

# Introduction to Deep Learning

Aug. 2019

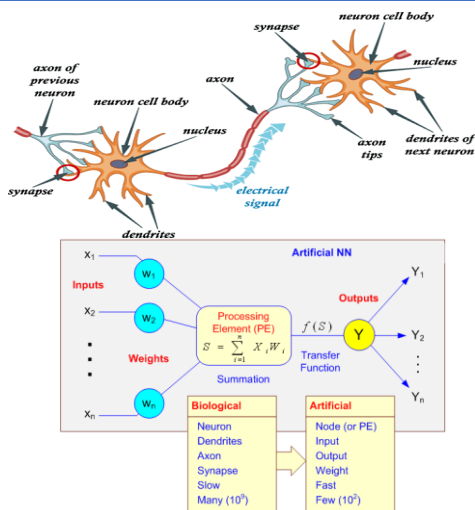
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## Modeling a neuron

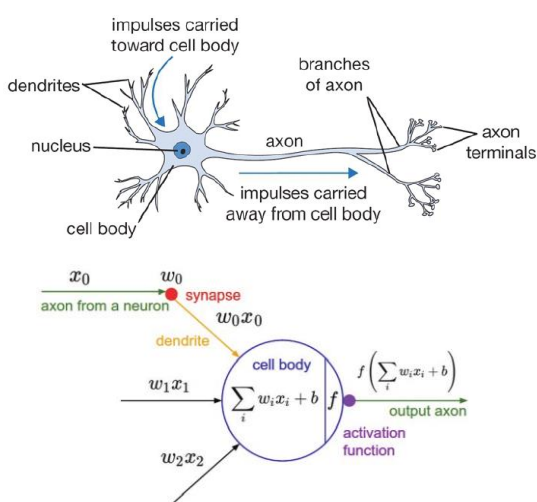


<https://www.quora.com/What-is-deep-learning>

- **Neuron: 신경세포(神經細胞)**
  - ▶ Dendrite: 수상돌기(樹狀突起)
    - input
  - ▶ Axon: 축삭돌기(軸索突起)
    - output
    - Branches of axon
    - Terminals of axon (axon tip)
      - synaptic knob
  - ▶ Synapse: 연결
    - junction between two nerve cells
- **Human**
  - ▶ whole brain
    - ~86 billion neurons (Giga,  $10^9$ )
    - ~100 trillion synapses (Tera,  $10^{12}$ )
  - ▶ cerebral cortex: 대뇌피질
    - 19~23 billion neurons

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## Modeling a neuron



### Activation functions

[https://en.wikipedia.org/wiki/Activation\\_function](https://en.wikipedia.org/wiki/Activation_function)

Identity		$f(x) = x$
Binary step		$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$
Logistic (a.k.a. Soft step)		$f(x) = \frac{1}{1 + e^{-x}}$ <b>sigmoid</b>
TanH		$f(x) = \tanh(x) = \frac{2}{1 + e^{-2x}} - 1$
ArcTan		$f(x) = \tan^{-1}(x)$
Softsign [7][8]		$f(x) = \frac{x}{1 +  x }$
Rectified linear unit (ReLU) [9]		$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$

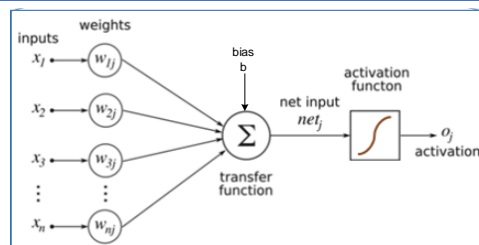
(a) Step function      (b) Sign function      (c) Sigmoid function

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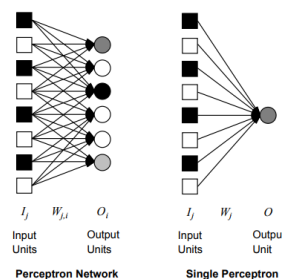
# Perceptron: single layer neural network

- **Perceptron** is a single artificial neuron that computes its weighted input and uses a threshold activation function.

- ▶ It is also called a TLU (threshold logic unit).
- ▶ It effectively separates the input space into two categories by the hyperplane:  $W \cdot X + b = 0$

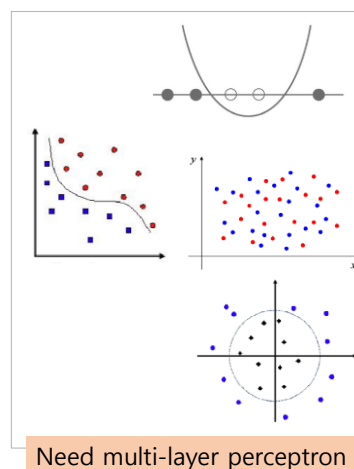
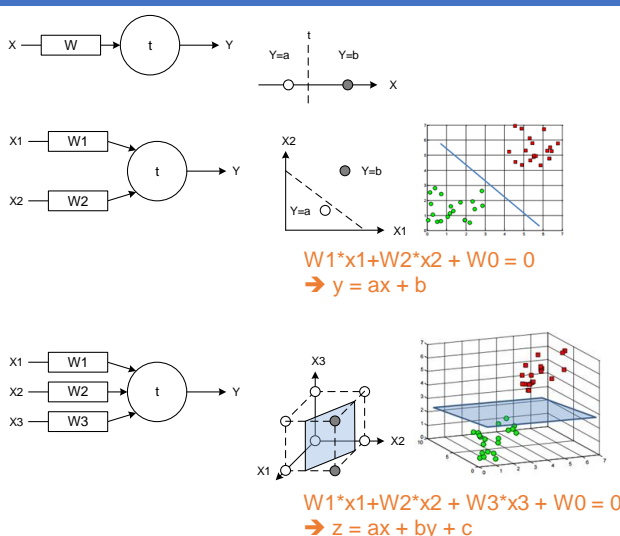


- ▶ Perceptron is a linear classifier.
  - ➔ Cannot deal with non-linear cases
- ▶ Perceptron refers to a particular supervised learning model with backpropagation learning algorithm.
- ▶ Perceptron is an algorithm for supervised learning of binary classifiers.



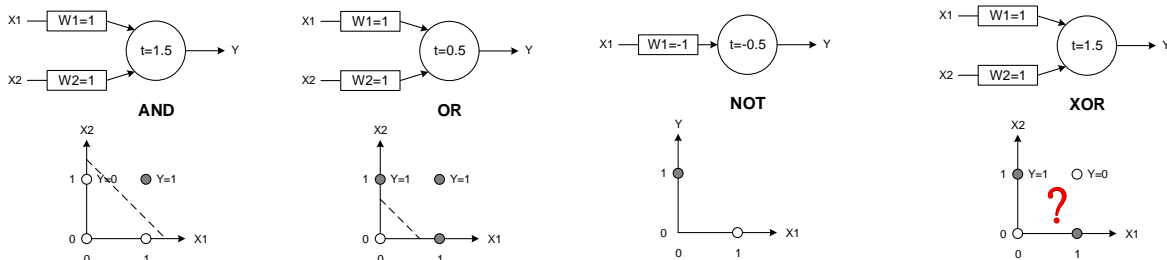
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## How perceptron classifies hyperplane



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# Perceptron: Boolean



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## Perceptron: Boolean AND training

- Step 1: initialize the weight and the threshold.
    - Weights may be initialized to 0 or to a small random value.
  - Step 2: repeat until error is less than a specific value
    - Calculate output (for j-th test set)
 
$$y_j(t) = f[\mathbf{w}(t) \cdot \mathbf{x}_j] = f[w_0(t)x_{j,0} + w_1(t)x_{j,1} + w_2(t)x_{j,2} + \dots + w_n(t)x_{j,n}]$$
    - Update weights (for i-th path for j-th test set) ( $d_j$  is desired or expected value)
 
$$w_i(t+1) = w_i(t) + (d_j - y_j(t))x_{j,i}, \text{ for all features } 0 \leq i \leq n.$$
    - Calculate error
 
$$\frac{1}{s} \sum_{j=1}^s |d_j - y_j(t)|$$
- Training set [{inputs: expected}]
    - $T_0=\{0,0;0\}$ ,  $T_1=\{0,1;0\}$ ,  $T_2=\{1,0;0\}$ ,  $T_3=\{1,1;1\}$
  - for  $T_0$  and  $T_1$  and  $T_2$  (assume all weights are 0)
    - $y = 0 \times 0 + 0 \times 0 = 0$
    - $e = 0 - 0 = 0$  (no error)
    - No update since no error
  - for  $T_3$ 
    - $y = 1 \times 0 + 1 \times 0 = 0$
    - $e = 1 - 0 = 1$
    - $w_0 = 0 + (1 - 0) = 1$
    - $w_1 = 0 + (1 - 0) = 1$
  - After updating
    - for  $T_3$ ,  $T_2$ , and  $T_1$ 
      - $y = 1 \times 1 + 1 \times 1 = 2 \Rightarrow$  apply threshold = 1.5
        - $e = 1 - 1 = 0$
      - $y = 1 \times 1 + 1 \times 0 = 1 \Rightarrow$  apply threshold = 1.5
        - $e = 0 - 0 = 0$
      - $y = 1 \times 0 + 1 \times 1 = 1 \Rightarrow$  apply threshold = 1.5
        - $e = 0 - 0 = 0$
      - $y = 1 \times 0 + 1 \times 0 = 0 \Rightarrow$  apply threshold = 1.5
        - $e = 0 - 0 = 0$

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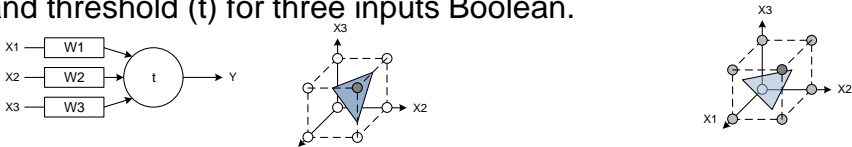
# Perceptron: Boolean OR training

- Training set [{inputs: expected}]
  - ▶ T0={0,0:0}, T1={0,1:1}, T2={1,0:1}, T3={1,1:1}
- for T0 (assume all weights are 0)
  - ▶  $y = 0 \times 0 + 0 \times 0 = 0$
  - ▶  $e = 0 - 0 = 0$  (no error)
  - ▶ No update since no error
- for T1
  - ▶  $y = 0 \times 0 + 0 \times 1 = 0$
  - ▶  $e = 1 - 1 = 1$
  - ▶  $w_0 = 0 + (1 - 1) = 1$
  - ▶  $w_1 = 0 + (1 - 1) = 1$
  - ▶ Update  $w_0$  and  $w_1$
- After updating
  - ▶ for T2
    - ⌚  $y = 1 \times 1 + 1 \times 0 = 1 \Rightarrow$  apply threshold = 1
    - ⌚  $e = 1 - 1 = 0$
  - ▶ No update since no error
- for T3
  - ▶  $y = 1 \times 1 + 1 \times 1 = 2 \Rightarrow$  apply threshold = 1
  - ▶  $e = 1 - 1 = 0$
  - ▶ No update since no error

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# Your project

- Find  $W$  and threshold ( $t$ ) for three inputs Boolean.


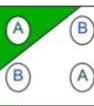

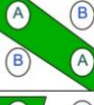

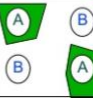


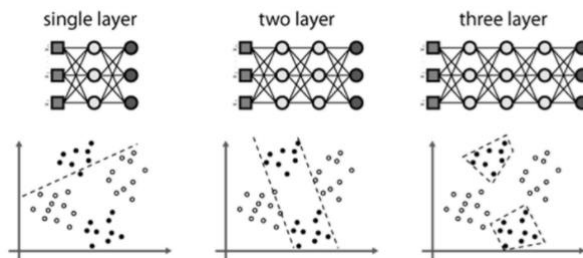
X1	X2	X3	Y=AND(X1,X2,X3)
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1

X1	X2	X3	Y=OR(X1,X2,X3)
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

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# MLP: Multi-layered perceptron (다층 퍼셉트론)

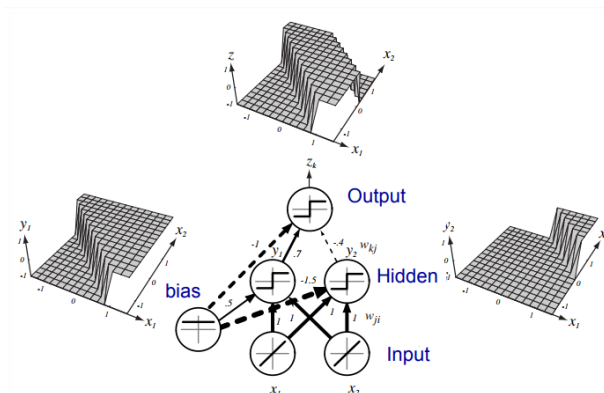
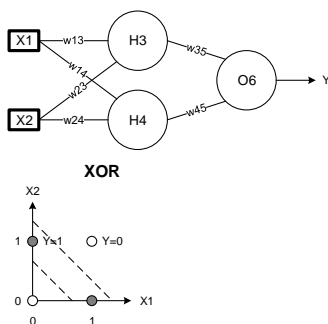
Structure	Types of Decision Regions	Exclusive-OR Problem
Single-Layer 	Half Plane Bounded By Hyperplane	
Two-Layer 	Convex Open Or Closed Regions	
Three-Layer 	Arbitrary (Complexity Limited by No. of Nodes)	



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## Multi-layered perceptron

### Two-unit network (two layers)



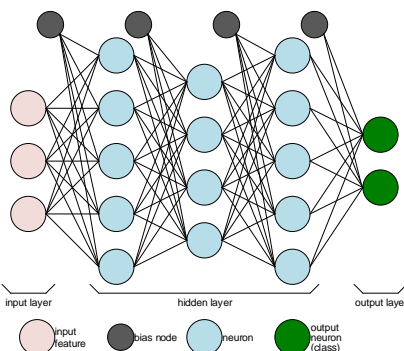
(from Pascal Vincent's slides)

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## Layer-wise organization

### 3 types of layers

- ▶ Input layer
- ▶ hidden layer
- ▶ output layer



fully-connected multi-layered neural network

- input layer: not counted for the number of layers
- hidden layer
- output layer

### For the picture on the left

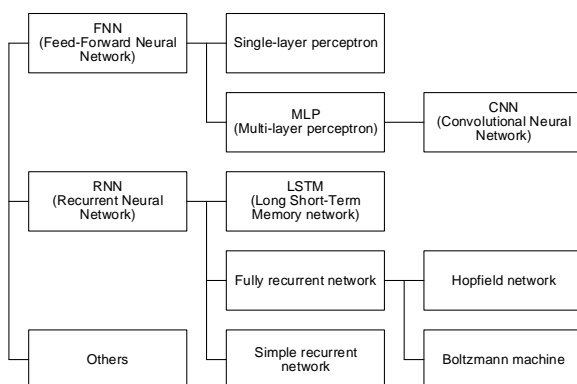
- ▶ assume fully connected
- ▶ 4-layered including 3-hidden layers
- ▶ 17 neurons:  $5+4+5+2$
- ▶ 65 weights:  $3 \times 5 + 5 \times 4 + 4 \times 5 + 5 \times 2$ 
  - not including bias
- ▶ 16 biases:  $5+4+5+2$
- ▶ 82 learnable parameters:  $65+16$

### Modern neural network

- ▶ 10~20 layers, ~100 million parameters
- ▶ How about 125 layers?

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## Categories of ANN (Artificial Neural network)



### Fully-Connected NN

- ▶ feed forward
- ▶ Multi-Layer Perceptron (MLP)

### Convolutional NN (CNN)

- ▶ feed forward, sparsely-connected
- ▶ Image recognition
- ▶ AlphaGo

### Recurrent NN (RNN)

- ▶ feedback

### Long Short-Term Memory (LSTM)

- ▶ feedback + storage
- ▶ Microsoft speech recognition
- ▶ Google neural machine translation (GNMT)

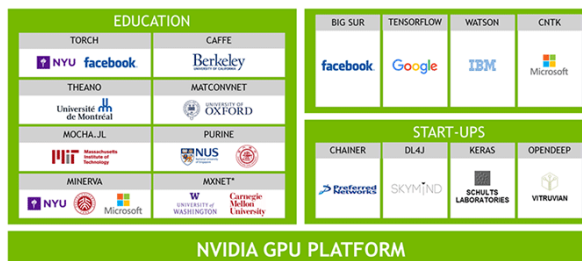
See neural network topology: <http://www.asimovinstitute.org/neural-network-zoo/>

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## Popular Frameworks

### ■ Popular Frameworks with supported interfaces

- ▶ Caffe
  - Berkeley / BVLC (Berkeley Artificial Intelligence Research)
  - C, C++, Python, Matlab
- ▶ TensorFlow
  - Google Brain
  - C++, Python
- ▶ PyTorch
- ▶ theano
  - U. Montreal
  - Python
- ▶ torch
  - Facebook / NYU
  - C, C++, Lua
- ▶ CNTK
  - Microsoft
- ▶ MXNet
  - Carnegie Mellon University / DMLC (Distributed Machine Learning Community)



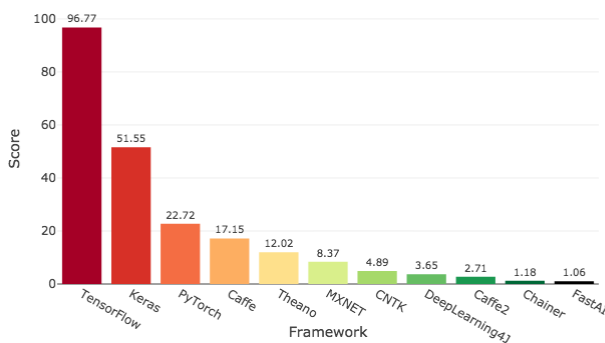
<https://blogs.nvidia.com/blog/2016/01/12/accelerating-ai-artificial-intelligence-gpus/>

<https://developer.nvidia.com/deep-learning-frameworks>

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## Popularity

Deep Learning Framework Power Scores 2018



<https://towardsdatascience.com/deep-learning-framework-power-scores-2018-23607ddf297a>

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