5

Due Tuesday March 6, at the start of the recitation.

Explain your reasoning. A correct answer poorly explained will not get full marks.

1. Do the following series converge or diverge?

(a) 
$$\sum_{n=1}^{\infty} \frac{2^n n!}{n^n}$$
, (b)  $\sum_{n=1}^{\infty} \frac{3^n n!}{n^n}$ .

HINT: Use the ratio test. It will help to remember that

$$\lim_{n\to\infty} \left(\frac{n+1}{n}\right)^n = \lim_{n\to\infty} \left(1 + \frac{1}{n}\right)^n = e \approx 2.718.$$