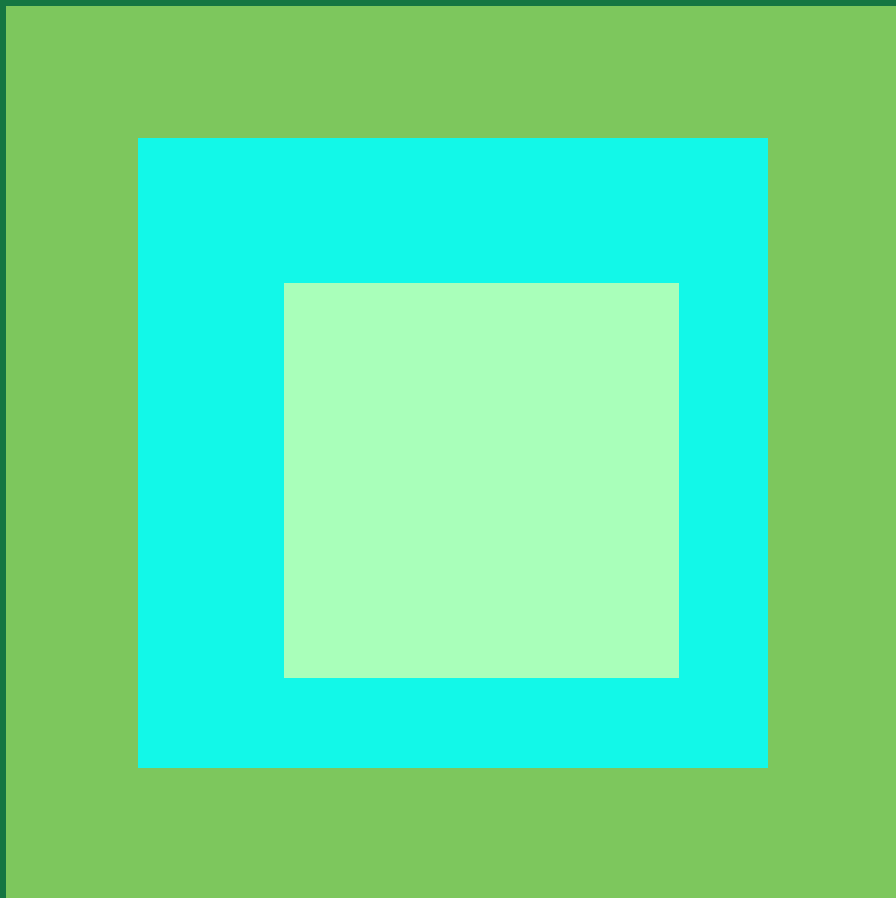


**Single and multiple step  
forecasting of solar  
power production:  
applying and evaluating  
potential models.**

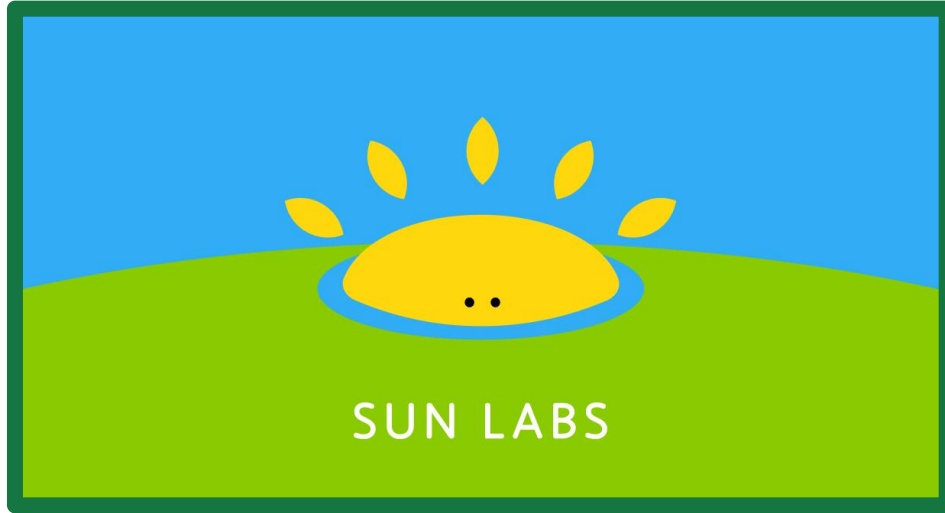


Process data

Machine learning

Start-up

# Sun Labs



Data  
visualization  
and  
real-time  
logging for  
solar cell  
facilities

# Primary research question

Create a solar power forecasting model based on Sun Labs collected data.

Can exogenous variables increase accuracy of the models?

# Sala Facility



*Photo from Solel i Sala och Heby*

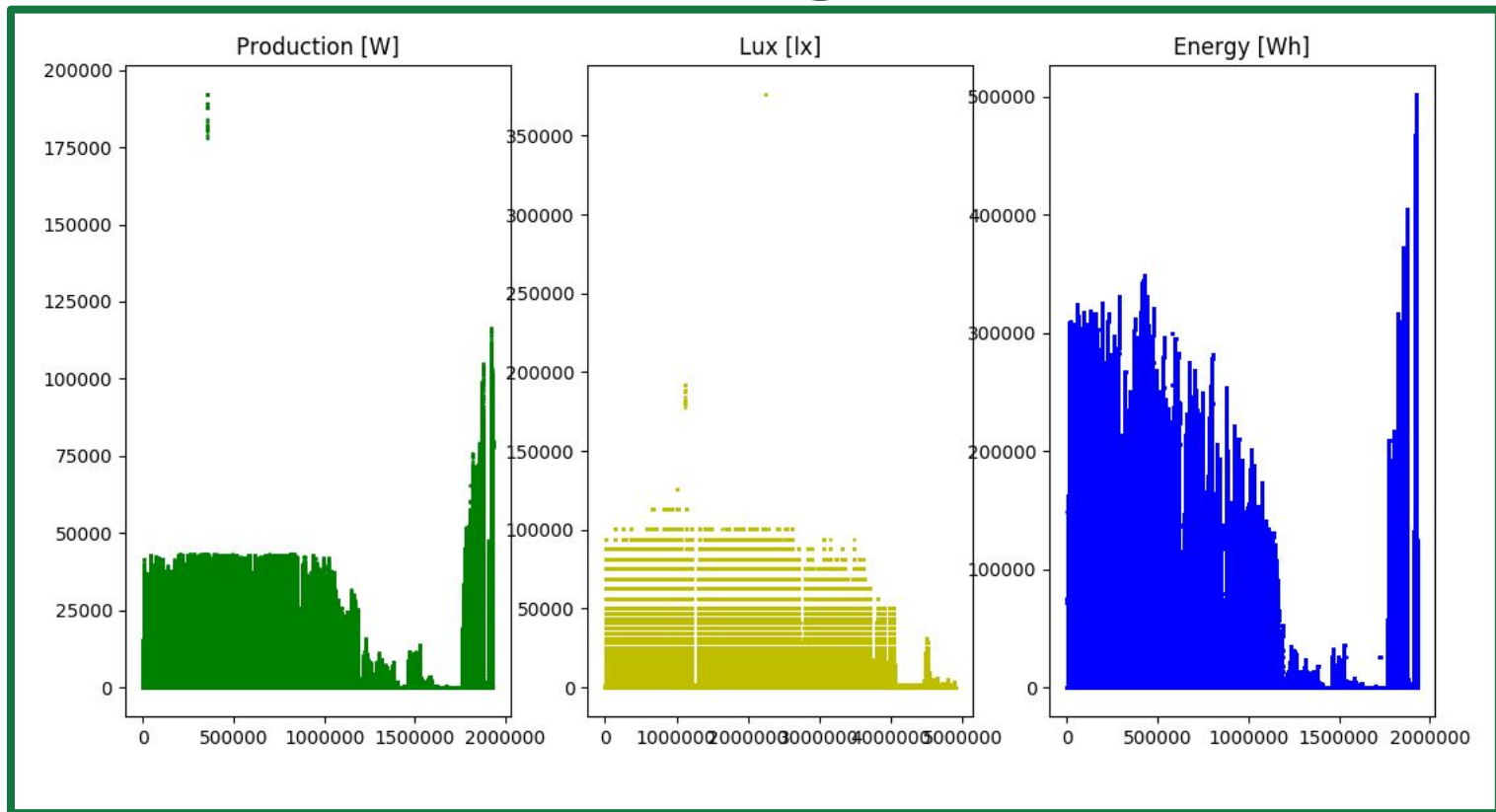
Installed max  
power: 47 kW

Yearly energy  
production:  
40 MWh

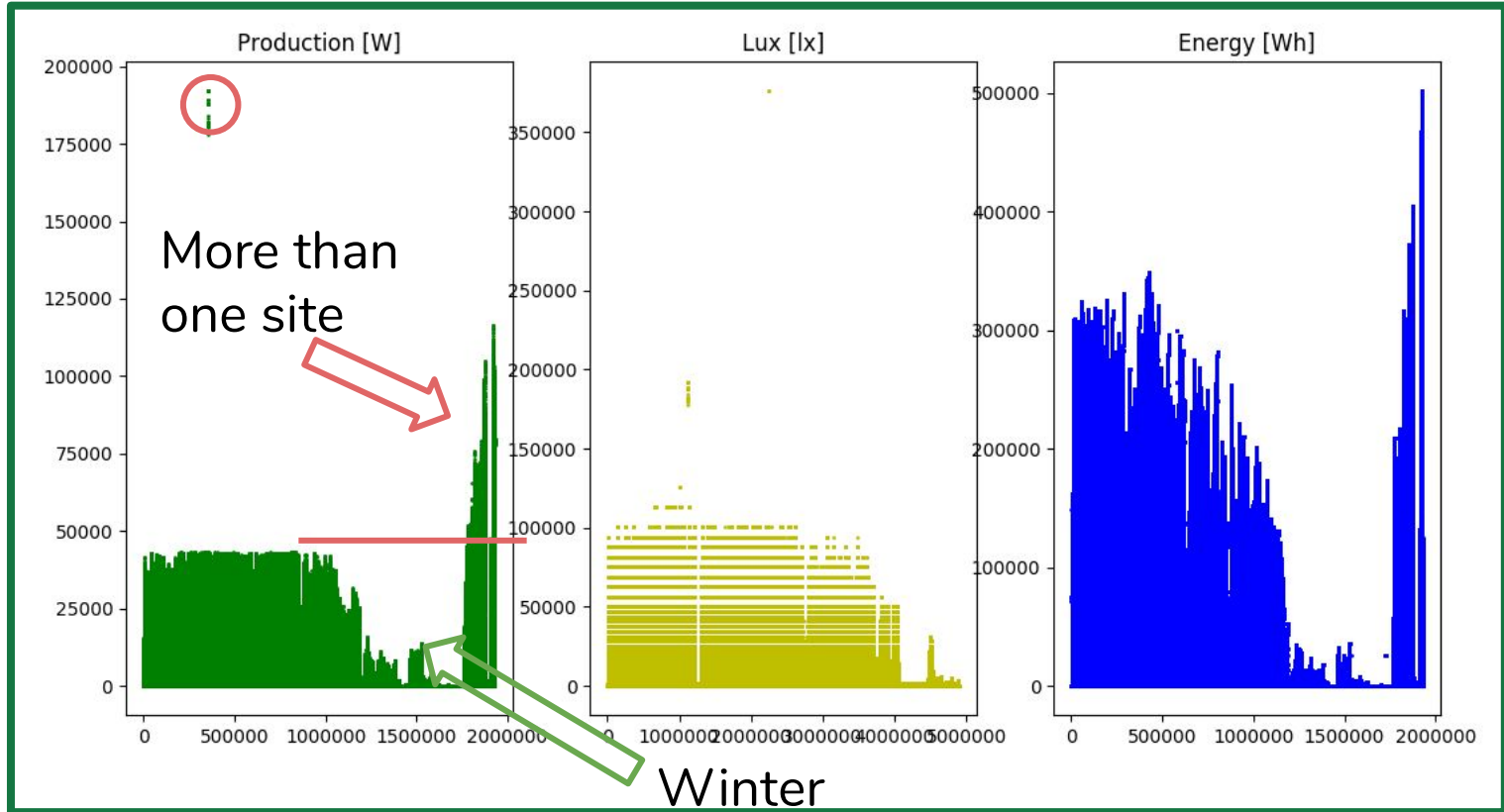
# Data Limitation



# Ex: Data cleaning



# Ex: Data cleaning





# Data Limitation: exogenous predictors

Meteorological  
conditions

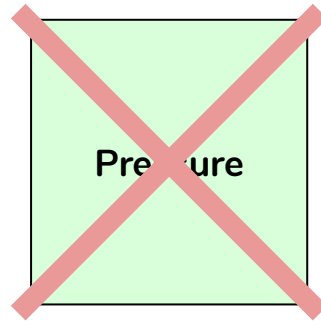
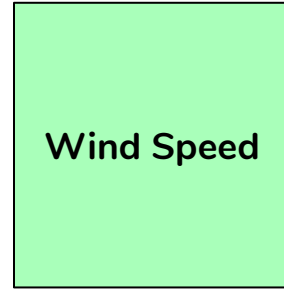
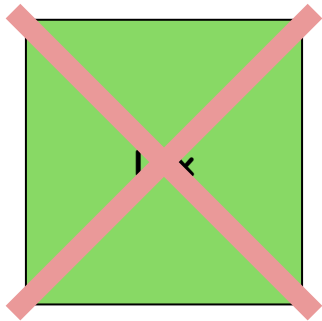
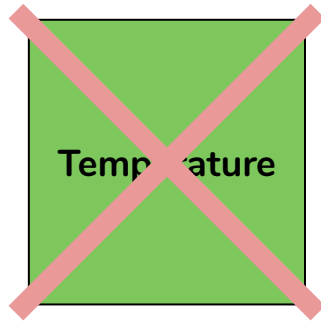
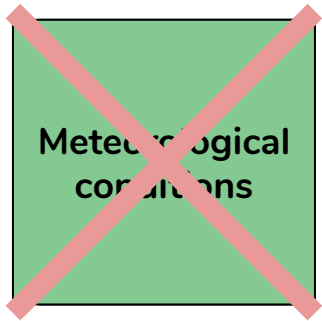
Temperature

Lux

Wind Speed

Pressure

# Data Limitation: exogenous predictors



# Model choice

1

Linear model: ARIMA and  
ARIMAX

# Model choice

1

Linear model: ARIMA and  
ARIMAX ->  
single step forecast

# Model choice




1

Linear model: ARIMA and  
ARIMAX ->  
single step forecast

2

Nonlinear model:  
Gaussian process ->  
multiple step forecast

# Research question

-  Which of the various compared models has the highest single-step forecasting accuracy?
-  How does the usage of an exogenous predictor change the performance of a forecasting model and ultimately the forecast accuracy?
-  Which of the two compared models has the highest multiple step forecasting accuracy?

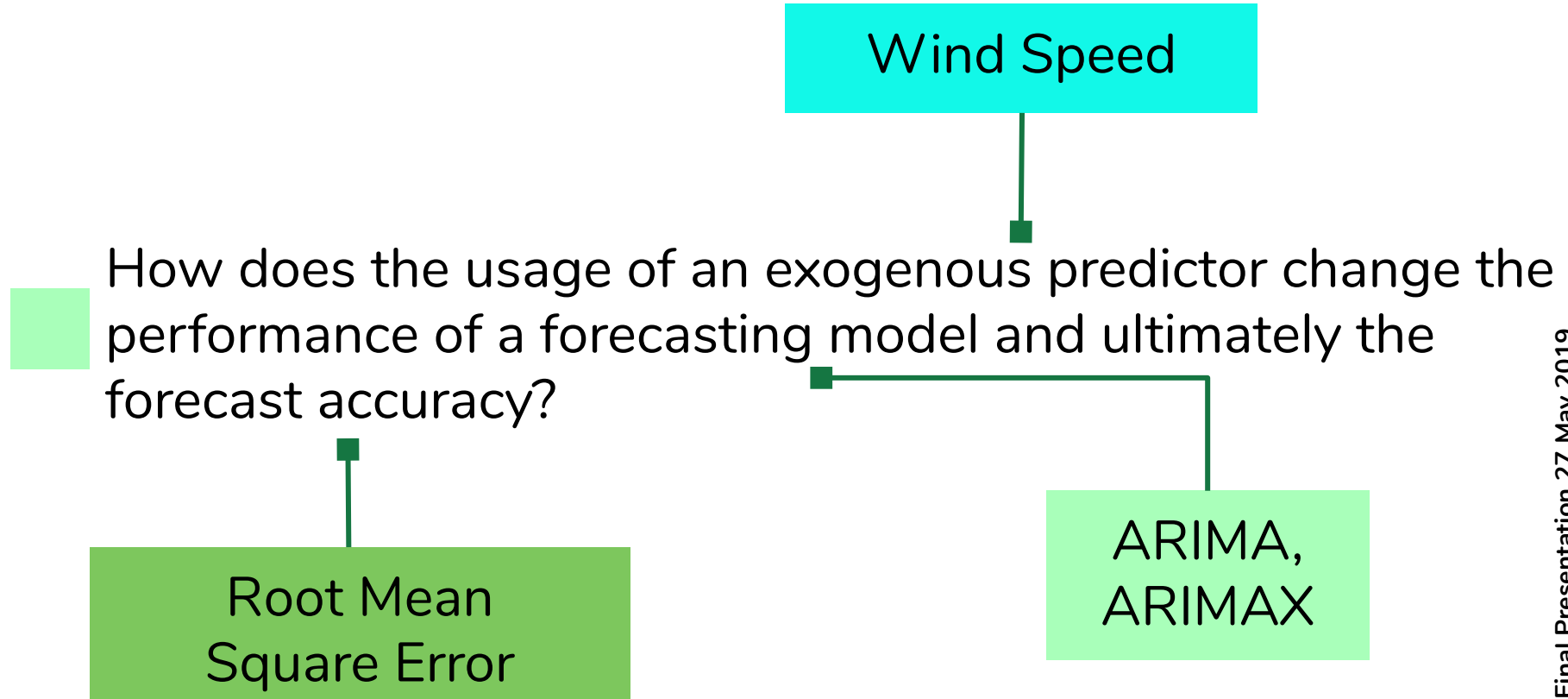
# Research question

■ Which of the various compared models has the highest single-step forecasting accuracy?

Root  
Mean  
Square  
Error

ARIMA,  
ARIMAX,  
Persistence

# Research question





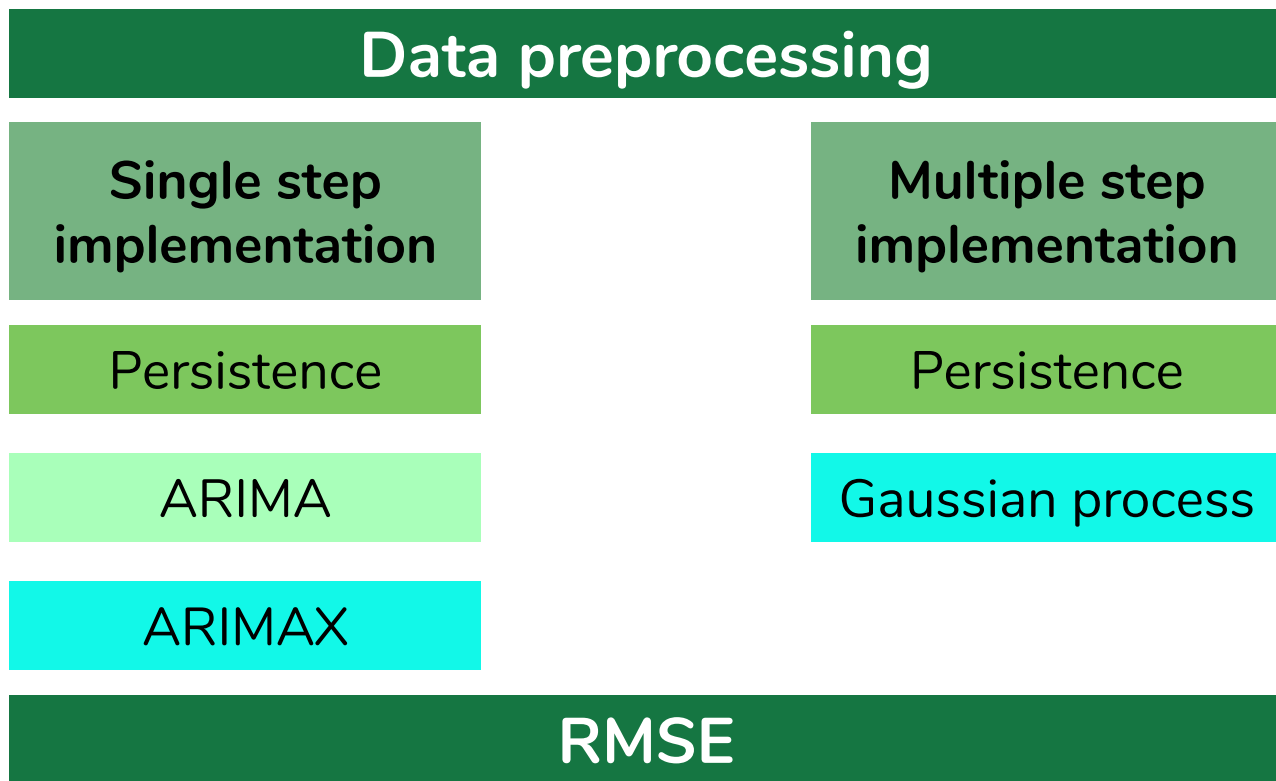
# Research question

Gaussian  
process,  
persistence

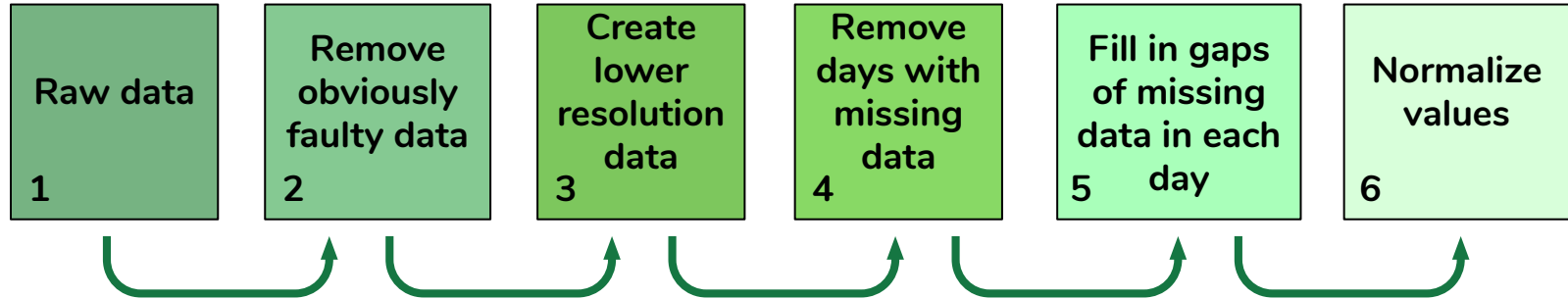
Root  
Mean  
Square  
Error

Which of the two compared models has the highest multiple step forecasting accuracy?

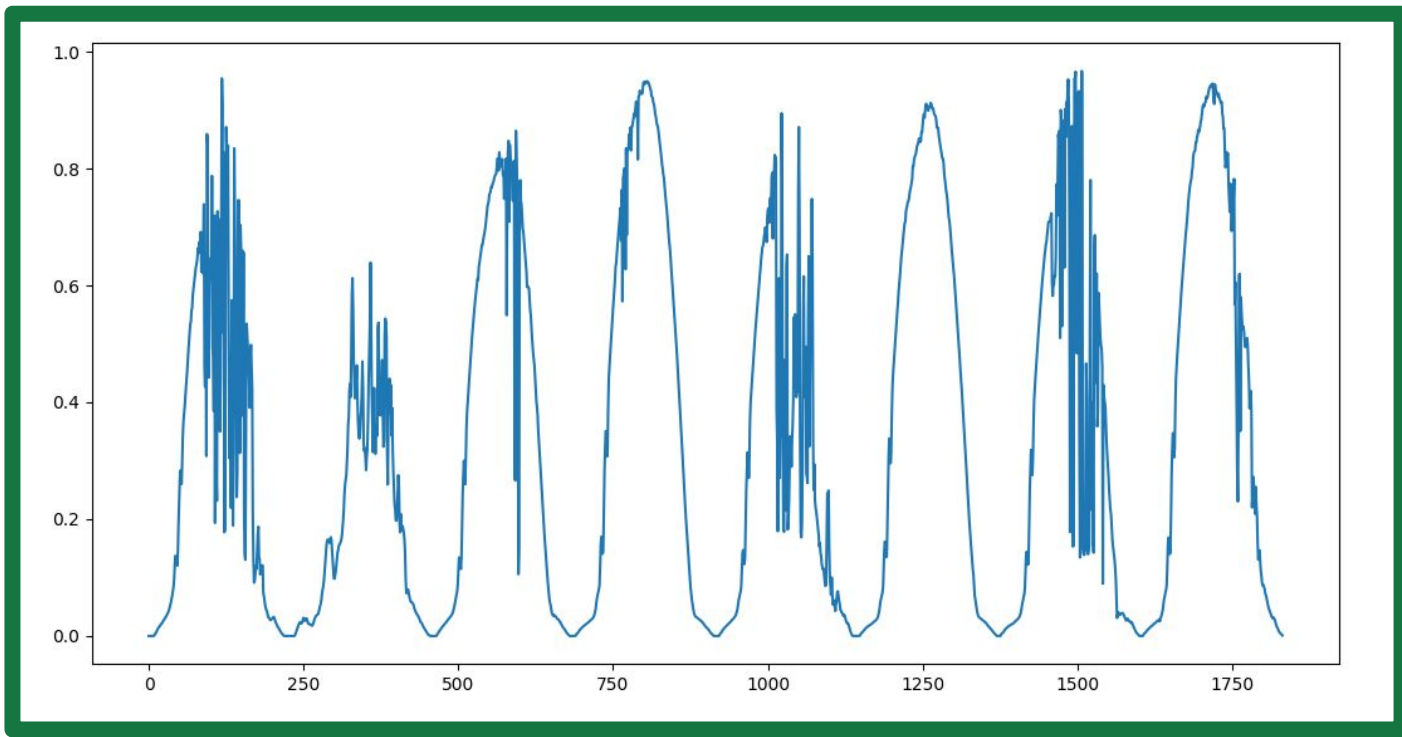
# To answer research questions



# Data preprocessing

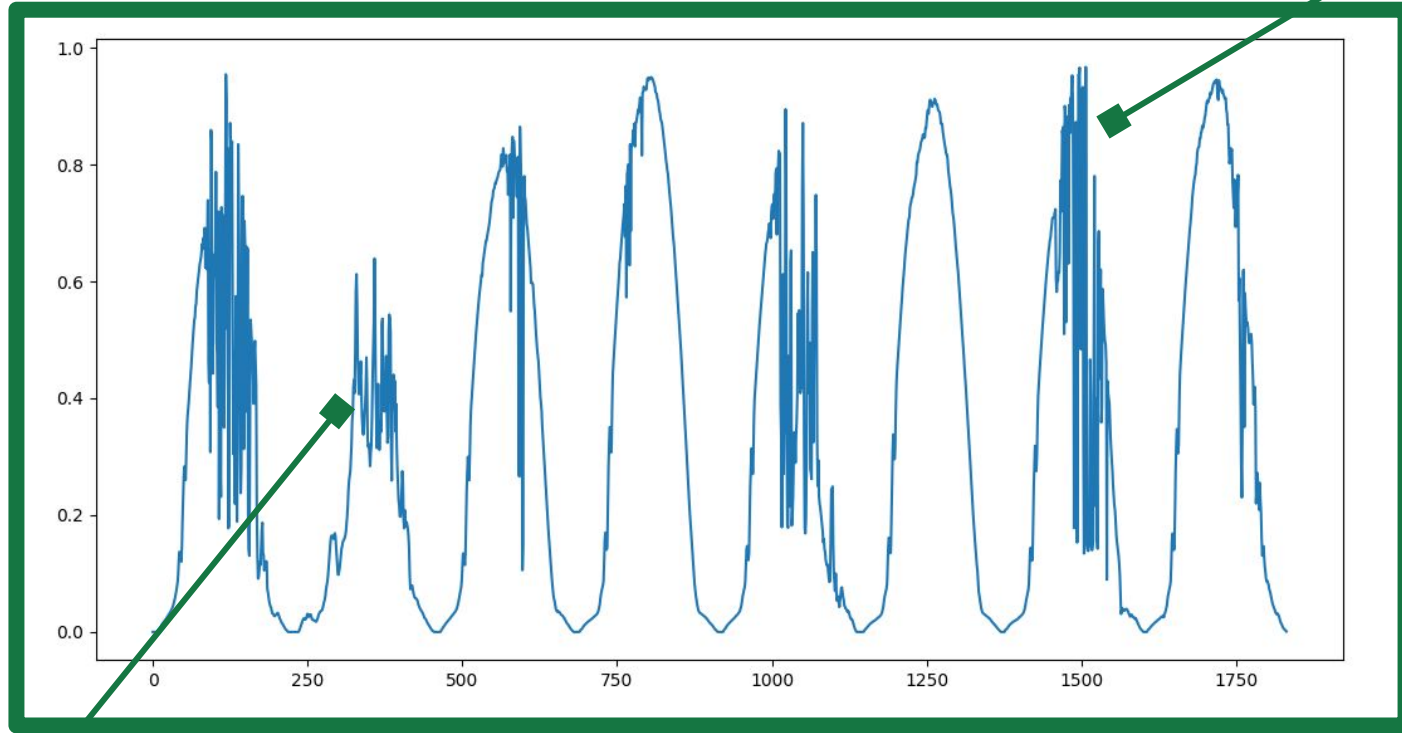


# Data preprocessing



Example 8 days of July

# Data preprocessing



"Rainy day"

Example 8 days of July

# Persistence

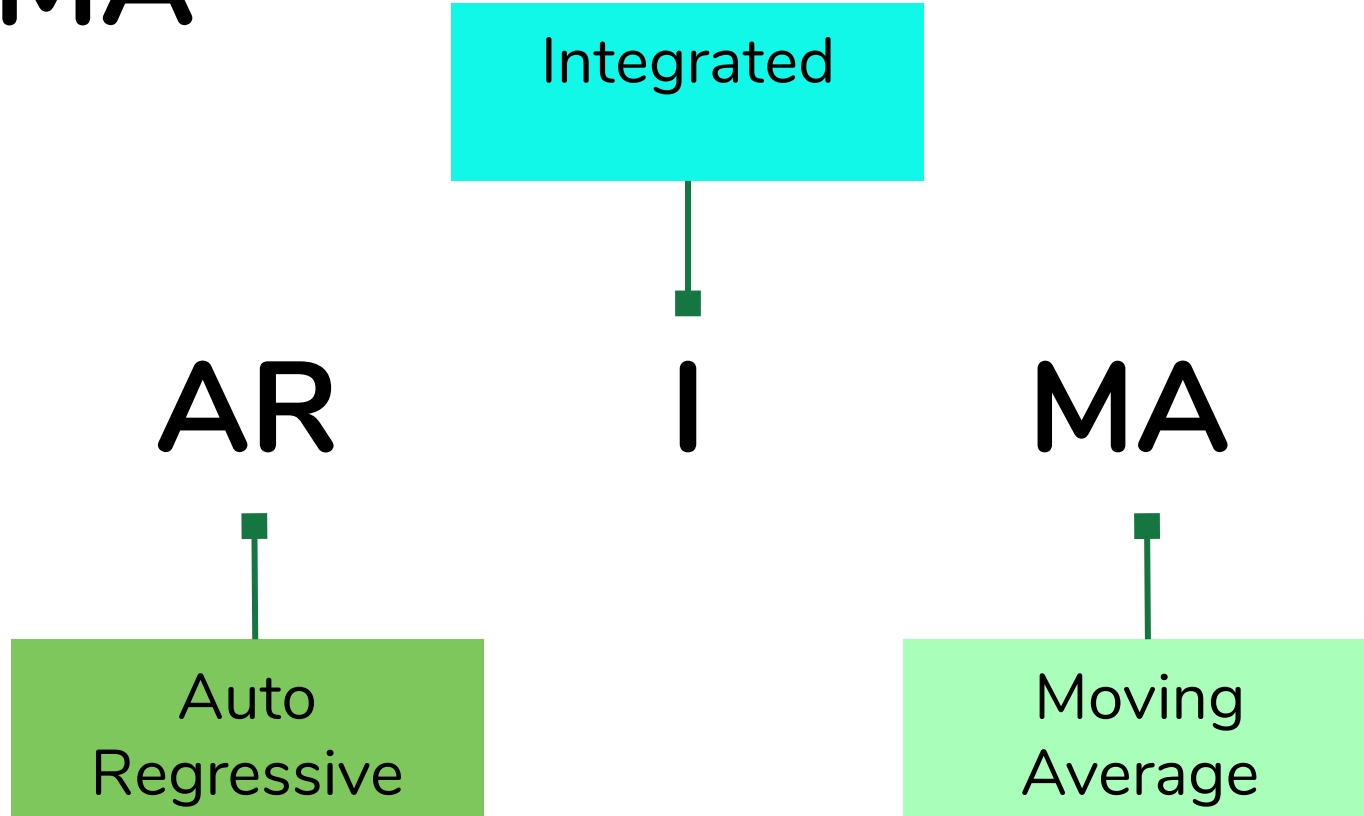
Forecast value the same  
as present value

# Persistence

Forecast value the same  
as present value

$$\hat{y}_t = y_{t-1},$$

# ARIMA





# ARIMA

ARIMA(p,d,q)

$$y'_t = c + \varphi_1 y'_{t-1} + \dots + \varphi_p y'_{t-p} + \theta_1 \varepsilon_{t-1} + \dots + \theta_q \varepsilon_{t-q} + \varepsilon_t ,$$

p: lags of earlier values

AR

d: order of differencing of y'

I

linear combination of q lags of forecasted errors.

MA

# ARIMAX

Integrated

Exogenous  
Wind Speed

AR

I

MA

X

Auto  
Regressive

Moving  
Average

# ARIMAX

$$y'_t = bx_t + \varphi_1 y'_{t-1} + \cdots + \varphi_p y'_{t-p} + \theta_1 \varepsilon_{t-1} + \cdots + \theta_q \varepsilon_{t-q} + \varepsilon_t ,$$

Exogenous  
Wind Speed

# Gaussian process

A Gaussian process is a finite collection of random variables, which have a joint distribution.

# Gaussian process

A Gaussian process is a finite collection of random variables, which have a joint distribution.

Different kernel characteristics (assumptions) decide forecast function form

# Gaussian process

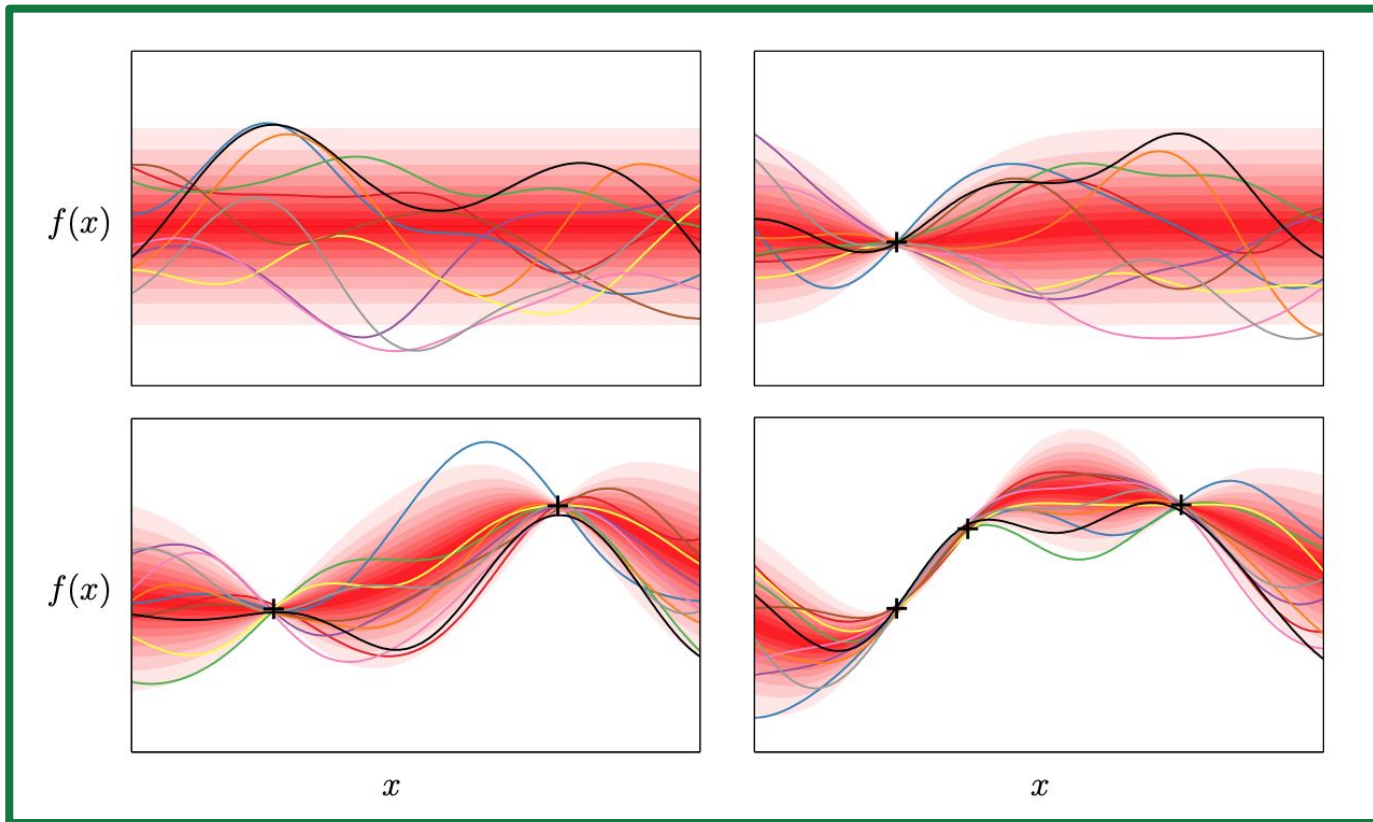


Figure from (Duvenaud, 2014)

# RMSE

Forecast

Actual value

$$RMSE = \sqrt{\frac{\sum_{n=1}^N (\hat{y}_n - y_n)^2}{N}}$$

# Single step model implementations

Compared models:  
Persistence,  
ARIMA,  
ARIMAX

Two different time steps  
5 minutes and 10 minutes

ARIMA and ARIMAX orders  
(5,1,0), (5,1,1) and (4,1,2).

Random shuffle days

Trained using the first 24 days ( $\approx 86\%$  of dataset) of July

Forecast next time step for 4 days ( $\approx 14\%$  of dataset) of July

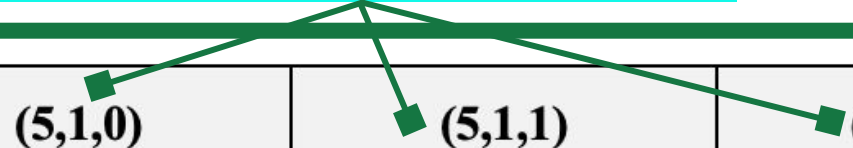


# Result: single step models

<i>RMSE</i>	(5,1,0)		(5,1,1)		(4,1,2)	
	5 minutes	10 minutes	5 minutes	10 minutes	5 minutes	10 minutes
Persistence	7.65%	8.89%	7.65%	8.89%	7.65%	8.89%
ARIMA	7.49%	8.72%	7.52%	8.73%	7.54%	8.69%
ARIMAX	7.47%	8.68%	7.49%	8.70%	7.52%	8.66%

# Result: single step models

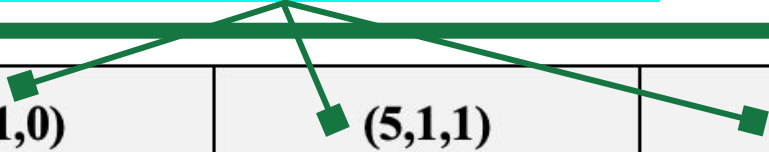
ARIMA, ARIMAX order



<i>RMSE</i>	(5,1,0)		(5,1,1)		(4,1,2)	
	5	10	5	10	5	10
	minutes	minutes	minutes	minutes	minutes	minutes
Persistence	7.65%	8.89%	7.65%	8.89%	7.65%	8.89%
ARIMA	7.49%	8.72%	7.52%	8.73%	7.54%	8.69%
ARIMAX	7.47%	8.68%	7.49%	8.70%	7.52%	8.66%

# Result: single step models

ARIMA, ARIMAX order



<i>RMSE</i>	(5,1,0)		(5,1,1)		(4,1,2)	
	5	10	5	10	5	10
	minutes	minutes	minutes	minutes	minutes	minutes
Persistence	7.65%	8.89%	7.65%	8.89%	7.65%	8.89%
ARIMA	7.49%	8.72%	7.52%	8.73%	7.54%	8.69%
ARIMAX	7.47%	8.68%	7.49%	8.70%	7.52%	8.66%

# Multiple step model implementations

Compared models:  
One week persistence,  
Gaussian process

Time step  
of 5  
minutes

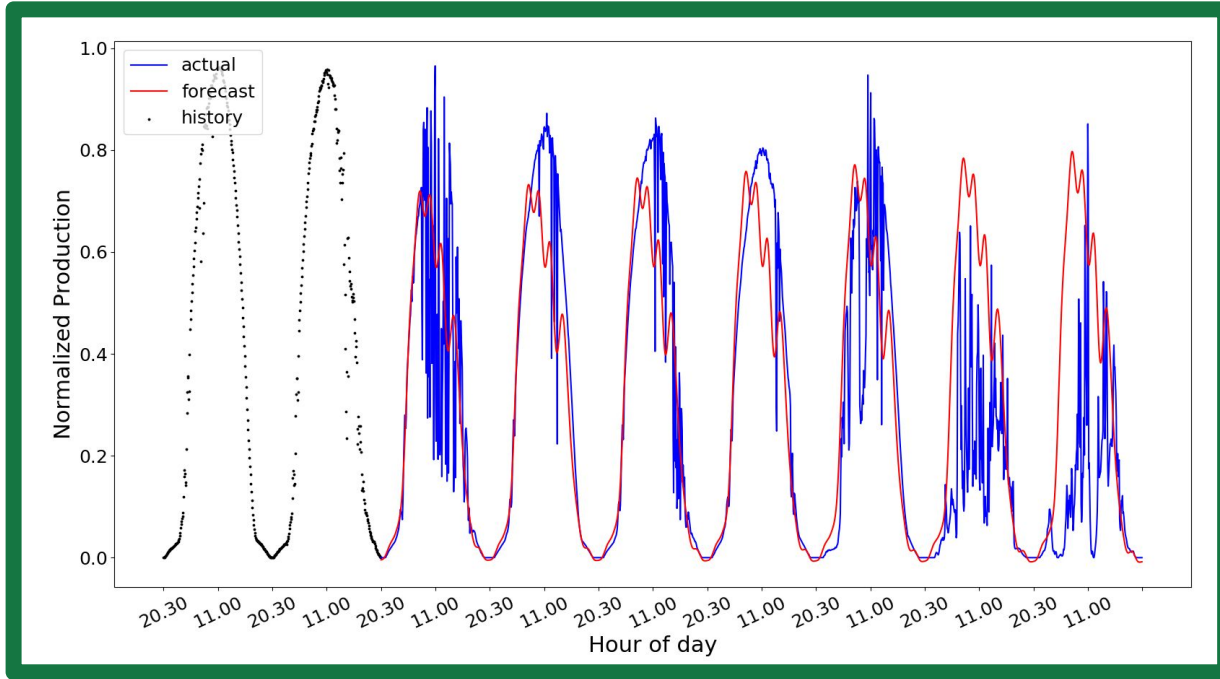
Only  
observing  
days  
between  
production  
start and  
end 1.30 -  
20.30

According  
to (Dahl,  
2017)

Trained  
using the  
first 21  
days (75%  
of dataset)  
of July

Forecast  
all time  
steps for 7  
days (25%  
of dataset)  
of July

# Result: multiple step models

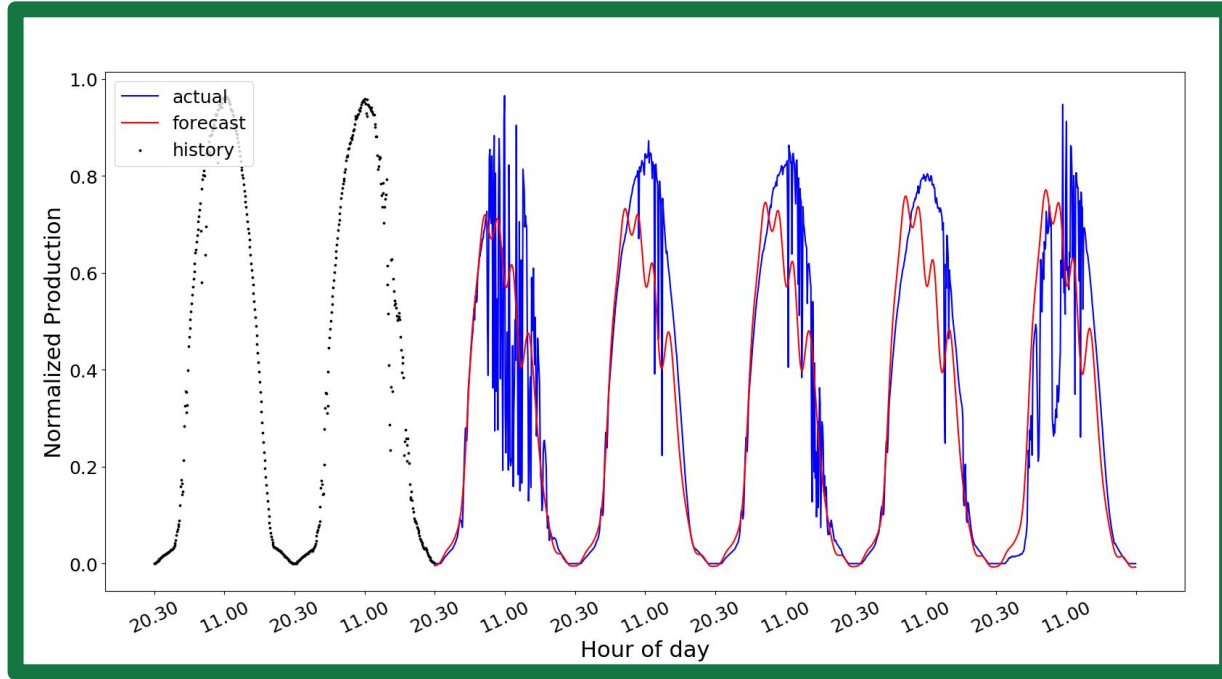


**Persistence**  
**RMSE: 22.61%**

**Gaussian process**  
**RMSE: 19.64%**

**7 days**

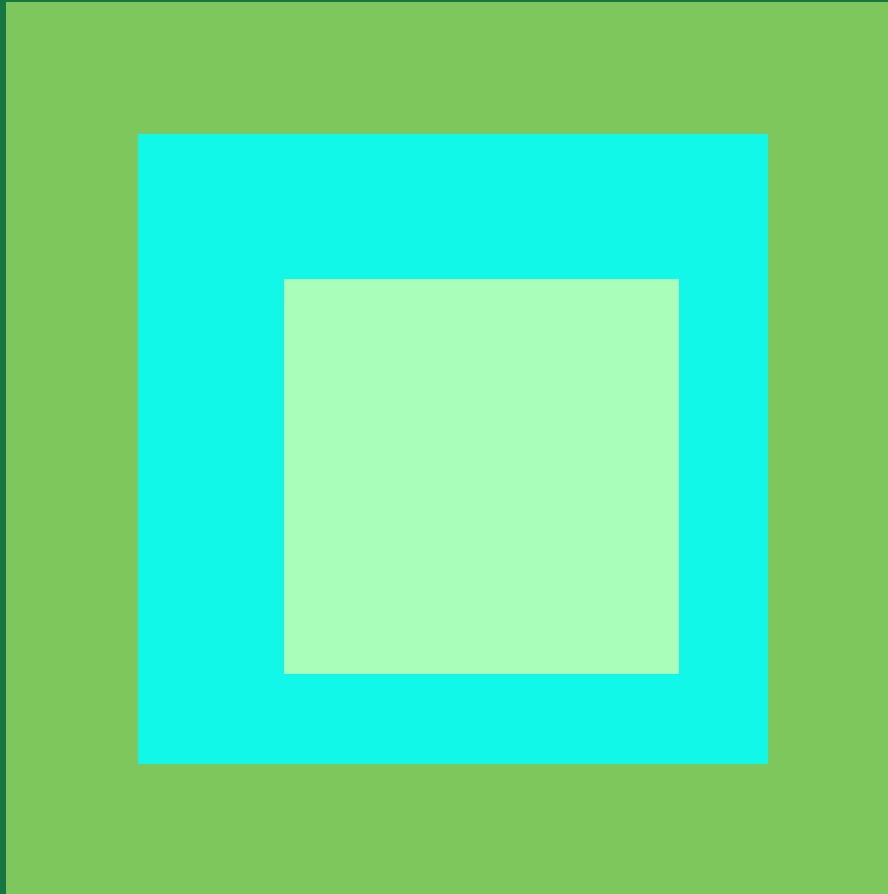
# Result: multiple step models



**Persistence**  
**RMSE: 20.0%**

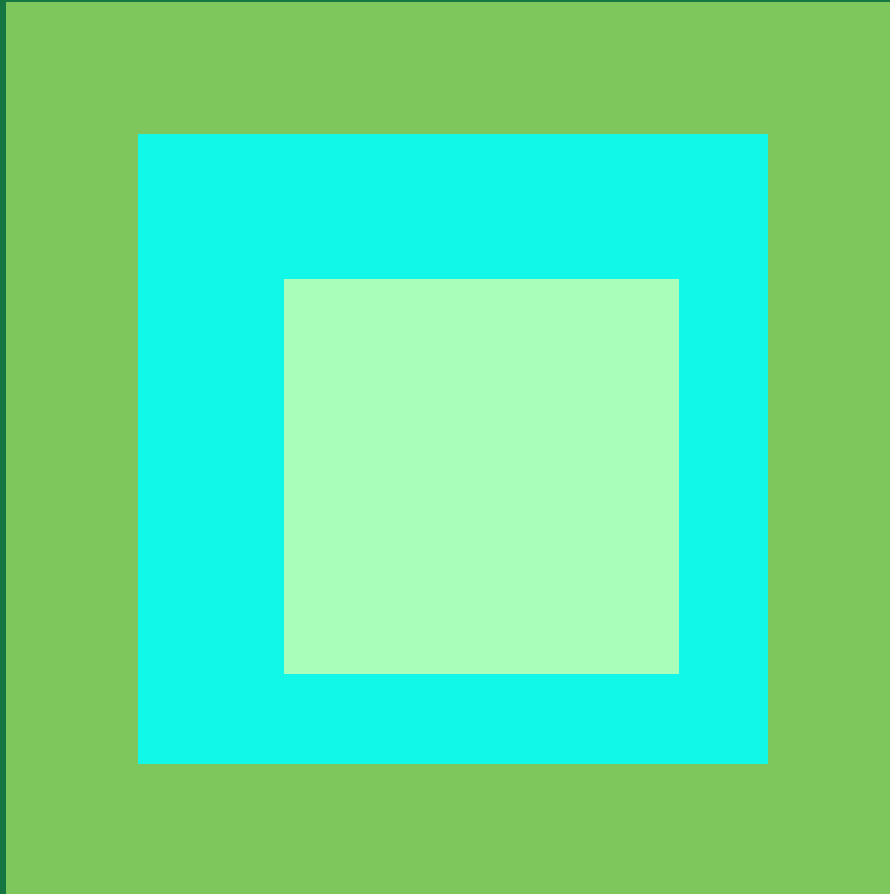
**Gaussian process**  
**RMSE: 13.7%**

**5 days**



ARIMA is more accurate than persistence in applied model

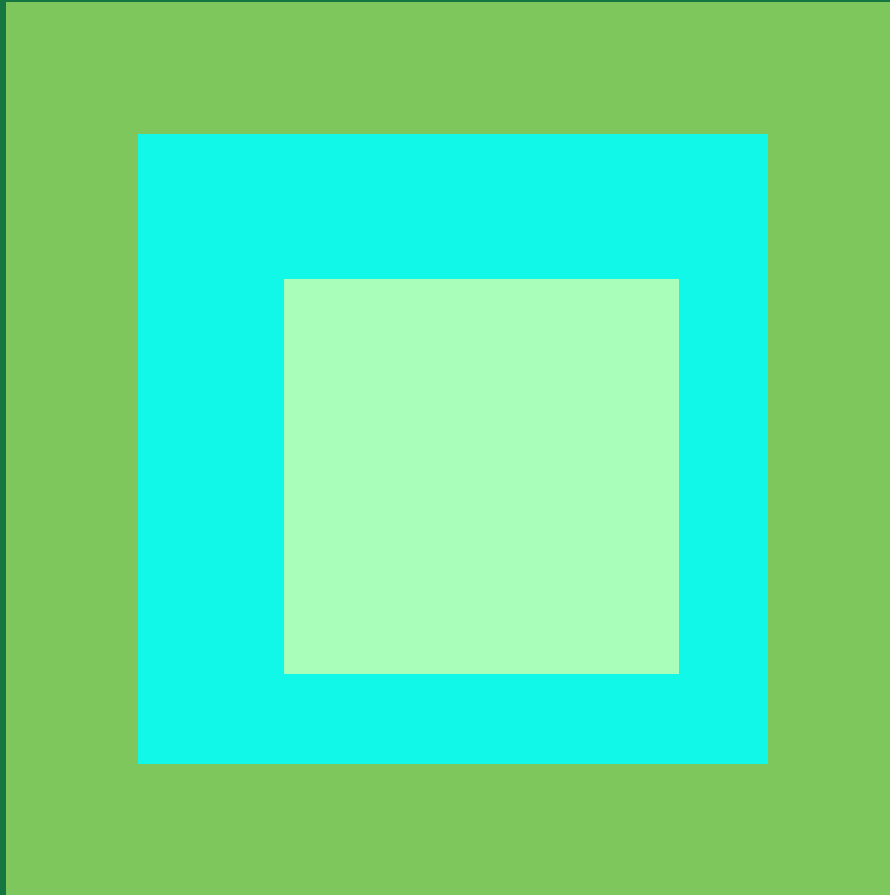
Adding an exogenous variable did not help improve accuracy significantly



Gaussian process  
is more accurate  
than persistence  
in applied model

However, the  
applied model  
can be further  
developed by  
adding exog.  
variable or more  
history





Computational  
time

& time...

**Thank you!**

