Assignment 4

Contents

- Notations: For a given variable, x, dx is its time derivative, ddx is
- create symbolic variable for x.
- specify your initial and final condition.
- Implement the Augmented PD control for set point tracking.
- Augmented PD Control

Notations: For a given variable, x, dx is its time derivative, ddx is

2nd-order derivative.

```
clc
clear all;
close all;
% the following parameters for the arm
I1=10; I2 = 10; m1=5; r1=.5; m2=5; r2=.5; l1=1; l2=1; g=9.8;

% we compute the parameters in the dynamic model
a = I1+I2+m1*r1^2+ m2*(l1^2+ r2^2);
b = m2*l1*r2;
d = I2+ m2*r2^2;
```

create symbolic variable for x.

x1 - theta1 x2 - theta2

```
symx= sym('symx',[4,1]);
global M C Gq
M = [a+2*b*cos(symx(2)), d+b*cos(symx(2));
    d+b*cos(symx(2)), d];
C = [-b*sin(symx(2))*symx(4), -b*sin(symx(2))*(symx(3)+symx(4)); b*sin(symx(2))*symx(3),0];
invM = inv(M);
invMC= inv(M)*C;

% Gravity Matrix
g1=-(m1+m2)*g*l1*sin(symx(2))-m2*g*l2*sin(symx(1)+symx(2));
g2=-m2*g*l2*sin(symx(1)+symx(2));
Gq=[g1;g2];
```

specify your initial and final condition.

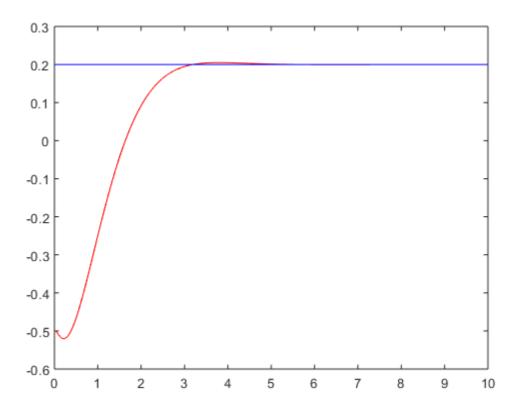
```
x0= [-0.5,0.2,0.1,0.1];
global w torque
w=0.2;
tf=10;
torque = [];
```

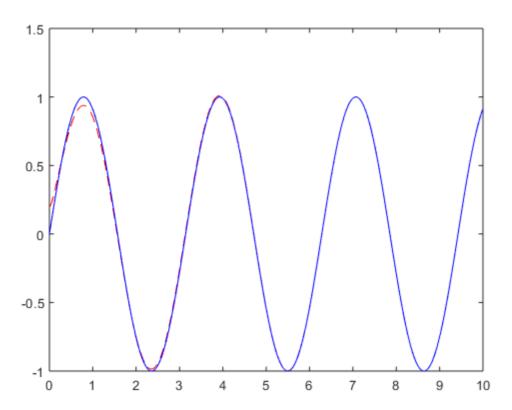
Implement the Augmented PD control for set point tracking.

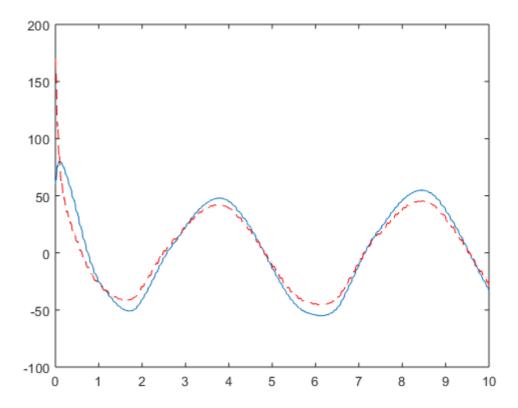
```
xf = [0, 0, 0, 0];
options = odeset('RelTol',1e-4, 'AbsTol',[1e-4, 1e-4, 1e-4, 1e-4]);
[T,X] = ode45(@(t,x) AugmentedPDControl(t,x),[0 tf],x0, options);
figure('Name', 'Theta_1 under PD SetPoint Control');
plot(T, X(:,1), 'r-');
hold on
plot(T, w*ones(size(T,1),1),'b-');
figure('Name','Theta_2 under PD SetPoint Control');
plot(T, X(:,2), 'r--');
hold on
plot(T, sin(2*T), 'b-');
figure('Name','Augmented PD Control');
plot(T, torque(1,1:size(T,1)),'-');
hold on
plot(T, torque(2,1:size(T,1)), 'r--');
hold off
torque=[];
```

Augmented PD Control

```
function dx = AugmentedPDControl(t,x)
    w=0.2;
    theta_d=[w;sin(2*t)]; % [x1d;x2d] Desired trajectory
    dtheta_d=[0;2*cos(2*t)]; % [x1d_dot;x2d_dot]
    ddtheta_d=[0;-4*sin(2*t)]; % [x1d_ddot;x2d_ddot]
    theta=x(1:2,1); % [x1;x2]=[x(1);x(2)]
    dtheta=x(3:4,1); % [x1_dot;x2_dot]=[x(3);x(4)]
    global M C Gq M_d C_d Gq_d
    symx= sym('symx',[4,1]);
    M = subs(M, [symx(1); symx(2); symx(3); symx(4)], [x(1); x(2); x(3); x(4)]);
    C = subs(C, [symx(1); symx(2); symx(3); symx(4)], [x(1); x(2); x(3); x(4)]);
    Gq = subs(Gq, [symx(1); symx(2); symx(3); symx(4)], [x(1);x(2);x(3);x(4)]);
    M_d = subs(M, [symx(1); symx(2); symx(3); symx(4)], [theta_d(1); theta_d(2); dtheta_d(1); dtheta_d(2)]);
     C_d = subs(C, [symx(1); symx(2); symx(3); symx(4)], [theta_d(1); theta_d(2); dtheta_d(1); dtheta_d(2)]); 
     \mathsf{Gq\_d} = \mathsf{subs}(\mathsf{Gq}, [\mathsf{symx}(1); \mathsf{symx}(2); \mathsf{symx}(3); \mathsf{symx}(4)], [\mathsf{theta\_d}(1); \mathsf{theta\_d}(2); \mathsf{dtheta\_d}(1); \mathsf{dtheta\_d}(2)]); 
    invM = inv(M);
    invMC= inv(M)*C;
    tau = Controler(theta_d,dtheta_d,dtheta_d,theta,dtheta);
    global torque
    torque = [torque, tau];
    dx = zeros(4,1);
    dx(1)=x(3); %dtheta1
    dx(2) = x(4); %dtheta2
    dx(3:4) = -invMC* x(3:4) + invM*tau;
end
function tau = Controler(theta_d,dtheta_d,dtheta_d,theta,dtheta)
   P_e = theta_d - theta;
   V_e = dtheta_d - dtheta;
   Kp = 100*eye(2);
   Kv = 100*eye(2);
   global M C Gq d
   tau = (Kp*P_e + Kv*V_e) + M*ddtheta_d + C*dtheta_d;
end
```







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Assignment 4

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Contents

- Notations: For a given variable, x, dx is its time derivative, ddx is
- create symbolic variable for x.
- specify your initial and final condition.
- Implement the Iterative Learning control for set point tracking.
- Iterative Learning control

Notations: For a given variable, x, dx is its time derivative, ddx is

2nd-order derivative.

```
clc
clear all;
close all;
% the following parameters for the arm
I1=10; I2 = 10; m1=5; r1=.5; m2=5; r2=.5; l1=1; l2=1; g=9.8;

% we compute the parameters in the dynamic model
a = I1+I2+m1*r1^2+ m2*(l1^2+ r2^2);
b = m2*l1*r2;
d = I2+ m2*r2^2;
```

create symbolic variable for x.

x1 - theta1 x2 - theta2

```
symx= sym('symx',[4,1]);
global M C Gq dGq
M = [a+2*b*cos(symx(2)), d+b*cos(symx(2));
    d+b*cos(symx(2)), d];
C = [-b*sin(symx(2))*symx(4), -b*sin(symx(2))*(symx(3)+symx(4)); b*sin(symx(2))*symx(3),0];
invM = inv(M);
invMC= inv(M)*C;

% Gravity Matrix
g1=-(m1+m2)*g*l1*sin(symx(2))-m2*g*l2*sin(symx(1)+symx(2));
g2=-m2*g*l2*sin(symx(1)+symx(2));
Gq=[g1;g2];
dGq = [diff(Gq, symx(1)), diff(Gq, symx(2))];
```

specify your initial and final condition.

```
x0= [-0.5,0.2,0.1,0.1];
global i w torque
i = 0;
w = 0.2;
tf=10;
torque = [];
```

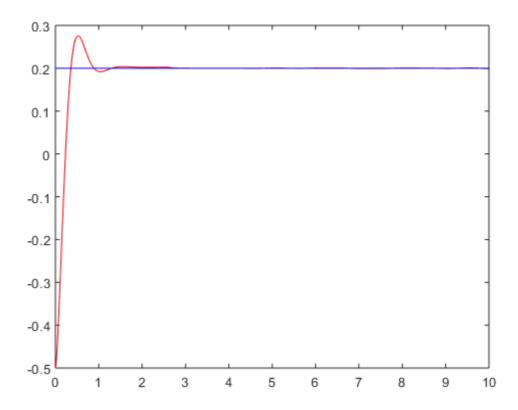
Implement the Iterative Learning control for set point tracking.

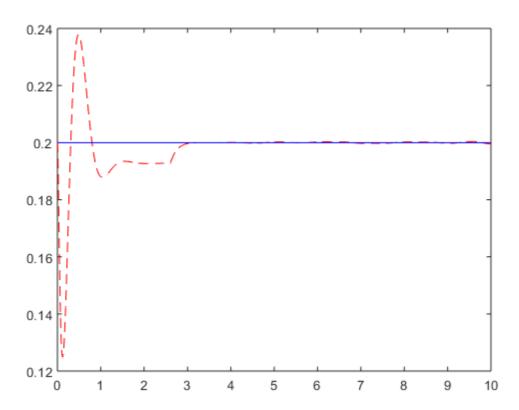
```
xf = [0, 0, 0, 0];
options = odeset('RelTol',1e-4, 'AbsTol',[1e-4, 1e-4, 1e-4, 1e-4]);
[T,X] = ode45(@(t,x) IterativeControl(t,x),[0 tf],x0, options);
figure('Name', 'Theta_1 under PD SetPoint Control');
plot(T, X(:,1), 'r-');
hold on
plot(T, w*ones(size(T,1),1),'b-');
figure('Name','Theta_2 under PD SetPoint Control');
plot(T, X(:,2), 'r--');
hold on
plot(T, w*ones(size(T,1),1),'b-');
figure('Name','Torque: Augmented PD Control');
plot(T, torque(1,1:size(T,1)),'-');
hold on
plot(T, torque(2,1:size(T,1)), 'r--');
hold off
torque=[];
```

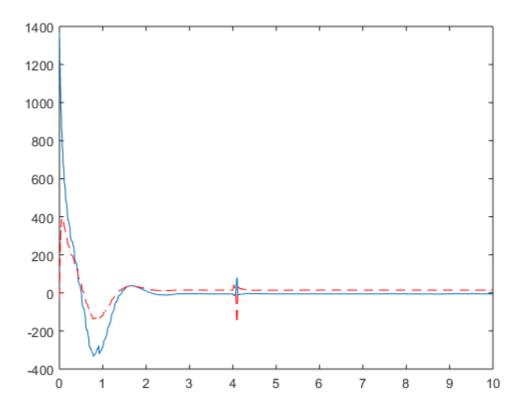
Iterative Learning control

```
function dx = IterativeControl(t,x)
   global i w
   w=0.2;
   theta_d=[w;w]; % [x1d;x2d] Desired trajectory
    dtheta_d=[0;0]; % [x1d_dot;x2d_dot]
    ddtheta_d=[0;0]; % [x1d_ddot;x2d_ddot]
    theta=x(1:2,1); % [x1;x2]=[x(1);x(2)]
   dtheta=x(3:4,1); % [x1_dot;x2_dot]=[x(3);x(4)]
   global M C Gq dGq
   symx= sym('symx',[4,1]);
   M = subs(M, [symx(1); symx(2); symx(3); symx(4)], [x(1);x(2);x(3);x(4)]);
   C = subs(C, [symx(1); symx(2); symx(3); symx(4)], [x(1); x(2); x(3); x(4)]);
   Gq = subs(Gq, [symx(1);symx(2);symx(3);symx(4)], [x(1);x(2);x(3);x(4)]);
    invM = inv(M);
    invMC= inv(M)*C;
    invMG= inv(M)*Gq;
   dGq = subs(dGq, [symx(1); symx(2)], [x(1);x(2)]);
   tau = Controler(theta_d,dtheta_d,dtheta_d,theta,dtheta,t);
   global torque
   torque = [torque, tau];
    dx = zeros(4,1);
    dx(1)=x(3); %dtheta1
    dx(2) = x(4); %dtheta2
    dx(3:4) = -invMC* x(3:4) + invM*tau -invMG;
end
function tau = Controler(theta_d,dtheta_d,ddtheta_d,theta,i)
  global u
  P_e = theta_d - theta;
  V_e = dtheta_d - dtheta; % dtheta_d = 0
% Kp = double(simplify(dGq*eye(2)))
% To calculate alpha value I have considered calculating partial
% differentiation of Gq (Gravity Matrix) with respect to joint angles q,
% which gives me dGq. The max of dGq is used for selecting the value of Kp
   Kp = 200*eye(2);
   Kv = 30*eye(2);
   beta = 0.1;
```

```
if (i == 0)
    u = zeros(2,1);
end
tau = (1/beta)*(Kp*P_e + Kv*V_e) + u;
if (norm(dtheta) < 0.0001)
    u = tau;
end
end</pre>
```







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Assignment #4	
For the dynamic model: show it no priving I M(q) q + C(q, q) q + N(q) = I and 8 is SPM +	0
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the max value of 11 2N(W) 11 was coming out }	
to also satisfy. To also satisfy works to have style produced to the satisfy.	
to also satisfy	
Herey control indoor relat roungotion.	•
~ win (kp) ≥ x	
also,	•
$B = 0.1$ which satisfies $0 \le B \le \frac{1}{2}$.	•
Thus, the system converges with global asymptotic stability.	
	(
	(<u>)</u>