

1.

a.

For $\theta = 45^\circ$

$$\vec{E} = \sin 45^\circ \hat{x} + \cos 45^\circ \hat{y}$$

$$= \frac{1}{\sqrt{2}} \hat{x} + \frac{1}{\sqrt{2}} \hat{y}$$

$$\vec{B} = -\frac{1}{\sqrt{2}} \hat{x} + \frac{1}{\sqrt{2}} \hat{y}$$

Direction of propagation
is $\vec{E} \times \vec{B} = 0\hat{x} + 0\hat{y} + 1\hat{z}$

Prop is in the $+\hat{z}$ dir.

b. For mag of wave vec $|\vec{k}| = \frac{2\pi}{\lambda} = \frac{2\pi}{785\text{nm}} = 0.002504\text{nm}^{-1}$

c. complex $n = \hat{n}(\lambda) = n(\lambda) - i\kappa(\lambda)$

$$\text{input wave} = \vec{E}_0 e^{-i \frac{2\pi}{\lambda} \cdot \hat{n}(\lambda) \cdot x + i\omega t}$$

$$= \vec{E}_0 e^{-i \frac{2\pi}{\lambda} \cdot \hat{n}(\lambda) \cdot x} e^{i\omega t}$$

$$= \vec{E}_0 e^{-i \frac{2\pi}{\lambda} x n_r} e^{\frac{2\pi}{\lambda} x \kappa} e^{i\omega t}$$

2.

a.

$$\mu_{\text{total}} = \underbrace{\epsilon_A C_A}_{\mu_A} + \underbrace{\epsilon_B C_B}_{\mu_B}$$

$$\mu_{\text{total}} = 0.5\text{cm}^{-1}$$

$$0.5\text{cm}^{-1} = \mu_A + 0.0575326 \underbrace{C_B}_{\text{after}} = \frac{6.5}{12} \text{MM}$$

$$\mu_A = 0.44246733$$

b.

for 5mm $\sin(15^\circ) = \boxed{0.258819}$

3. a.

$$\text{Scattering efficiency} = 3.605$$

$$\text{cross section} = \pi (2\text{mm})^2 = \pi \text{m}^2$$

$$\text{Scattering coefficient} = 1.052 \times 10^{-11}$$

b. Matlab code attached

4. a.

b. Matlab code attached

c.