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If P = Principal, R = Rate of interest, N = Time in years, I = Interest, A = Amount Then A = P + I

Simple Interest

$$S.I. = (P \times R \times N) / 100$$

Basic principal remains constant.

S.I. is good example of AP(Arithmetic Progression)

Compound Interest

$$A = P (1 + R/100)^T$$

C.I. = A - P

T = periods of compounding,

R = rate for compounding period

Basic principal keeps on increasing as we get interest on interest.

C.I. is good example of GP(Geometric Progression)



Q. A shopkeeper with an OD facility at 18% with a bank borrowed Rs. 15000 on Jan 8, 2011 and returned the money on June 3, 2011 so as to clear the debt. The amount that he paid was -

A. Rs. 16080

B. Rs. 16280

C. Rs. 16400

D. None of these

Soln:

- P = 15000, r= 18%,
- T = 23(jan) + 28(febNonleap) + 31(march) + 30(April) + 31(may) + 3(june) = 146 days
- 146/365 days = 2/5 years.
- $SI = 15000 \times 18 \times 2/5 \times 1/100 = 30 \times 18 \times 2 = 1080$

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Amount = P + SI
=15000+1080
=Rs. 16080
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Q. A sum of money at simple interest amounts to Rs. 815 in 3 years and to Rs. 854 in 4 years. The sum is:

A. Rs. 650

B. Rs. 690

C. Rs. 698

D. Rs. 700

Soln:-

amount after 4 years = amount after 3 years + simple interest in one year

S.I. in one year = Rs. (854 - 815) = Rs. 39.

S.I. for 3 years = $Rs.(39 \times 3) = Rs. 117$.

Principal = amount - interest

Principal = 815 - 117 = Rs. 698.



Q. A farmer borrowed Rs.3600 at 15% simple interest per annum. At the end of 4 years, he cleared this account by paying Rs.4000 and a donkey. The cost of the donkey is -

A. Rs. 1000

B. Rs. 1200

C. Rs. 1550

D. Rs. 1760

Soln:

SI for 4 years = $Rs.(3600 \times 0.15 \times 4) = Rs.2160$

Amount after 4 years = Rs. (3600+2160) = Rs. 5760

Cost of donkey = Rs. (5760-4000) = Rs. 1760

Ans: D



Q. P =Rs. 2000, R =10%, N =2yrs, Find A and CI

Soln:

A =
$$2000(1 + \frac{10}{100})^2$$

= $2000(\frac{110}{100})^2$
= $2000(\frac{121}{100})$
= Rs. 2420
CI = $2420 - 2000$ = Rs. 420

2000 → 10% = 200
10% 10%
2000 → 2200 → 2420

$$CI = 2420 - 2000 = 420$$



Q. Simple interest on a certain sum of money for 3 years at 8% per annum is half the compound interest on Rs. 4000 for 2 years at 10% per annum. The sum placed on simple interest is:

A. Rs. 1550

B. Rs. 1650

C. Rs. 1750 D. Rs. 2000

Soln:

A = P(1+R/100)^N = 4000(1+
$$\frac{10}{100}$$
)² = 4000 x ($\frac{11}{10}$)² = 4000 x $\frac{11}{10}$ x $\frac{11}{10}$ = Rs. 4840

<u>OR</u>

$$CI = A - P$$

$$CI = 4840 - 4000 = Rs. 840$$

$$SI = \frac{1}{2} CI$$

$$\frac{PNR}{100} = \frac{1}{2} \times 840$$

$$\frac{P \times 3 \times 8}{100} = 420$$

P(sum) =
$$\frac{420 \times 100}{3 \times 8}$$

= Rs. 1750



Q. P =Rs. 4000, R =20% per annum, N =6months.Find CI computed quarterly for given period.

Soln:

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N =6months(2 quarterly)
rate(R) = 20 % per annum = 5 % quarterly
After every 3 months CI will be calculated.
by 5\%=200 by 5\%=210
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4000 4200

4410

I = 4410 -4000

= Rs. 410



Q. Difference between Compound interest & simple interest on a sum placed at 8% p.a. compounded annually for 2 years is Rs 128. Find the Principal

• A.20000

B. 24000

C. 26000

D. 15000

- Soln:
- Let the principal be P = Rs. 100.
- time N = 2 years, rate of interest R = 8% per annum
- simple interest = $PNR/100 = \frac{100 * 8 * 2}{100} = Rs. 16$
- CI (for 2 years)
- 8% 8%
- 100_____ 108 _____ 116.64
- 16.64
 P SI CI Diff
 100 16 16.64 0.64
- 0.64 -> 100
- 128 -> ?
- $\frac{12800}{0.64}$ = Rs. 20000



Q. Difference between Compound interest & simple interest on a sum placed at 8% p.a. compounded annually for 2 years is Rs 128. Find the principal

• A.20000

B. 24000

C. 26000

D. 15000

· Soln:

• Let the principal be P = Rs. 100.

time N = 2 years, rate of interest R = 8% per annum

• simple interest = $PNR/100 = \frac{100 \times 8 \times 2}{100} = Rs. 16$

compound amount= P(1+R/ 100)^N

• = $100*(1+\frac{8}{100})^2 = 100*(\frac{108}{100})^2 = 100(\frac{11664}{10000}) = \frac{11664}{100} = 116.64$

compound interest = compound amount – principal

• C.I = A - P =116.64-100=Rs. 16.64

• the difference between the compound interest and simple interest = 16.64-16.00 = Rs. 0.64

• 0.64 -> 100

• 128 -> ?

 $\bullet = \frac{128*100}{0.64} = 20000$

Thus, the principal is Rs. 20000.

- If the difference between compound and simple interest is of two years than,
 Difference = P(R)²/(100)²
 Where P = principal amount, R = rate of interest
- If the difference between compound and simple interest is of three years than,
 Difference = 3 x P(R)²/(100)² + P (R/100)³.
 Here also, P = principal amount, R = rate of interest



- Q. A sum of money placed at compound interest doubles in 7 years. In how many years the principal becomes
 - a. 4 times of itself
 - b. 8 times of itself

Soln:

Let initial value be 100

7yrs 7yrs 7yrs
$$100 \longrightarrow 200 \longrightarrow 400 \longrightarrow 800$$
doubles 14 yrs 21yrs

- a. In 14yrs
- b. In 21 yrs

<u>OR</u>

100---->200 in 7 years 200---->400 in again 7 years then, 400---->800 in 7 years again, thus the time becomes= 7+7+7= 21 years.



Q. When annual compounding is done, a sum amounts to Rs 5000 in 6 years and 7200 in 8 years. What is the int rate?

A. 10%

B. 15%

C. 20%

D. 25%

<u>Soln</u>

Let P be the principal & R the int rate

→ 5000

 $= P(1+R/100)^6....(1)$

→ 7200

 $= P(1+R/100)^8....(2)$

→ 36/25

 $= (1+R/100)^2$

→ Taking square roots of both sides

→ 1+R/100

= 6/5

→ R/100

=1/5

 \rightarrow R

= 20%



Q. A sum fetched a total simple interest of Rs.7056 at the rate of 8 percent per year in 7 years. What is the sum?

A. Rs 12600

B) Rs 15120

C) Rs 10080

D) Rs 7560

Ans: A



Q. Find the compound interest on Rs. 15,625 for 9 months at 16% per annum compounded quarterly.

A. Rs. 1851

B. Rs. 1941

C. Rs. 1951

D. Rs. 1961



Q. What is the difference between the simple interest on a principal of Rs. 500 being calculated at 5% per annum for 3 years and 4% per annum for 4 years?

A.Rs. 5 B.Rs. 10 C.Rs. 20

D.Rs. 40 E. None of these

$$SI_1 = P N_1 R_1 / 100$$

= $\frac{500 \times 3 \times 5}{100} = Rs. 75$

$$SI_2 = P N_2 R_2 / 100$$

= $\frac{500 \times 4 \times 4}{100} = Rs. 80$

Difference = 80 - 75 = Rs. 5

$$500 == 15\% \uparrow \Rightarrow 575 \text{ (1st case)}$$

$$500 == 16\% \uparrow \Rightarrow 580 (2^{nd} case)$$

difference = 580 - 575 = Rs. 5

Ans: A



Q. A sum of money placed at compound interest doubles itself in 4 years. In how many years will it amount to 8 times?

A. 9 years

B. 8 years

C. 27 years

D. 12 years

Ans: D



Q. Difference between Compound interest & simple interest on a sum placed at 20% per annum compounded annually for 2 years is Rs. 72. Find the sum.

A. Rs. 2400

B.Rs. 8400

C. Rs.1800

D.Rs. 900



Q. What is the simple interest on a sum of Rs. 700 if the rate of interest for the first 3 years is 8% per annum and for the last 2 years is 7.5% per annum?

A.Rs. 269.5 B.Rs. 283 C.Rs. 273 D.Rs. 280 E. None of these



Q. Rs.2100 is lent at compound interest of 5% per annum for 2 years. Find the amount after two years.

• A.Rs. 2300

- B.Rs. 2315.25
- C.Rs. 2310

- D.Rs. 2320 E. None of these

- Soln:
- $A = P (1 + R/100)^T$
- $A = 2100(1+5/100)^2$
- A=2100×[105/100]2
- $A = \frac{2100 \times 11025}{100 \times 11025}$
- Amount, A=Rs.2315.25
- Ans : B



Q. A man borrowed total Rs 2500 at Simple interest from two money lenders. He paid interest at 12% p.a. to one and 14% p.a. to the other. The total interest paid for the year was Rs.326. How much did he borrow at 14%?

A. Rs 1000

B. Rs 1200

C. Rs 1300

D. Rs 1500

Soln:

Let,
$$x = Principal at 12\%$$

&

2500-x = Principal at 14%

SI at Rs.x =
$$\frac{x \times 1 \times 12}{100} = \frac{12x}{100} = \frac{3x}{25}$$

SI at Rs.2500 -x =
$$\frac{2500-x\times1\times14}{100}$$
 = $\frac{(2500-x)\times7}{50}$ = $\frac{17500x-7x}{50}$

SI at x + SI at 2500 - x = 326

Substitute and solving the equation gives x = Rs. 1200

We need Principal at 2500-x = 2500 - 1200 = Rs. 1300



Q.A certain sum of money amounts to Rs. 704 in two years and Rs 800 in 5 years. Find the Principal.

A. Rs. 640

B. Rs. 600

C. Rs. 550

D. Rs. 450

Ans: A



Q. What should be the simple interest obtained on an amount of Rs 5,760 at the rate of 6% p.a. after 3 years?

A. Rs 1036.80

B. Rs 1666.80

C. Rs 1336.80

D. Rs 1063.80

E. None of these

Ans: A



Q. The simple interest on Rs.1820 from March 9, 2012 to May 21, 2012 at 7.5% rate will be

A. Rs. 22.50

B. Rs. 27.30

C. Rs. 28.80

D. Rs. 29

Ans: B



IMPORTANT FORMULAE

- I.1.Area of a rectangle=(length x breadth)
- Therefore length = (area/breadth) and breadth=(area/length)
- 2.Perimeter of a rectangle = 2 x (length + breadth)
- II.Area of a square = (side)^2 =1/2(diagonal)^2
- III Area of four walls of a room = 2*(length + breadth)*(height)
- IV 1.Area of the triangle=1/2(base*height)
- 2. Area of a triangle = $(s^*(s-a)(s-b)(s-c))^(1/2)$, where a,b,c are the sides of a triangle & $s = \frac{1}{2}(a+b+c)$
- 3.Area of the equilateral triangle =((3^1/2)/4)*(side)^2



IMPORTANT FORMULAE

- V₋1.Area of the parellogram =(base *height)
- 2.Area of the rhombus=1/2(product of the diagonals)
- 3.Area of the trapezium=1/2(size of parallel sides)*distance between them.
- **VI** 1.Area of a circle =pi*r^2, where r is the radius
- 2. Circumference of a circle = 2ΠR.
- 3. Length of an arc = $2\Pi R\theta/(360)$ where θ is the central angle
- 4. Area of a sector = (1/2) (arc x R) = $pi*R^2*\theta/360$.
- VII. 1. Area of a semi-circle = (pi)*R^2.
- 2. Circumference of a semi-circle = (pi)*R.
- where, pi = 3.142



VOLUME AND SURFACE AREA – IMPORTANT FORMULAE

- I. CUBOID
- Let length = I, breadth = b and height = h units. Then,
- 1. Volume = (I x b x h) cubic.units.
- 2. Surface area= 2(lb + bh + lh) sq.units.
- **3. Diagonal**.= $\sqrt{l^2 + b^2 + h^2}$ units
- II. CUBE
- Let each edge of a cube be of length a. Then,
- 1. Volume = a^3 cubic units.
- 2. Surface area = $6a^2$ sq. units.
- 3. Diagonal = $\sqrt{3}$ a units.
- III. CYLINDER
- Let radius of base = r and Height (or length) = h. Then,
- 1. Volume = (r2h) cubic units.
- 2. Curved surface area = $(2 \square \text{ rh})$. units.
- 3. Total surface area =2 ∏ r (h+r) sq. units



VOLUME AND SURFACE AREA – IMPORTANT FORMULAE

- IV. CONE
- Let radius of base = r and Height = h. Then,
- 1. Slant height, $I = \sqrt{h2+r2}$
- 2. Volume = $(1/3) \prod r^2 h$ cubic units.
- 3. Curved surface area = (☐ rl) sq. units.
- 4. Total surface area = $(\prod rl + \prod r^2)$ sq. units.
- V. SPHERE
- Let the radius of the sphere be r. Then,
- 1. Volume = $(4/3) \prod r^3$ cubic units.
- 2. Surface area = $(4 \prod r^2)$ sq. units.
- VI. HEMISPHERE
- Let the radius of a hemisphere be r. Then,
- 1. Volume = $(2/3) \prod r^3$ cubic units.
- 2. Curved surface area = $(2 \prod r^2)$ sq. units.
- 3. Total surface area = $(3 \sqcap r^2)$ units.



Surds and Indices

Rules of Indices: -

i.
$$a^n * a^m = a^{m+n}$$

ii.
$$\frac{a^m}{a^n} = a^{m-n}$$

iii.
$$(a^n)^m = a^{mn}$$

iv.
$$(ab)^n = a^n * b^n$$

v.
$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

vi.
$$a^0 = 1$$
 (where $a \neq 0$)

vii.
$$a^{-n} = \frac{1}{a^n}$$

Rules of Surds: -

i.
$$\sqrt[n]{a} = a^{\frac{1}{n}}$$

ii.
$$\sqrt[n]{ab} = a^{\frac{1}{n}} * b^{\frac{1}{n}}$$

iii.
$$\sqrt[n]{\frac{a}{b}} = \frac{a^{\frac{1}{n}}}{b^{\frac{1}{n}}}$$

iv.
$$\left(\sqrt[n]{a}\right)^n = a$$

v.
$$\left(\sqrt[n]{a}\right)^m = a^{\frac{m}{n}}$$



Races

Races

- A contest of speed in running, riding, driving, sailing or rowing is called a race.
- If in a race Ram is at starting point & Shyam starts from 20 mts ahead, then it is said that Ram has given Shyam a start of 20 mts or Ram gives Shyam 20 mts.
- This means that if they start from same point Ram would beat Shyam by 20 mts.



Races

Q. In a 100 mt race A gives B a start of 25 mt & still wins by 9 sec. Find the speed of A if speed of B is 6 kmph.

A.8 kmph

B. 9 kmph

C. 10 kmph

D. 12 kmph

Soln

!-----!

A<---25--->B<-----> A=t-9, B=t

Sb = 6 kmph = $6 \times 5/18 = 5/3 \text{ m/s}$

Tb = Db/Sb = 75/(5/3) = 45 sec

Ta = Tb-9 = 36 sec

Sa = Da/Ta = 100/36 m/s

 $= 100/36 \times 18/5$

= 10 kmph



Races(Assignment)

Q. In a 100 m race, A can beat B by 25 m and B can beat C by 4 m. In the same race, A can beat C by:

A. 21 m

B. 26 m

C. 28 m

D. 29 m

• Soln:-

A : B = 100 : 75

B:C=100:96

A:C=
$$(\frac{A}{B} \times \frac{B}{C}) = (\frac{100}{75} \times \frac{100}{96}) = 100:72$$

A beats C by (100–72)=28 m.

Circular Motion

- Use of both relative speed & LCM
- Let Sa, Sb = speeds of two persons.

Sr = Their relative speed

Distance traveled in 1 round = circumference

Case A: Both running in Same direction

Both meet again first time when → Time = dist/Sr = Circumference/Sa-Sb

Case B: Both running in opposite directions(DistA+ DistB = Circumference)

Both meet first time when → Time = Circumference/Sa+Sb

Case C: Both running in same/opposite directions

Both meet again at starting point at LCM of their Lap times.



Circular Motion(Races)

Two friends P & Q start from same point at the same time on a circular track 336 meters long in opposite directions at 6 m/s & 8 m/s respectively. After how much time will they meet again at the starting point for the first time?

A. 56 sec

B. 112 sec C. 168 sec D. 214 sec

Ans: C

Step1 – find the time taken by each member /player to complete 1 round

Step2 – Calculate LCM(Lap time)

LapTm(P) =
$$\frac{\text{Circumference}}{\text{Sp}} = \frac{336}{6} = 56 \text{ sec}$$

LapTm(Q) =
$$\frac{\text{Circumference}}{\text{SQ}} = \frac{336}{8} = 42 \text{ sec}$$

LCM(42,56) = 168 sec

Circular Motion(Assignment)

Q. A, B & C start together running along a circular track of 500 m at 8 km/hr, 5 km/hr & 3 km/hr respectively. After how much time will all three meet again at the starting point for the first time?

A. 20 min

B. 24 min

C. 30 min

D. 36 min





