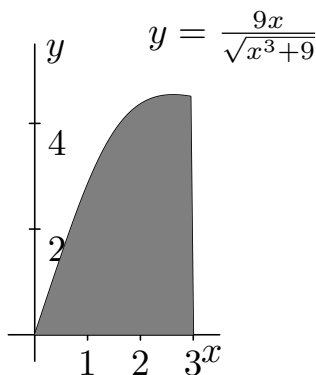


- 5 1. Set up an integral to find the volume of the solid generated by revolving the region bounded by  $y = \frac{9x}{\sqrt{x^3+9}}$ , the  $x$ -axis and the vertical line  $x = 3$  about the  $y$ -axis. You do not need to evaluate the integral.

*Solution.*



The shell is parallel to the axis of revolution. So the shell height is height =  $\frac{9x}{\sqrt{x^3+9}}$  and the shell radius (i.e. the distance from the axis of revolution) is radius =  $x$ . The shell thickness variable is  $x$ , so the limits of integrations are  $a = 0$  and  $b = 3$ . The volume of the solid is given by:

$$\begin{aligned} V &= 2\pi \int_a^b \left( \begin{array}{c} \text{shell} \\ \text{radius} \end{array} \right) \left( \begin{array}{c} \text{shell} \\ \text{height} \end{array} \right) dx \\ &= 2\pi \int_0^3 x \frac{9x}{\sqrt{x^3+9}} dx = \\ &= 18\pi \int_0^3 \frac{x^2}{\sqrt{x^3+9}} dx \end{aligned}$$

- 5 2. Set up the integral for the arc length of the portion of the curve  $f(x) = x^4$  with  $1 \leq x \leq 2$ . You do not need to evaluate the integral.

*Solution.* The arc length for  $f(x) = x^4$  on  $[1, 2]$  is given by

$$\int_1^2 \sqrt{1 + [f'(x)]^2} dx = \int_1^2 \sqrt{1 + (4x^3)^2} dx = \int_1^2 \sqrt{1 + 16x^6} dx .$$