

6. Stabilește valoarea de adevăr a următoarelor enunțuri:

a) $2 \in \{x \mid x \in \mathbb{N}, 3 \cdot x = 1\}$; b) $3 \in \{x \mid x = 2n, n \in \mathbb{N}\}$; c) $0 \notin \{x \mid x \in \mathbb{N}, x^2 \leq 4\}$.

7. Reprezintă fiecare mulțime prin enumerarea elementelor sale:

$A = \{x \mid x \in \mathbb{N}, x < 7\}$, $B = \{x \mid x \in \mathbb{N}, 3 \leq x < 8\}$, $C = \{x \mid x \in \mathbb{N}, 7 \mid x\}$,

$D = \{x \mid x \in \mathbb{N}, x + 3 = 4\}$, $E = \{x \mid x \in \mathbb{N}^*, x - 1 \leq 2\}$.

(6a)

$$A = \{x \mid x = 3k - 1, k \in \mathbb{N}^*\}$$

$\mathbb{N} = \{0, 1, 2, 3, \dots\} \Rightarrow$ mult. m. naturale

$\mathbb{N}^* = \{1, 2, 3, \dots\} \Rightarrow$ mult. m. naturale nenule

$$A = \{2, 5, 8, 11, 14, 17, 20, \dots\} \Rightarrow 2 \in A \text{ (A)}$$

(6b) $B = \{x \mid x = 2m, m \in \mathbb{N}\} = \{0, 2, 4, 6, 8, 10, \dots\} \Rightarrow 3 \in B \text{ (F)}$

(6c) $C = \{x \mid x \in \mathbb{N}, x^2 \leq 4\} = \{0, 1, 2\}$, deoarece:

$$\mathbb{N} = \{0, 1, 2, 3, 4, 5, \dots\} \quad \begin{array}{l} x=0 \Rightarrow x^2 = 0, 0 \leq 4 \\ x=1 \Rightarrow x^2 = 1, 1 \leq 4 \end{array} \quad \begin{array}{l} x=2 \Rightarrow x^2 = 4, 4 \leq 4 \\ x=3 \Rightarrow x^2 = 9, 9 \leq 4 \end{array} \quad (\text{FALSE})$$

$0 \notin C \text{ (F)}$

$B = \{x \mid x \in \mathbb{N}, 3 \leq x < 8\}$,

$$\Rightarrow B = \{3, 4, 5, 6, 7\}$$

$E = \{x \mid x \in \mathbb{N}^*, x - 1 \leq 2\}$

$$x - 1 \leq 2 \Leftrightarrow x \leq 2 + 1 \Leftrightarrow x \leq 3$$

$$E = \{1, 2, 3\}$$

$C = \{x \mid x \in \mathbb{N}, 7 \mid x\} \Rightarrow C = \{1, 7\} = D_7$

$\forall x: x \rightarrow x \mid 7 \Rightarrow x \in D_7 \quad \begin{array}{l} 7 \mid 0, 7 \cdot 0 = 0 \\ 7 \mid 7, 7 \cdot 1 = 7 \end{array}$

$P = \{x \mid x \in \mathbb{N}, 7 \mid x\} = \{0, 7, 14, 21, 28, 35, 42, \dots\} = \mathbb{N}_7$