

Prepare a summary of the material & look at homework and quizzes before doing the review.

1. Convert the following equations from polar to rectangular coordinates, as appropriate:

(a)  $x^2 + y^2 - 3x = 0$ ,

(b)  $r = -4 \sin \theta$ .

2. Sketch the following (polar) equations:

(a)  $r = \cos 2\theta$ ,

(b)  $r = 1 + 2 \cos \theta$ ,

(c)  $r = 2/(1 - \cos \theta)$

3. Find the following areas:

(a) Shared by  $r = 2(1 - \sin \theta)$  and  $r = 2(1 + \sin \theta)$ .

(b) Bounded by one leaf of  $r = 4 \sin 3\theta$ .

(c) Inside  $r = 1 + \cos 2\theta$  and outside  $r = 1$ .

4. Find the length of the curves given by the following polar equations:

(a)  $r = 2 \sin \theta + 2 \cos \theta$ ,  $0 \leq \theta \leq \pi/2$ .

(b)  $r = \sqrt{1 + \cos 2\theta}$ ,  $-\pi/2 \leq \theta \leq \pi/2$ .

5. Show that the vector  $\mathbf{u} + \mathbf{v}$  bisects the angle between vectors  $\mathbf{u}$  and  $\mathbf{v}$  if and only if  $|\mathbf{u}| = |\mathbf{v}|$ .

6. If  $P = (3, 1, 2)$ ,  $Q = (1, 0, 1)$  and  $R = (4, 2, -1)$ , is  $\triangle PQR$  a right-angled triangle? What is the area of this triangle?

7. Find the distance between the given objects:

(a)  $(0, -1, 1)$  and the plane  $2x - 3y = 2$ ,

(b)  $(2, 0, 1)$  and the line through  $(1, -2, 2)$  and  $(3, 0, 2)$ ,

(c)  $(2, -1, -1)$  and the plane determined by  $(1, 1, 4)$ ,  $(3, 0, 1)$ , and  $(0, -2, 2)$ .

8. (a) Find the line of intersection of the planes  $x + 2y + z = 1$  and  $x - y + 2z = -8$ .  
(b) Find  $A$  so that, for the planes  $x + 2y + z = 3$  and  $Ax - 4y + 3z = 5$ , the line of intersection contains  $(2, 0, 1)$ .

9. See Problem 62 on page 659. The figure in this problem shows a parallelogram with vertices  $A = (2, -1, 4)$ ,  $B = (1, 0, -1)$ ,  $C = (1, 2, 3)$  and  $D$ . Find:

(a) the coordinates of  $D$ ,

(b) the cosine of the interior angle at  $B$ ,

(c) the vector projection of  $\overrightarrow{BA}$  onto  $\overrightarrow{BC}$ ,

- (d) the area of the parallelogram, and
  - (e) the equation of the plane containing the parallelogram.
10. (a) Find the velocity and acceleration vectors for  $\mathbf{r}(t) = (e^{-t})\vec{i} + (2 \cos 3t)\vec{j} + (2 \sin 3t)\vec{k}$ .
- (b) Find the tangent line to the curve  $\mathbf{r}(t) = (\cos t)\vec{i} + (\sin t)\vec{j} + (\sin 2t)\vec{k}$  at  $t = \pi/2$ .