

$$\underbrace{(x^2 + 4x + 3) \cdot (x^2 - 9)}_{E(x)} < 0 \quad (1)$$

$$x^2 + 4x + 3 = x^2 + 3x + x + 3 = \overbrace{x(x+3)} + \overbrace{(x+3) \cdot 1} = (x+3)(x+1)$$

$$x^2 + 4x + 3 = 0 \Leftrightarrow x+3=0 \text{ SAU } x+1=0$$

$$x = -3 \qquad x = -1$$

$$x^2 - 9 = 0 \Leftrightarrow x^2 - 3^2 = 0 \Leftrightarrow (x-3)(x+3) = 0$$

$$\Rightarrow x = 3 \text{ SAU } x = -3$$

$$(1) \Leftrightarrow \underbrace{(x+3)} \cdot (x+1) \cdot \underbrace{(x-3)} \cdot (x+3) < 0 \Leftrightarrow$$

$$(x+3)^2 \cdot (x+1)(x-3) < 0$$

x	$-\infty$	-3	-1	0	3	$+\infty$
$(x+3)^2$	+	+	+	0	+	+
$x+1$	-	-	-	0	+	+
$x-3$	-	-	-	-	0	+
$E(x)$	+	+	+	0	-	+

$$S = (-1; 3)$$

$m \in \mathbb{R}$ - parameter -

$$m \cdot x - 3 \geq x + 1, \quad 2 \in S \Rightarrow m = ?$$

$$2 \in S \Rightarrow m \cdot 2 - 3 \geq 2 + 1 \Leftrightarrow 2m \geq 3 + 3 \Leftrightarrow \\ 2m \geq 6 \Leftrightarrow m \geq \frac{6}{2} \Leftrightarrow m \geq 3$$

$$\Rightarrow m \in [3, +\infty)$$

PROBĂ : $m = 5 \Rightarrow 5x - 3 \geq x + 1 \quad | -1$
 $4x \geq 4 \Leftrightarrow x \geq 1 \Rightarrow$
 $S = [1, +\infty), 2 \in S (A)$

$$x \cdot m - 6 \geq x + 1, \quad -1 \in S \Rightarrow m = ?$$

$$-1 \in S \Rightarrow (-1) \cdot m - 6 \geq -1 + 1 \Leftrightarrow \\ -m \geq 6 \quad | \cdot (-1) \Rightarrow m \leq -6$$

Răspuns: $m \in (-\infty, -6]$

$$m \cdot (x - 3) + x < x + 5, \quad \underline{\underline{3 \in S}} \Rightarrow m$$

$$3 \in S \Rightarrow m \cdot (3 - 3) + 3 < 3 + 5 \Leftrightarrow \\ m \cdot 0 < 5 \Rightarrow m \in \mathbb{R}$$

$$\begin{array}{l}
 \text{R} \vec{a} \rightarrow \text{purs} : m \in \mathbb{R} \\
 \text{P} \vec{a} \rightarrow \vec{a} : m = -1
 \end{array}
 \left\{ \begin{array}{l}
 (-1) \cdot (x - 3) + x < x + 5 \Leftrightarrow \\
 -\cancel{x} + 3 + \cancel{x} < x + 5 \Leftrightarrow \\
 3 - 5 < x \Leftrightarrow x > -2
 \end{array} \right.$$

$$S = (-2, +\infty), \quad 3 \in (-2, +\infty) \quad (A)$$

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