

DLD Assignment 1

(Q1) Convert $(1073)_{10}$ into a binary number.

$\begin{array}{r} 1073 \\ \hline 2 \end{array}$

$$\begin{array}{r} 536 \text{ } - 1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 268 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 134 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 67 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 33 \text{ } - 1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 16 \text{ } - 1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 8 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 4 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 2 \text{ } - 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 1 \text{ } - 0 \\ \hline \end{array}$$

$$(1073)_{10} \Rightarrow (10000110001)_2$$

(Q2) Convert $(81)_{10}$ to Binary :-

$\begin{array}{r} 81 \\ \hline 2 \end{array}$

$$\begin{array}{r} 40 \rightarrow 1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 20 \rightarrow 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 10 \rightarrow 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 5 \rightarrow 0 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 2 \rightarrow 1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 1 \text{ } - 0 \\ \hline \end{array}$$

$$(81)_{10} \Rightarrow (1010001)_2$$

Q3) Convert Decimal 27.315 to Binary

$$\begin{array}{r} 2 | 27 & \text{27.315} \\ 2 | 13 & 27.315 \rightarrow (1011.0101)_2 \\ 2 | 6 & \\ 2 | 3 & 0 \quad 0.315 \times 2 = 0.63 \times 2 = 1 \\ 1 - 1 & 0.26 \times 2 = 0.52 \times 2 = 0 \end{array}$$

a) a) $(1010)_2 + (1100)_2$

$$\begin{array}{r} 1010 \\ + 1100 \\ \hline 110110 \end{array}$$

b) $(101011)_2 + (110101)_2$

$$\begin{array}{r} 101011 \\ + 110101 \\ \hline 110000 \end{array}$$

Q5) a) $(101110)_2 - (100100)_2$

$$\begin{array}{r} 101110 \\ - 100100 \\ \hline 00110 \end{array}$$

b) $(1001100)_2 = (110)_2$

1001100

- 110

1000110

c) Convert Hexadecimal to octal

a) $(FA25)_{16}$

F A 2 5

11110100010 0101.

1875045.

$(FA25)_{16} \Rightarrow (175045)_8$

b) $(F920)_{16}$

F 9 2 0

1111100100000 0000.

174440.

$(F920)_{16} \Rightarrow (174440)_8$

c) $(1100)_{16}$

$$\begin{array}{r} 1 \ 1 \ 0 \ 0 \\ 0001 \ 0001 \ 0000 \ 0000 \\ \hline 010400 \end{array}$$

$$(1100)_{16} \Rightarrow (10400)_8$$

Q7) Convert octal to Hexadecimal:-

a) $(777)_8$

$$\begin{array}{r} 7 \ 7 \ 7 \\ 111 \ 111 \ 111 \\ \hline 1 \ F \ F \end{array}$$

$$(777)_8 \Rightarrow (1FF)_{16}.$$

b) $(123)_8$

$$\begin{array}{r} 1 \ 2 \ 3 \\ 001 \ 010 \ 011 \\ 0 \ 010 \ 0011 \\ \hline 0 \ 5 \ 3 \end{array}$$

$$(123)_8 \Rightarrow (53)_{16}$$

c) $(635)_8$

6 3 5
1 10 0 11 1 01,

1 10 01 11 01

1 4 D

$$(635)_8 \Rightarrow (19D)_{16}$$

Q8) Express each decimal number in binary as
8-bit sign-magnitude numbers.

a) -83

2 | 83
2 | 41 - 1 $(1010011) \Rightarrow 83$
2 | 20 - 1
2 | 10 - 0 $(11010011) \Rightarrow -83$
2 | 5 - 0
2 | 2 - 1
1 - 0

b) +101

2 | 101
2 | 50 - 1
2 | 25 - 0 $(1100101) \Rightarrow 101$
2 | 12 - 1
2 | 6 - 0 $(01100101) \Rightarrow +101$
2 | 3 - 0
1 - 1

c) -114

$$\begin{array}{r} 2 | 114 \\ 2 | 57 \rightarrow 0 & (111.0010)_2 \Rightarrow -114 \\ 2 | 28 \rightarrow 1 \\ 2 | 14 \rightarrow 0 & (11110010)_2 \Rightarrow -114 \\ 2 | 7 \rightarrow 0 \\ 2 | 3 \rightarrow 1 \\ 1 \rightarrow 1 \end{array}$$

Q9) Express each decimal as an 8 bit number in the 2's complement form.

a) -66

$$\begin{array}{r} 2 | 66 \\ 2 | 33 \rightarrow 0 & (01000010)_2 \Rightarrow 66 \\ 2 | 16 \rightarrow 1 & \Downarrow \text{1st complement} \\ 2 | 8 \rightarrow 0 & (10111101)_2 \Rightarrow -66 \\ 2 | 4 \rightarrow 0 \\ 2 | 2 \rightarrow 0 \\ 1 \rightarrow 0 \end{array}$$

b) + 102

2 | 102

$$2 \Big| 51 - 0$$

$$(1100110) \Rightarrow 102$$

$$2 \Big| 25 - 1$$

$$(01100110) \Rightarrow 102$$

$$2 \Big| 12 - 1$$

$$2 \Big| 6 - 0$$

$$2 \Big| 3 - 0$$

$$1 - 1$$

c) - 94

2 | 94

$$2 \Big| 49 - 1$$

$$(1100011) \Rightarrow -94$$

$$2 \Big| 24 - 1$$

$$2 \Big| 12 - 0$$

$$(10011100) \Rightarrow -94$$

$$2 \Big| 6 - 0$$

$$2 \Big| 3 - 0$$

$$1 - \cancel{0}1$$

Q10) Express each decimal as an 8-bit number in 2's complement form.

a) -59

$$\begin{array}{r} 2 \mid 59 \\ 2 \mid 29 - 1 \quad (111011) \Rightarrow 59 \\ 2 \mid 14 - 1 \\ 2 \mid 7 - 0 \quad 1000100 \\ 2 \mid 3 - 1 \quad +1 \\ 1 - 1 \quad (1000101) \Rightarrow -59 \end{array}$$

b) +102

$$\begin{array}{r} 2 \mid 102 \\ 2 \mid 51 - 0 \quad (01100110)_2 \Rightarrow 102 \\ 2 \mid 25 - 1 \\ 2 \mid 12 - 1 \\ 2 \mid 6 - 0 \\ 2 \mid 3 - 0 \\ 1 - 1 \end{array}$$

c) -126

2 + 126

$$\begin{array}{r} 2 \\ | \\ 63 = 0 \end{array}$$

$$\begin{array}{r} 2 \\ | \\ 31 = 1 \end{array}$$

$$\begin{array}{r} 2 \\ | \\ 15 = 1 \end{array}$$

$$\begin{array}{r} 2 \\ | \\ 7 = 1 \end{array}$$

$$\begin{array}{r} 2 \\ | \\ 3 = 1 \end{array}$$

$$\begin{array}{r} 1 \\ | \\ 1 \end{array}$$

$$(0|111110) \rightarrow 126$$

10000001

$$\overline{(10000010)} \rightarrow 126$$

a) Determine decimal value of each signed binary number in the sign-magnitude form.

a) 10011101

10011101

$$-(16+8+4+1) = \boxed{-29} \text{ ans.}$$

b) 01110100

01110100

$$+ 64+32+16+4 \Rightarrow \boxed{+116} \text{ ans.}$$

c) 10111011

10111011

$$- 32+16+8+2+1 = \boxed{-59}.$$

Q12) Determine the decimal value of each signed binary number in the 1's complement form.

a) 10111001

~~128 64 32 16 8 4 2 1~~
10111001

$$-128 + 32 + 16 + 8 + 4 + 1 \Rightarrow -71 + 1$$

$$\Rightarrow \boxed{-70} \text{ ans.}$$

b). 01100100

~~64 32 16 8 4 2 1~~
01100100

$$64 + 32 + 4 \Rightarrow \boxed{100} \text{ ans.}$$

c) 10111101

~~128 64 32 16 8 4 2 1~~
10111101

$$-128 + 32 + 16 + 8 + 4 + 1 \Rightarrow -68 + 1$$

$$\Rightarrow \boxed{-67}$$

$$\boxed{-66} \text{ ans.}$$

Q13) A system uses 8 bit two's complement representation for signed numbers. What is the decimal equivalent of the following binary number?

d) 10101100

~~128 64 32 16 8 4 2 1~~
10101100

$$-128 + 32 + 8 + 4 + 1 \Rightarrow \boxed{-69} \text{ ans.}$$

b) $\begin{array}{r} 0111001 \\ \text{---} \\ 64+32+16+8+1 \\ 0111001 \end{array}$

$$64+32+16+8+1 \Rightarrow [121]_{\text{ans.}}$$

c) $\begin{array}{r} 1110000 \\ \text{---} \\ 11110000 \\ 11110000 \end{array}$

$$-128+64+32+16 \Rightarrow [-16]_{\text{ans.}}$$

Q15) What is Binary Coded Decimal, and how does it differ from Regular Binary representation?

Ans) In BCD each decimal digit (0-9) is represented by its own group of binary bits, typically using 4 bits per digit. This means that the decimal number is broken up into its individual digits, and each digit is then converted to its 4-bit binary equivalent.

For example, number 45 in BCD would be written as 0100 0101 whereas in regular binary the number 45 would be written as 101101. BCD makes reading of binary numbers easier for humans.

Q16) Analyze your surroundings and think of applications of BCD where it is being used?

→ Digital clocks

→ watches

→ calculators

→ Embedded Systems.

a) Convert decimal to BCD

i) 57

⇒ 01010111

b) 109

⇒ 000100001001

Q18) Add the numbers after conversion to BCD.

i) $7 + 9$

$\begin{array}{r} 1 \\ 1 \\ 1 \\ 1 \end{array}$

$\underline{+ 1001}$

$1\ 0\ 0\ 0\ 0$

$\underline{+ 0110}$

2001 0110

1 6

0001 0110

⇒ ans.

b) $25 + 58$

$$\begin{array}{r} 0010 \quad 0101 \\ + 0101 \quad 1000 \\ \hline 0111 \quad 1101 \\ + 0110 \quad \quad \quad (1000 \text{ } 0011) \\ \hline 1000 \quad 0011 \\ \hline 8 \quad \quad \quad 3 \end{array}$$

c) $76 + 84$

$$\begin{array}{r} 0111 \quad 0110 \\ + 1000 \quad 0100 \\ \hline 111111 \quad 11010 \\ + 0110 \quad \quad \quad (10110 \text{ } 0000) \\ \hline 10000 \text{ } 0000 \\ + 0110 \quad \quad \quad \text{or.} \\ \hline 1.0110 \text{, } 0000 \\ \hline 1 \quad 6 \quad 0 \end{array}$$

d) $89 + 68$

$$\begin{array}{r} 1001 \quad 1001 \\ 0110 \quad 1000 \\ \hline 11111 \quad 0001 \quad (10101 \text{ } 0111) \\ + 0110 \quad 110 \\ \hline 10101 \text{, } 0001 \\ \hline 1 \quad 5 \quad 7 \end{array}$$

Q9) a) 110011001

5 ones; the even parity code is in error.

b) 1011111010001010

10 ones; the even parity code is not in error.

c) 010101110

5 ones; the even parity code is in error.

d) 0111000100101101

8 ones; the even parity code is not in error.

Q10) a) 0110

2 ones; need 1 more for odd

= 10110

b) 101101

4 ones; need 1 more for odd

= 1101101

c) 010101110

5 ones; the even parity code is in error.

d) 0111000100101101

8 ones; the even parity code not in error.

Q14) a) -38 and -27

2 | 38

2 | 19 - 0

2 | 4 - 1

2 | 4 - 1

2 | 2 - 0

1 - 0

00100110 $\xrightarrow{1's}$ 11011001

2 | 27

2 | 13 - 1

2 | 6 - 1

2 | 3 - 0

1 - 1

00011011 $\xrightarrow{1's}$

+1

11011010

11100100

+1

11100101

11011010

+11100101

X 10111111 \Rightarrow -65 \Rightarrow ans.

$\Rightarrow -102$ and -85

$$\begin{array}{r} 2 \\ \hline 102 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 51.0 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 25.1 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 12.1 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 6.0 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 3.0 \end{array}$$

$$\begin{array}{r} 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 85 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 42.1 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 21.0 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 10.1 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 5.0 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 2.1 \end{array}$$

$$\begin{array}{r} 1 \\ \hline 0 \end{array}$$

$$01100110 \rightarrow 10011001$$

$$\begin{array}{r} +1 \\ \hline 10011010 \end{array}$$

$$1010101 \rightarrow 1010101$$

$$\begin{array}{r} +1 \\ \hline 1010101 \end{array}$$

$$110011010$$

$$+1010101$$

$$\cancel{\times 01000101} \Rightarrow \text{overflow}$$

c) -58 and 65

2	58
2	29 0
2	14 1
2	7 0
2	3 1
	1 1

2	65
2	32 1
2	16 0
2	8 0
2	4 0
2	2 0
	1 0

$$00111010 \rightarrow 11000101$$

$$0100000\cancel{0} \xrightarrow{+1}$$

$$\underline{+1}$$

$$11000110$$

$$\begin{array}{r} 11000110 \\ +01000005 \\ \hline \end{array}$$

$$X000001101 \Rightarrow 77 \text{ ans}$$

b) 59 and -39

$$\begin{array}{r} 2 | 59 \\ 2 | 29 \quad 1 \\ 2 | 19 \quad 1 \\ 2 | 7 \quad 0 \\ 2 | 3 \quad 1 \\ \hline 1-1 \end{array}$$

00111011

$$\begin{array}{r} 2 | 39 \\ 2 | 19 \quad 1 \\ 2 | 9 \quad 1 \\ 2 | 4 \quad 1 \\ 2 | 2 \quad 0 \\ \hline 1-0 \end{array}$$

00100111 \rightarrow 11011000

$$\begin{array}{r} 111111 \\ 100111011 \\ + 11011001 \\ \hline \times 00010100 \end{array}$$

= 20 \Rightarrow ans

11011001