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1. Consider the demand function

$$q = 48,000 - 10p^2$$

where p is the price and q is the demand.

Find the elasticity E (as a function of p).

Solution. Recall the elasticity is defined as

$$E = -\frac{p}{q}\frac{dq}{dp}$$

and so

$$E = -\frac{p}{48000 - 10p^2} (-20p) = \frac{20p^2}{48000 - 10p^2}.$$

2. Find $\int \left(\frac{9}{x} - 3e^x\right) dx$.

Solution. We have

$$\int \left(\frac{9}{x} - 3e^x\right) dx = 9 \int \frac{1}{x} dx - 3 \int e^x dx = 9 \ln|x| - 3e^x + C$$