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1. Consider the demand function

$$q = 37,500 - 5p^2$$

where p is the price and q is the demand.

Find the elasticity E (as a function of p).

Solution. Recall the elasticity is defined as

$$E = -\frac{p}{q}\frac{dq}{dp}$$

and so

$$E = -\frac{p}{37500 - 5p^2} \left(-10p\right) = \frac{10p^2}{37500 - 5p^2}.$$

2. Find
$$\int \left(10e^x - \frac{4}{x}\right) dx$$
.

Solution. We have

$$\int \left(10e^x - \frac{4}{x}\right) dx = 10 \int e^x dx - 4 \int \frac{1}{x} dx = 10e^x - 4 \ln|x| + C$$