

6. Stabilește valoarea de adevăr a următoarelor enunțuri:

a)  $2 \in \{x \mid x \in \mathbb{N}, 3 \cdot x - 1\}$ ;

b)  $3 \in \{x \mid x = 2n, n \in \mathbb{N}\}$ ;

c)  $0 \notin \{x \mid x \in \mathbb{N}, x^2 \leq 4\}$ .

7. Reprezintă fiecare mulțime prin enumerarea elementelor sale:

$A = \{x \mid x \in \mathbb{N}, x < 7\}$ ,

$B = \{x \mid x \in \mathbb{N}, 3 \leq x < 8\}$ ,

$C = \{x \mid x \in \mathbb{N}, 7 \mid x\}$ ,

$D = \{x \mid x \in \mathbb{N}, x + 3 = 4\}$ ,

$E = \{x \mid x \in \mathbb{N}^*, x - 1 \leq 2\}$ .

6a

$A = \{x \mid x = 3k - 1, k \in \mathbb{N}^*\}$

$\mathbb{N} = \{0, 1, 2, 3, \dots\} \Rightarrow$  mulț. m. naturale

$\mathbb{N}^* = \{1, 2, 3, \dots\} \Rightarrow$  mulț. m. naturale nenule

$$\left\{ \begin{array}{l} 3 \cdot 1 - 1 = 2 \\ 3 \cdot 2 - 1 = 5 \\ 3 \cdot 3 - 1 = 8 \end{array} \right. \Rightarrow$$

$A = \{2, 5, 8, 11, 14, 17, 20, \dots\} \Rightarrow 2 \in A$  (A)

6b)  $B = \{x \mid x = 2m, m \in \mathbb{N}\} = \{0, 2, 4, 6, 8, 10, \dots\} \Rightarrow 3 \notin B$  (F)

6c)  $C = \{x \mid x \in \mathbb{N}, x^2 \leq 4\} = \{0, 1, 2\}$ , deoarece:

$\mathbb{N} = \{0, 1, 2, 3, 4, 5, \dots\}$   $x=0 \Rightarrow x^2=0, 0 \leq 4$   $x=2 \Rightarrow x^2=4, 4 \leq 4$   
 $x=1 \Rightarrow x^2=1, 1 \leq 4$   $x=3 \Rightarrow x^2=9, 9 \leq 4$  (FALS)

$0 \notin C$  (F)

$B = \{x \mid x \in \mathbb{N}, 3 \leq x < 8\}$ ,

$\Rightarrow B = \{3, 4, 5, 6, 7\}$

$E = \{x \mid x \in \mathbb{N}^*, x - 1 \leq 2\}$

$x - 1 \leq 2 \Leftrightarrow x \in 2 + 1 \Leftrightarrow x \in 3$

$E = \{1, 2, 3\}$

$C = \{x \mid x \in \mathbb{N}, 7 \mid x\} \Rightarrow C = \{1; 7\} = \mathbb{D}_7$

$7 \mid x \Rightarrow x \mid 7 \Rightarrow x \in \mathbb{D}_7$

$7 \mid 0, 7 \cdot 0 = 0$   $7 \mid 7, 7 \cdot 1 = 7$

$P = \{x \mid x \in \mathbb{N}, 7 \mid x\} = \{0, 7, 14, 21, 28, 35, 42, \dots\} = \mathbb{N}_7$

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