

## Decomponere in factori - 2 -

$$\begin{aligned}
 & 2x^{m+3} \cdot y^{m-2} - 8x^{m-4} \cdot y^{m+2} + 12x^m \cdot y^{m-5} = \\
 & = 4 \cdot x^{m-4} \cdot y^{m-5} \cdot 6 \cdot x^7 \cdot y^3 - 4 \cdot x^{m-4} \cdot y^{m-5} \cdot y^7 \cdot 2 + 4 \cdot 3 \cdot x^{m-4} \cdot y^{m-5} \cdot x^4 = \\
 & = 4x^{m-4} \cdot y^{m-5} \cdot (6x^7 \cdot y^3 - 2y^7 + 3 \cdot x^4)
 \end{aligned}$$

$$\begin{aligned}
 & x^{m+3} \cdot y^{m-4} - x^{m-3} \cdot y^{m+5} - x^{m-1} \cdot y^{m-2} = \\
 & = x^{m-3} \cdot y^{m-4} \cdot x^6 - x^{m-3} \cdot y^{m-4} \cdot y^9 - x^{m-3} \cdot y^{m-4} \cdot x^2 \cdot y^2 = \\
 & = x^{m-3} \cdot y^{m-4} \cdot (x^6 - y^9 - x^2 y^2) \quad \left. \begin{array}{l} a^2 + 2ab + b^2 = (a+b)^2 \\ (a+b)(a-b) = a^2 - b^2 \end{array} \right\}
 \end{aligned}$$

$$\begin{aligned}
 & -2\sqrt{75}x^4 + 3\sqrt{27}x^5 - 2\sqrt{243}x^2 = \\
 & = -25\sqrt{3}x^4 + 3 \cdot 3\sqrt{3}x^5 - 2 \cdot 3\sqrt{3}x^2 = \sqrt{3}x^2 \cdot (9x^3 - 10x^2 - 18)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 6x + y^2 + 4y + 13 = x^2 - 2 \cdot 3x + 3^2 + y^2 + 2 \cdot 2y + 2^2 = \\
 & = (x-3)^2 + (y+2)^2 \quad \xrightarrow{\text{nu se decompune in } \mathbb{R}}
 \end{aligned}$$

$$\begin{aligned}
 & x^2 + 10x - y^2 - 8y + 9 = x^2 + 2 \cdot 5x + 5^2 - y^2 - 2 \cdot 4y - 4^2 = \\
 & = (x+5)^2 - 1 \cdot (y^2 + 2 \cdot 4y + 4^2) = (x+5)^2 - (y+4)^2 = \\
 & = [(x+5) + (y+4)] \cdot [(x+5) - (y+4)] = \\
 & = (x+y+9) \cdot (x-y+1)
 \end{aligned}$$

$$\begin{aligned}
 & x^2 - 6x - y^2 - 4y + 5 = x^2 - 2 \cdot 3x + 3^2 - y^2 - 2 \cdot 2y - 2^2 = \\
 & = (x-3)^2 - (y+2)^2 = (x-3+y+2)(x-3-y-2) = (x+y-1)(x-y-5)
 \end{aligned}$$

$$x^2 + 7x + 12 = \underbrace{x^2 + 4x}_{x} + \underbrace{3x + 12}_{+3} = x(x+4) + 3(x+4) = (x+4)(x+3)$$

$$x^2 - ax + bx - b \cdot a = x(x-a) + b(x-a) = (x-a)(x+b)$$

$$x^2 - x - 42 = x^2 + 6x - 7x - 42 = x(x+6) - 7(x+6) = (x+6)(x-7)$$

$$x^2 - x + \frac{1}{4} = x^2 - 2x \cdot \frac{1}{2} + \left(\frac{1}{2}\right)^2 = \left(x - \frac{1}{2}\right)^2$$

$$9x^2 - 3xy + \frac{y^2}{4} = \underbrace{(3x)}_{\sim}^2 - 2 \cdot 3x \cdot \frac{y}{2} + \underbrace{\left(\frac{y}{2}\right)^2}_{\sim} = \left(3x - \frac{y}{2}\right)^2$$

$$x^2 + x + 2 = ? \quad x^2 + x + 2 = \underbrace{1 \cdot x^2}_{a} + \underbrace{1 \cdot x}_{b} + \underbrace{2}_{c}$$

$$a=1 \quad b=1 \quad c=2 \quad \Delta = b^2 - 4ac = 1^2 - 4 \cdot 1 \cdot 2 = 1 - 8 = -7$$

$\Delta < 0 \Rightarrow x^2 + x + 2$  non se descompone in R

$$\textcircled{V1} \quad 1. x^2 + 9x + 14 = ? \quad a=1 \quad b=9 \quad c=14$$

$$\Delta = b^2 - 4ac = 9^2 - 4 \cdot 1 \cdot 14 = 81 - 56 = 25 \quad \sqrt{\Delta} = 5$$

$$x_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a} = \begin{cases} \frac{-9+5}{2 \cdot 1} = -2 \\ \frac{-9-5}{2 \cdot 1} = -7 \end{cases} \Rightarrow ax^2 + bx + c = a(x-x_1)(x-x_2)$$

$$x^2 + 9x + 14 = (x-(-2))(x-(-7)) = \underline{\underline{(x+2)(x+7)}}$$

$$\textcircled{V2} \quad x^2 + 9x + 14 = x^2 + 2x + 7x + 14 = x(x+2) + 7(x+2) = \underline{\underline{(x+2)(x+7)}}$$

$$\textcircled{V1} \quad x^2 - x - 20 = ? \quad 1 \cdot x^2 + (-1) \cdot x + (-20) = ?$$

$$a=1 \quad b=-1 \quad c=-20$$

$$\Delta = b^2 - 4ac = (-1)^2 - 4 \cdot 1 \cdot (-20) = 1 + 80 = 81 \Rightarrow \sqrt{\Delta} = \sqrt{81} = 9$$

$$x_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a} = \begin{cases} \frac{-(-1)+9}{2 \cdot 1} = 5 \\ \frac{-(-1)-9}{2 \cdot 1} = -4 \end{cases} \quad \left\{ \begin{array}{l} x^2 - x - 20 = (x-5)(x-(-4)) = \\ = (x-5)(x+4) \end{array} \right.$$

$$\textcircled{V2} \quad x^2 - x - 20 = x^2 - 5x + 4x - 20 = x(x-5) + 4(x-5) = \underline{\underline{(x-5)(x+4)}}$$

$$2x^2 - x - 3 = ? \quad \left\{ \begin{array}{l} \Delta = b^2 - 4ac = (-1)^2 - 4 \cdot 2 \cdot (-3) = 25 \quad \sqrt{\Delta} = \sqrt{25} = 5 \\ a=2 \quad b=-1 \quad c=-3 \end{array} \right. \quad x_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a} = \begin{cases} \frac{1+5}{4} = \frac{3}{2} \\ \frac{1-5}{4} = -1 \end{cases}$$

$$\underline{2x^2 - x - 3 = 2 \cdot (x - (-1)) \cdot (x - \frac{3}{2}) = (x+1) \cdot (2x - 2 \cdot \frac{3}{2}) = (x+1)(2x-3)}$$

$$3x^2 + 2\sqrt{3}x + 1 = (\sqrt{3}x)^2 + 2 \cdot \sqrt{3} \cdot x \cdot 1 + 1^2 = (\sqrt{3}x + 1)^2$$

$$2x^2 + 2\sqrt{2}x + 3 = (\sqrt{2}x)^2 + 2 \cdot \sqrt{2} \cdot \sqrt{2}x + (\sqrt{3})^2 = (\sqrt{2}x + \sqrt{3})^2$$

$$5x^2 + \sqrt{5} = \sqrt{5} \cdot \sqrt{5} \cdot x^2 + \sqrt{5} \cdot 1 = \sqrt{5} (5x^2 + 1)$$

$$x^4 + 5x^2 + 6 = \underbrace{x^4 + 3x^2}_{x^2(x^2+3)} + \underbrace{2x^2 + 6}_{2 \cdot (x^2+3)} = x^2(x^2+3) + 2 \cdot (x^2+3) = (x^2+3)(x^2+2)$$

$$x^4 - 5x^2 + 4 = x^4 - x^2 - 4x^2 + 4 = x^2 \cdot (x^2 - 1) - 4(x^2 - 1) = \\ = (x^2 - 1) \cdot (x^2 - 4) = (x^2 - 1^2) \cdot (x^2 - 2^2) = (x-1)(x+1)(x-2)(x+2)$$

$$x^4 + x^2 + 1 = \underbrace{x^4 + 2x^2 \cdot 1 + 1 - x^2}_{(x^2+1)^2 - x^2} = \left\{ \begin{array}{l} 3x^4 + x^2 - 4 = ? \\ x^2 = t \Rightarrow x^4 = t^2 \\ 3t^2 - t - 4 = ? \end{array} \right. \\ = (x^2 + 1 - x)(x^2 + 1 + x) = \left\{ \begin{array}{l} \Delta = b^2 - 4ac = 1 - 4 \cdot 3 \cdot (-4) = 49 \Rightarrow \sqrt{\Delta} = 7 \\ t_{1,2} = \frac{-b \pm \sqrt{\Delta}}{2a} = \frac{1 \pm 7}{6} = \begin{cases} 1 \\ -\frac{4}{3} \end{cases} \end{array} \right.$$

$$3t^2 + t - 4 = 3 \cdot \left(t - 1\right) \cdot \left(t + \frac{4}{3}\right) = (t-1) \cdot (3t + 4) =$$

$$= \underbrace{(t-1) \cdot (3t+4)}_{3x^4 + x^2 - 4} =$$

$$3x^4 + x^2 - 4 = (x^2 - 1) (3x^2 + 4) = (x-1)(x+1) (\underbrace{3x^2 + 4}_{3x^2 + 4})$$