fv4*s^2 + \\
& K1*fv2*fv4*s + K2*fv1*fv4*s + K2*fv2*fv4*s + K2*fv3*fv4*s) / (K1*K2*M3 + \\
& K1*fv4^2*s^2 + K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 - \\
& fv1*fv4^2*s^2 + fv1*fv4^2*s^3 - fv3*fv4^2*s^2 + fv3*fv4^2*s^3 - \\
& K1*fv4^2*s - K2*fv4^2*s + K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + \\
& M1*M2*M3*s^4 + K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + \\
& K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + \\
& M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + \\
& M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + \\
& K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + \\
& M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + \\
& M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + K1*K2*fv3*s + \\
& K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + \\
& K2*M3*fv3*s + K2*M3*fv4*s - K2*fv3*fv4*s) ]
\end{aligned}$$

[

To find the inverse, simply take the inverse of the transfer function.

```
%taking the matrix inverse

Ginv1 == inv(G1(s))

Ginv2 == inv(G2(s))

Ginv3 == inv(G3(s))

Ginv1 =

[ (K2^2*M3 + K2*M3 + K1*K2*M3 + K1*fv4^2*s^2 + K2*fv3^2*s^2 +
K2*fv4^2*s^2 - M1*fv4^2*s^3 + M1*fv4^2*s^4 + M2*fv3^2*s^4 -
fv1*fv4^2*s^2 + fv1*fv4^2*s^3 + fv2*fv3^2*s^3 - fv3*fv4^2*s^2 +
fv3*fv4^2*s^3 + fv3^2*fv4*s^3 + K2*fv3*s + K2*fv4*s - K1*fv4^2*s
+ K2^2*fv3*s - K2*fv4^2*s + K2^2*fv4*s + fv3*fv4*s^2 +
K1*M2*M3*s^2 + K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 +
K1*M2*fv3*s^3 + K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 +
K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 +
M1*M2*fv3*s^5 + M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 +
K1*fv2*fv3*s^2 + K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 +
K2*fv1*fv4*s^2 + K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 +
K2*fv2*fv4*s^2 + 2*K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 +
M1*fv2*fv3*s^4 + M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 +
M3*fv2*fv3*s^2 + M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 +
M1*fv3*fv4*s^4 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 +
fv1*fv2*fv3*s^3 + fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 +
fv2*fv3*fv4*s^3 + K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s +
K2*M3*fv1*s + K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s +
K2*M3*fv4*s)/(K2*M3 + K2*fv3*s + K2*fv4*s + fv3*fv4*s), K1 + K2
+ fv1*s + fv3*s + M1*s^2, (K2*fv3 + K2^2*fv3 + K2^2*fv4 +
M2*fv3^2*s^3 + K1*K2*fv3 + K1*K2*fv4 + fv2*fv3^2*s^2 +
fv3^2*fv4*s^2 - K2*fv3*s + K2*fv3^2*s + K1*M2*fv3*s^2 +
K2*M1*fv3*s^2 + K2*M1*fv4*s^2 + K2*M2*fv3*s^2 + M1*M2*fv3*s^4 +
M1*fv2*fv3*s^3 + M2*fv1*fv3*s^3 + M1*fv3*fv4*s^3 +
fv1*fv2*fv3*s^2 + fv1*fv3*fv4*s^2 + K1*fv2*fv3*s + K2*fv1*fv3*s
+ K2*fv1*fv4*s + K2*fv2*fv3*s + K1*fv3*fv4*s +
2*K2*fv3*fv4*s)/(K2*M3 + K2*fv3*s + K2*fv4*s + fv3*fv4*s)]

[
-(K2^2*M3 - fv4^2*s + K2*M3 + fv4^2*s^2 + K2*fv4^2*s^2 +
K2*fv3*s + K2*fv4*s + M3*fv2*s + M3*fv4*s + M2*M3*s^2 +
K2^2*fv3*s - K2*fv4^2*s + K2^2*fv4*s + M2*fv3*s^3 + M2*fv4*s^3 +
fv2*fv3*s^2 + fv2*fv4*s^2 + fv3*fv4*s^2 + K2*M2*M3*s^2 +
K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + K2*fv2*fv3*s^2 + K2*fv2*fv4*s^2
+ K2*fv3*fv4*s^2 + K2*M3*fv2*s + K2*M3*fv4*s)/(K2*M3 + K2*fv3*s
+ K2*fv4*s + fv3*fv4*s), -K2,
-(K2*fv3 + K2*fv4 + K2^2*fv3 + K2^2*fv4 + fv2*fv3*s + fv3*fv4*s
```

$$\begin{aligned}
& + M2*fv3*s^2 + K2*M2*fv3*s^2 + K2*fv2*fv3*s + \\
& K2*fv3*fv4*s)/(K2*M3 + K2*fv3*s + K2*fv4*s + fv3*fv4*s)] \\
& [ \\
& -(K2*fv3^2*s^2 + M2*fv3^2*s^4 + fv2*fv3^2*s^3 - fv3*fv4^2*s^2 + \\
& fv3*fv4^2*s^3 + fv3^2*fv4*s^3 + M2*M3*fv3*s^3 + K2*fv3*fv4*s^2 + \\
& M3*fv2*fv3*s^2 + M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + \\
& fv2*fv3*fv4*s^3 + K2*M3*fv3*s)/(K2*M3 + K2*fv3*s + K2*fv4*s + \\
& fv3*fv4*s), \\
& -fv3*s, \\
& -(M2*fv3^2*s^3 - K2*M3 + fv2*fv3^2*s^2 + fv3^2*fv4*s^2 - \\
& K2*fv3*s - K2*fv4*s - fv3*fv4*s + K2*fv3^2*s + \\
& K2*fv3*fv4*s)/(K2*M3 + K2*fv3*s + K2*fv4*s + fv3*fv4*s)]
\end{aligned}$$

$$Ginv2 =$$

$$\begin{aligned}
& [ \\
& (K1*M3 - K2^2*M3 + K2*M3 + K1*fv3*s + K1*fv4*s + K2*fv3*s + \\
& K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 - K2^2*fv3*s - \\
& K2^2*fv4*s + M1*fv3*s^3 + M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 \\
& + fv3*fv4*s^2 - K2*fv3*fv4*s)/(K1*M3 + K2*M3 + K1*fv3*s + \\
& K1*fv4*s + K2*fv3*s + K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 \\
& + M1*fv3*s^3 + M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + \\
& fv3*fv4*s^2), \\
& -K2, \\
& -(K2^2*fv4 + K1*K2*fv4 + K2^2*fv3*s + K2*M1*fv4*s^2 + \\
& K2*fv1*fv4*s + K2*fv3*fv4*s)/(K1*M3 + K2*M3 + K1*fv3*s + \\
& K1*fv4*s + K2*fv3*s + K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 \\
& + M1*fv3*s^3 + M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + \\
& fv3*fv4*s^2)] \\
& [ (K2^2*M3 - K2*M3 + K2*fv4^2*s^2 + fv3*fv4^2*s^2 - K2*fv3*s - \\
& K2*fv4*s - fv3*fv4*s + K2^2*fv3*s + K2^2*fv4*s + K2*M2*M3*s^2 + \\
& K2*M2*fv3*s^3 + K2*M2*fv4*s^3 + K2*fv2*fv3*s^2 + K2*fv2*fv4*s^2 \\
& + K2*fv3*fv4*s^2 + M2*fv3*fv4*s^3 + fv2*fv3*fv4*s^2 + \\
& K2*M3*fv2*s + K2*M3*fv4*s + K2*fv3*fv4*s)/(K1*M3 + K2*M3 + \\
& K1*fv3*s + K1*fv4*s + K2*fv3*s + K2*fv4*s + M3*fv1*s + M3*fv3*s \\
& + M1*M3*s^2 + M1*fv3*s^3 + M1*fv4*s^3 + fv1*fv3*s^2 + \\
& fv1*fv4*s^2 + fv3*fv4*s^2), K2 + fv2*s + fv4*s + M2*s^2, \\
& (K2^2*fv4 - K2*fv4 - K1*fv4 + M1*fv4^2*s^3 + K1*K2*fv4 + \\
& fv1*fv4^2*s^2 + fv3*fv4^2*s^2 - K2*fv3*s - fv1*fv4*s - fv3*fv4*s \\
& + K1*fv4^2*s + K2^2*fv3*s + K2*fv4^2*s - M1*fv4*s^2 + \\
& K1*M2*fv4*s^2 + K2*M1*fv4*s^2 + K2*M2*fv3*s^3 + K2*M2*fv4*s^2 + \\
& M1*M2*fv4*s^4 + K2*fv2*fv3*s^2 + K2*fv3*fv4*s^2 + M1*fv2*fv4*s^3 \\
& + M2*fv1*fv4*s^3 + M2*fv3*fv4*s^3 + fv1*fv2*fv4*s^2 + \\
& fv2*fv3*fv4*s^2 + K1*fv2*fv4*s + K2*fv1*fv4*s + K2*fv2*fv4*s + \\
& K2*fv3*fv4*s)/(K1*M3 + K2*M3 + K1*fv3*s + K1*fv4*s + K2*fv3*s + \\
& K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 + M1*fv3*s^3 + \\
& M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + fv3*fv4*s^2)]
\end{aligned}$$

```
[
-(K2*fv4^2*s^2 + fv3*fv4^2*s^2 + K2*fv3*fv4*s^2 +
K2*M3*fv4*s)/(K1*M3 + K2*M3 + K1*fv3*s + K1*fv4*s + K2*fv3*s +
K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 + M1*fv3*s^3 +
M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + fv3*fv4*s^2),
-fv4*s,
(K1*M3 + K2*M3 - M1*fv4^2*s^3 - fv1*fv4^2*s^2 - fv3*fv4^2*s^2 +
K1*fv3*s + K1*fv4*s + K2*fv3*s + K2*fv4*s + M3*fv1*s + M3*fv3*s
+ M1*M3*s^2 - K1*fv4^2*s - K2*fv4^2*s + M1*fv3*s^3 + M1*fv4*s^3
+ fv1*fv3*s^2 + fv1*fv4*s^2 + fv3*fv4*s^2 -
K2*fv3*fv4*s^2)/(K1*M3 + K2*M3 + K1*fv3*s + K1*fv4*s + K2*fv3*s
+ K2*fv4*s + M3*fv1*s + M3*fv3*s + M1*M3*s^2 + M1*fv3*s^3 +
M1*fv4*s^3 + fv1*fv3*s^2 + fv1*fv4*s^2 + fv3*fv4*s^2)]
```

Ginv3 =

```
[
(K1*fv4 + K2*fv3 + K2*fv4 - M2*fv3^2*s^3 - fv2*fv3^2*s^2 -
fv3^2*fv4*s^2 + fv1*fv4*s + fv3*fv4*s - K2*fv3^2*s + M1*fv4*s^2
- K2*fv3*fv4*s)/(K1*fv4 + K2*fv3 + K2*fv4 + fv1*fv4*s +
fv3*fv4*s + M1*fv4*s^2),
-fv3*s,
-(M2*fv3^2*s^3 + K1*K2*fv3 + fv2*fv3^2*s^2 + fv3^2*fv4*s^2 +
K2*fv3^2*s + K1*M2*fv3*s^2 + K2*M1*fv3*s^2 + K2*M2*fv3*s^2 +
M1*M2*fv3*s^4 + M1*fv2*fv3*s^3 + M2*fv1*fv3*s^3 + M1*fv3*fv4*s^3
+ fv1*fv2*fv3*s^2 + fv1*fv3*fv4*s^2 + K1*fv2*fv3*s +
K2*fv1*fv3*s + K2*fv2*fv3*s + K1*fv3*fv4*s +
K2*fv3*fv4*s)/(K1*fv4 + K2*fv3 + K2*fv4 + fv1*fv4*s + fv3*fv4*s
+ M1*fv4*s^2)]
[
-(K2*fv3 + K2*fv4 + K2*fv4^2 + K2*fv3*fv4 + fv2*fv3*s +
fv3*fv4*s + M2*fv3*s^2 + fv3*fv4^2*s + fv2*fv3*fv4*s +
M2*fv3*fv4*s^2)/(K1*fv4 + K2*fv3 + K2*fv4 + fv1*fv4*s +
fv3*fv4*s + M1*fv4*s^2),
-fv4,
-(K1*K2 + M1*fv4^2*s^3 + K1*K2*fv4 + fv1*fv4^2*s^2 +
fv3*fv4^2*s^2 + K1*fv2*s + K2*fv1*s + K2*fv2*s + K1*fv4*s +
K2*fv3*s + K2*fv4*s + K1*M2*s^2 + K2*M1*s^2 + K2*M2*s^2 +
M1*M2*s^4 + K1*fv4^2*s + K2*fv4^2*s + M1*fv2*s^3 + M2*fv1*s^3 +
M1*fv4*s^3 + M2*fv3*s^3 + fv1*fv2*s^2 + fv1*fv4*s^2 +
fv2*fv3*s^2 + fv3*fv4*s^2 + K1*M2*fv4*s^2 + K2*M1*fv4*s^2 +
K2*M2*fv4*s^2 + M1*M2*fv4*s^4 + M1*fv2*fv4*s^3 + M2*fv1*fv4*s^3
+ M2*fv3*fv4*s^3 + fv1*fv2*fv4*s^2 + fv2*fv3*fv4*s^2 +
K1*fv2*fv4*s + K2*fv1*fv4*s + K2*fv2*fv4*s +
K2*fv3*fv4*s)/(K1*fv4*s + K2*fv3*s + K2*fv4*s + M1*fv4*s^3 +
fv1*fv4*s^2 + fv3*fv4*s^2)]
[ (M2*fv3^2*s^3 + K2*M3*fv3 + K2*M3*fv4 + fv2*fv3^2*s^2 +
fv3*fv4^2*s^2 + fv3^2*fv4*s^2 + K2*fv3^2*s + K2*fv4^2*s +
```

$$\begin{aligned}
& M2*M3*fv3*s^2 + M2*fv3*fv4*s^3 + fv2*fv3*fv4*s^2 + \\
& 2*K2*fv3*fv4*s + M3*fv2*fv3*s + M3*fv3*fv4*s) / (K1*fv4 + K2*fv3 + \\
& K2*fv4 + fv1*fv4*s + fv3*fv4*s + M1*fv4*s^2), M3 + fv3*s + \\
& fv4*s, (K1*K2*M3 + K1*fv4^2*s^2 + K2*fv3^2*s^2 + K2*fv4^2*s^2 + \\
& M1*fv4^2*s^4 + M2*fv3^2*s^4 + fv1*fv4^2*s^3 + fv2*fv3^2*s^3 + \\
& fv3*fv4^2*s^3 + fv3^2*fv4*s^3 + K1*fv4*s + K2*fv3*s + K2*fv4*s + \\
& M1*fv4*s^3 + fv1*fv4*s^2 + fv3*fv4*s^2 + K1*M2*M3*s^2 + \\
& K2*M1*M3*s^2 + K2*M2*M3*s^2 + M1*M2*M3*s^4 + K1*M2*fv3*s^3 + \\
& K2*M1*fv3*s^3 + K1*M2*fv4*s^3 + K2*M1*fv4*s^3 + K2*M2*fv3*s^3 + \\
& K2*M2*fv4*s^3 + M1*M3*fv2*s^3 + M2*M3*fv1*s^3 + M1*M2*fv3*s^5 + \\
& M1*M3*fv4*s^3 + M2*M3*fv3*s^3 + M1*M2*fv4*s^5 + K1*fv2*fv3*s^2 + \\
& K2*fv1*fv3*s^2 + K1*fv2*fv4*s^2 + K2*fv1*fv4*s^2 + \\
& K2*fv2*fv3*s^2 + K1*fv3*fv4*s^2 + K2*fv2*fv4*s^2 + \\
& 2*K2*fv3*fv4*s^2 + M3*fv1*fv2*s^2 + M1*fv2*fv3*s^4 + \\
& M2*fv1*fv3*s^4 + M3*fv1*fv4*s^2 + M3*fv2*fv3*s^2 + \\
& M1*fv2*fv4*s^4 + M2*fv1*fv4*s^4 + M1*fv3*fv4*s^4 + \\
& M3*fv3*fv4*s^2 + M2*fv3*fv4*s^4 + fv1*fv2*fv3*s^3 + \\
& fv1*fv2*fv4*s^3 + fv1*fv3*fv4*s^3 + fv2*fv3*fv4*s^3 + \\
& K1*K2*fv3*s + K1*K2*fv4*s + K1*M3*fv2*s + K2*M3*fv1*s + \\
& K2*M3*fv2*s + K1*M3*fv4*s + K2*M3*fv3*s + K2*M3*fv4*s) / (K1*fv4*s \\
& + K2*fv3*s + K2*fv4*s + M1*fv4*s^3 + fv1*fv4*s^2 + fv3*fv4*s^2)]
\end{aligned}$$