



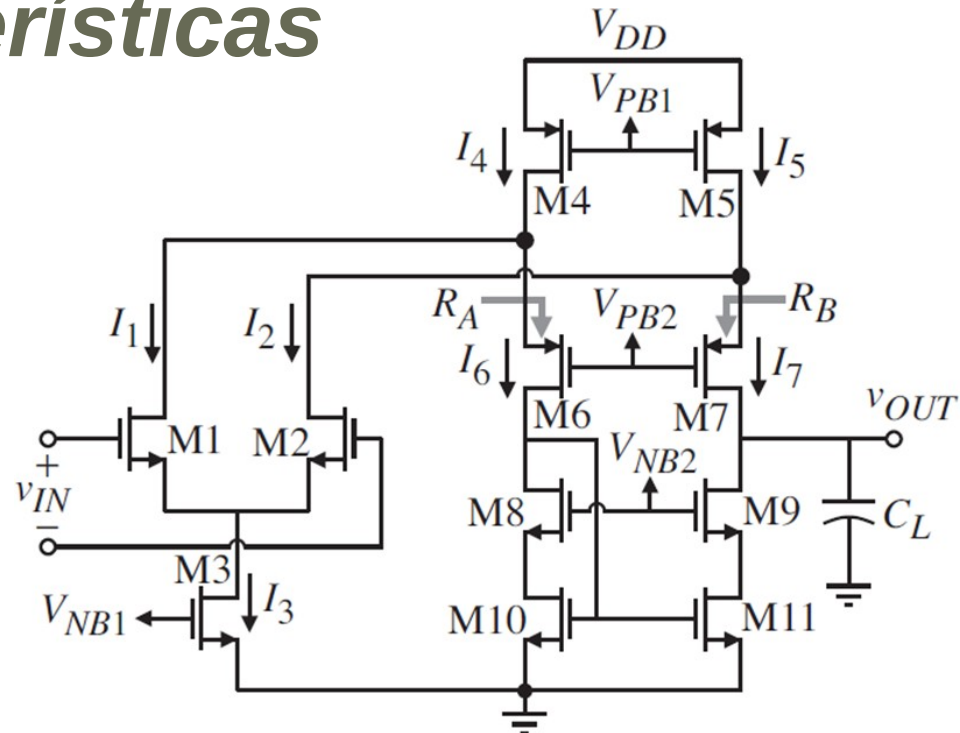
# Projeto de Circuitos Eletrônicos Integrados 2

## Amplificadores Operacionais Avançados *Folded Cascode*

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# Características

- Auto compensado
- Bom PSRR
- Bom ICMR
- $I_4$  e  $I_5$  devem ser projetados de tal maneira que  $I_6$  e  $I_7$  nunca sejam 0 (Ex.  $I_4 = I_5 = 1.5 \cdot I_3$ )



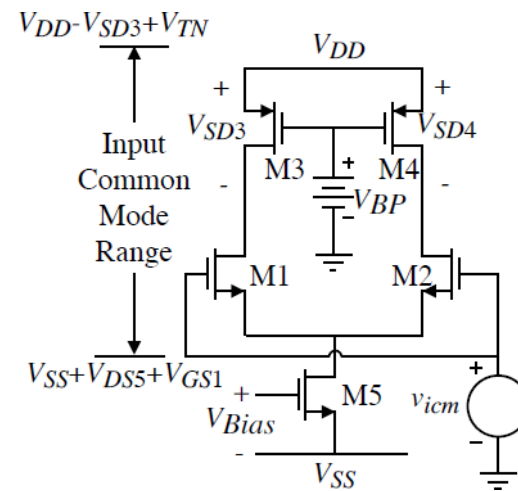
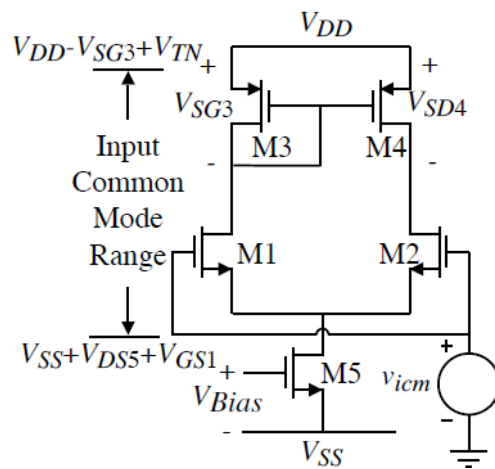
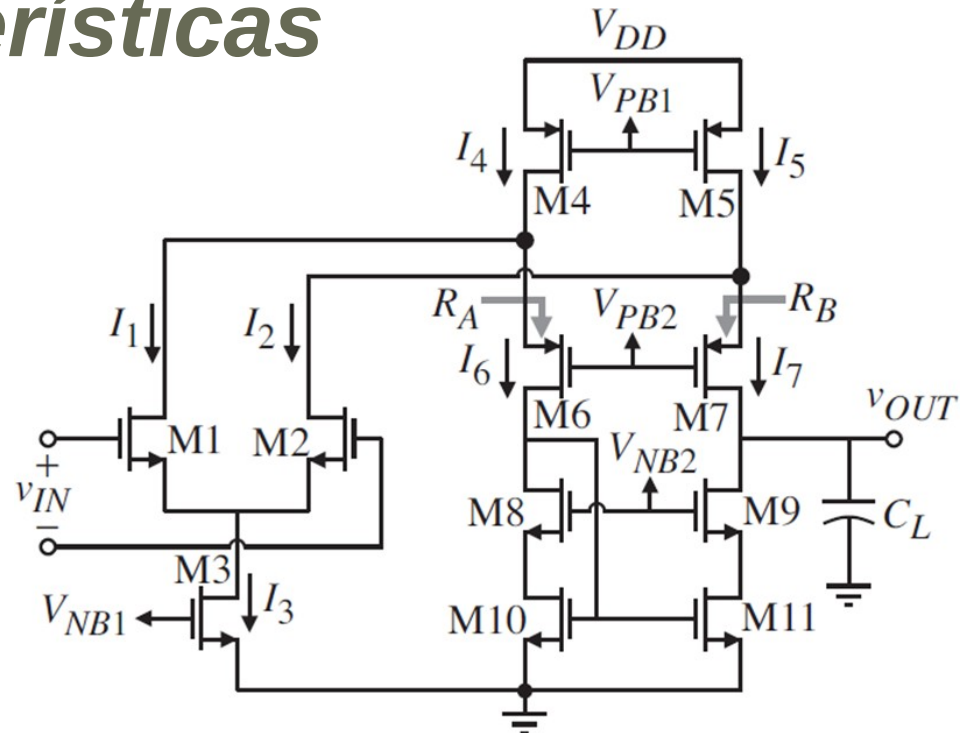
# Características

➤ Auto compensado

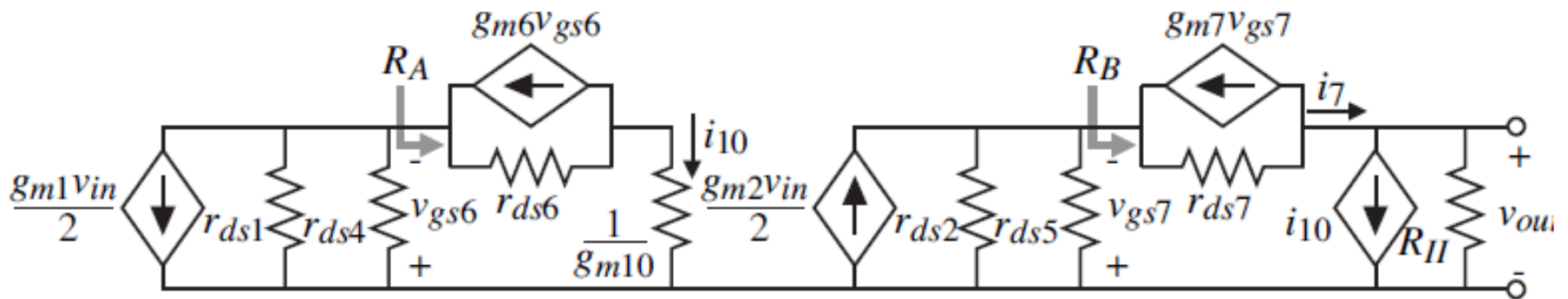
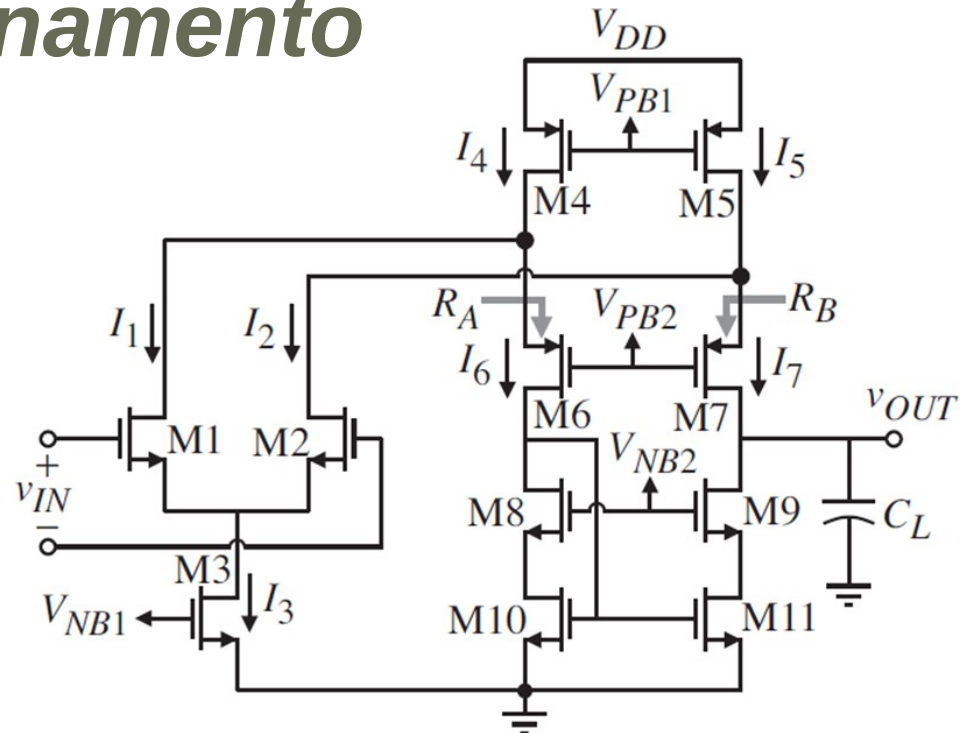
➤ Bom PSRR

➤ Bom ICMR

➤ I4 e I5 devem ser projetados de tal maneira que I6 e I7 nunca sejam 0 (Ex.  $I_4 = I_5 = 1.5 \cdot I_3$ )



# Equacionamento



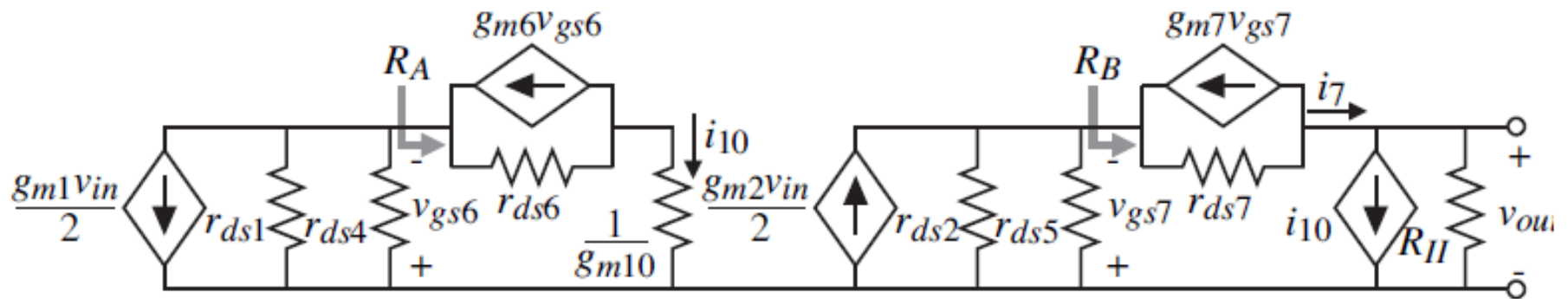
# Equacionamento

$$R_A = \frac{r_{ds6} + (1/g_{m10})}{1 + g_{m6}r_{ds6}} \approx \frac{1}{g_{m6}}$$

$$R_B = \frac{r_{ds7} + R_{II}}{1 + g_{m7}r_{ds7}} \approx \frac{R_{II}}{g_{m7}r_{ds7}} \quad \text{onde, } R_{II} \approx g_{m9}r_{ds9}r_{ds11}$$

$$i_{10} = \frac{-g_{m1}(r_{ds1} \parallel r_{ds4})v_{in}}{2[R_A + (r_{ds1} \parallel r_{ds4})]} \approx \frac{-g_{m1}v_{in}}{2}$$

$$i_7 = \frac{\frac{g_{m2}(r_{ds2} \parallel r_{ds5})v_{in}}{2 \left[ \frac{R_{II}}{g_{m7}r_{ds7}} + (r_{ds2} \parallel r_{ds5}) \right]}} = \frac{\frac{g_{m2}v_{in}}{2} \left( 1 + \frac{R_{II}(g_{ds2} + g_{ds5})}{g_{m7}r_{ds7}} \right)}{2(1+k)} \quad \text{where } k = \frac{R_{II}(g_{ds2} + g_{ds5})}{g_{m7}r_{ds7}}$$



## Equacionamento

$$R_A = \frac{r_{ds6} + (1/g_{m10})}{1 + g_{m6}r_{ds6}} \approx \frac{1}{g_{m6}}$$

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$$i_{10} = \frac{-g_{m1}(r_{ds1} \parallel r_{ds4})v_{in}}{2[R_A + (r_{ds1} \parallel r_{ds4})]} \approx \frac{-g_{m1}v_{in}}{2}$$

$$i_7 = \frac{g_{m2}(r_{ds2} \parallel r_{ds5})v_{in}}{2\left[\frac{R_{II}}{g_{m7}r_{ds7}} + (r_{ds2} \parallel r_{ds5})\right]} = \frac{g_{m2}v_{in}}{2\left(1 + \frac{R_{II}(g_{ds2} + g_{ds5})}{g_{m7}r_{ds7}}\right)} = \frac{g_{m2}v_{in}}{2(1+k)} \quad \text{where } k = \frac{R_{II}(g_{ds2} + g_{ds5})}{g_{m7}r_{ds7}}$$

$$\frac{v_{out}}{v_{in}} = \left(\frac{g_{m1}}{2} + \frac{g_{m2}}{2(1+k)}\right)R_{out} = \left(\frac{2+k}{2+2k}\right)g_{mI}R_{out} \quad \begin{aligned} R_{out} &\approx (g_{m9}r_{ds9}r_{ds11}) \parallel [g_{m7}r_{ds7}(r_{ds2} \parallel r_{ds5})] \\ &\approx \left(\frac{g_{m}r_{ds}^2}{3}\right) \end{aligned}$$



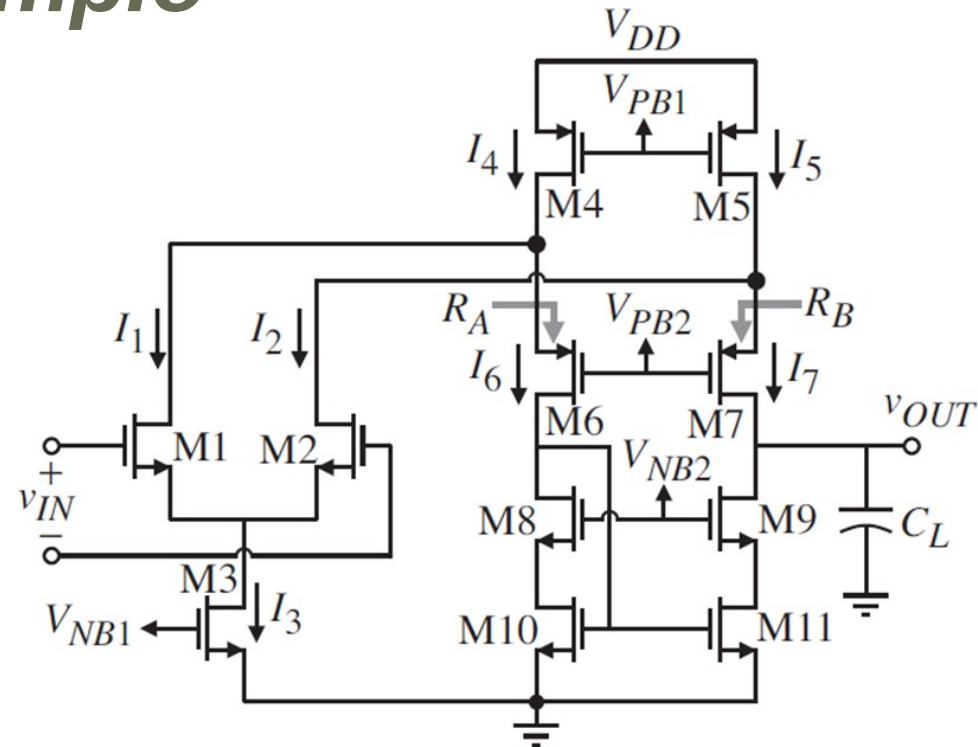
## Etapas de projeto

Step	Relationship	Design Equation/Constraint	Comments
1	Slew Rate	$I_3 = SR \cdot C_L$	
2	Bias currents in output cascodes	$I_4 = I_5 = 1.2I_3$ to $1.5I_3$	Avoid zero current in cascodes
3	Maximum output voltage, $v_{out(max)}$	$S_5 = \frac{2I_5}{K_P \cdot V_{SD5}^2}, S_7 = \frac{2I_7}{K_P \cdot V_{SD7}^2}, (S_4 = S_5 \text{ and } S_6 = S_7)$	$V_{SD5(sat)} = V_{SD7(sat)} = 0.5[V_{DD} - V_{out(max)}]$
4	Minimum output voltage, $v_{out(min)}$	$S_{11} = \frac{2I_{11}}{K_N \cdot V_{DS11}^2}, S_9 = \frac{2I_9}{K_N \cdot V_{DS9}^2}, (S_{10} = S_{11} \text{ and } S_8 = S_9)$	$V_{DS9(sat)} = V_{DS11(sat)} = 0.5[V_{out(min)} - V_{SS}]$
5	$GB = \frac{g_{m1}}{C_L}$	$S_1 = S_2 = \frac{g_{m1}^2}{K_N \cdot I_3} = \frac{GB^2 C_L^2}{K_N \cdot I_3}$	
6	Minimum input CM	$S_3 = \frac{2I_3}{K_N \cdot (V_{in(min)} - V_{SS} - \sqrt{(I_3/K_N \cdot S_1)} - V_{T1})^2}$	
7	Maximum input CM	$S_4 = S_5 = \frac{2I_4}{K_P \cdot (V_{DD} - V_{in(max)} + V_{T1})^2}$	$S_4$ and $S_5$ must meet or exceed value in step 3
8	Differential Voltage Gain	$\frac{v_{out}}{v_{in}} = \left( \frac{g_{m1}}{2} + \frac{g_{m2}}{2(1+k)} \right) R_{out} = \left( \frac{2+k}{2+2k} \right) g_{m1} R_{out}$	$k = \frac{R_{II}(g_{ds2} + g_{ds4})}{g_{m7} r_{ds7}}$
9	Power dissipation	$P_{diss} = (V_{DD} - V_{SS})(I_3 + I_{10} + I_{11})$	

# Exemplo

➤ Projete o Amp. Op ao lado com as seguintes especificações:

$V_{DD} = 2.5V$	$A_v \geq 3000V/V$
$GB = 10MHz$	$ICMR = 1V$ a $2.5V$
Slew rate = $10V/\mu s$ com $10pF$ de carga	
Dissipação de Potência $< 5mW$	
$0.5V < \text{Output swing} < 2V$	



➤ Dados da tecnologia:

$V_{tn} = 0.5V$	$\lambda_N = 0.06V^{-1}$
$V_{tp} = 0.5V$	$\lambda_P = 0.08V^{-1}$
$K_n = 120\mu A/V^2$	
$K_p = 25\mu A/V^2$	

➤ Demais dados de projeto:

$L = 0.5\mu m$



(1) Slew Rate

$$I_3 = SR \cdot C_L = 10 \times 10^6 \cdot 10^{-11} = 100 \mu A$$

(2) Correntes de polarização na saída

$$I_4 = I_5 = 125 \mu A$$

(3) Tensão de saída máxima

$$S_4 = S_5 = \frac{2 \cdot 125 \mu A}{25 \mu A/V^2 \cdot (0.25 V)^2} = \frac{2 \cdot 125 \cdot 16}{25} = 160$$

e, assumindo um valor de corrente para o pior caso (M1 em corte)

$$S_6 = S_7 = \frac{2 \cdot 125 \mu A}{25 \mu A/V^2 (0.25 V)^2} = \frac{2 \cdot 125 \cdot 16}{25} = 160$$

(4) Tensão de saída mínima

$$S_8 = S_9 = S_{10} = S_{11} = \frac{2 \cdot I_8}{K_N' V_{DS8}^2} = \frac{2 \cdot 125}{120 \cdot (0.25)^2} = 33$$

(5) Cálculo de  $S_1$  e  $S_2$  a partir de GB

$$S_1 = S_2 = \frac{GB^2 \cdot C_L^2}{K_N' I_3} = \frac{(20\pi \times 10^6)^2 (10^{-11})^2}{120 \times 10^{-6} \cdot 100 \times 10^{-6}} = 32.9 \approx 33$$

(6) ICM mínimo

$$S_3 = \frac{2I_3}{K_N' \left( V_{in(min)} - V_{SS} - \sqrt{\frac{I_3}{K_N' S_1}} - V_{T1} \right)^2} = \frac{200 \times 10^{-6}}{120 \times 10^{-6} \left( 1.0 + 0 - \sqrt{\frac{100}{120 \cdot 33}} - 0.5 \right)^2} = 14.3 \approx 15$$

(7) ICM máximo

$$S_4 = S_5 \geq \frac{2I_4}{K_P' [V_{DD} - V_{in(max)} + V_{T1}]^2} = \frac{2 \cdot 125 \mu A}{25 \times 10^{-6} \mu A/V^2 [0.5V]^2} = 40$$

## (8) Cálculo do Ganho

$$S_4, S_5: g_m = \sqrt{2 \cdot 125 \cdot 25 \cdot 160} = 1000 \mu\text{S} \quad \text{and} \quad g_{ds} = 125 \times 10^{-6} \cdot 0.08 = 10 \mu\text{S}$$

$$S_6, S_7: g_m = \sqrt{2 \cdot 75 \cdot 25 \cdot 1600} = 774.6 \mu\text{S} \quad \text{and} \quad g_{ds} = 75 \times 10^{-6} \cdot 0.08 = 6 \mu\text{S}$$

$$S_8, S_9, S_{10}, S_{11}: g_m = \sqrt{2 \cdot 75 \cdot 120 \cdot 20} = 600 \mu\text{S} \quad \text{and} \quad g_{ds} = 75 \times 10^{-6} \cdot 0.06 = 4.5 \mu\text{S}$$

$$S_1, S_2: g_{mI} = \sqrt{2 \cdot 50 \cdot 120 \cdot 33} = 629 \mu\text{S} \quad \text{and} \quad g_{ds} = 50 \times 10^{-6} (0.06) = 3 \mu\text{S}$$

$$R_{II} \approx g_{m9} r_{ds9} r_{ds11} = (600 \mu\text{S}) \left( \frac{1}{4.5 \mu\text{S}} \right) \left( \frac{1}{4.5 \mu\text{S}} \right) = 38.25 \text{ M}\Omega$$

$$R_{out} \approx 29.63 \text{ M}\Omega \parallel (774.6 \mu\text{S}) \left( \frac{1}{6 \mu\text{S}} \right) \left( \frac{1}{10 \mu\text{S} + 3 \mu\text{S}} \right) = 7.44 \text{ M}\Omega$$

$$k = \frac{R_{II}(g_{ds2} + g_{ds4})}{g_{m7} r_{ds7}} = \frac{38.25 \text{ M}\Omega (3 \mu\text{S} + 10 \mu\text{S}) (6 \mu\text{S})}{774.6 \mu\text{S}} = 3.85$$

$$A_{vd} = \left( \frac{2+k}{2+2k} \right) g_{mI} R_{out} = 2987 \text{ V/V}$$

Próximo da especificação (3000V/V)



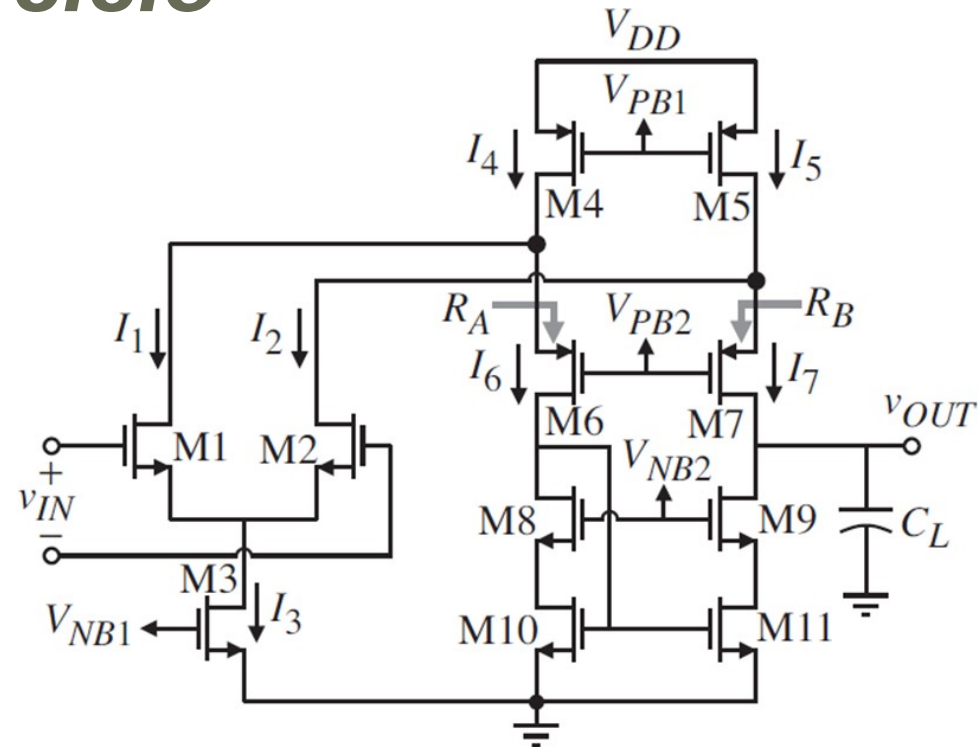
(9) Dissipação de potência

$$P_{diss} = 2.5V(100\mu A + 125\mu A + 125\mu A) = 0.875mW$$

# Exercício

➤ Projete o Amp. Op ao lado com as seguintes especificações:

$V_{DD} = 1,8V$	$A_v \approx 5000V/V$
$GB = 5MHz$	$ICMR = 0,8V$ a $1,3V$
Slew rate = $2V/\mu s$ com $5pF$ de carga	
$GB = 5MHz$ com $2pF$ de carga	
Dissipação de Potência $< 5mW$	
$0,3V < \text{Output swing} < 0,8V$	



➤ Dados da tecnologia:

$V_{tn} = 0,397V$	$\lambda_n = 0,06V^{-1}$
$V_{tp} = 0,457V$	$\lambda_p = 0,08V^{-1}$
$K_n = 591\mu A/V^2$	$C_{ox} = 8,82E-15 F/\mu m^2$
$K_p = 216\mu A/V^2$	

➤ Demais dados de projeto:

$L_{min}$ e $W_{min} = 0,5\mu m$



# *Referências*

- Phillip Allen, Douglas Holberg, " CMOS Analog Circuit Design", **Capítulo 6** Oxford, 2a ed., 2002.