

# Clicker Questions

Allan Donsig

September 30, 2019

# Review of Limits

If a function  $y = f(x)$  is not defined at  $x = a$ , then

- a)  $\lim_{x \rightarrow a} f(x)$  cannot exist.
- b)  $\lim_{x \rightarrow a} f(x)$  could be zero.
- c)  $\lim_{x \rightarrow a} f(x)$  must approach  $\infty$
- d) None of the above are true.

Recall that we defined the *instantaneous velocity* as the limit of the average rate of change of position.

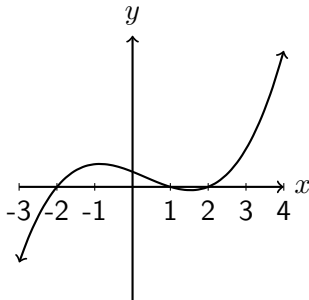
Can the average rate of change on an interval  $[1, 2]$  equal the instantaneous velocity at  $t = 1$ ?

- a) Yes
- b) No

# Order derivative values

For the function  $g(x)$  shown below, arrange the following numbers in increasing order.

- a) 0
- b)  $g'(-2)$
- c)  $g'(0)$
- d)  $g'(1)$
- e)  $g'(3)$



# Derivative Function I

1. Which of the following graphs is the graph of the derivative of the function shown in Figure 2.6?

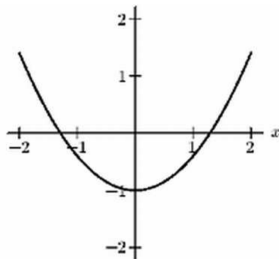
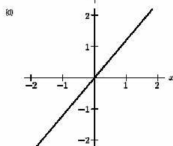
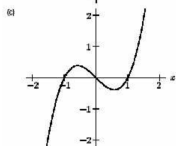
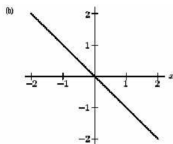
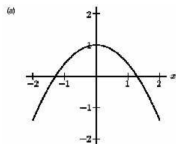


Figure 2.6

# Derivative Function II

2. Which of the following graphs is the graph of the derivative of the function shown in Figure 2.8?

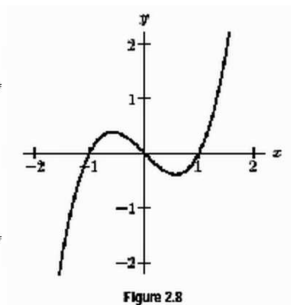
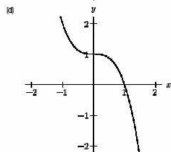
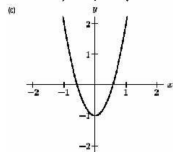
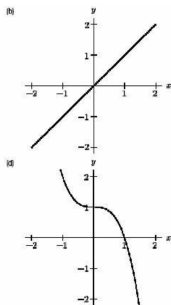
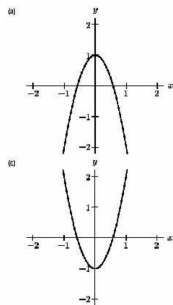


Figure 2.8

13. If  $f(x) = x^2 + \frac{3}{x}$ , then what is  $f'(x)$ ?

(a)  $2x - 3x^{-2}$

(b)  $2x + 3x^{-1}$

(c)  $2x - 3x^2$

(d)  $x^2 - 3x^{-1}$

If  $f(x) = \pi^2$ , then what is  $f'(x)$ ?

(a)  $2\pi$

(b)  $\pi^2$

(c)  $0$

(d)  $2$



The derivative of the function  $f(x) = e^{x+2}$  is

- a)  $(x + 2)e^{x+1}$
- b)  $e^2e^x$
- c)  $e^2$
- d) 0
- e) Cannot be determined from what we know

The 10th derivative of  $\sin x$  is

(a)  $\sin x$

(b)  $\cos x$

(c)  $-\sin x$

(d)  $-\cos x$

# Product Rule I

1.  $\frac{d}{dx} (x^2 e^x) =$

(a)  $2xe^x$

(b)  $x^2 e^x$

(c)  $2xe^x + x^2 e^{x-1}$

(d)  $2xe^x + x^2 e^x$

# Product Rule II

5. When differentiating a constant multiple of a function (like  $3x^2$ ) the Constant Multiple Rule tells us  $\frac{d}{dx}cf(x) = c\frac{d}{dx}f(x)$  and the Product Rule says  $\frac{d}{dx}cf(x) = c\frac{d}{dx}f(x) + f(x)\frac{d}{dx}c$ . Do these two rules agree?
- (a) Yes, they agree, and I am very confident.
  - (b) Yes, they agree, but I am not very confident.
  - (c) No, they do not agree, but I am not very confident.
  - (d) No, they do not agree, and I am very confident.

$$11. \frac{d}{dt} \frac{\sqrt{t}}{t^2+1} =$$

$$(a) \frac{\frac{1}{2}t^{-1/2}-2t}{(t^2+1)^2}$$

$$(b) \frac{\frac{1}{2}t^{-1/2}t^2-2t\sqrt{t}}{(t^2+1)^2}$$

$$(c) \frac{\frac{1}{2}t^{-1/2}(t^2+1)-2t\sqrt{t}}{(t^2+1)^2}$$

$$(d) \frac{t^{-1/2}(t^2+1)-2t\sqrt{t}}{(t^2+1)^2}$$

# Product Rule III

12. If  $f(3) = 2$ ,  $f'(3) = 4$ ,  $g(3) = 1$ ,  $g'(3) = 3$ , and  $h(x) = f(x)g(x)$ , then what is  $h'(3)$ ?

- (a) 2
- (b) 10
- (c) 11
- (d) 12
- (e) 14

14. If  $h = \frac{ab^2e^b}{c^3}$  then what is  $\frac{dh}{db}$ ?

(a)  $\frac{2abe^b}{c^3}$

(b)  $\frac{2abe^b}{3c^2}$

(c)  $\frac{2abe^b + ab^2e^b}{c^3}$

(d)  $\frac{2abe^b c^3 - 3c^2 ab^2 e^b}{c^6}$

3.  $\frac{d}{dx}\sqrt{1-x} =$

(a)  $\frac{1}{2}(1-x)^{-1/2}$

(b)  $-\frac{1}{2}(1-x)^{-1/2}$

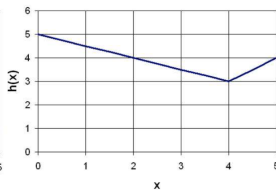
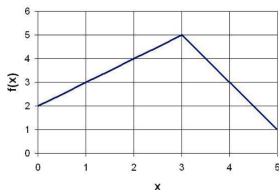
(c)  $-(1-x)^{-1/2}$

(d)  $-\frac{1}{2}(1-x)^{1/2}$



# Chain Rule II

12. The functions  $f(x)$  and  $h(x)$  are plotted below. The function  $g(x) = f(h(x))$ . What is  $g'(2)$ ?



- (a)  $g'(2) = -\frac{1}{2}$
- (b)  $g'(2) = 1$
- (c)  $g'(2) = 3$
- (d)  $g'(2) = 4$
- (e)  $g'(2)$  is undefined

The derivative of the function  $f(z) = \ln(z^2 + 1)$  is

- a)  $2z \ln(z^2 + 1)$
- b)  $\frac{2z}{z^2 + 1}$
- c)  $\frac{-1}{z^2 + 1}$
- d) None of the above

10. If  $q = a^2 \ln(a^3 c \sin b + b^2 c)$ , then  $\frac{dq}{db}$  is

(a)  $\frac{a^2}{a^3 c \sin b + b^2 c}$

(b)  $\frac{a^5 c \cos b + 2a^2 bc}{a^3 c \sin b + b^2 c}$

(c)  $\frac{a^3 c \cos b + 2bc}{a^3 c \sin b + b^2 c}$

(d)  $\frac{6a^3 \cos b + 4ab}{a^3 c \sin b + b^2 c}$

# Implicit Differentiation

The derivative of the implicit function  $x^3 + y^3 - 9xy = 0$  is

a)  $\frac{dy}{dx} = \frac{-3x^2 - y}{y^2 - 3x}$

b)  $\frac{dy}{dx} = \frac{x^2}{y^2 + 3x}$

c)  $\frac{dy}{dx} = \frac{3y - x^2}{y^2 - 3x}$

d)  $\frac{dy}{dx} = -\frac{x^2 + y}{y^2 + 3x}$

e) None of the above