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Proving Trigonometric Formulas using Euler's Formula: $e^{ix} = \cos(x) + i \sin(x)$

We are going to prove some formulas from trigonometry, directly from Euler's formula, $e^{ix} = \cos(x) + i \sin(x)$.

▶ $\sin^2(x) + \cos^2(x) = 1$

This can be proven from the Pythagorean theorem and the definitions of the trigonometric functions, but we are going to do it using Euler's formula.

▶ $e^{ix} = \cos x + i \sin x$

First, use the fact that $e^{i(-x)}$, we know that's $\cos(x) + i \sin(x)$.



$$e^{-ix} = e^{i(-x)} = \cos(-x) + i \sin(-x) = \cos(x) - i \sin(x)$$

Next, we are going to multiply together these two equations right here.

▶ $e^{ix} \cdot e^{-ix} = (\cos x + i \sin x)(\cos x - i \sin x)$

These exponents we will add them together, get zero for an exponent, and e^0 is 1.