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1. Find the equation, in slope-intercept form, for the line through (4,1) which is perpendicular to the line 4x-2y=5

Solution. First, we find the slope, m. Rearranging 4x-2y=5, we get y=2x-5/2, so this line has slope 2. Thus, m satisfies $m \cdot 2 = -1$, so m = -1/2. The equation of the line, starting from the point-slope form with (4,1), is

$$y - 1 = \frac{-1}{2}(x - 4)$$
$$y = \frac{-1}{2}x + 2 + 1 = \frac{-1}{2}x + 3.$$

2. Find the vertex for the parabola $y = 2x^2 - 8x + 13$

Solution. Using the process of completing the square, we have

$$y = 2(x^{2} - 4x) + 13$$

$$= 2(x^{2} - 4x + 4 - 4) + 13$$

$$= 2(x^{2} - 4x + 4) - 8 + 13$$

$$= 2(x - 2)^{2} + 5$$

Thus, the vertex is (2,5).